Similarity and Clustering

Raf Alvarado UVA DS 5001

Similarity and distance, distance measures, normalization, clustering, hierarchical, dendrograns, wine review examples

Review: Vector Space Models

Vector space models are the **foundation** of much of text analytics

Vector Space Models allow us to treat **texts as points** in a coordinate space

This allows us to **compare texts** using various **distance measures**

See Salton, Wong, and Yang (1975) for an **early description** of the method — IR, not Al!

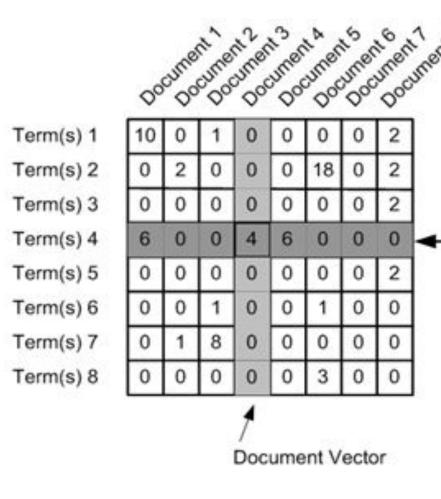
Vector spaces have a general **structure** that applies to many things

Features = items

Events = **containers** = baskets = contexts = embeddings

More of a form of representation than a model

Similarity and Difference



Recall that a bag-of-words representation of the TOKEN table in our data model can be converted into a matrix, which can be viewed as a vector space, either of word or document vectors

Word Vector
 (Passage Vector)

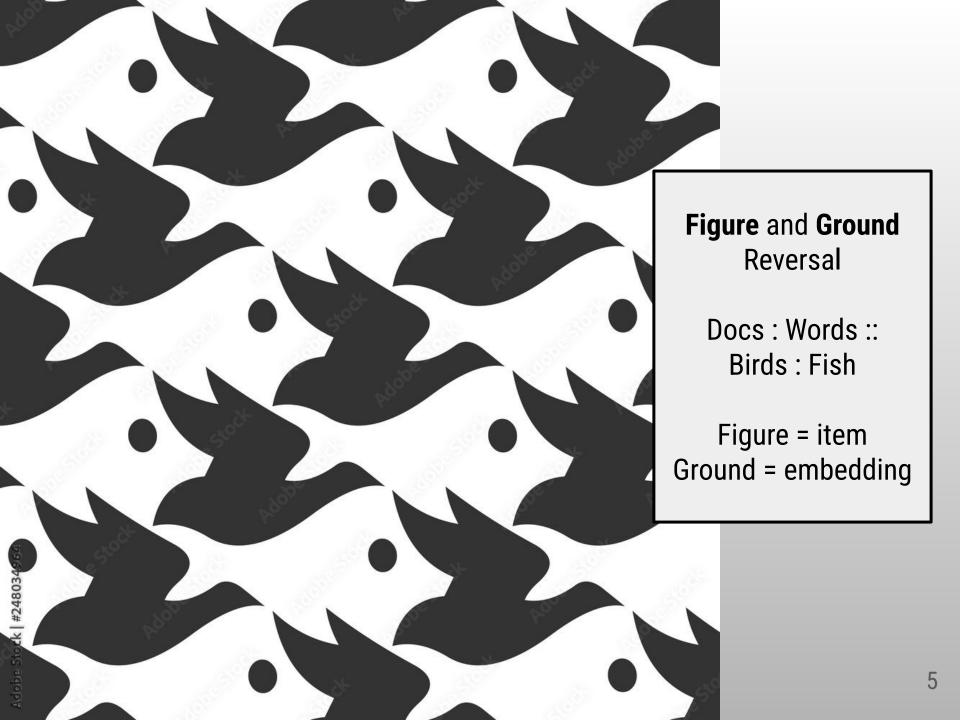
This matrix consists of a collection of vector **pairs**

$$t_2 = (0, 2, 0, 0, 0, 18, 0, 0)$$

 $t_8 = (0, 0, 0, 0, 0, 3, 0, 0)$

$$d_1 = (10, 0, 0, 6, 0, 0, 0, 0)$$

 $d_2 = (0, 0, 0, 4, 0, 0, 0)$



Uses of Document and Word Vectors

The **vector space model** allows us to to **find similar documents or words**

With **document vectors** we can

find documents that match queries

group similar documents together (**clustering**)

With word vectors we can

find synonyms or generate word networks

In **combination** we can

Use word networks to **connect** documents

where documents are **nodes** and words are **edges**

Term-Term Matrices and Vector Semantics

Word-Context matrices are often **converted** into **term-term** matrices to explore **word similarity**

Both axes contain the vocabulary

Each cell contains the number of times the row and column words **co-occur** (in an OHCO container)

Word **similarity** is computed by comparing word vector pairs

We will explore these relations (vector semantics) in more detail when we look at PCA and word embedding

	aardvark	•••	computer	data	pinch	result	sugar	•••
apricot	0		0	0	1	0	1	
pineapple	0	•••	0	0	1	0	1	
digital	0		2	1	0	1	0	
information	0		1	6	0	4	0	

Figure 6.5 Co-occurrence vectors for four words, computed from the Brown corpus, showing only six of the dimensions (hand-picked for pedagogical purposes). The vector for the word *digital* is outlined in red. Note that a real vector would have vastly more dimensions and thus be much sparser.

Role of TF-IDF

We often **use TF-IDF weighted document vectors** to compute similarities among documents

Documents that **share the same significant words** are considered **similar**

We also can **cull the most significant terms** to create shorter vectors of significant words

Shorter vectors mean **faster** compute times

Useful when comparing all pairs of vectors

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$n$$
 = number of vectors (docs)
 k = 2 (for pairs)
= 1,249,975,000.0
for n = 50,000

Comparing Documents in Word Space

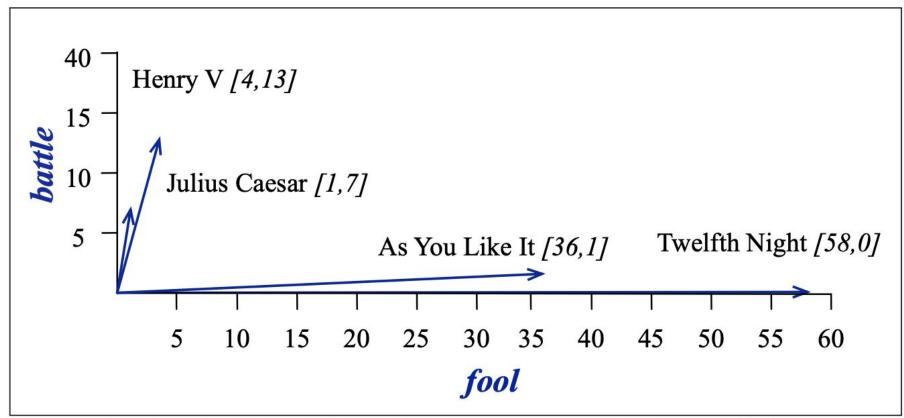
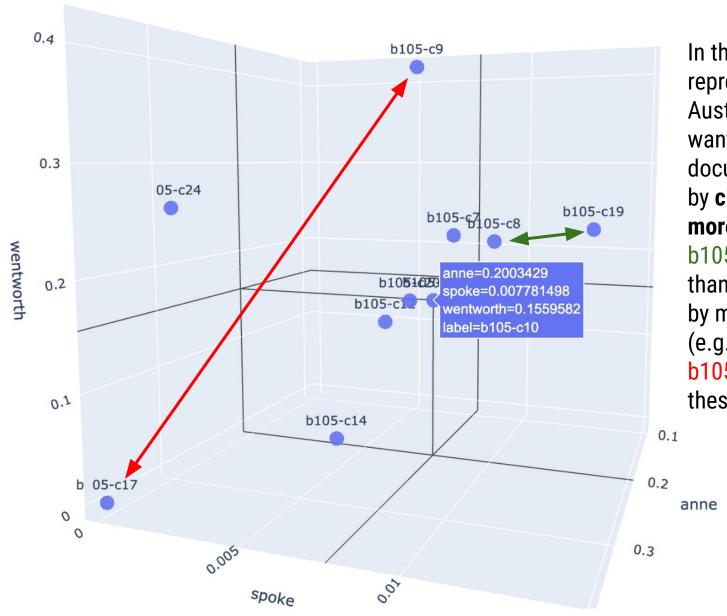


Figure 6.4 A spatial visualization of the document vectors for the four Shakespeare play documents, showing just two of the dimensions, corresponding to the words *battle* and *fool*. The comedies have high values for the *fool* dimension and low values for the *battle* dimension.



In this vector space representation of Jane Austen's Persuasion, we want to say that documents represented by close coordinates are more similar (e.g. b105-c8 and b105-c19 than those represented by more distant ones (e.g. b105-c17 and b105-c9) relative to these dimensions

Similarity and Distance Measures

A variant of the Statistical Semantics Hypothesis

Perhaps: Geometrical Semantics Hypothesis?

Geometry of/as Meaning → Structuralism

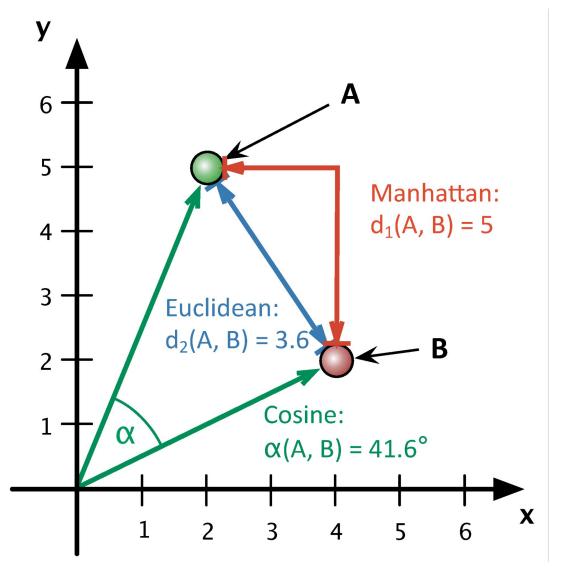
Qualitative concept operationalized in terms of **space**

similarity → **proximity** in vector space **difference** → **distance** in vector space

Expressed as a **functions** of vector pairs

similarity: sim(a, b) greater is **closer** is **more** similar **distance**: d(a, b) greater is **farther** is **less** similar

Many functions have been developed for each measure



Here are **three common measures** in Cartesian space

A, B = Documents x, y = Words (terms)

Euclidean and Manhattan are **distance** measures

Cosine is a **similarity** measure

We will look at each of these and others

Similarity and Distance Measures

Quantitatively, **similarity** is often computed as a **reverse function of distance**

Method depends on range of distance function

By inversion

```
sim(a, b) = 1 / d(a, b) sim(a, b) = 1 / (d(a, b) + 1) \text{ to avoid division by zero where } a = b
```

By subtraction

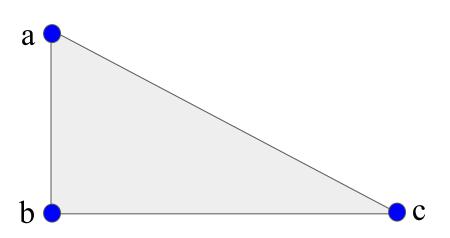
$$sim(a, b) = 1 - d(a, b)$$

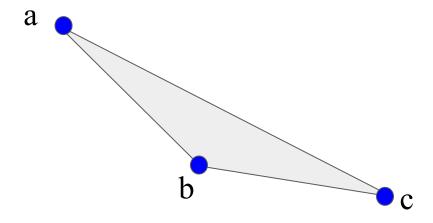
 $d(a, b) = 1 - sim(a, b)$

Some Properties of Distance Measures

Distance, as a true metric, is subject to the triangle inequality law

$$d(a, c) \le d(a, b) + d(b, c)$$





Distance is also a **symmetric** property

$$d(a, b) = d(b, a)$$

Divergence measures (such as Kullback-Leibler) **are not** subject to these laws (!)

Why is Divergence Asymmetric?

Definition 5. Conditional Entropy of X given Y

$$H(X \mid Y) \triangleq \mathbb{E}\left[\log \frac{1}{p(X \mid Y)}\right]$$

$$= \sum_{x,y} p(x,y) \log \frac{1}{p(x \mid y)}$$

$$= \sum_{y} p(y) \left[\sum_{x} p(x \mid y) \log \frac{1}{p(x \mid y)}\right]$$

$$= \sum_{y} p(y)H(X \mid Y = y).$$
(30)
(31)

Source (Weissman 2018)

Entropy measures are transformations of probability measures

Relative entropy is a transformation of **conditional probability**

Varieties of Measures

There are **many** measures of distance, similarity, and divergence

These may be **grouped according to the kind of count values** in the vector space:

For binary counts, use measures based on set theory

For **numeric** counts, use measures based on **geometry**

For **probabilities** (vectors normed to values that sum to one), use measures based on **information theory**

For **strings** (discrete symbol sequences), use edit distance measures (also based on info theory)

	Binary counts Set theory	Numeric counts Geometry	Probabilities Info. Theory
SIMILARITY	Matching coefficient Dice Jaccard Overlap Cosine	Dot product Cosine Harmonic Mean Pearson's Corr.	
DISTANCE		Manhattan Euclidean Minkowski	Manhattan
DIVERGENCE			Kullback-Leibler Jensen-Shannon Info Radius Mutual Information

Count Distance Measures

Manhattan

$$d(a,b) = \sum_{i=1}^{n} |a_i - b_i|$$

This is also called cityblock and taxicab distance.

Euclidean

$$d(a, b) = \sqrt{\sum_{i=1}^{n} (a_i - b_i)^2}$$

This is just the Pythagorean theorem.

Minkowski

$$d(a, b) = (\sum_{i=1}^{n} |a_i - b_i|^p)^{\frac{1}{p}}$$

Note that Minkowski distance is just the general rule.

- Manhattan distance is just where p = 1
- Euclidean distance is just where p = 2.

a, b: a pair of vectors of equal length

n: number of elements in each vector

i: index of element in a vector

Count Similarity Measures

Simple dot product

$$sim(a, b) = \sum_{n=i}^{n} a_i b_i = a \cdot b$$

Remember that the **dot product** of two vectors is just the **sum** of their elements' products

This returns an unbounded value, and favors long documents.

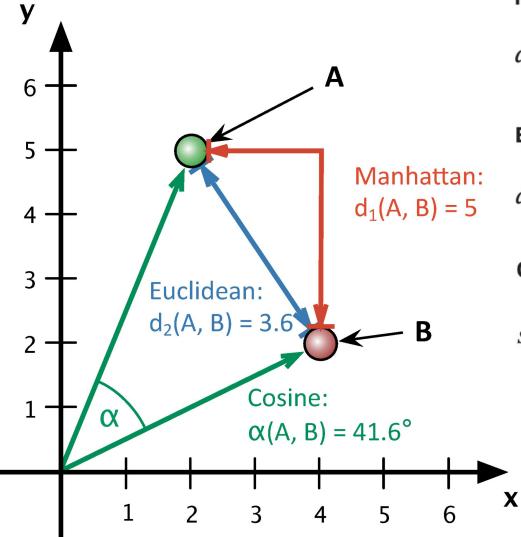
Cosine

$$sim(a,b) = \frac{\sum_{i=1}^{n} x_i y_i}{\sqrt{\sum_{i=1}^{n} a_i^2} \sqrt{\sum_{i=1}^{n} b_i^2}} = \frac{a \cdot b}{\|a\| \|b\|}$$

This is better — it returns a values between -1 and 1, or 0 and 1 if all values are non-negative.

By far the most common metric used in text analytics. Assumes Euclidean space.

Also written as CosSim(a, b).



Manhattan

$$d(a,b) = \sum_{i=1}^{n} |a_i - b_i|$$

Euclidean

$$d(a, b) = \sqrt{\sum_{i=1}^{n} (a_i - b_i)^2}$$

Cosine

$$sim(a,b) = \frac{\sum_{i=1}^{n} x_i y_i}{\sqrt{\sum_{i=1}^{n} a_i^2} \sqrt{\sum_{i=1}^{n} b_i^2}} = \frac{a \cdot b}{\|a\| \|b\|}$$

Normalization

To normalize a vector is to divide each element by the length of its norm $\boldsymbol{L}_{_{\boldsymbol{D}}}$

Useful when we want to **discount length** (e.g. length of docs)

Also for computational advantages

Length measures vary by p

 L_1 = sum of absolute value of each element (Probability)

 L_2 = square root of sum of each element squared

$$L_{\mathbf{p}} = \left(\sum_{i=1}^{n} |x_i|^p\right)^{1/p}$$

Sum of L_p normed values raised to p should = 1

 $\boldsymbol{L}_{\!_{\boldsymbol{p}}}$ is Minkowski distance from origin, the general formula

Normalization as Distance to Origin

$$d(a,b) = (\sum_{i=1}^{n} |a_i - b_i|^p)^{\frac{1}{p}}$$

Minkowski Distance

$$L_{p} = \left(\sum_{i=1}^{n} |a_{i}|^{p}\right)^{1/p}$$
 A norm is just the distance from the origin, i.e. where $b_{i} = 0$

Cosine Similarity is just the L₂ **normalized dot product** of two vectors

It is identical to taking the dot product of two L₂ normalized vectors

 L_2 = Euclidean

Intuitive Understanding of Vector Difference

	Likes Cats	Likes Dogs	Likes Meat	Likes Movies	Likes Python	SUM
Bob	0	1	1	1	0	
Sue	1	1	0	1	1	
DIFF	1	0	-1 = 1	0	1	3

Here **distance** is **difference** (subtraction)

Same as logical **XOR** for truth tables

The higher the value, the more different

What would the SUM be if they are identical?

Intuitive Understanding of Vector Similarity

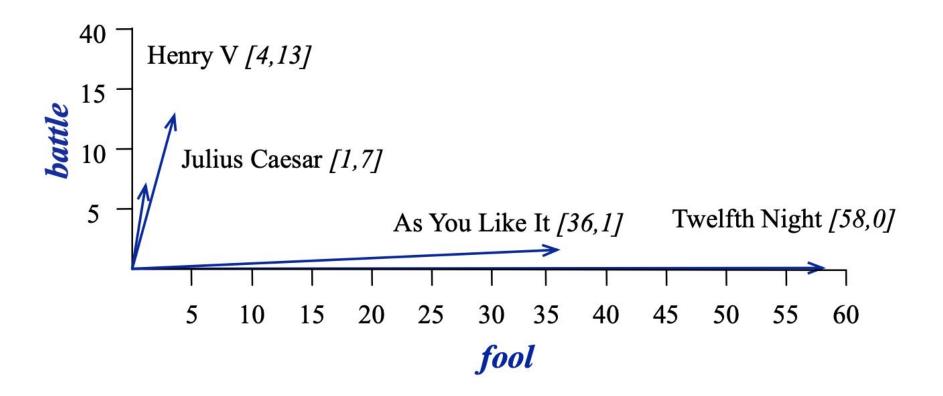
	Likes Cats	Likes Dogs	Likes Meat	Likes Movies	Likes Python	SUM
Bob	0	1	1	1	0	
Sue	1	1	0	1	1	
MATCH	0	1	0	1	0	2

Here **similarity** is a computed by **multiplication**

Same as logical **AND** for truth tables

The higher the value, the more similar

If each MATCH value is 0, how are the vectors oriented?



Two vectors that have nothing in common are orthogonal

Their angle is 90° (and the cosine of $90^{\circ} = 0$)

You can see how **Henry V** and **Twelfth Night** are roughly orthogonal in this space

Negative Values for Cosine Similarity

Negative values are sometimes considered uninterpretable

Sample sizes need to be large to ensure meaningful values

Often **converted** to 0

In ETA, we may consider negatives

May signify **oppositions** — a key concept in **structuralist poetics**

Human symbolic structures are built out dyads

left / right, male / female, sun / moon, etc.

Statistical significance not as important to establish non-randomness

Writer's intent and/or reader's response may account for "significance"

Binary Similarity Measures (Set Theory)

Matching Coefficient

$$sim(a,b) = |a \cap b|$$

This is just the sum of the intersection of ones in both vectors. Recall that as a set operation, intersection counts **unique** terms shared by both vectors.

The value is unbounded, so privileges vector length.

Dice

$$sim(a,b) = \frac{2|a \cap b|}{|a| + |b|}$$

This normalizes the matching coefficient, and returns of a value of 0 or 1.

Jaccard

$$sim(a,b) = \frac{|a \cap b|}{|a \cup b|} = \frac{|ab|}{|a \cup b|}$$

This penalizes vectors that have small overlap.

Overlap

$$sim(a,b) = \frac{|a \cap b|}{min(|a|,|b|)}$$

Cosine

$$sim(a,b) = \frac{|a \cap b|}{\sqrt{|a| \times |b|}}$$

Probability Divergence Measures

Kullback-Leibler (KL)

$$D_{KL}(a||b) = \sum_{i=1}^{n} a_i log(\frac{a_i}{b_i})$$

This is asymmetric; $D(a||b) \neq D(b||a)$.

Jensen-Shannon (JSD)

$$D_{JSD}(a||b) = \frac{D_{KL}(a||b) + D_{KL}(b||a)}{2}$$

Makes KL symmetric.

Review: Relative Entropy

Shannon, 1948: 24 The ratio of the entropy of a source to the maximum value it could have while still restricted to the same symbols will be called its relative entropy. This is the maximum compression possible when we encode into the same alphabet. One minus the relative entropy is the redundancy.

$$H/H_{max}$$

Wikipedia

In mathematical statistics, the **Kullback–Leibler (KL) divergence** (also called **relative entropy** and **I-divergence**^[1]), denoted $D_{\mathrm{KL}}(P \parallel Q)$, is a type of statistical distance: a measure of how one probability distribution P is different from a second, reference probability distribution Q.^{[2][3]}

$$D_{\mathrm{KL}}(P \parallel Q) = \sum_{x \in \mathcal{X}} P(x) \; \log igg(rac{P(x)}{Q(x)}igg)$$

$$P:Q::H:H_{\text{max}}$$

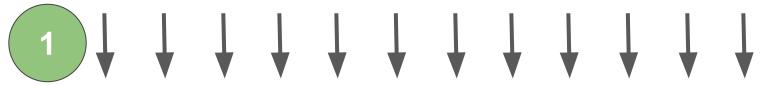
Lee (1999) proposed that, for finding word similarities, measures that focused more on overlapping coordinates and less on the importance of negative features (i.e., coordinates where one word has a nonzero value and the other has a zero value) appear to perform better. In Lee's experiments, the Jaccard, Jensen-Shannon, and L1 measures seemed to perform best. Weeds et al. (2004) studied the linguistic and statistical properties of the similar words returned by various similarity measures and found that the measures can be grouped into three classes:

- 1. high-frequency sensitive measures (cosine, Jensen-Shannon, α -skew, recall),
- 2. low-frequency sensitive measures (precision), and
- 3. similar-frequency sensitive methods (Jaccard, Jaccard+MI, Lin, harmonic mean).

Given a word w_0 , if we use a high-frequency sensitive measure to score other words w_i according to their similarity with w_0 , higher frequency words will tend to get higher scores than lower frequency words. If we use a low-frequency sensitive measure, there will be a bias towards lower frequency words. Similar-frequency sensitive methods prefer a word w_i that has approximately the same frequency as w_0 . In one experiment on determining the compositionality of collocations, high-frequency sensitive measures outperformed the other classes (Weeds et al., 2004). We believe that determining the most appropriate similarity measure is inherently dependent on the similarity task, the sparsity of the statistics, the frequency distribution of the elements being compared, and the smoothing method applied to the matrix.

Common Structure of Distance Measures

	0	1	2	3	4	5	6	7	8	9	10	11
a	\mathbf{a}_0	a_1	\mathbf{a}_2	a_3	a_4	a_5	a_6	\mathbf{a}_7	a_8	a_9	a ₁₀	a ₁₁
b	b_0	b ₁	b_2	b_3	b_4	b ₅	b_6	b ₇	b ₈	b_9	b ₁₀	b ₁₁





- 1: Pair-wise operations e.g. add, subtract, multiply, square, etc.
- 2. Result-wise operation, e.g. sum
- 3. Normalize result from 2

A Caution — The Curse of Dimensionality

As the number of dimensions increase, the less significant distance becomes

Distances between pairs have less difference among them

Therefore distance functions lose their meaning

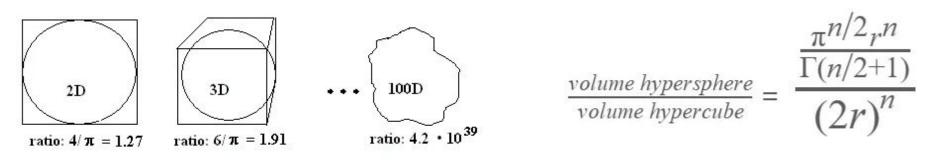
Related to the **exponential growth in volume** ...

Ratio of inscribed hypersphere to hypercube becomes small

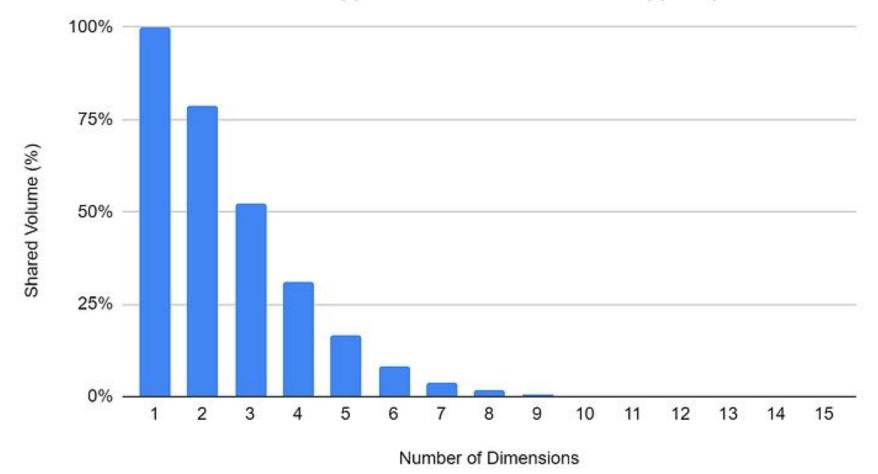
The hypersphere is the **unit sphere**, which is related to normalization

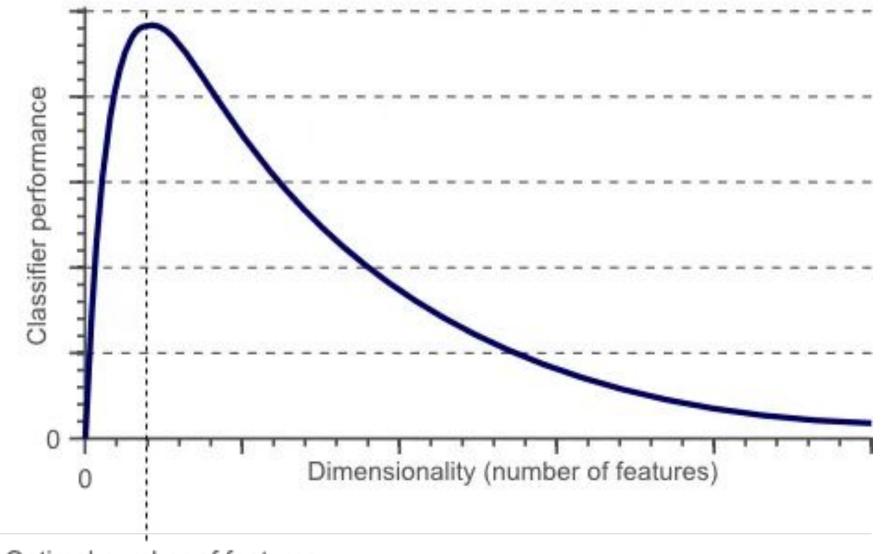
This is complex and weird

Just know that distance measures have a sweet spot for dimensionality



Shared Volume between Hypercube with Inscribed Hypersphere





Optimal number of features

Source (Raj 2019)

Summary

The most **common** measurements in text analytics are:

Manhattan, Euclidean, Cosine, Jaccard, and Jensen-Shannon

Among these, cosine similarity is often used because it is already normalized for length

Euclidean distance on non-normalized vectors is sensitive to length

Two documents will rank as dissimilar if they discuss the same content but have different lengths

Equivalent to the dot product of two normalized vectors

Jensen-Shannon has the value of being based in information theory

Tools

Python offers a number of libraries to compute distances, etc.

NumPy

norm() to normalize vectors (and matrices)

SciPy

scipy.spatial.distance → pdist(), squareform()
To create pair matrices of vectors by distance metric

SciKit Learn

preprocessing.normalize() to normalize vectors and matrices

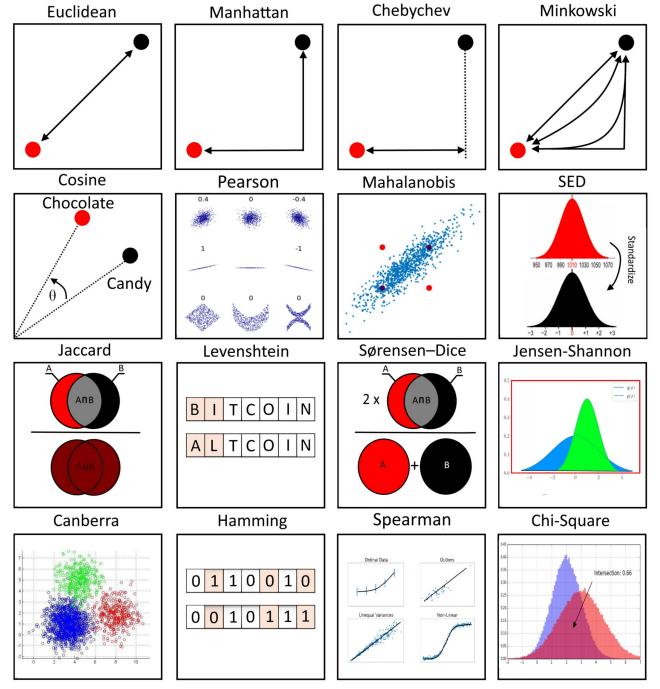
Pandas

df.corr(), $df.cov() \rightarrow but$ these are slow

Pydist2

pdist1() and pdist2()

Methods for calculating distances between observations



https://towardsdatascience.com/17-types-of-similarity-and-dissimilarity-measures-used-in-data-science-3eb914d2

Clustering

Clustering

Often used as a synonym for unsupervised learning

Actually, one of a few methods (include graph-based methods)

Clustering

Clustering is just the **grouping of vectors** (coordinates) based on their distances to each other

Generates groups of documents based on their **pairwise distances**

Two main uses in NLP (and ETA):

Exploration (EDA): Hence prominence of clustering for exploratory text analytics

Generalization: Creating groups that may be used to draw inferences

e.g. our data has the prepositions for some **days of the week**, but not all. If days of the week form a cluster, we can treat them as a class and induce that all days of week take the seme preposition.

41

Clustering Algorithms

Many clustering algorithms, but in general there are **two types**:

Flat

Start with a set number of unrelated clusters (k)

Iteratively assign vectors to each cluster

K-means is classic example

 \rightarrow Fast

Hierarchical

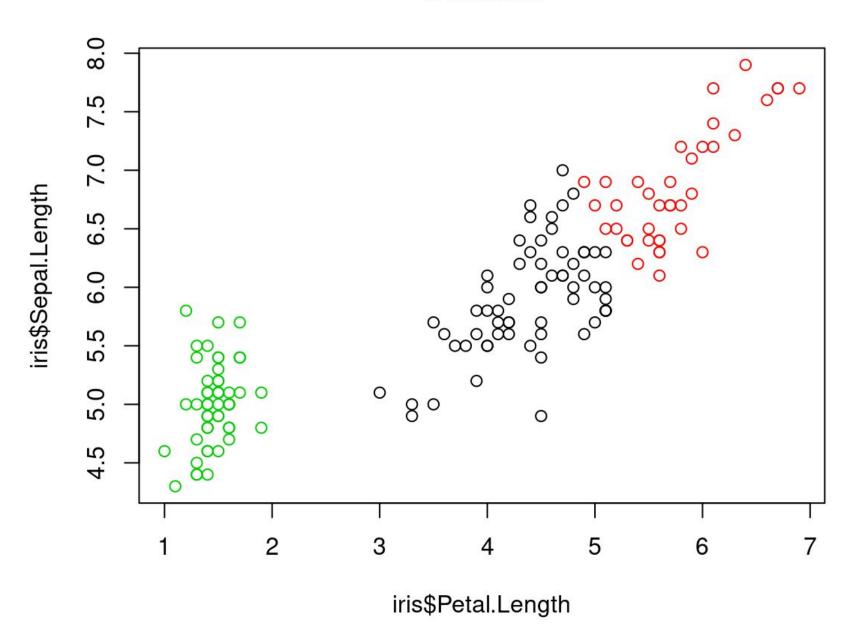
Clusters are related in a parent-child graph (classes+subclasses)

Terminal nodes (leaves) stand for clustered objects

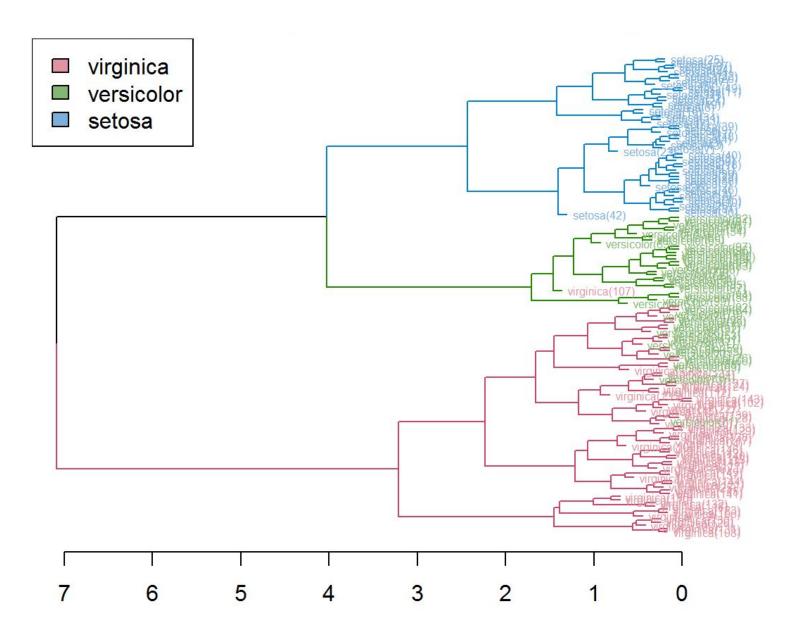
E.g. Hierarchical Agglomerative Clustering

→ Intuitive

k-means



Hierarchical



Comparison

Hierarchical

Better for **detailed data analysis** -- gives more info -- than flat

No single best algo (see diagram below)

Less efficient than flat

No objective way to know how many clusters result

Flat

Have to guess at number of clusters (k)

Better for **efficiency**

Conceptually simplest, so use first on new data

Meant for continuous data, so no good for nominal data

See K-Modes

Hierarchical Clustering Algorithms

Bottom-up vs Top-Down

Both iterative

Bottom-up

Begins with **one cluster for each doc**Uses **similarity** to determine which clusters get merged each step
Also called **agglomerative** — HAC

Top-down

Begins with **one cluster for all docs** (one big cluster)
Uses **coherency** (max within-group similarity) to split clusters at each step
Also called **divisive**

Think of clusters as provisional **labels** (d, c)

Agglomerative Clustering Algorithms

Greedy — starts with a **separate cluster for each object**

In each step, the two most similar clusters are determined and then merged into a new cluster

Terminates when one large cluster containing all objects has been formed

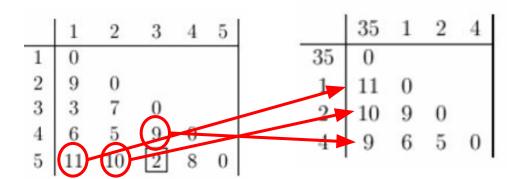
Agglomerative Clustering Algorithms

- Compute the distance between each document pair (as matrix)
- 2. Consider each individual document as its own cluster
- 3. Do:
 - 1. Find and **merge** two **closest**¹ clusters in the matrix
 - 2. **Update** the distance table
- 4. Repeat 3 **until** one single cluster remains, |C| = 1

¹ Re 3.1 -- There are **many ways to measure the distance**, aka **linkage**, between two clusters

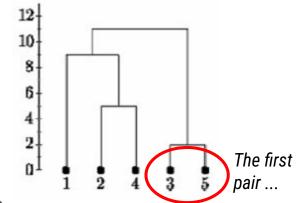
Different from the distance measure in 1

Linkage defines what is measured, not how

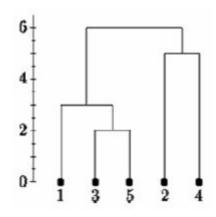


- Start with **closest** pair, e.g. d(3, 5) = 2
 - 2 0 2
- Combine pair into one (35), and pick maximum value from two in comparison to the rest, i.e. Complete Link
 - The same data closest by taking the **minimum** value of the group pair, i.e. Single Link

In either case, no objective way to define groups, i.e. pick a cut-off line



After 6 steps, everything is clustered



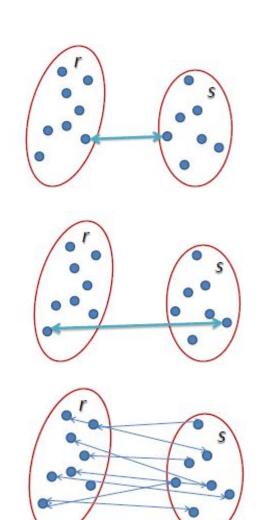
Linkage Measures

Single link distance: minimum distance between two points in each cluster (two most similar members)

Complete link distance: <u>maximum</u> distance between two points in each cluster (two least similar members)

Average link distance: <u>average</u> distance between each point in one cluster to every point in the other cluster

Centroid distance: distance between <u>centroid</u> two clusters



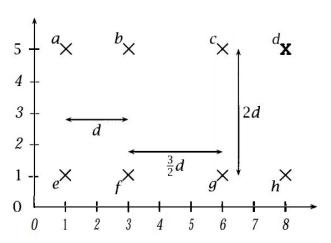


Figure 14.4 A cloud of points in a plane.

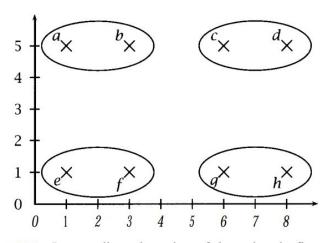


Figure 14.5 Intermediate clustering of the points in figure 14.4.

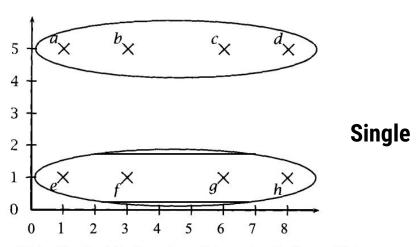


Figure 14.6 Single-link clustering of the points in figure 14.4.

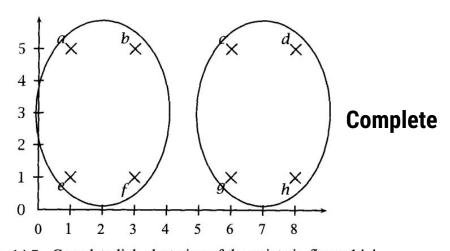


Figure 14.7 Complete-link clustering of the points in figure 14.4.

Single vs Complete link results

Linkage Measures

Single Link	Can handle non-elliptical shapes Good local coherence, but bad global quality i.e. produces long, elongated clusters (chaining). Sensitive to outliers and noise.	
Complete Link	Focuses on global qualities of clusters Produces more balanced clusters (with equal diameter). Less susceptible to noise. Often breaks very large clusters. Small clusters are merged with large ones.	
Group Average Link	Compromise. Less susceptible to noise and outliers. Biased towards globular clusters.	

The most appropriate measure depends on the underlying process

E.g. volcano chains modeled by single link

For **language** modeling, **complete link** clustering is preferable

i.e. linkage methods that are more **spherical**

E.g. Ward clustering

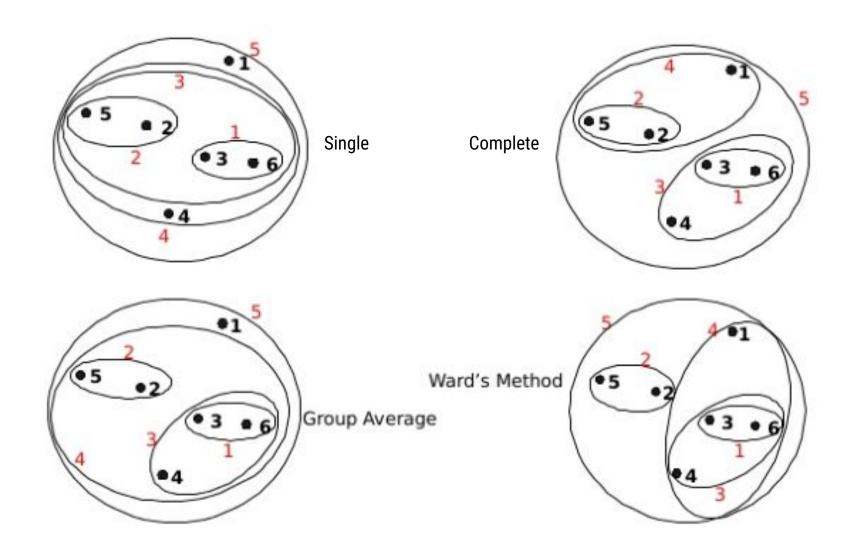
Ward Distance

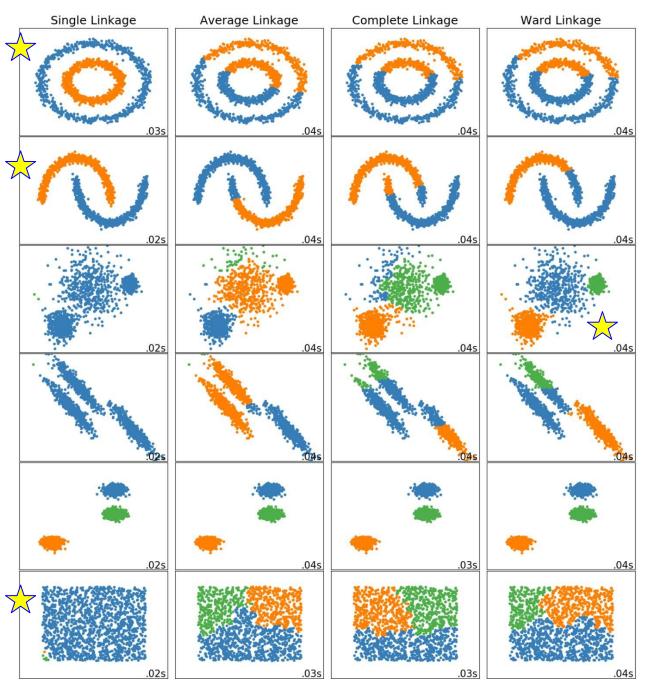
The difference between the **total within-cluster sum of squares** (WCSS) for the two clusters **separately**, and the WCSS resulting from **merging** the two clusters

$$D_W(C_i, C_j) = \sum_{x \in C_i} (x - r_i)^2 + \sum_{x \in C_j} (x - r_j)^2 - \sum_{x \in C_{ij}} (x - r_{ij})^2$$

where r is the centroid of cluster C

Favors minimal increase of sum of squares





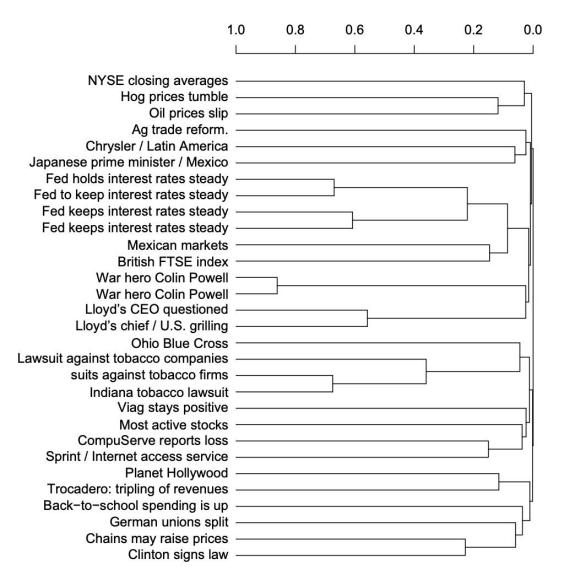
No single best algo
Depends on underlying
process

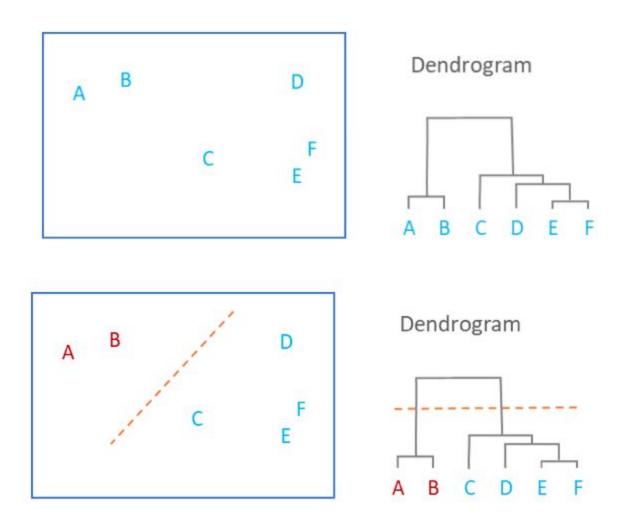
Dendrograms

Hierarchical clusters are often represented in **dendrograms** like the one on the right

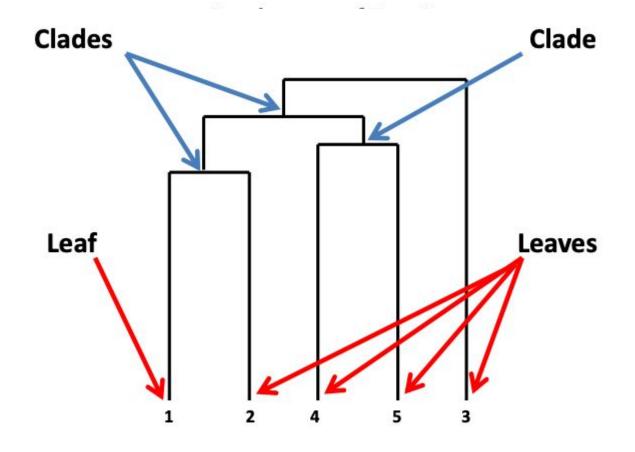
The diagram shows which documents are most similar by a given metric

The **length** of the grouped branches denotes the **distance** between the grouped items





Here we see the relationship between point space and cluster diagrams



lexomics.wheatoncollege.edu

Here are some terms used to describe dendrograms

Clustering and ETA

Hierarchical **Agglomerative** Clustering (HAC) works well for many ETA tasks

E.g. Showing distances among novels from an author or set of authors

The **Ward** methods also works well for linkage

Requires Euclidean distance measures (incl. Cosine)

We also reduce the **dimensionality** of the document-term matrix

e.g. DF-IDF to yeild ~4,000 significant terms

In addition, for display purposes, we want a relatively **small number** of observations

We often take an aggregate by some label or container

E.g. group documents by author, year, book, etc.

Tools for Computing Clusters

Python offers at least two libraries to compute clusters

SciPy

scipy.cluster

https://docs.scipy.org/doc/scipy-1.2.1/reference/cluster.html

scipy.cluster.hierarchy.dendrogram
To generate dendrogram images; used by SciKit Learn

SciKit Learn

sklearn.cluster

https://scikit-learn.org/stable/modules/classes.html#module-sklearn.cluster

Clustering Wine Reviews

The Corpus

129,971 wine reviews from *Wine Enthusiast*

Pre-scraped and downloaded from Kaggle

Each review is **very short** — one or two sentences, e.g.

"A year in wood and 30 months in bottle before release have allowed this attractive wine to fully develop its solid yet smooth texture. It has concentration, layers of bright black currant fruit and vibrant acidity. Ready to drink."

Review of *Adega Cooperativa de Borba*, 2012, Montes Claros Garrafeira Red (Alentejo) by Roger Voss.

The Corpus – Salient Features

Title — unique identifier

Taster – 19, with Twitter names

Variety – 707, includes blends

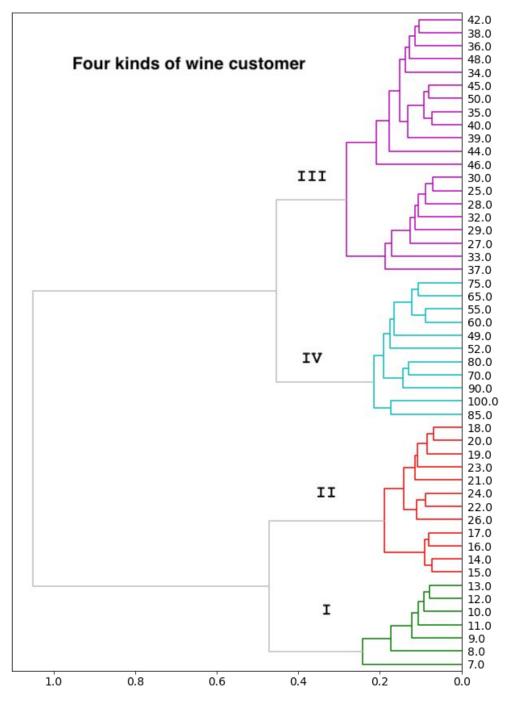
Country -43

Province -425

Points — a rating from 80 to 100 (integers); Mean = 88

Price – from \$4 to \$3,300; Median = \$25

country	description designation	points	price	province	1
Italy	Aromas include tropical fruit, broom, b Vulkà Bianco	87		Sicily & Sardi	E
Portugal	This is ripe and fruity, a wine that is sm Avidagos	87	15	Douro	
US	Tart and snappy, the flavors of lime flesh and rind dor	mina 87	14	Oregon	١
US	Pineapple rind, lemon pith and orange Reserve Late	Harv 87	13	Michigan	l
US	Much like the regular bottling from 201 Vintner's Rese	erve \ 87	65	Oregon	١
Spain	Blackberry and raspberry aromas shor Ars In Vitro	87	15	Northern Spa	1
Italy	Here's a bright, informal red that open: Belsito	87	16	Sicily & Sardi	١
France	This dry and restrained wine offers spice in profusion	. Bal: 87	24	Alsace	1
Germany	Savory dried thyme notes accent sunn Shine	87	12	Rheinhessen	
France	This has great depth of flavor with its fr Les Natures	87	27	Alsace	1
US	Soft, supple plum envelopes an oaky Mountain Cuv	ée 87	19	California	t
France	This is a dry wine, very spicy, with a tight, taut texture	and 87	30	Alsace	1
US	Slightly reduced, this wine offers a chalky, tannic bac	kbon 87	34	California	,
Italy	This is dominated by oak and oak-driv Rosso	87		Sicily & Sardi	E
US	Building on 150 years and six generations of winema	iking 87	12	California	(
Germany	Zesty orange peels and apple notes a Devon	87	24	Mosel	
Argentina	Baked plum, molasses, balsamic vine; Felix	87	30	Other	(
Argentina	Raw black-cherry aromas are direct ar Winemaker Se	electi 87	13	Mendoza Pro	1
Spain	Desiccated blackberry, leather, charre Vendimia Sele	eccio 87	28	Northern Spa	f
US	Red fruit aromas pervade on the nose, with cigar box	and 87	32	Virginia	١
US	Ripe aromas of dark berries mingle wi Vin de Maison	87	23	Virginia	١
US	A sleek mix of tart berry, stem and herb, along with a	hint c 87	5.000.00	Oregon	(
Italy	Delicate aromas recall white flower an Ficiligno	87	19	Sicily & Sardi	4
US	This wine from the Geneseo district off Signature Sele	ection 87	22	California	F
Italy	Aromas of prune, blackcurrant, toast a Aynat	87	35	Sicily & Sardi	4
US	Oak and earth intermingle around robi King Ridge Vin	neya 87	69	California	4
Italy	Pretty aromas of yellow flower and sto Dalila	87	13	Sicily & Sardi	-
Italy	Aromas recall ripe dark berry, toast and a whiff of cak	e spi 87	2007	Sicily & Sardi	-
Italy	Aromas suggest mature berry, scorche Mascaria Barr		- 1000	Sicily & Sardi	-



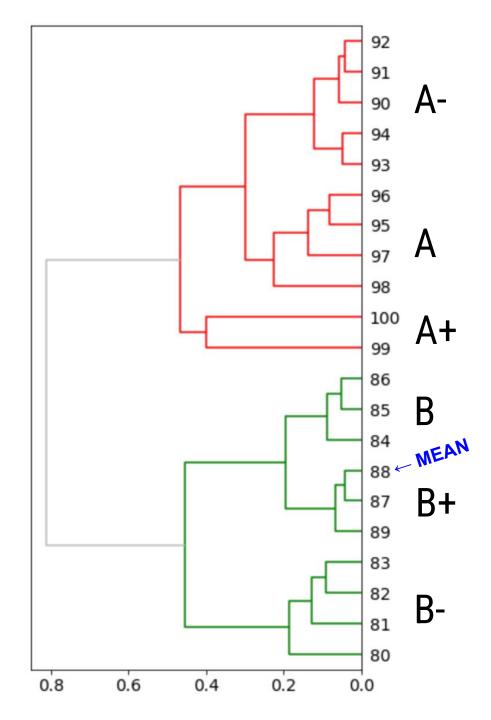
The top 50 prices (\$7 to \$100)

Reviews appear to chunk prices into **four main groups** — note the distance between the clusters.

Each group doubles the range of the previous.

Note that some prices are out of group — e.g. 25 is in group III not II

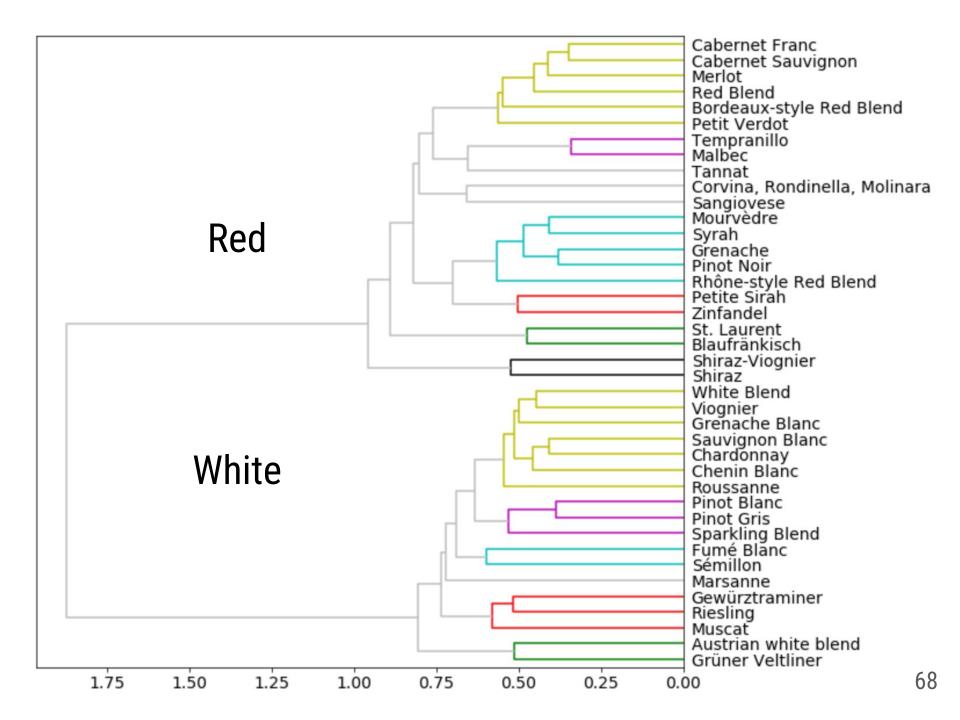
66

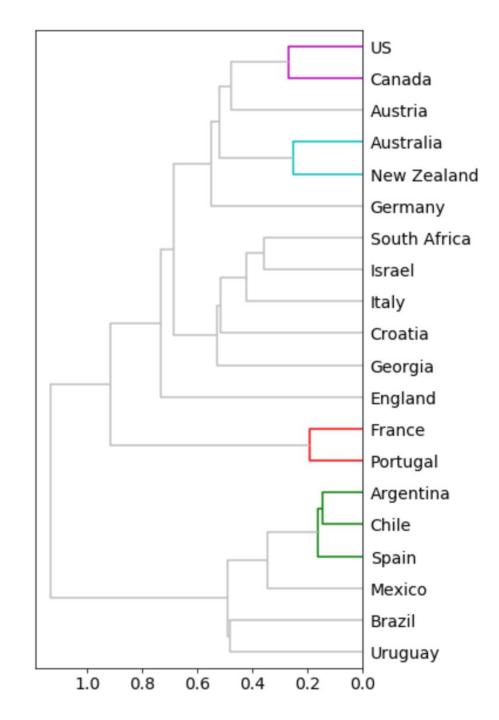


Grades appear to fall into clusters as well, matching a mental model that reflects special treatment for certain numbers and ranges.

Note that B- and A+ are on their own, and the both B and B+ and A- and A are grouped.

This suggests a bias to distinguish the very best and from very worst (or lowest).



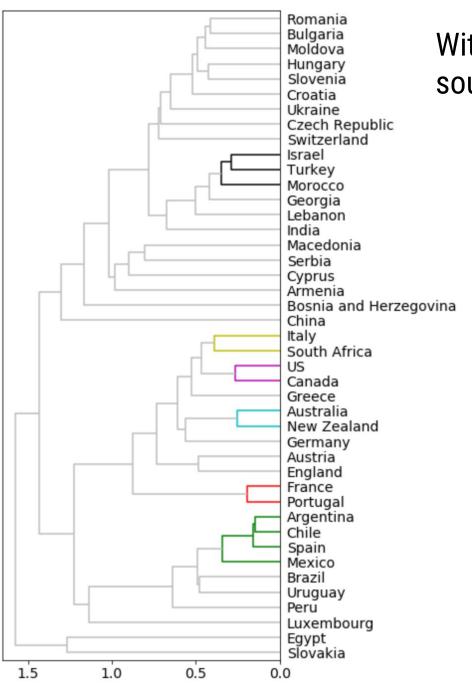


Clustering of top 20 countries by number of reviews

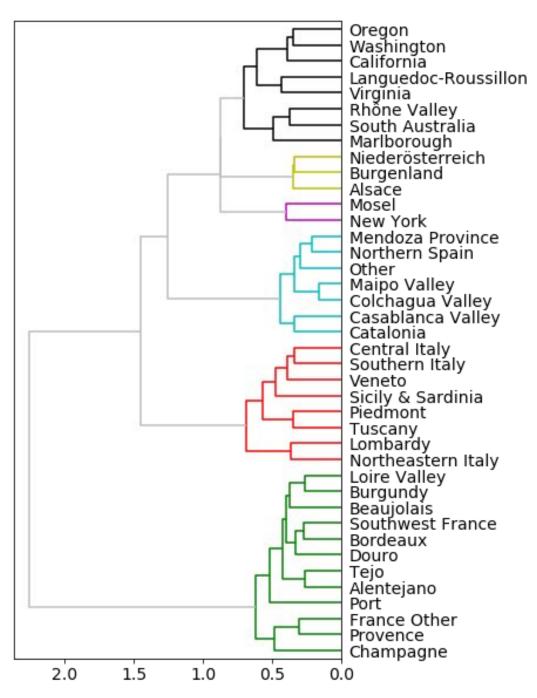
France is always grouped with Portugal (Why?)

Spain, Argentina, and Chile are always grouped

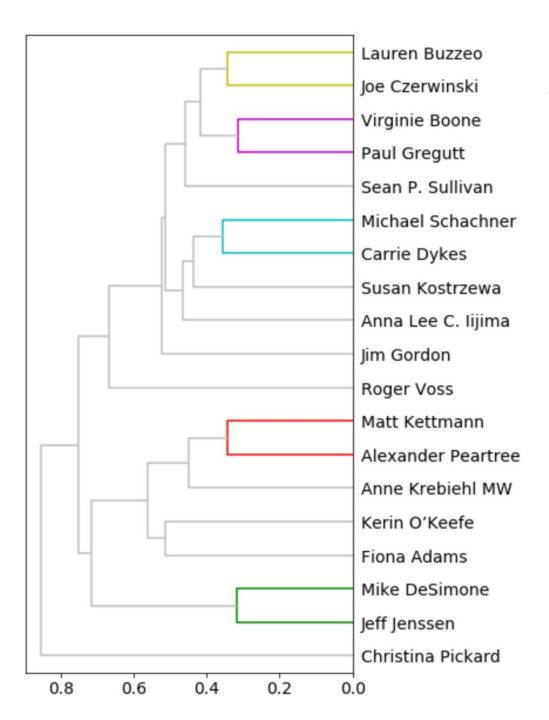
The **US** is always closer to **Italy** than to France



With more countries to the source data ...



Provinces group as expected



Not sure what to make of this

May be due to shared topic, but the first two don't overlap

Maybe stylistic differences