

# **Wrong Models in Ecology I**

**Neutral Theory: Demographic Stochasticity & Ecological Equivalence**

**Jacopo Grilli, Bengaluru 14/1/2025**

A week ago



## Statistical ecology

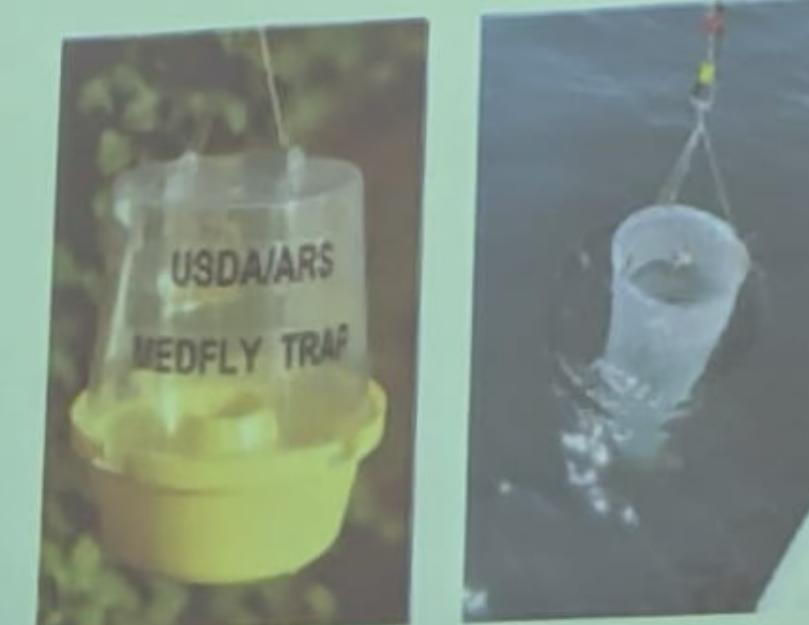
Predict species "fitness" (presence, abundance, reproduction, other measurements...) from environment & own traits

### Ecological data

#### Controlled studies



#### Natural observation



#### Data matrix

Species	Sample					Descriptor			
	a	b	c	d	e	I	II	III	IV
1									
2									
3						Abundance data			
4									
5									
6									
7									

Factor	Sample					Descriptor			
	X	Y	Z	W		I	II	III	IV
X									
Y									
Z						Environment data			
W									

Tends to be noisy and sparse

# Today and Tomorrow

		Sample				
		a	b	c	d	e
Species	1					
	2					
	3					Abundance data
	4					
	5					
	6					
	7					

Tends to be noisy and sparse

# Today

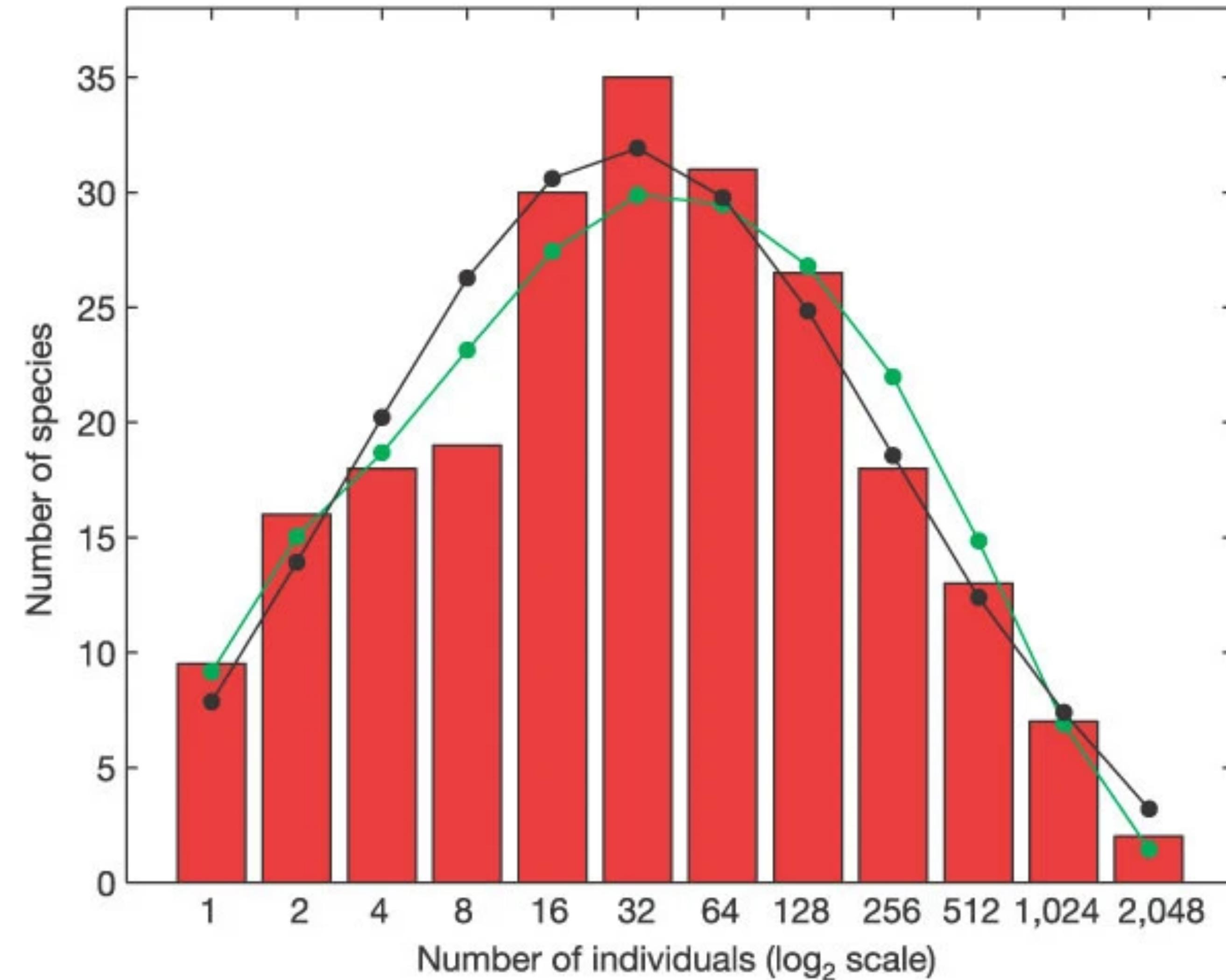
Species	a
1	
2	
3	Abs
4	
5	
6	
7	

# A very basic phenomenology

There are many different “things” (species/types)

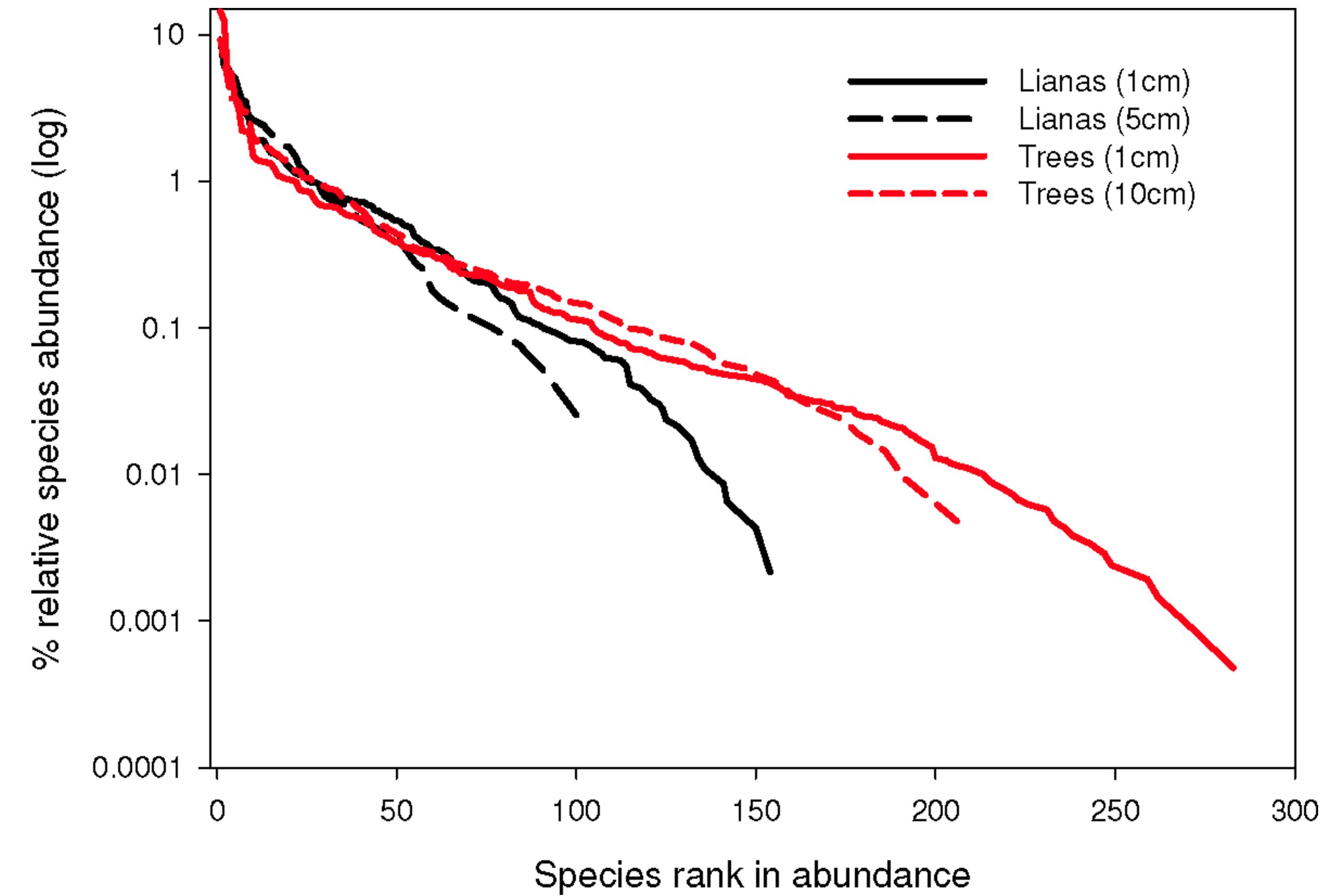
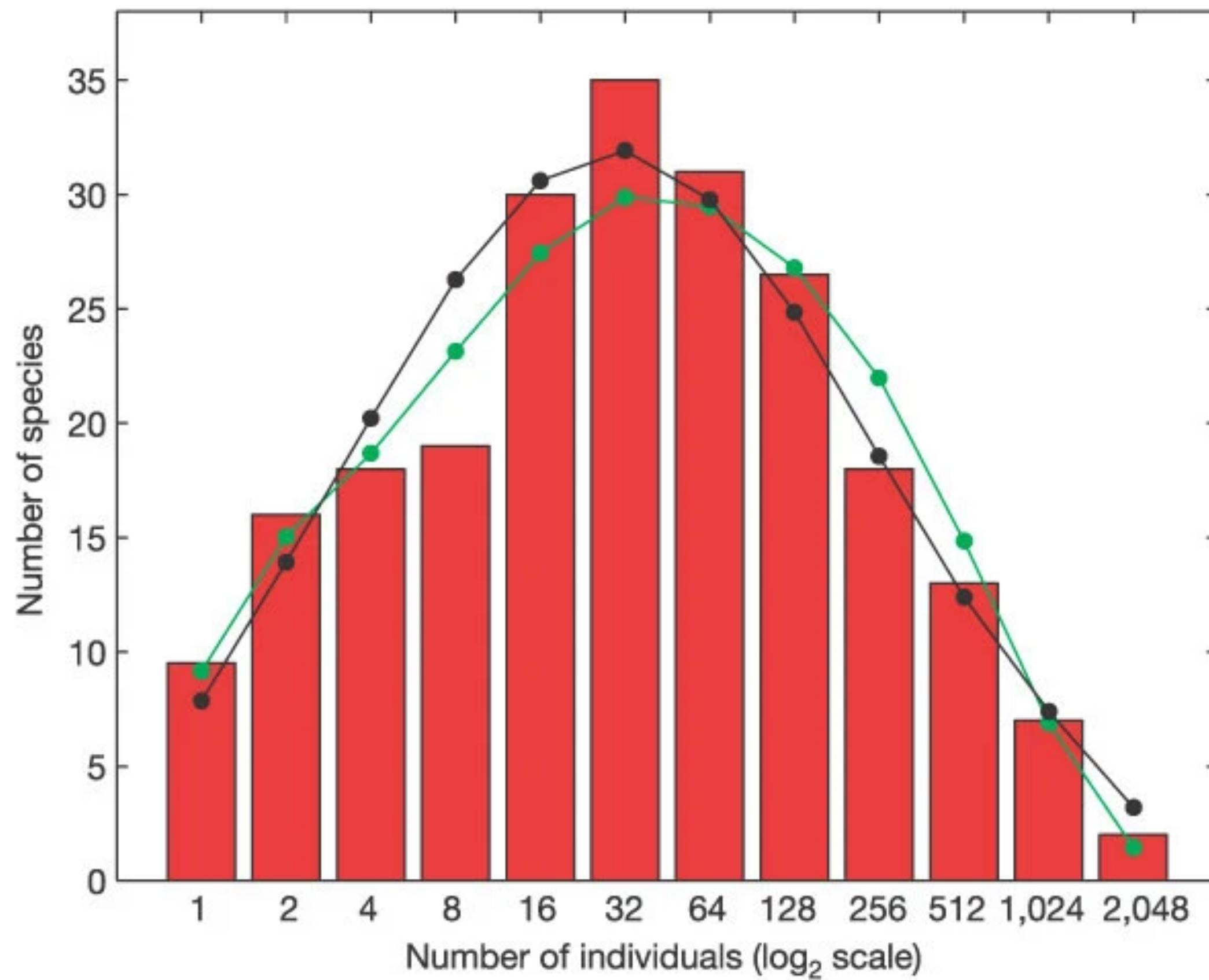
There are “common” and “rare” species

# Making the observation more quantitative

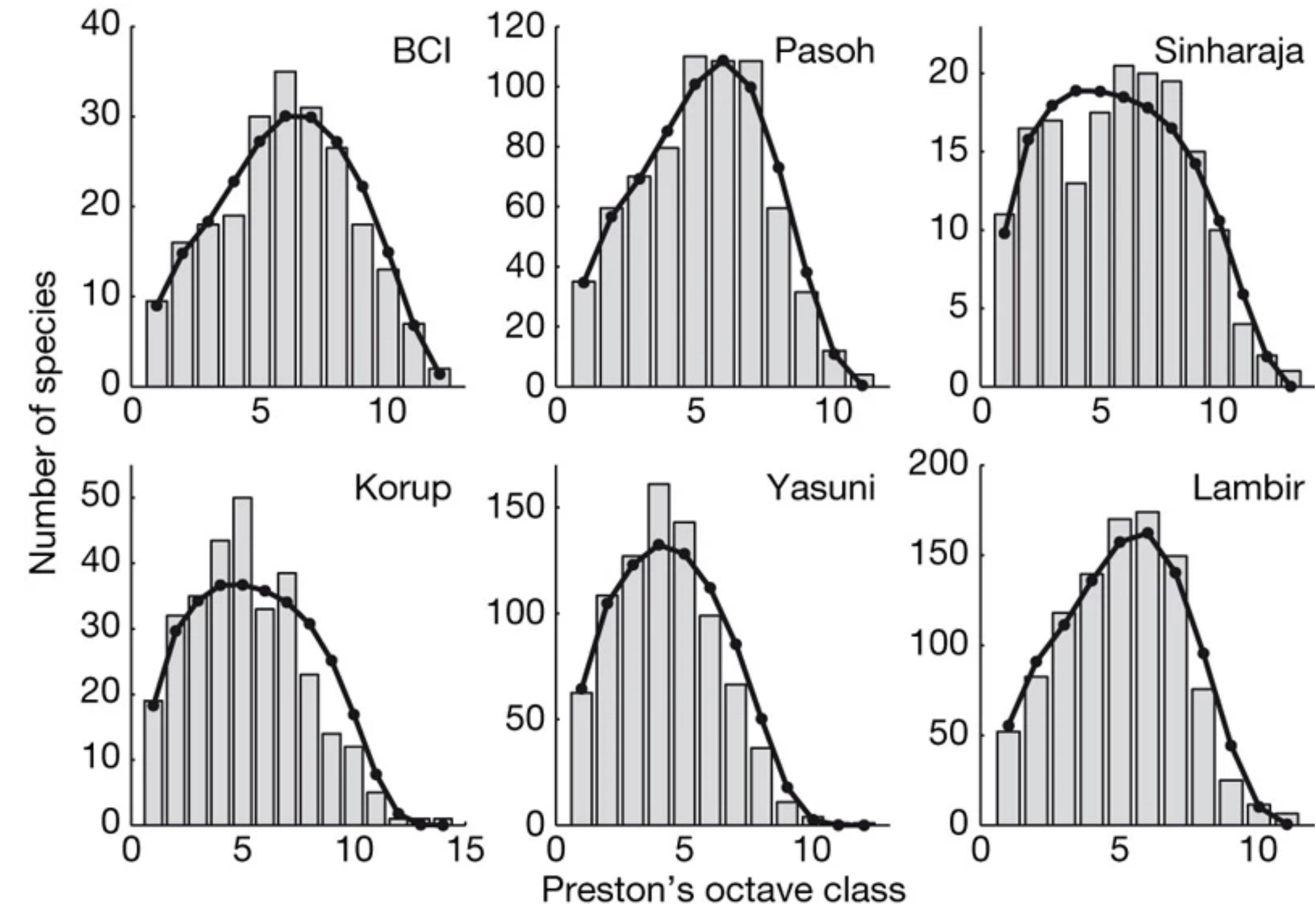


[Volkov et al., 2003]

# Same observation in a different form

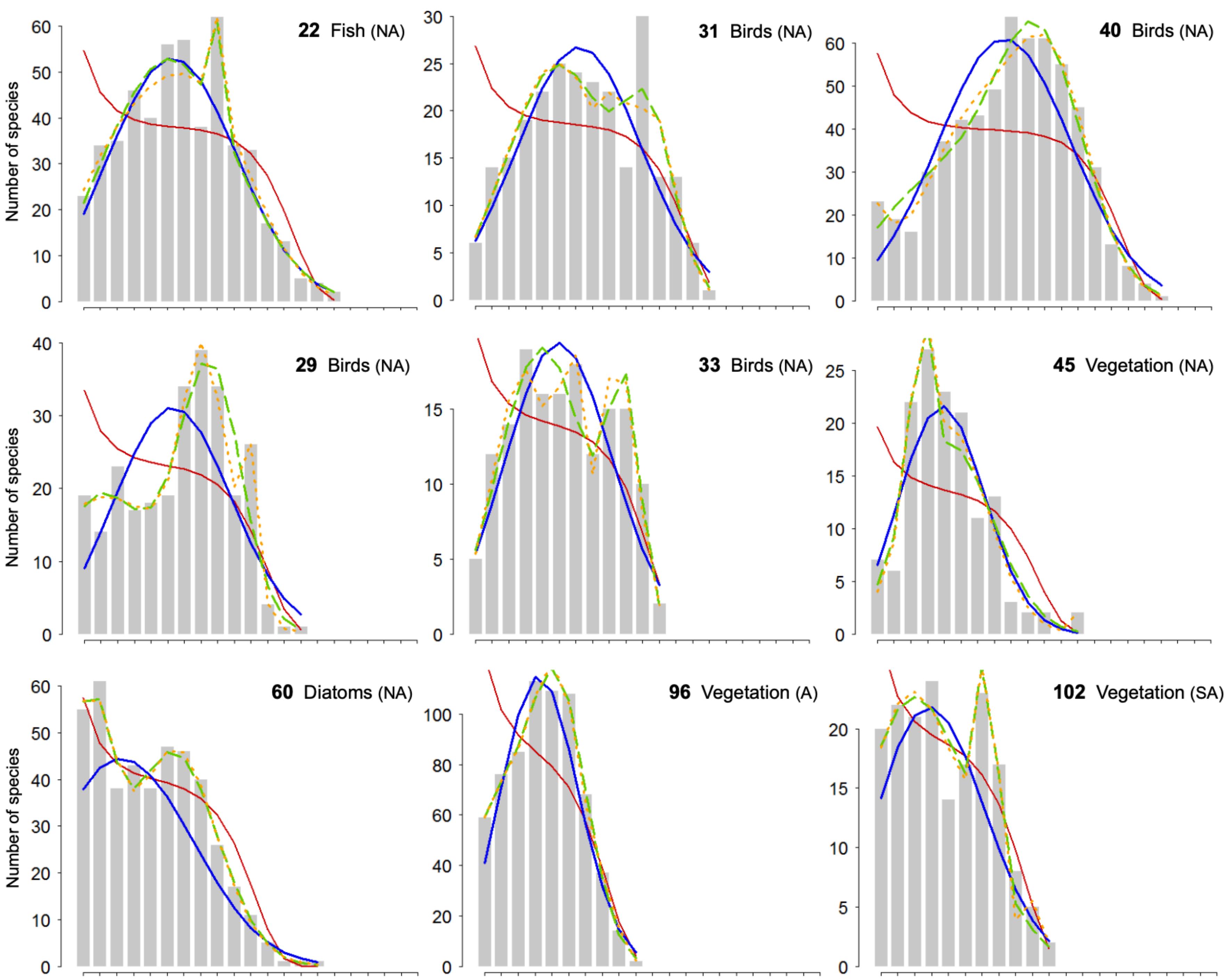


# Across tropical forests



[Volkov et al., 2007]

# not just trees

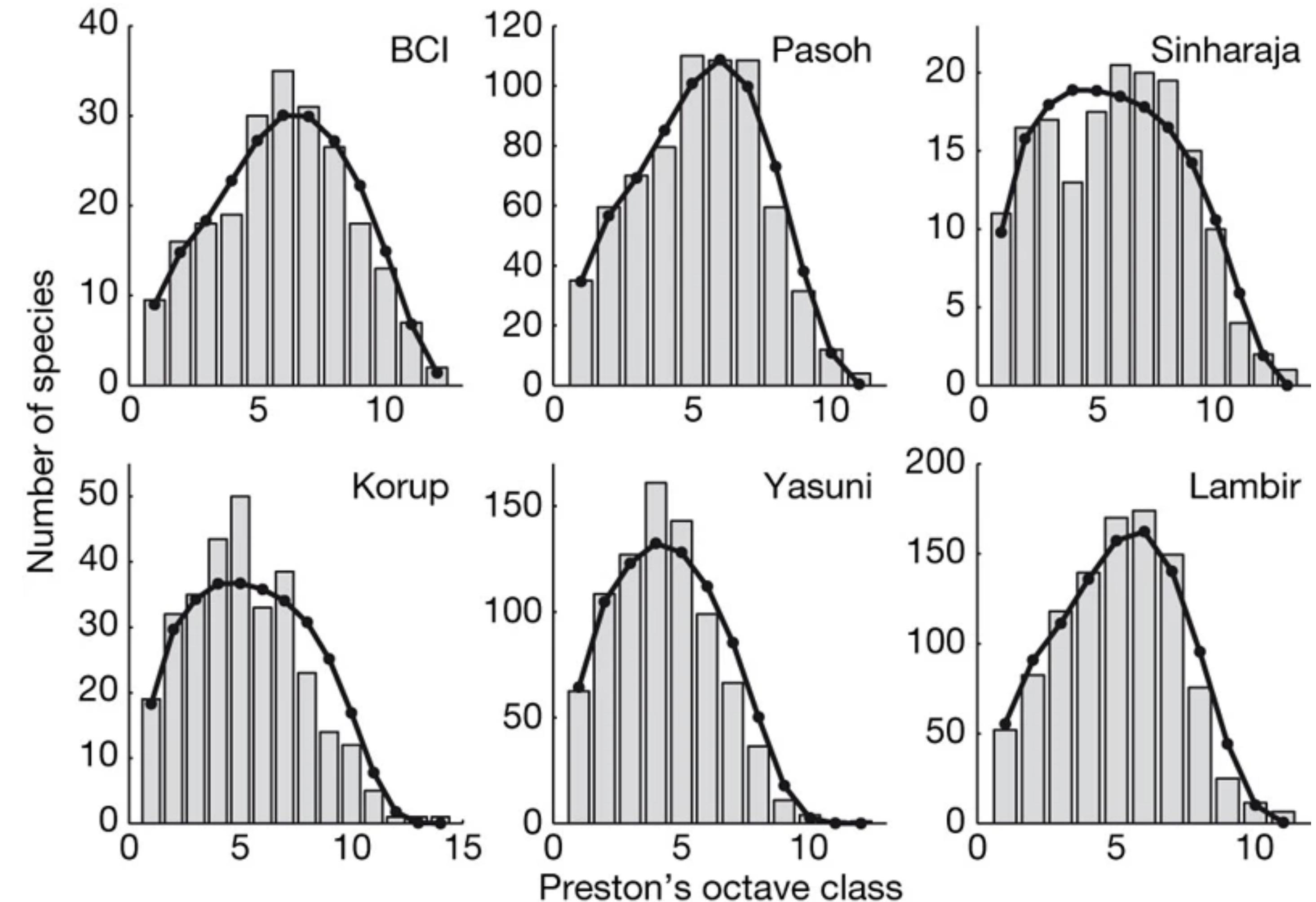


**What we should expect “by chance”?**  
**what is a minimal model?**

<- board

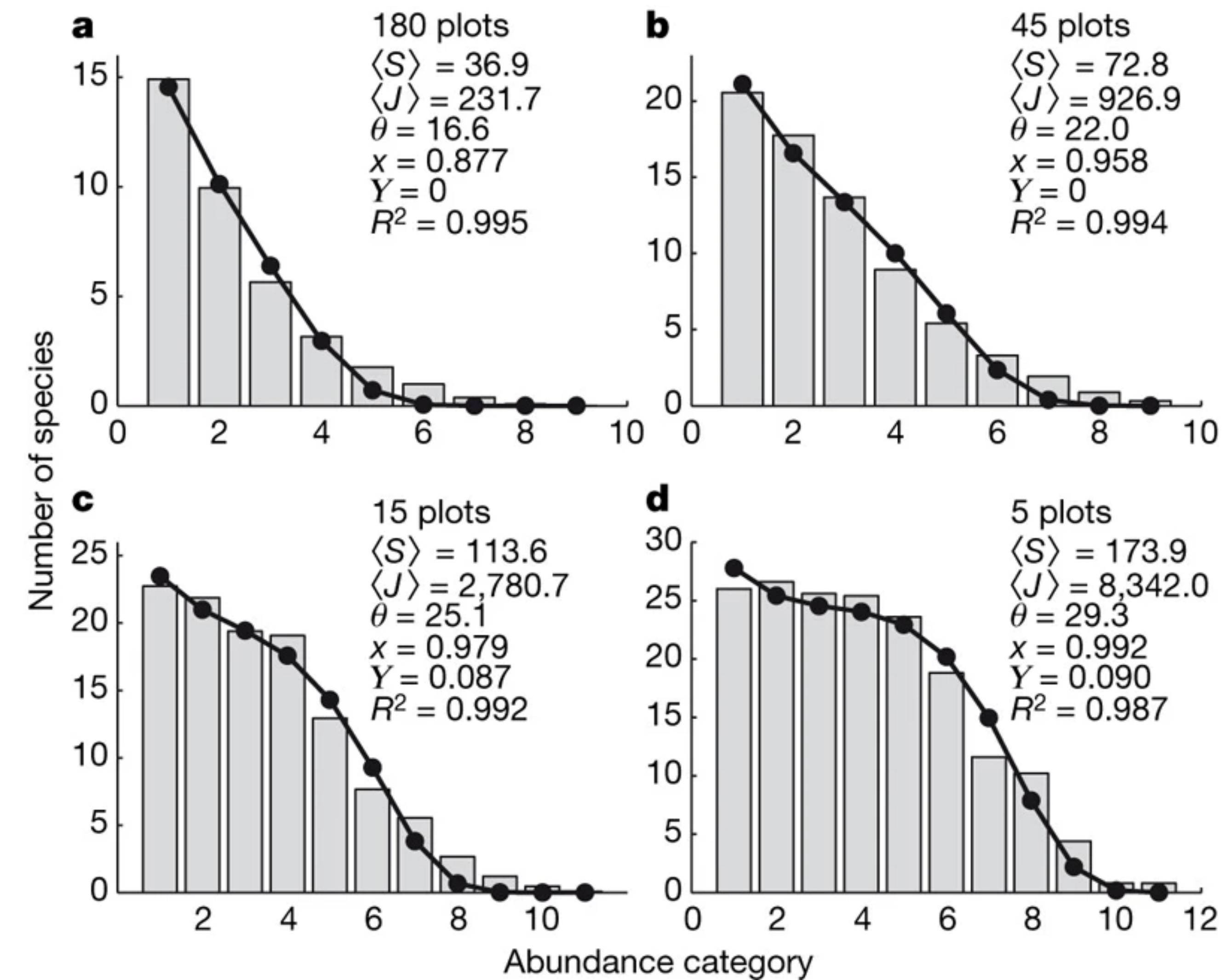
# NT reproduces species abundance distributions

tropical forests



# NT reproduces species abundance distributions

coral  
reefs



# **What else can you do with neutral theory?**

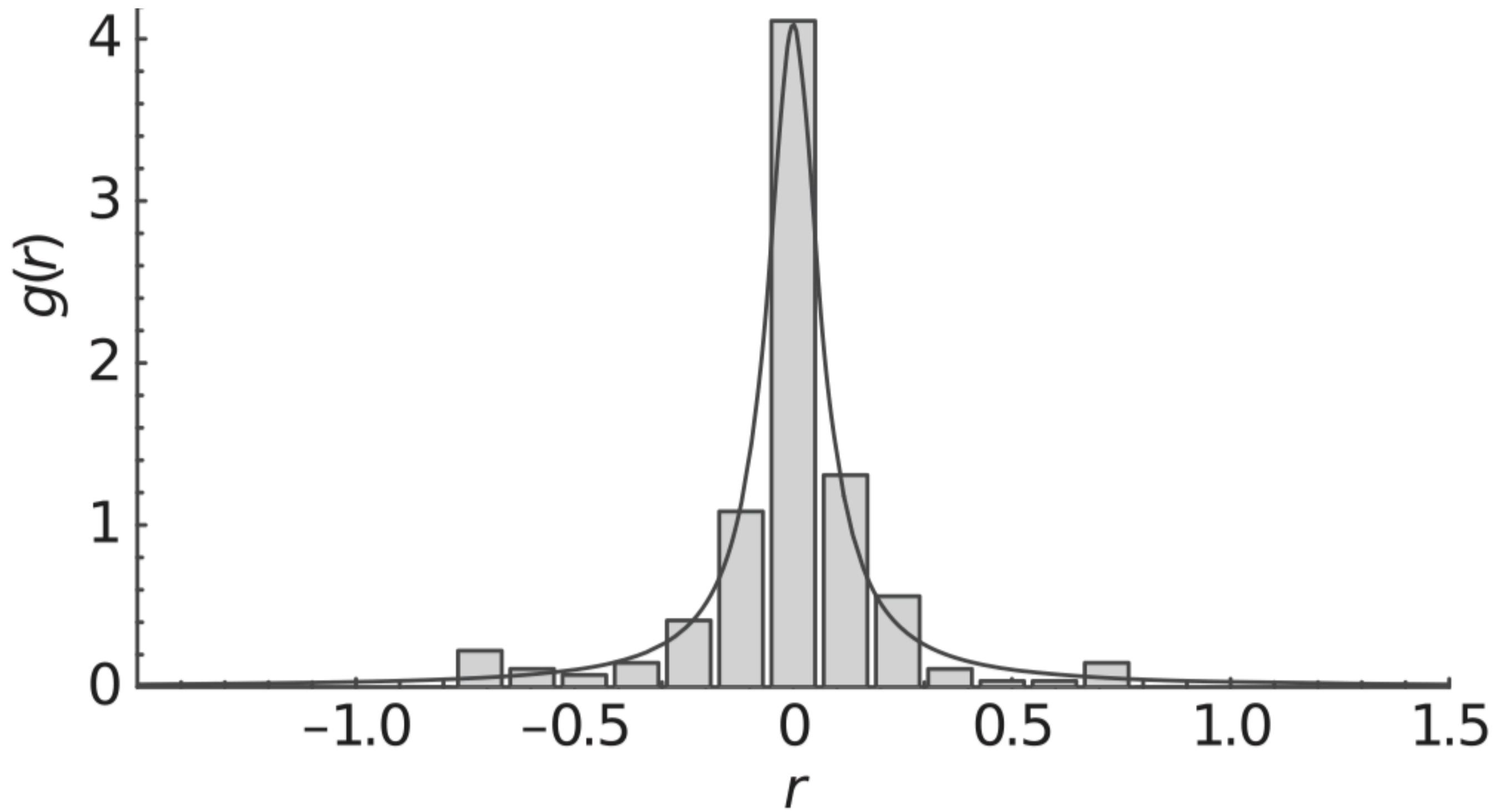
# Dynamics

$$\mathcal{P}(\lambda, t) = \langle \delta(\lambda - x/x_0) \rangle$$

$$= \int_0^\infty dx_0 \int_0^\infty dx P(x, t|x_0, 0) P_0(x_0) \delta(\lambda - x/x_0)$$

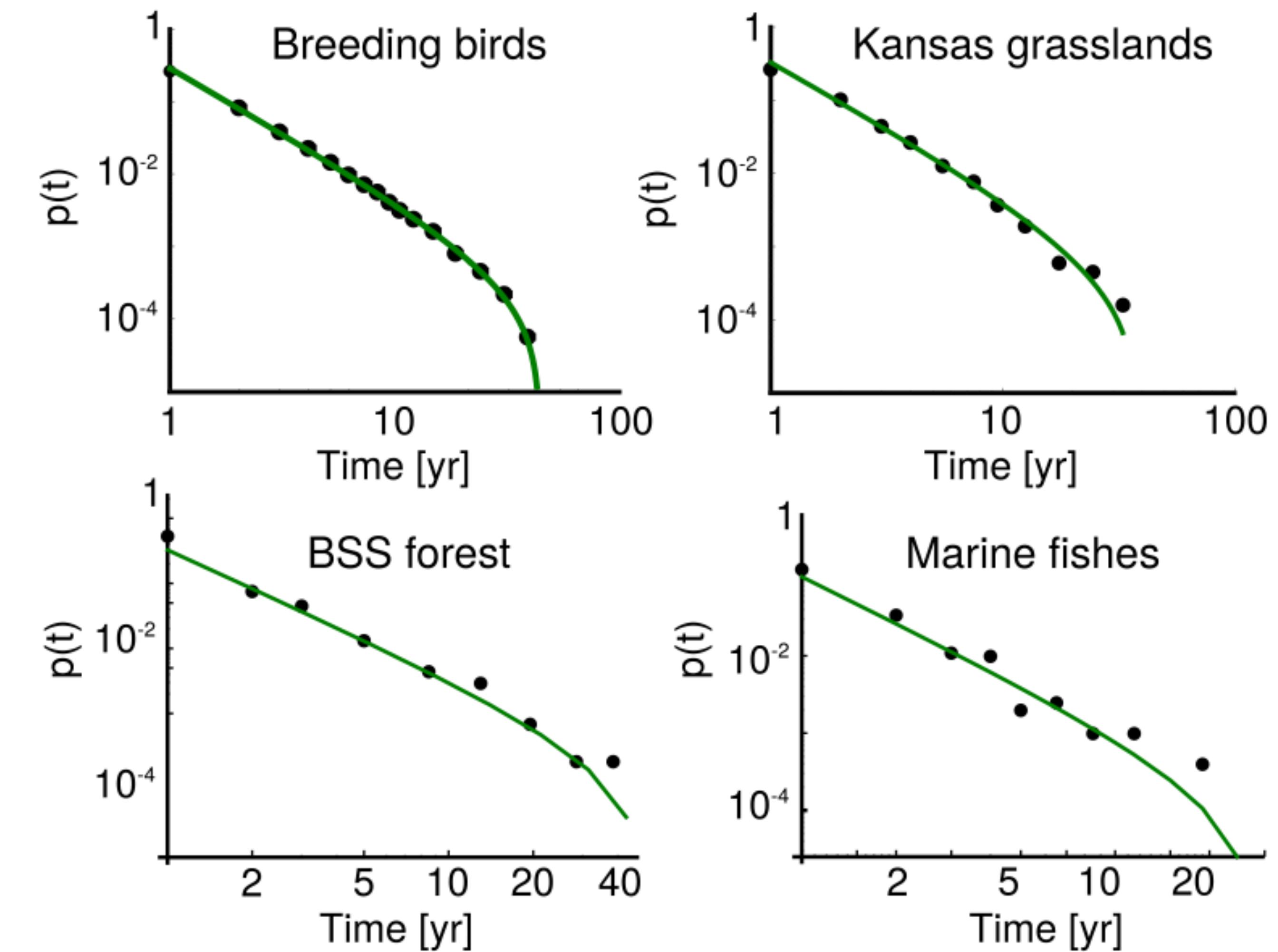
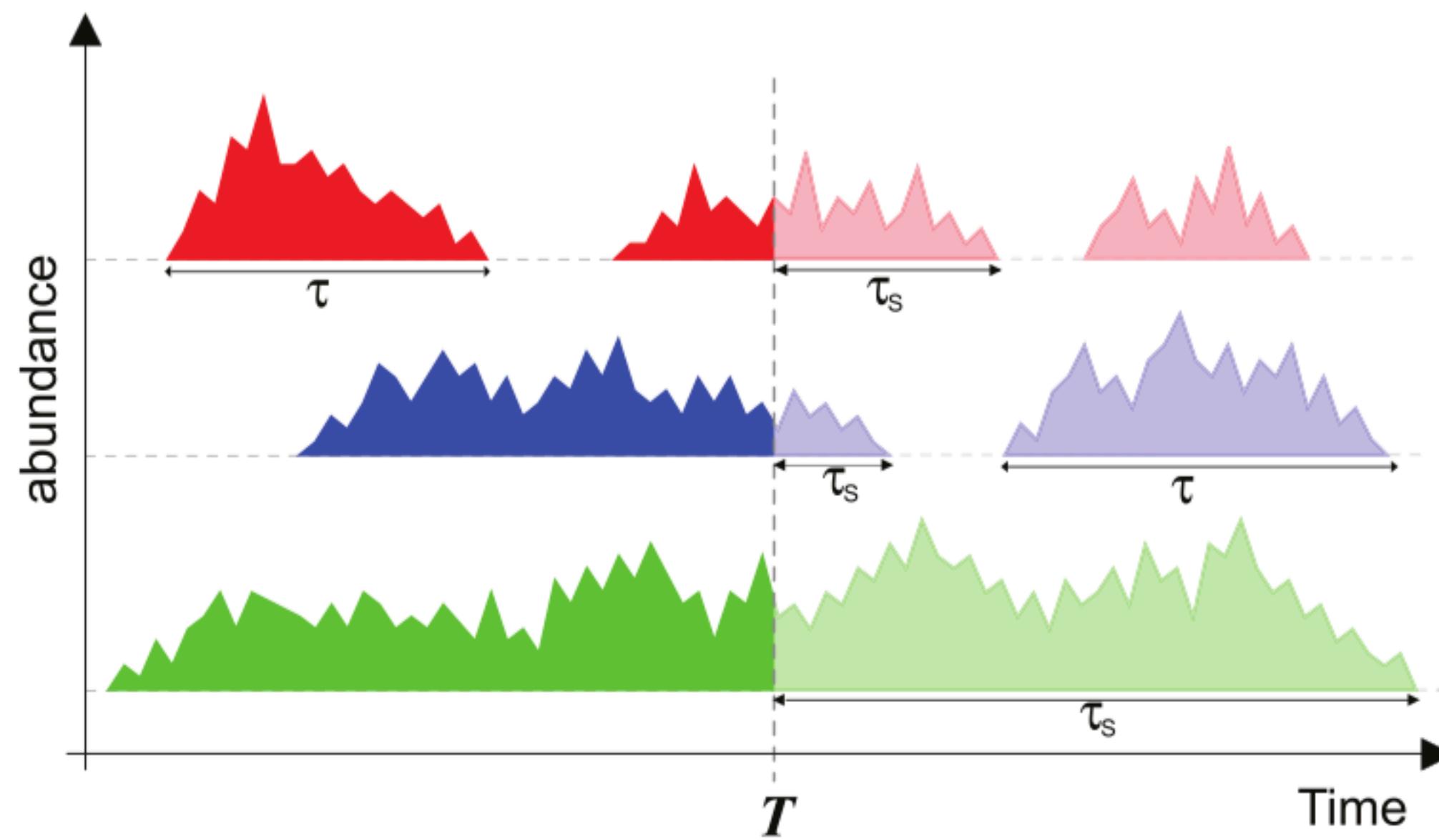
$$r = \log \lambda$$

$$g(r) = e^r P(e^r, t)$$



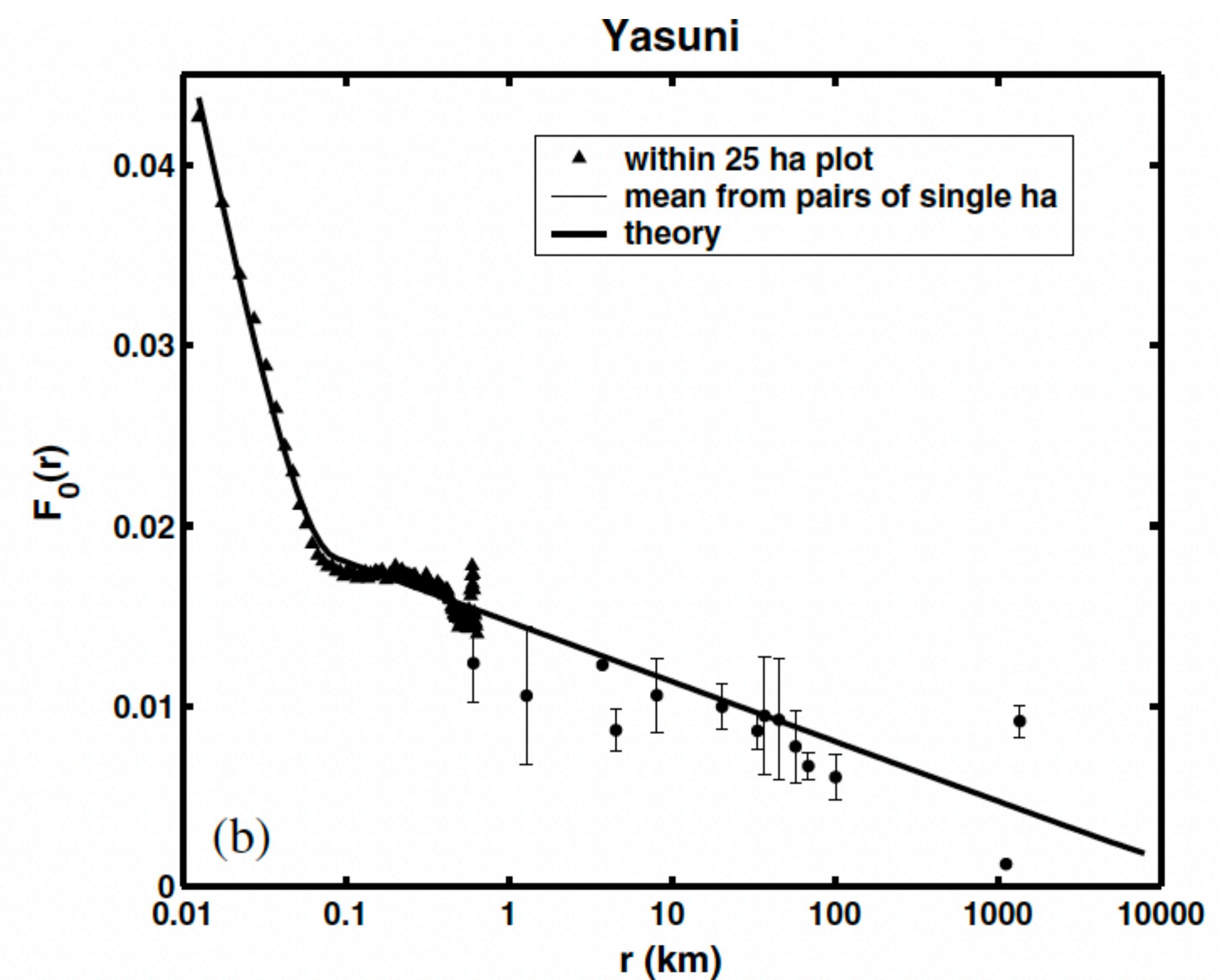
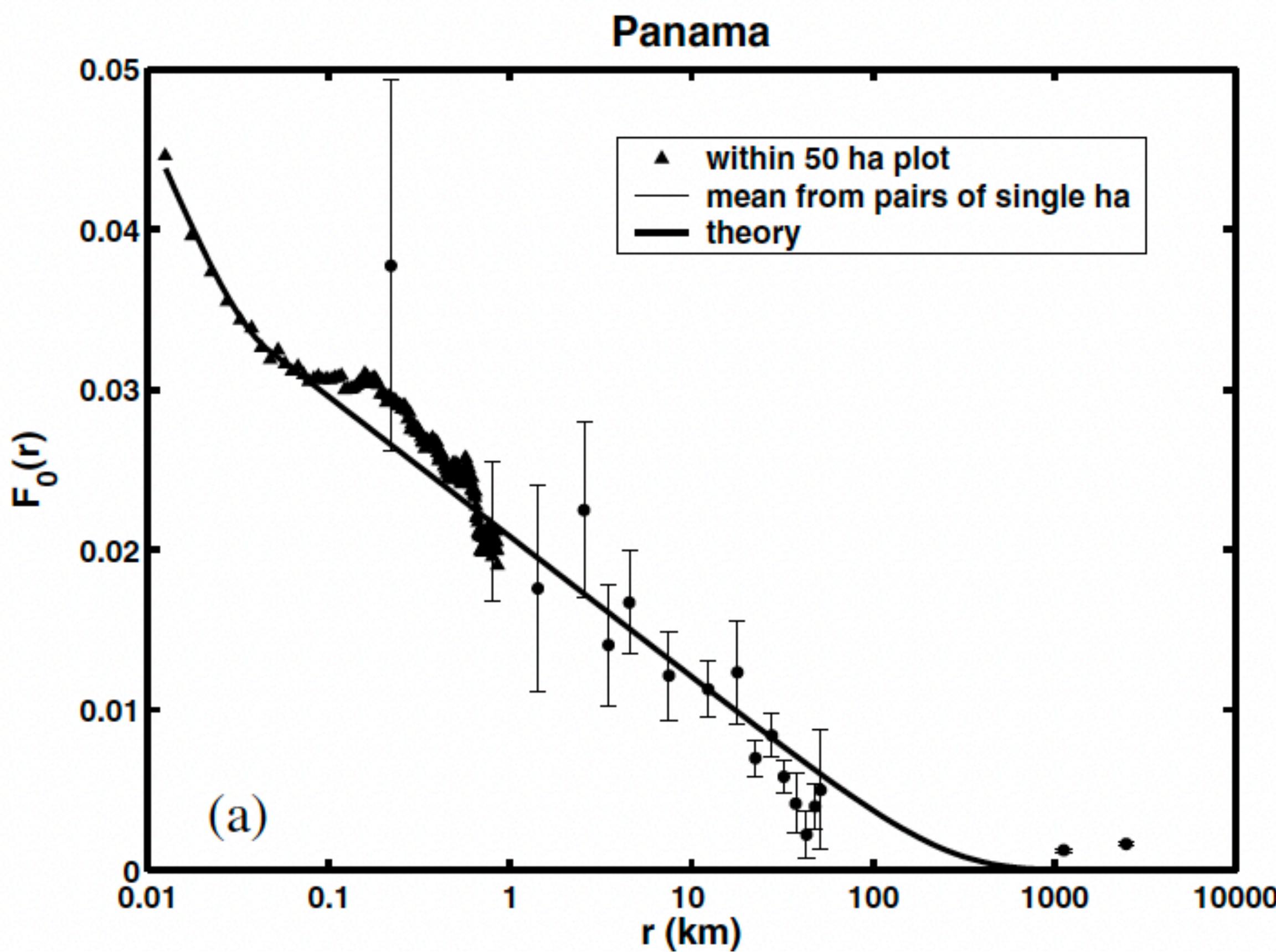
[Azaele et al., 2006]

# Dynamics



# Space

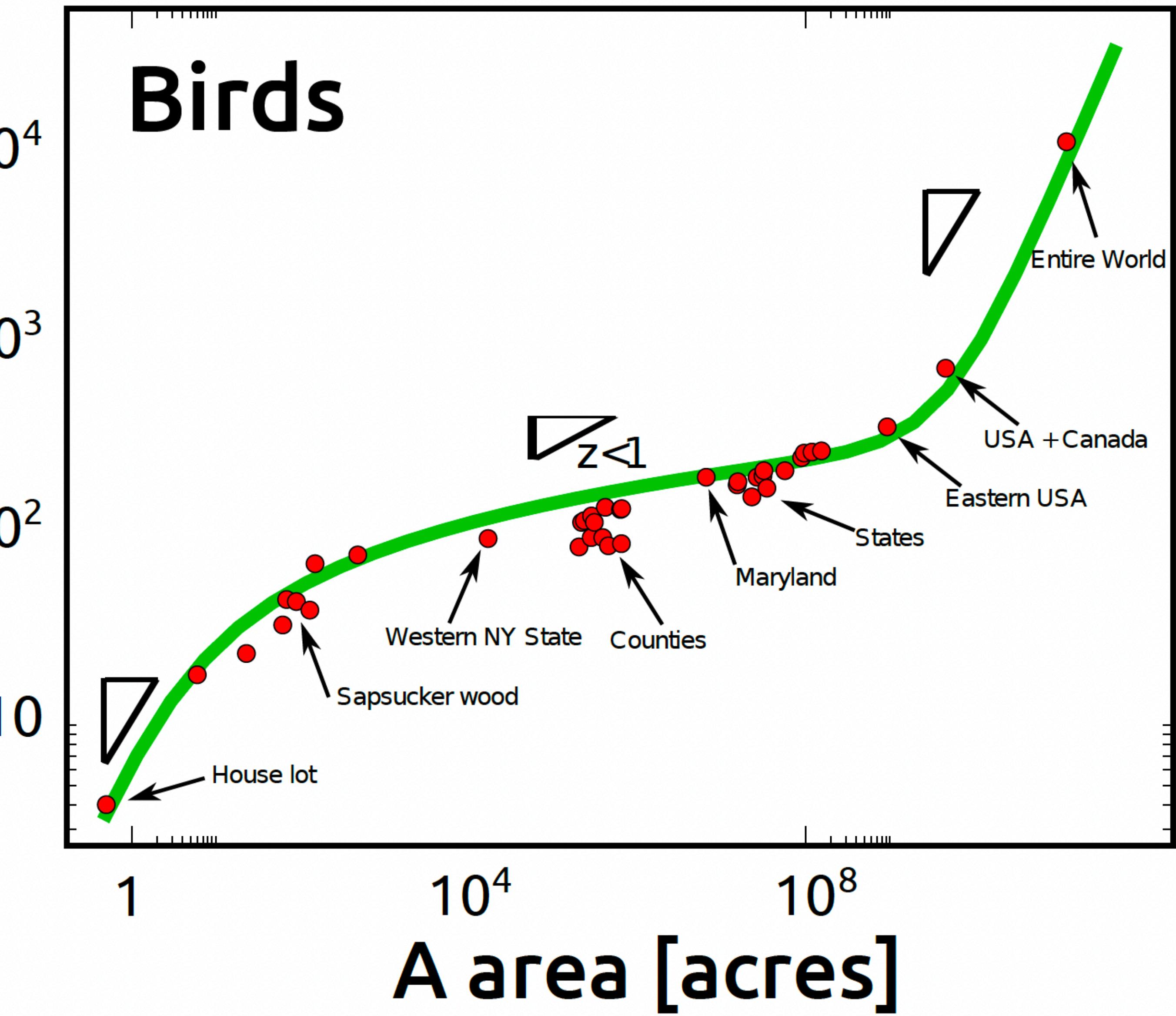
Probability that two random individuals are conspecific



# Space

Species Area Relationship

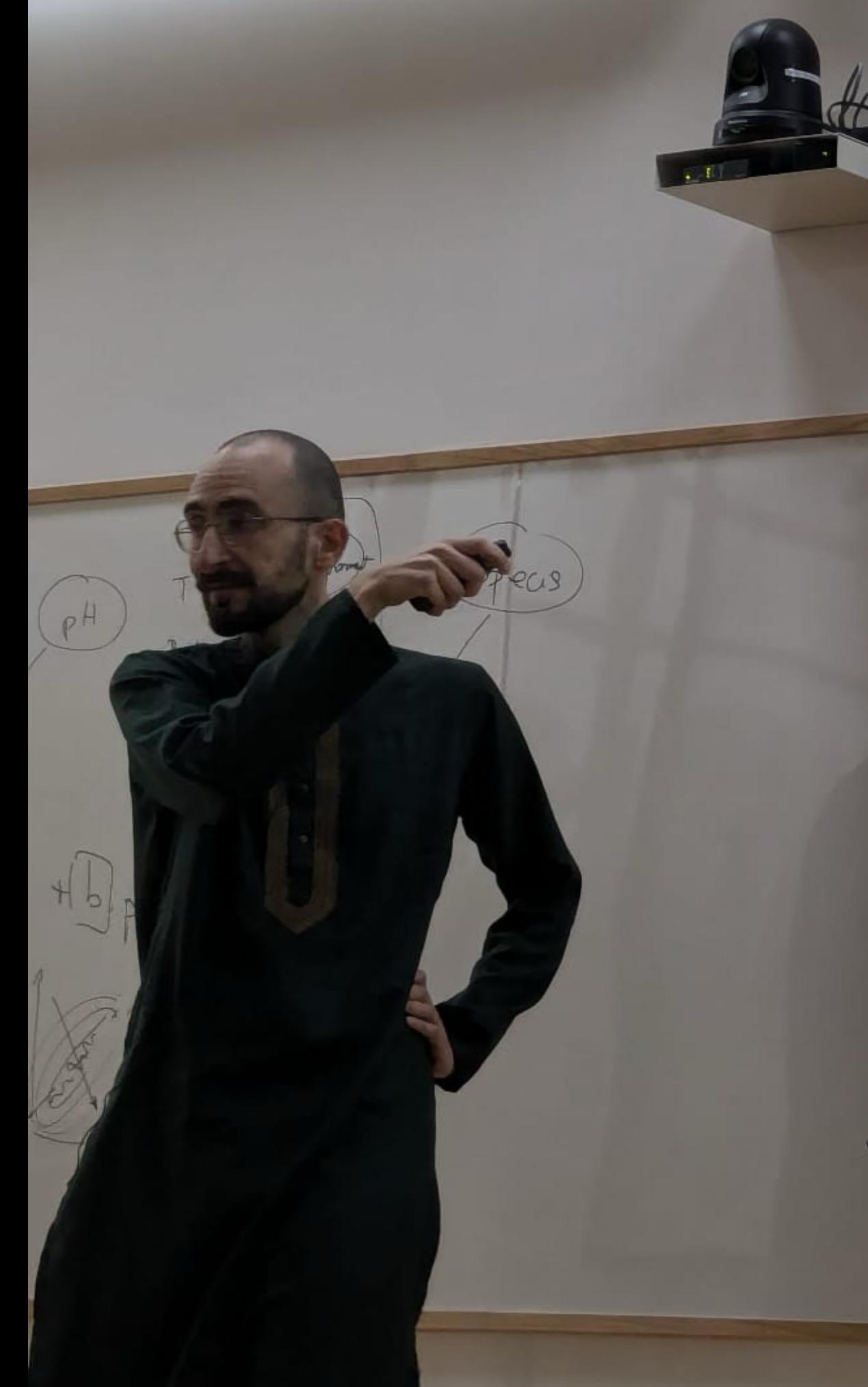
Number of species



[Grilli et al., 2012]

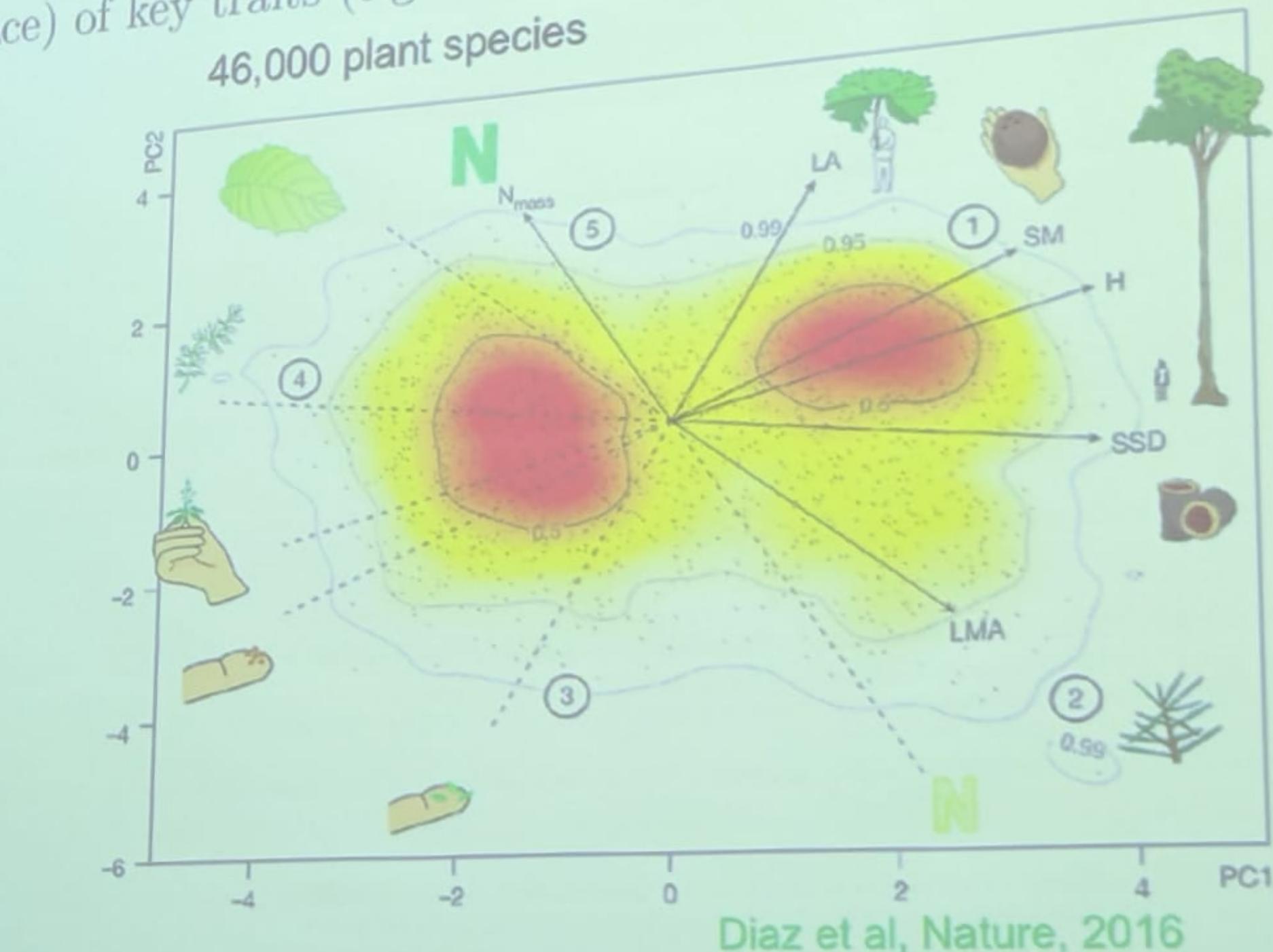
# **How neutral theory fails**

# Species are very different

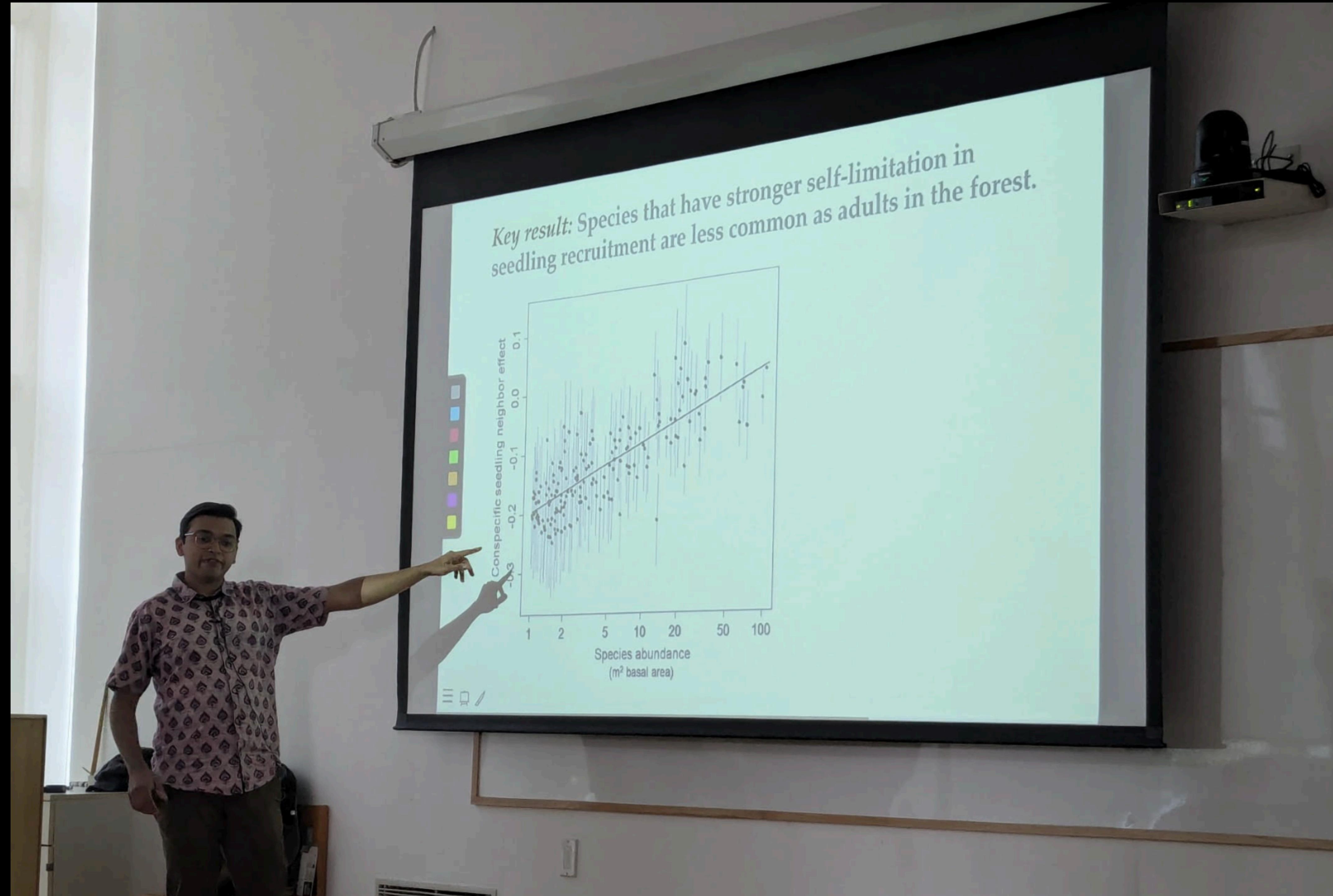


## Low-dim tradeoff surfaces

Like for environments, in each class of organisms, few axes (low-dimensional surfaces) of key traits (e.g. for plants: leaf and seed features)  
46,000 plant species



# Species differences play a role



# Timescales

Speciation as source of diversity

How “old” is a species with a given relative abundance  $x$ ?

$$a(x) = -2N \frac{x}{1-x} \log x$$

[Kimura 1983]

Amazon rainforest

Total number of trees:  $N \sim 10^{11}$

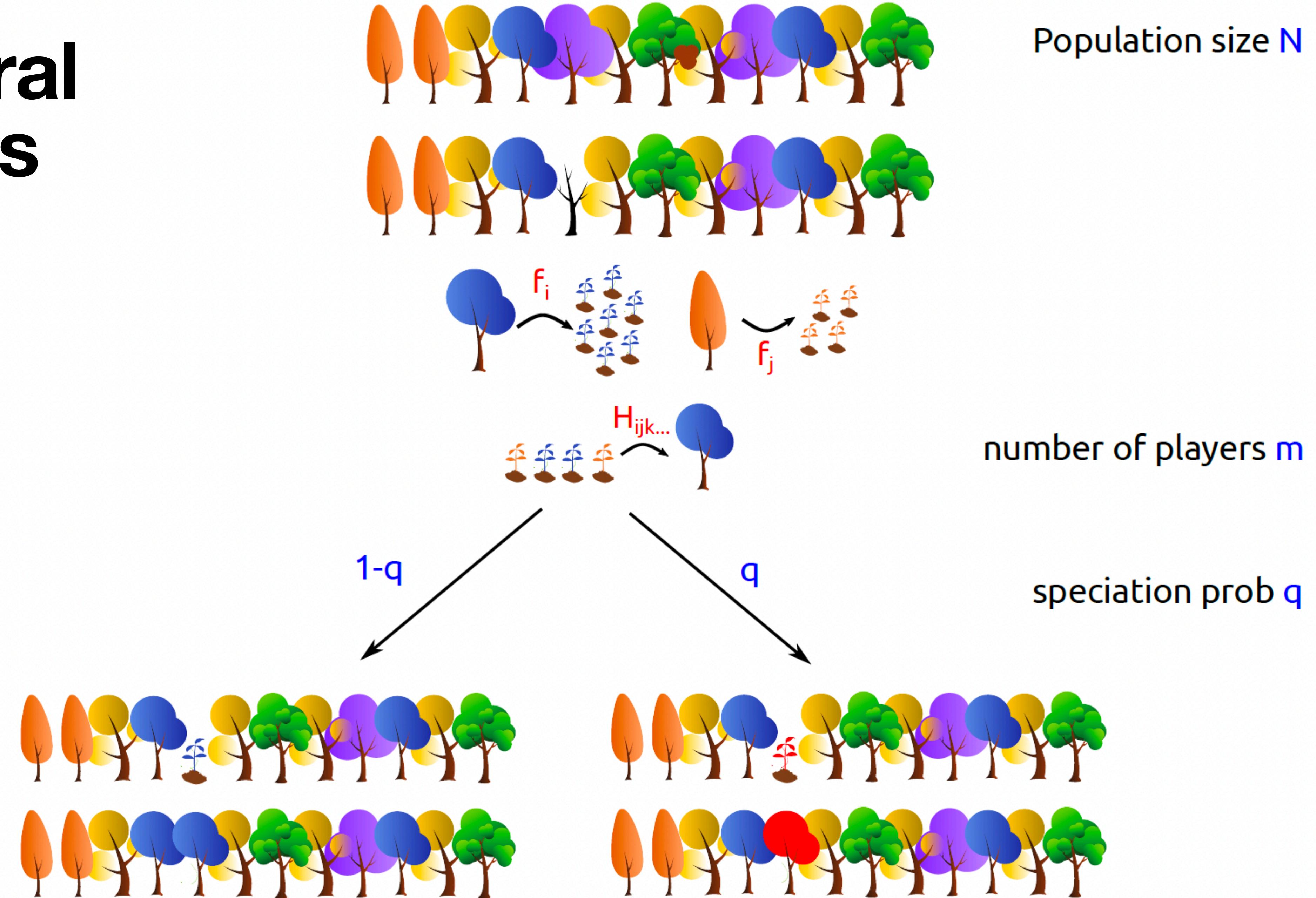
Most abundant species tree:  $x \sim 10^{-2}$

Generation time of trees:  $\sim 30$  years

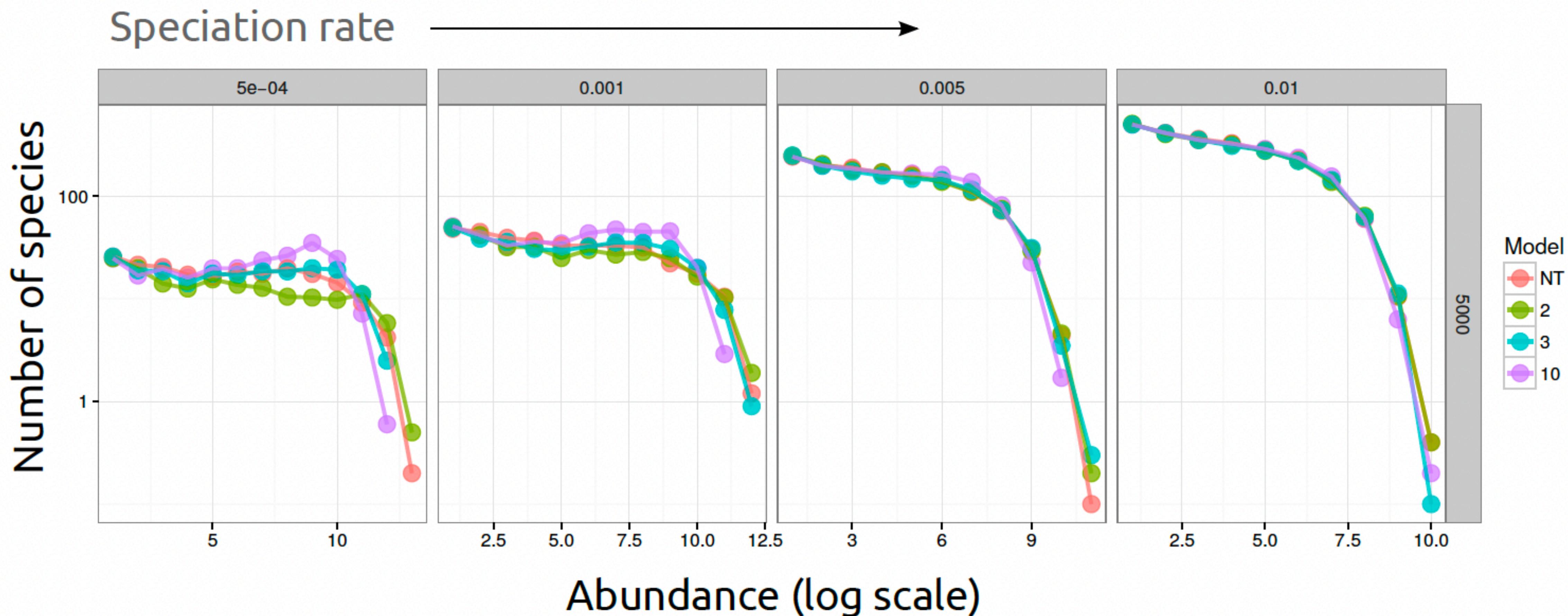
Age of the most abundant species:  $\sim 10^{11}$  years

Age of the universe:  $\sim 10^{10}$  years , First tree:  $\sim 10^8$  years ago

# Non-neutral extensions



# Species Abundance Distribution is insensitive to interactions



# Time to extinction is sensitive to neutrality

