

Math 31

Derivatives of Trig and Exponential Functions

Jad Chehimi

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Unfinished!

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Review

You need to review the following for this unit. There are good review resources in the notes booklet.

- Trigonometry
- Exponents and Logs
- The graphs of the above two

Exponent Appearance

$$\sin(x+2)^3 = \sin(x^3+2^3)$$

$$\sin^3(x+2) = (\sin(x+2))^3$$

Derivatives of Trigonometric Functions

These are on your formula sheet.

Primary

$$\frac{d}{dx} \sin u = \cos u \cdot \frac{du}{dx}$$

$$\frac{d}{dx} \cos u = -\sin u \cdot \frac{du}{dx}$$

In simpler terms...

- Swap between sin and cos
- cos to sin prepends negative
- Multiply by derivative of trig function argument

Reciprocal

$$\frac{d}{dx} \csc u = -\csc u \cot u \cdot \frac{du}{dx}$$

$$\frac{d}{dx} \sec u = \sec u \tan u \cdot \frac{du}{dx}$$

$$\frac{d}{dx} \tan u = \sec^2 u \cdot \frac{du}{dx}$$

$$\frac{d}{dx} \cot u = -\csc^2 u \cdot \frac{du}{dx}$$

Related Rates

Related rates is done the same way as before. Here are some formulas you could derive and plug in.

- **Cosine Law:** For non-right triangles, on your formula sheet

$$c^2 = a^2 + b^2 - 2ab \cos C$$

(remember that angle C is opposite to side c)

- Use trigonometric ratios for right triangles (stuff like $\sin \theta = \frac{x}{2}$)

Revolutions

Related rates questions often involve radians per second/minute for rate of change of theta.

Some, however, have revolutions per minute (rpm). To convert, multiply it by 2π .

$$32 \frac{\text{rev}}{\text{min}} \cdot \frac{2\pi \text{rad}}{\text{rev}} = 64\pi \frac{\text{rad}}{\text{min}}$$

Euler's Number

$$e \approx 2.71828$$

$$\ln x = \log_e x$$

Derivative of Exponential Functions

$$\frac{d}{dx} e^u = e^u \cdot \frac{du}{dx}$$