

1a.)  $R = \{(1, 1), (4, 4), (2, 2), (3, 3)\}$ .

1b.)  $R$  is reflexive.

1a.)  $R = \{('a', 'a'), ('c', 'c')\}$ .

1b.)  $R$  is not reflexive.

1c.)  $R^* = \{('a', 'a'), ('c', 'c'), ('b', 'b'), ('d', 'd')\}$ .

2a.)  $R = \{(1, 2), (4, 4), (2, 1), (3, 3)\}$ .

2b.)  $R$  is symmetric.

2a.)  $R = \{(1, 2), (3, 3)\}$ .

2b.)  $R$  is not symmetric.

2c.)  $R^* = \{(1, 2), (3, 3), (2, 1)\}$ .

3a.)  $R = \{('a', 'b'), ('d', 'd'), ('b', 'c'), ('a', 'c')\}$ .

3b.)  $R$  is transitive.

3a.)  $R = \{(1, 1), (1, 3), (2, 2), (3, 1), (3, 2)\}$ .

3b.)  $R$  is not transitive.

3c.)  $R^* = \{(1, 1), (1, 2), (1, 3), (2, 2), (3, 1), (3, 2)\}$ .

4a.)  $R = \{(1, 1), (1, 2), (2, 2), (3, 3), (4, 1), (4, 2), (4, 4)\}$ .

4b.)  $R$  is not an equivalence relation.

4c.)  $R$  is not an equivalence relation because it is not symmetric and transitive.

4a.)  $R = \{(\emptyset, \emptyset), (\emptyset, 1), (\emptyset, 2), (\emptyset, 3), (1, \emptyset), (1, 1), (1, 2), (1, 3), (2, \emptyset), (2, 2), (3, 3)\}$ .

4b.)  $R$  is not an equivalence relation.

4c.)  $R$  is not an equivalence relation because it is not symmetric.

5a.)  $S = \{1, 2, 3, 4\}$ .

5b.)  $R = \{(1, 1), (1, 2), (2, 2), (3, 3), (4, 1), (4, 2), (4, 4)\}$ .

5c.)  $(S, R)$  is not a poset because it is not transitive.

5a.)  $S = \{\emptyset, 1, 2, 3\}$ .

5b.)  $R = \{(\emptyset, \emptyset), (\emptyset, 1), (\emptyset, 2), (\emptyset, 3), (1, \emptyset), (1, 1), (1, 2), (1, 3), (2, \emptyset), (2, 2), (3, 3)\}$ .

5c.)  $(S, R)$  is not a poset because it is not antisymmetric.