

11

a) $h_0(t) = \frac{\xi}{1 + \xi(t)}$

to obtain the cumulative hazard function, we integrate the baseline.

$$\int \frac{\xi}{1 + \xi(t)} dt$$

↓

$$\xi \int \frac{1}{1 + \xi(t)} \xrightarrow{u\text{-sub}} \xi \int \frac{1}{\xi(u)} du$$

$$\xi \frac{1}{\xi} \cdot \int \frac{1}{u} du \rightarrow \xi \frac{1}{\xi} \ln |u|$$

$$\xi \frac{1}{\xi} \ln |1 + \xi(t)| = \ln |1 + \xi(t)|$$

The survival function is equal to

$$\exp(-H(t))$$

$$e^{-(\ln |1 + \xi(t)|)}$$

$$\frac{1}{e^{\ln |1 + \xi(t)|}} \rightarrow \frac{1}{|1 + \xi(t)|}$$

2)

a) The hazard function is a log-logistic AFT model.

$$\text{baseline : } h_0(t) = \frac{e^{\theta} K t^{K-1}}{1 + e^{\theta} t^K}$$

hazard

$$h_i(t) = e^{-\alpha x_i} h_0(t e^{-\alpha x_i})$$

$$x_i = \begin{cases} 1 & \text{group 1} \\ 0 & \text{group 2} \end{cases}$$

b) $\mu = 6.4723$

$\sigma = 0.9831$

$\theta = -6.4723 / 0.5567 = -11.6265$

$K = 1 / 0.9831 = 1.01719052$

$\alpha = -1.3272$

c) The hazard ratio is $e^{0.832005}$
or 2.2979177

A treated patient will have
2.2979 the odds of resolving their
sickness in comparison to an
untreated patient.

d) $\frac{159.3667}{55.5236} = 2.87025$

People who were on the treated
experienced a survival time
2.8703 times that of those
who were not.

e) $e^{1.372} = 3.77047$. People in
the treated group had a ^{median} survival
time which was 3.7705 times
that of those in the untreated
group.

f) see attached plot.

g) In comparing the log-likelihood,
we can see that the Weibull
model has a 135.408 log-likelihood,
and the log-logistic has a
132.494 likelihood. Using this statistic,
we would say the Weibull fits
the data better.

