

given:

coordinates = {x, y, z}

length A

length E

length F

needed:angle ω angle ϕ angle θ

$$C = \sqrt{Z^2 + Y^2}$$

$$D = \sqrt{C^2 - A^2}$$

$$= \sqrt{\sqrt{Z^2 + Y^2} - A^2}$$

$$\alpha = \tan^{-1} \frac{Z}{Y}$$

$$\beta = \tan^{-1} \frac{D}{A}$$

$$\omega = \alpha + \beta$$

$$G = \sqrt{D^2 + X^2}$$

$$G^2 = E^2 + F^2 - 2EF \times \cos \phi$$

$$\phi = \cos^{-1} \frac{G^2 - E^2 - F^2}{-2EF}$$

$$\gamma = \tan^{-1} \left(\frac{X}{D} \right)$$

$$\delta = \sin^{-1} \left(\frac{\sin \phi}{G} \times F \right)$$

$$\theta = \gamma + \delta$$

$$\omega = \tan^{-1} \frac{Z}{Y} + \tan^{-1} \frac{\sqrt{\sqrt{Z^2 + Y^2} - A^2}}{A}$$

$$\phi = \cos^{-1} \frac{G^2 - E^2 - F^2}{-2EF}$$

$$\theta = \tan^{-1} \left(\frac{X}{D} \right) + \sin^{-1} \left(\frac{\sin \left(\cos^{-1} \left(\frac{G^2 - E^2 - F^2}{-2EF} \right) \right)}{G} \times F \right)$$