

Executed Command

Reference: pipelines/PIPELINE\_RUN\_GUIDE.md

Script: pipelines/compare\_hardcoded\_vs\_qiskit\_pipeline.py

```
/opt/anaconda3/bin/python3 pipelines/compare_hardcoded_vs_qiskit_pipeline.py --l-values 2 --with-per-l-pdfs  
--initial-state-source vqe --num-times 401 --trotter-steps 256 --hardcoded-vqe-reps 2 --hardcoded-vqe-  
restarts 5 --hardcoded-vqe-maxiter 1800 --qiskit-vqe-reps 2 --qiskit-vqe-restarts 5 --qiskit-vqe-maxiter  
1800 --skip-qpe
```

## L=2 Run Settings & Metrics Summary

L=2 t=1.0 u=4.0 dv=0.0 boundary=periodic ordering=blocked initial\_state\_source=vqe t\_final=20.0 num\_times=401 suz

thresholds:

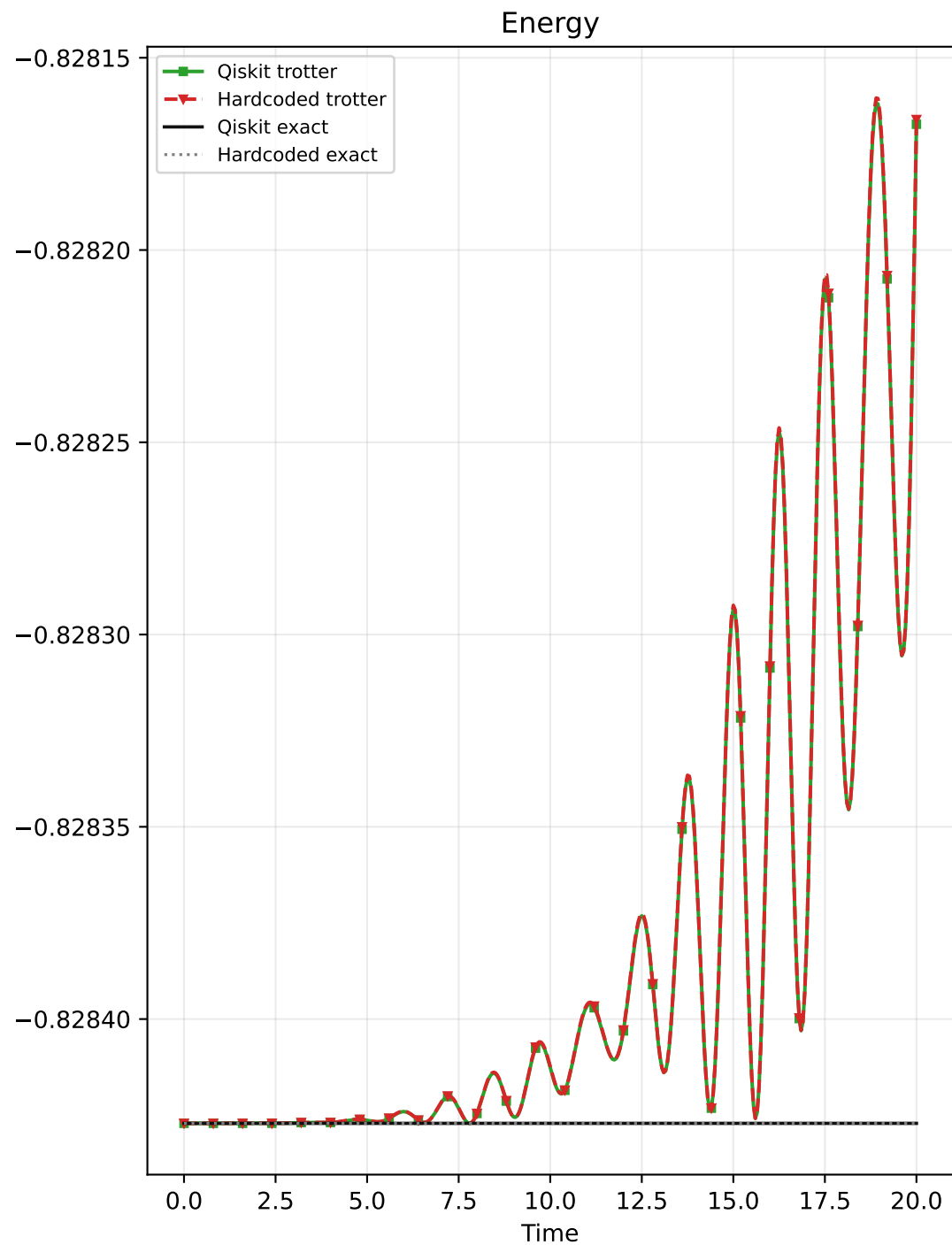
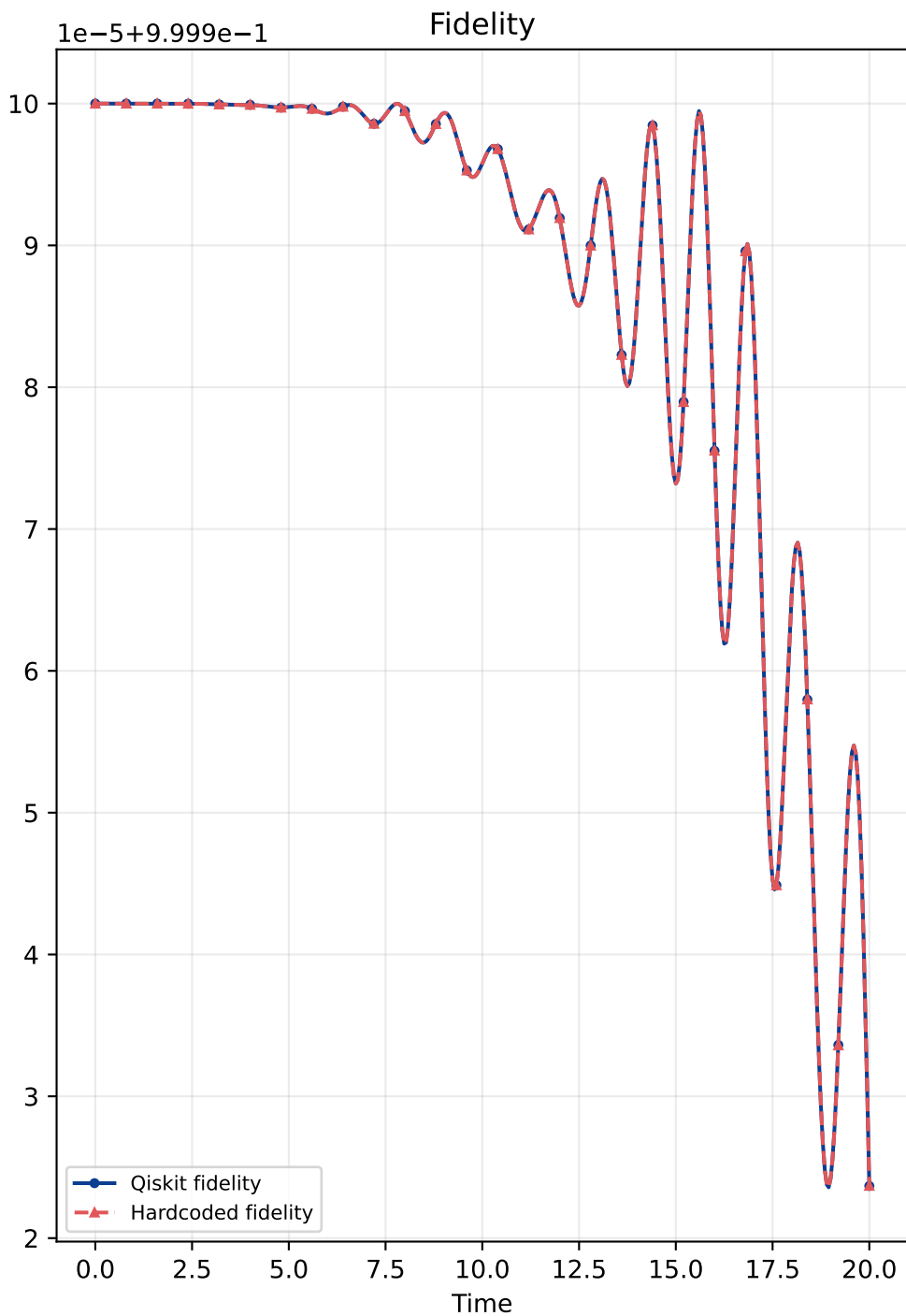
doublon\_trotter\_max\_abs\_delta: 1.00e-03  
energy\_trotter\_max\_abs\_delta: 1.00e-03  
fidelity\_max\_abs\_delta: 1.00e-04  
ground\_state\_energy\_abs\_delta: 1.00e-08  
n\_dn\_site0\_trotter\_max\_abs\_delta: 5.00e-03  
n\_up\_site0\_trotter\_max\_abs\_delta: 5.00e-03

max  $|\Delta|$ :

gs\_energy: 0.00e+00  
doublon\_trotter: 4.84e-07  
energy\_trotter: 1.40e-06  
fidelity: 2.26e-08  
n\_dn\_site0\_trotter: 2.79e-05  
n\_up\_site0\_trotter: 2.78e-05

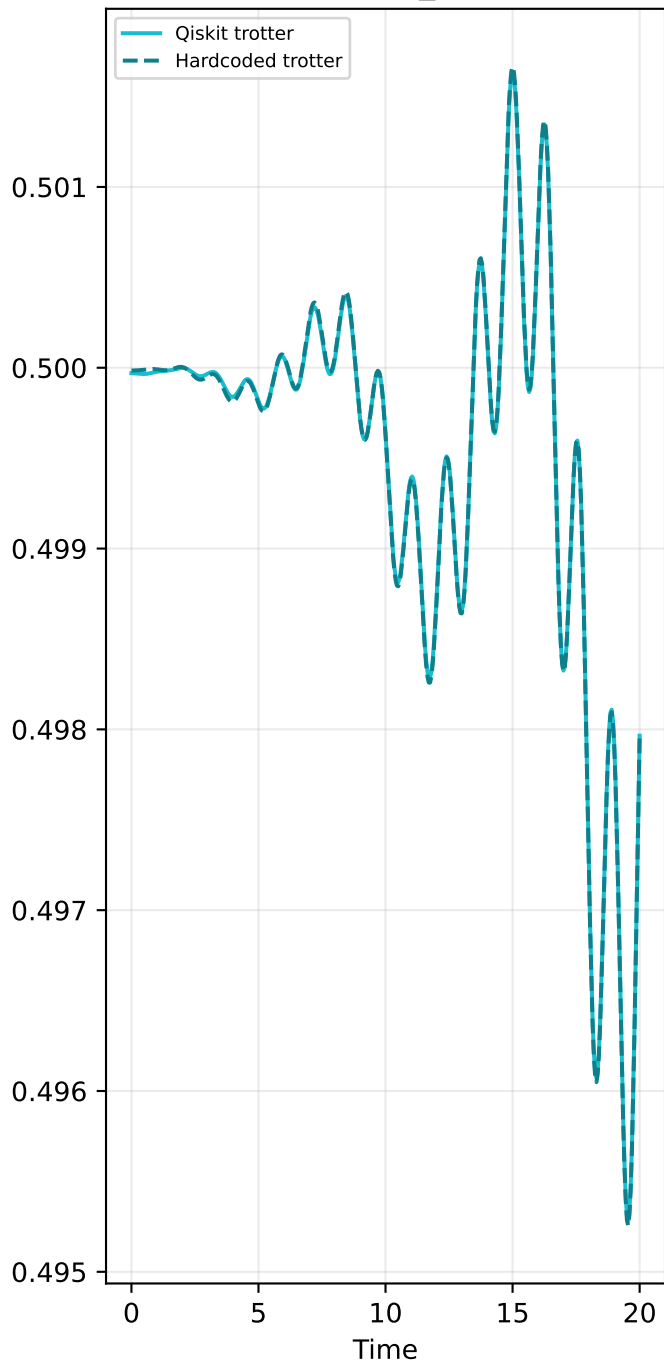
result: PASS

# Pipeline Comparison L=2: Hardcoded vs Qiskit (Fidelity & Energy)

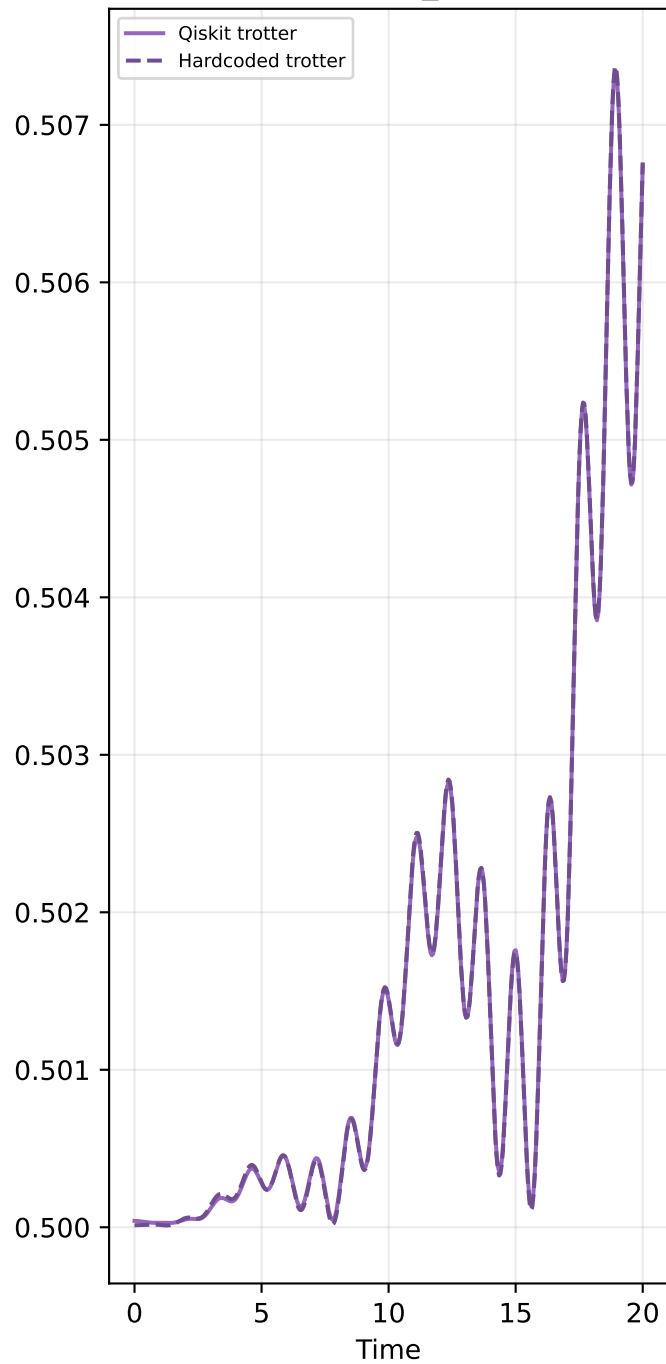


# Pipeline Comparison L=2: Occupations & Doublon (auto-zoomed)

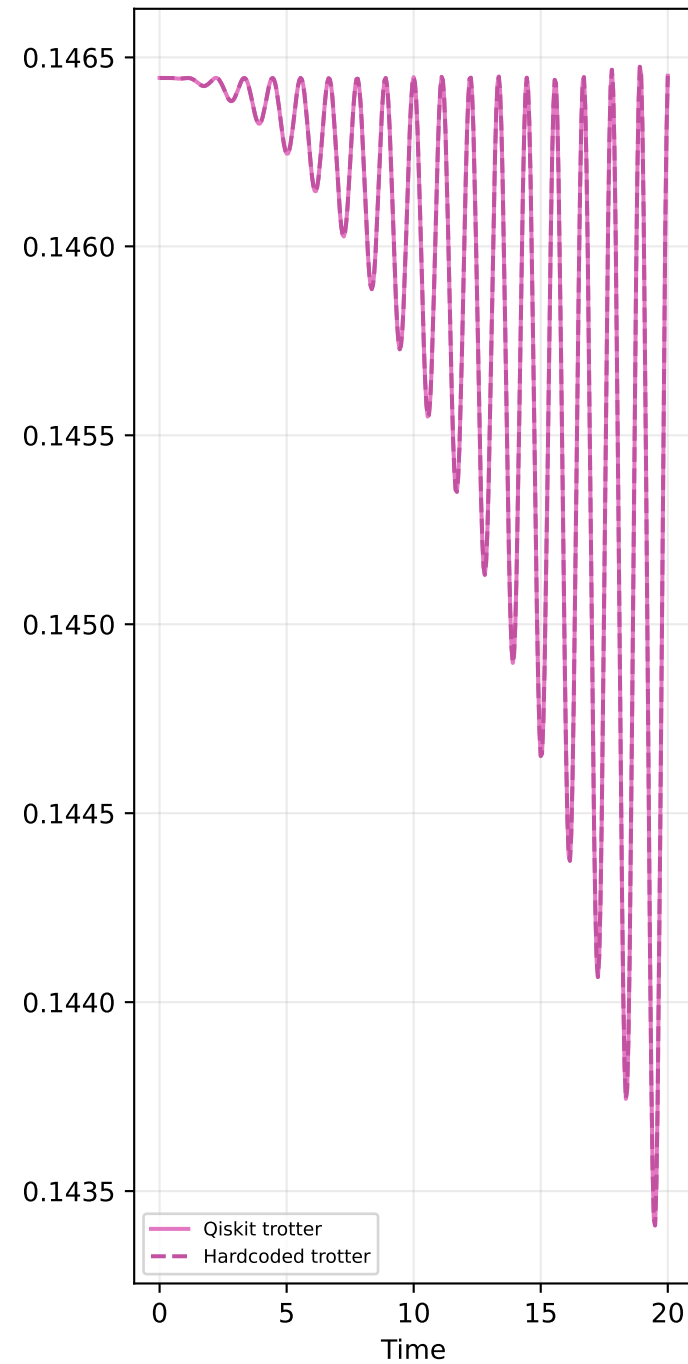
## Site-0 $n_{up}$



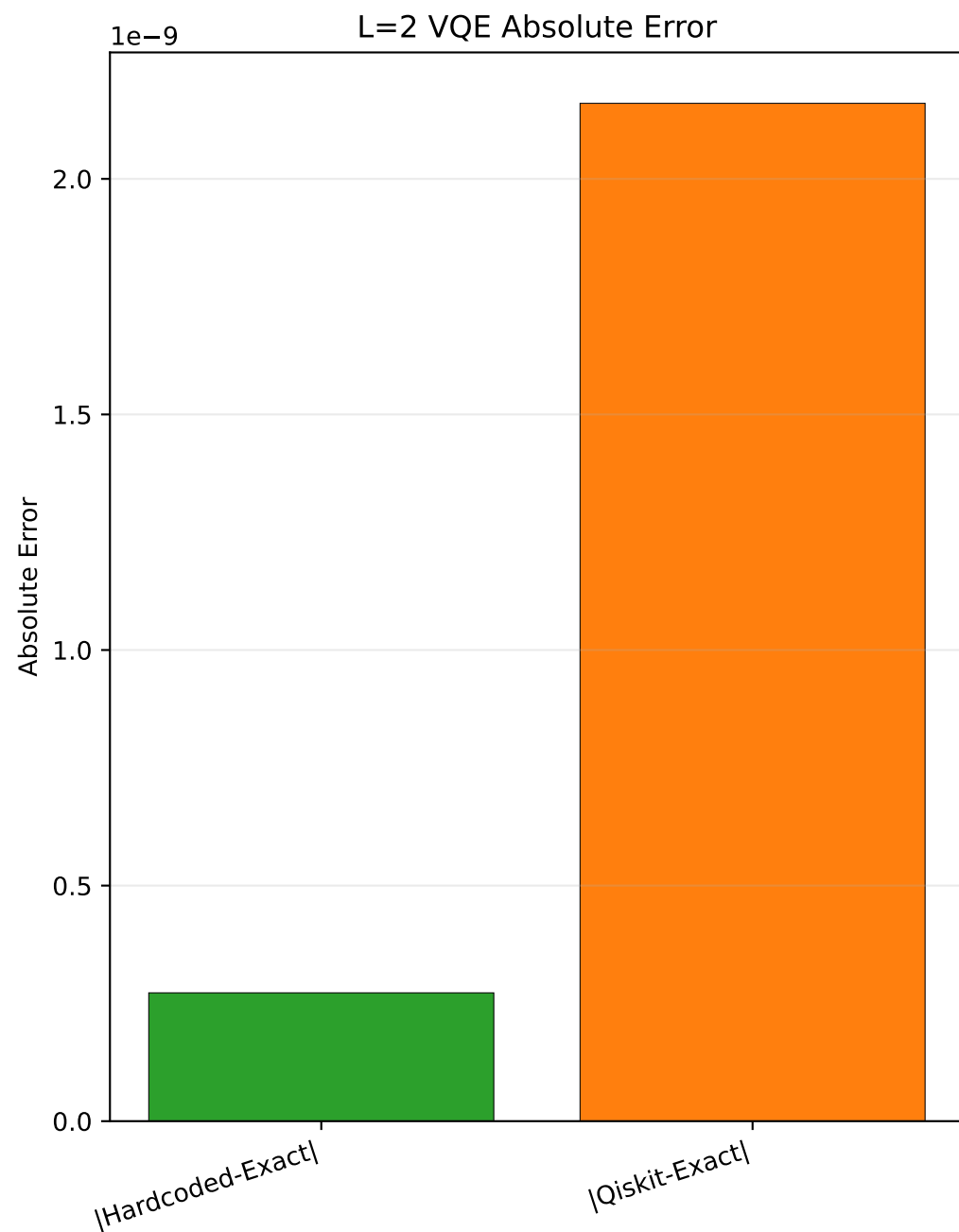
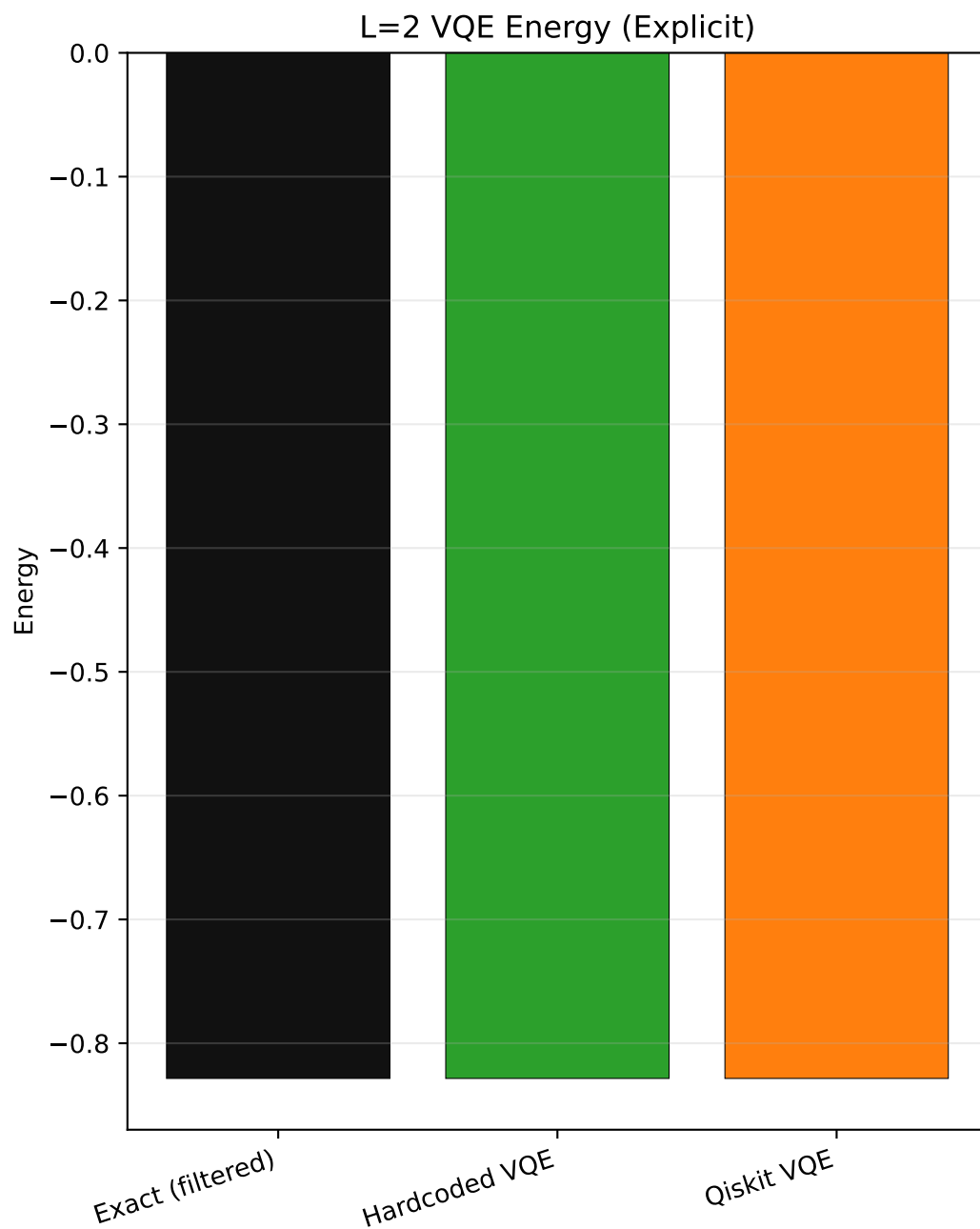
## Site-0 $n_{dn}$



## Doublon

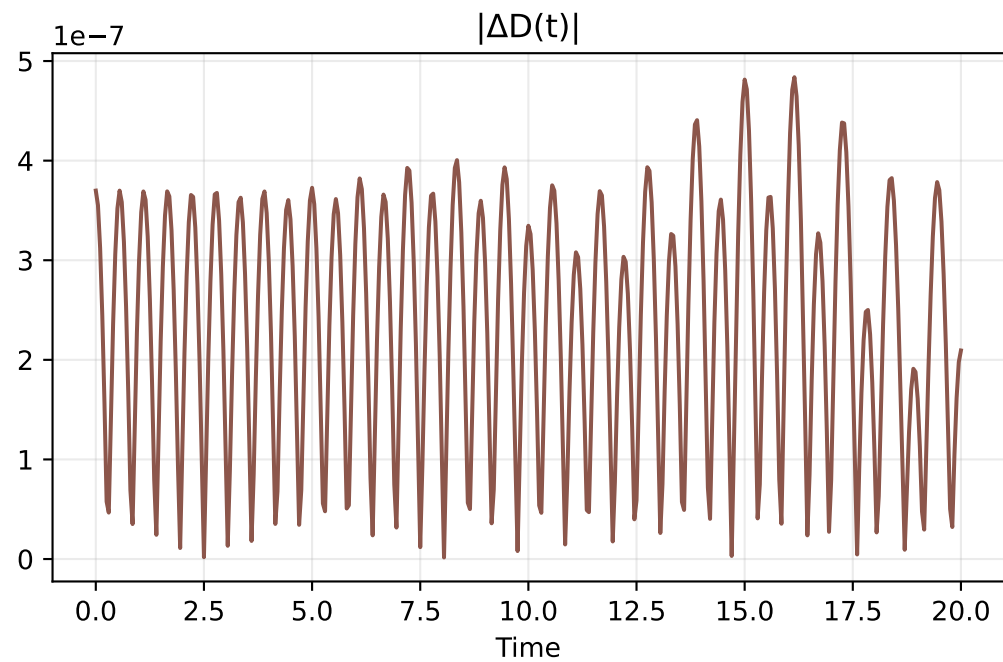
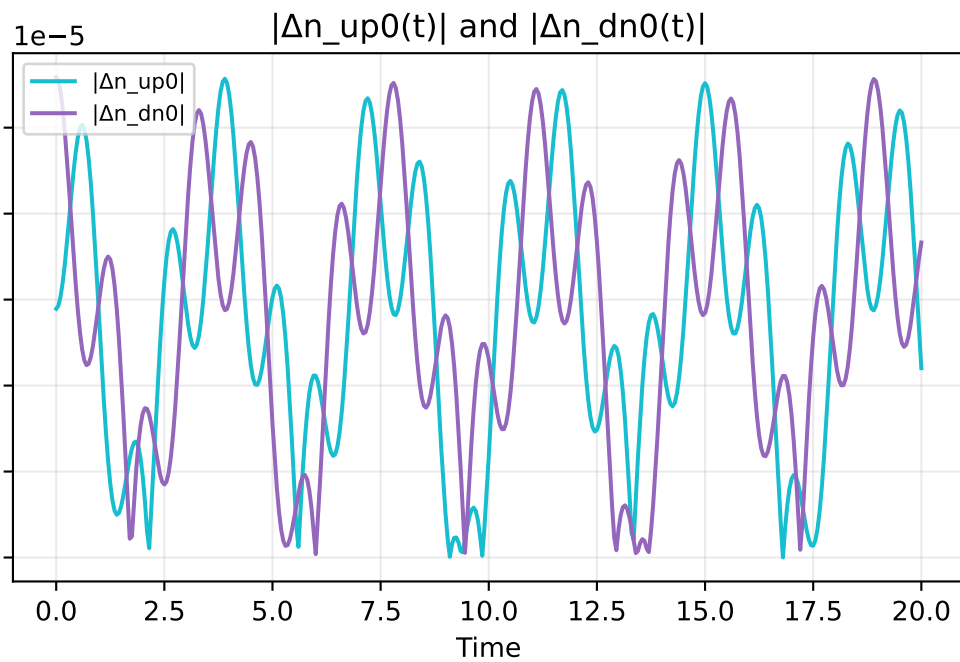
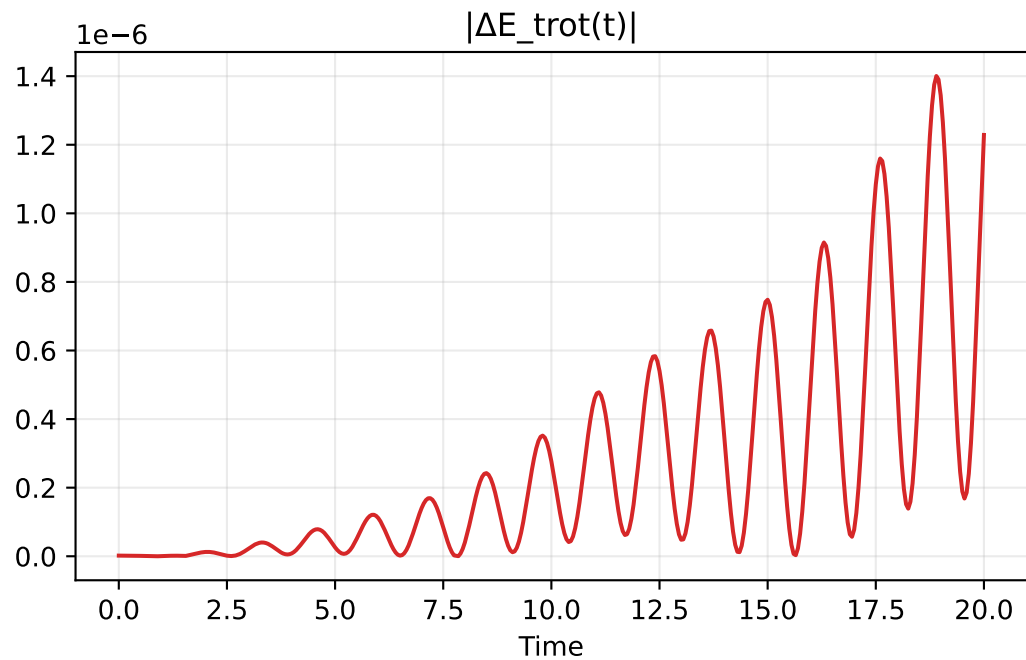
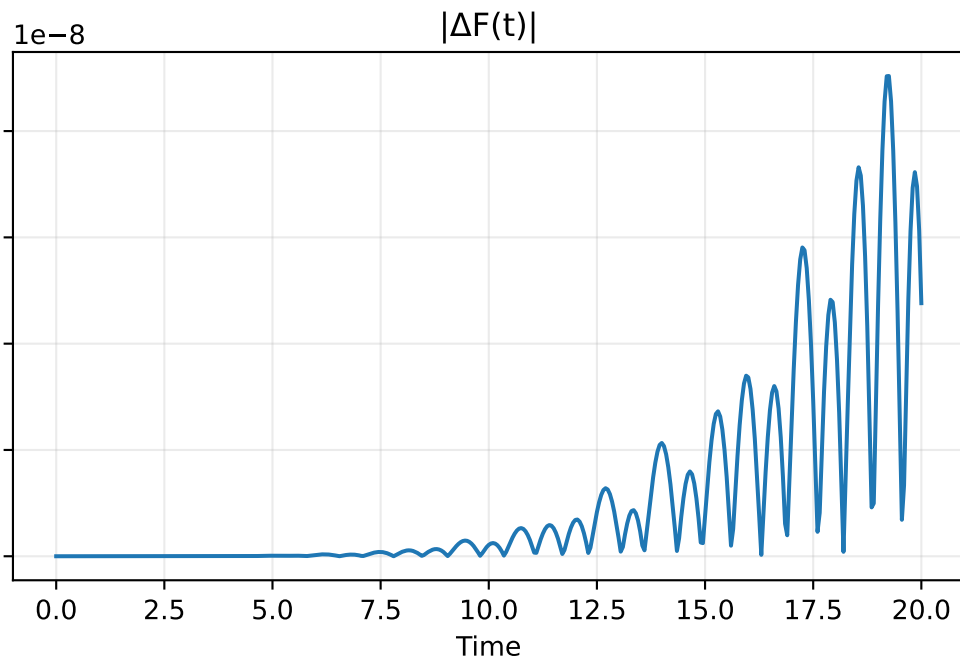


When initial\_state\_source=vqe, Trotter  $E(t=0) = \langle \psi_{\text{vqe}} | H | \psi_{\text{vqe}} \rangle = \text{VQE energy}$ .  
VQE energy  $\neq$  exact ground state energy unless VQE fully converged.



# Delta Diagnostics L=2

$\Delta X(t) = |X_{hc}(t) - X_{qk}(t)|$ , where  $X_{pipeline}(t)$  is that pipeline's stored trajectory value.



L=2 metrics summary

Delta metric definitions:

$\Delta F(t) = |F_{hc}(t) - F_{qk}(t)|$

$\Delta E_{trot}(t) = |E_{trot_{hc}}(t) - E_{trot_{qk}}(t)|$

$\Delta n_{up0}(t) = |n_{up0_{hc}}(t) - n_{up0_{qk}}(t)|$

$\Delta n_{dn0}(t) = |n_{dn0_{hc}}(t) - n_{dn0_{qk}}(t)|$

$\Delta D(t) = |D_{hc}(t) - D_{qk}(t)|$

$F_{pipeline}(t)$  is the pipeline's stored trajectory fidelity value (as computed internally vs that pipeline's exact evolution).

ground\_state\_energy\_abs\_delta = 0.0

fidelity max/mean/final = 2.2590508352848815e-08 / 2.6804744024278294e-09 / 1.190507825654663e-08

energy\_trotter max/mean/final = 1.400460892919675e-06 / 2.561722049860173e-07 / 1.228592043989174e-06

n\_up\_site0\_trotter max/mean/final = 2.7846824668553705e-05 / 1.4103046424698389e-05 / 1.1012572472712812e-05

n\_dn\_site0\_trotter max/mean/final = 2.7934482115687942e-05 / 1.406226762311699e-05 / 1.8319372432129555e-05

doublon\_trotter max/mean/final = 4.837666837398391e-07 / 2.3529349619561587e-07 / 2.0937875369608783e-07

checks:

```
{'doublon_trotter_max_abs_delta': True,  
 'energy_trotter_max_abs_delta': True,  
 'fidelity_max_abs_delta': True,  
 'ground_state_energy_abs_delta': True,  
 'n_dn_site0_trotter_max_abs_delta': True,  
 'n_up_site0_trotter_max_abs_delta': True}
```

PASS = True