

- Category laws:

$$\begin{aligned}
\text{idl} & : \forall \{\Gamma \Delta\} (\gamma : \text{Sub } \Delta \Gamma) \rightarrow \text{id} \circ \gamma \equiv \gamma \\
\text{idr} & : \forall \{\Gamma \Delta\} (\gamma : \text{Sub } \Delta \Gamma) \rightarrow \gamma \circ \text{id} \equiv \gamma \\
[]_ & : \forall \{\Theta \Delta \Gamma\} (C : \text{Ty } \Gamma) (\gamma : \text{Sub } \Delta \Gamma) (\delta : \text{Sub } \Theta \Delta) \rightarrow \\
& \quad C [_\gamma]_ \text{T} [_\delta]_ \text{T} \equiv C [_\gamma \circ \delta]_ \text{T} \\
[\text{id}] & : \forall \{\Gamma\} (C : \text{Ty } \Gamma) \rightarrow C [_\text{id}]_ \text{T} \equiv C
\end{aligned}$$

- Family structure:

$$\begin{aligned}
[]_ \text{t} & : c [_\gamma]_ \text{t} [_\delta]_ \text{t} \equiv c [_\gamma \circ \delta]_ \text{t} \\
[\text{id}] \text{t} & : c [_\text{id}]_ \text{t} \equiv c
\end{aligned}$$

- (Positive) Context extension

$$\begin{aligned}
\triangleright \beta_1 & : \forall \{\Delta \Gamma C\} \{\sigma : \text{Sub } \Delta \Gamma\} \{t : \text{Tm } \Delta (C [_\sigma]_ \text{T})\} \rightarrow \\
& \quad \pi_1 (_ , _ + _ \{C = C\} \sigma t) \equiv \sigma \\
\triangleright \beta_2 & : \forall \{\Delta \Gamma C\} \{\sigma : \text{Sub } \Delta \Gamma\} \{t : \text{Tm } \Delta (C [_\sigma]_ \text{T})\} \rightarrow \\
& \quad \pi_2 (_ , _ + _ \{C = C\} \sigma t) \equiv t \\
\triangleright \eta & : \forall \{\Delta \Gamma C\} \{\tau : \text{Sub } \Delta (\Gamma \triangleright C)\} \rightarrow \pi_1 \tau ,_+ \pi_2 \tau \equiv \tau \\
\pi_1 \circ & : \forall \{\Delta \Gamma C\} \{\tau : \text{Sub } \Delta (\Gamma \triangleright C)\} \{\Theta\} \{\delta : \text{Sub } \Theta \Delta\} \rightarrow \\
& \quad \pi_1 (\tau \circ \delta) \equiv \pi_1 \tau \circ \delta \\
\pi_2 [] & : \forall \{\Delta \Gamma C\} \{\tau : \text{Sub } \Delta (\Gamma \triangleright C)\} \{\Theta\} \{\delta : \text{Sub } \Theta \Delta\} \rightarrow \\
& \quad \pi_2 \tau [_\delta]_ \text{t} \equiv \pi_2 (\tau \circ \delta)
\end{aligned}$$

- Negation

$$\begin{aligned}
\blacklozenge^{-} & \equiv : \blacklozenge^{-c} \equiv \blacklozenge \\
\text{invC} & : \forall \{\Gamma\} \rightarrow (\Gamma^{-c})^{-c} \equiv \Gamma \\
\text{invS} & : \forall \{\Delta \Gamma\} \{\sigma : \text{Sub } \Delta \Gamma\} \rightarrow (\sigma^{-s})^{-s} \equiv \sigma \\
\text{invT} & : \forall \{\Gamma\} \{C : \text{Ty } \Gamma\} \rightarrow (C^{-t})^{-t} \equiv C \\
\text{id}^{-} & \equiv : \forall \{\Gamma\} \rightarrow (\text{id } \{\Gamma = \Gamma\})^{-s} \equiv \text{id} \\
_ \circ^{-} \equiv _ & : \forall \{\Theta \Delta \Gamma\} (\gamma : \text{Sub } \Delta \Gamma) (\delta : \text{Sub } \Theta \Delta) \rightarrow \\
& \quad (\gamma \circ \delta)^{-s} \equiv (\gamma^{-s}) \circ (\delta^{-s}) \\
\text{nat}^{-} & : \forall \{\Delta \Gamma C\} (\gamma : \text{Sub } \Delta \Gamma) \rightarrow (C [_\gamma]_ \text{T})^{-t} \equiv (C^{-t}) [_\gamma]_ \text{T}
\end{aligned}$$