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Blockchain simulation and analysis on mining weaknesses

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Chapter 1

Introduction

1.1 Abstract

A blockchain is a list of blocks linked together using cryptography. Each block holds a list of transactions and the previous block's hash.

The first idea of the blockchain came from 1991 by Stuart Haber and W. Scott Stornetta but it was really used the first time by Satoshi Nakamoto in 2008 to serve its most famous application, the cryptocurrency Bitcoin.

The main advantage of blockchain is the decentralization, it means there is no need of a third party to validate transactions while keeping essential properties as integrity, durability, reliability and longevity.

To ensure security, blockchain rests on cryptography methods like public-key based signatures to protect transactions and hash functions for the mining process, which is the way to add a block in the blockchain.

The main goal of this work is, first, to understand how mining works by simulating a blockchain. Then, we'll analyze the weaknesses and possible attacks on mining.

1.2 Blockchain structure

In this part, we'll try to understand in more detail the blockchain's components and how they work together. Bitcoin is a specific implementation of the blockchain but it's the starting point of our analysis.

As we mentioned before, the blockchain is based on decentralized implementation. Actually, it's based on a peer-to-peer network.

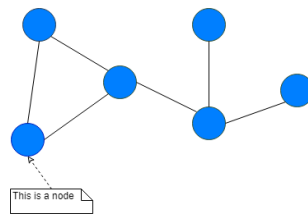


Figure 1.1: Peer-to-peer network

Each node has three responsibilities :

- Keeping a copy of confirmed transactions, which is the blockchain itself.
- Validating transaction compliance.
- Sharing information with their neighbors such as unconfirmed but valid transactions and mined blocks.

C++ Code We've written a C++ code to simulate blockchains focusing on the mining process. The code is written in C++ using the library MPI to parallelize the process. Moreover, the executions were made on the Geneva University cluster to truly parallelize the code.

A full chapter of this work is dedicated to the results we found in these simulations.

Thus, we can simulate several miners trying to mine blocks and keep the blockchain synchronized. The goal is to deeply understand the network structure and to observe the evolution of the blockchain in the time.

All along with the presentation of the blockchain's principles, we'll show the implementation in our code.

1.2.1 Transaction

The main feature of the blockchain is to record transactions.

A transaction is composed of a list of inputs and a list of outputs (see Figure 1.2). Outputs can include the payer itself.

While doing a transaction, one wants to be sure that the payer is the true owner of the money. Then, to check this, we use digital signatures :

- The inputs of the transaction are encrypted with the public key of the payer.
- To prove he owns the coins, the payer "unlock" them by decrypting the signature with his private key.
- Then, he "locks" the outputs with the public key of the payees.

Technically, this is done with scripts linked to each input and output (see [1] for more details).

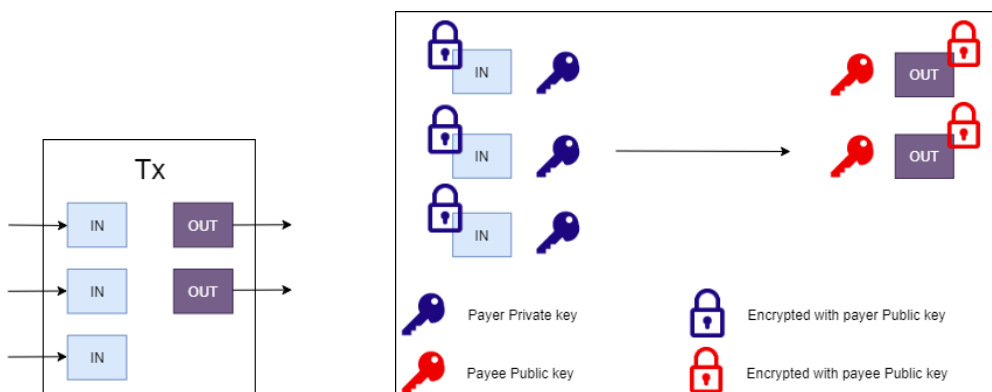


Figure 1.2: A transaction diagram and digital signatures

C++ code As we mentioned, the code focus on the mining process so we've simplified transaction management.

In our simulation, a transaction is just a string, for example: (each line is a transaction)

```
User 7 starts with 76 bitcoin(s).
User 8 starts with 67 bitcoin(s).
User 10 starts with 28 bitcoin(s).
User 3 gives 16 bitcoin(s) to 9.
User 6 gives 8 bitcoin(s) to 7.
User 10 gives 15 bitcoin(s) to 3.
```

So we don't have to manage signatures, inputs and outputs and it won't affect the mining process.

To generate those transactions, we've created a specific generator which creates a given number of transactions with limitations in the amount of money exchanged for a given number of users.

```
class TransactionsGenerator {  
  
    private:  
        int nbUsers;  
        int nbTransactions;  
        int minTransfer = 1;  
        int maxTransfer = 20;  
  
        int chooseRandomUser(int previousChoice);  
  
    public:  
        TransactionsGenerator(int nbUsers, int nbTransactions);  
        vector<string> generateVectorTransactions();  
};
```

1.2.2 Block

Now that we have a transaction, we can transmit it to a node of the network. There, it needs to pass verification and if it's correct, it will be broadcasted to other nodes.

Once the transaction is accepted by a node, it will stay in a special area called the Mempool (Memory pool), this is where all unconfirmed transactions wait to be added in a block. A node can prioritize the transactions in its Mempool, especially if he's running out of memory, he can choose the order of arrival or, more probably, the highest transaction fee.

When a node receives the information that a new block has been added to the blockchain, he removes all newly confirmed transactions from his Mempool.

To form a new block candidate, a miner gathers transactions from the Mempool. Then, he will try to mine this block to add it to the blockchain. The miner will also add a block header which gives more information about the block (see 1.2.3).

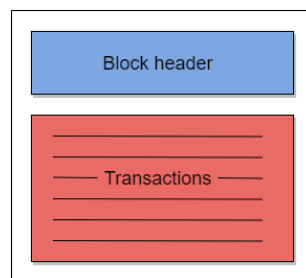


Figure 1.3: A transaction diagram and digital signatures

C++ code A block is an object with the following fields:

- A vector of string representing the transactions.
- A block header (see explanations below).
- An ID to get its position in the blockchain.
- We also add a reference to the previous block, this is used to build the blockchain.

```
class Block {
private:
    int id = 0; //Block ID to locate it in the blockchain
    Block* prev; //Pointer on the previous block
    BlockHeader* blockHeader; //Block header
    vector<string> transactions; //List of transactions
}
```

A block can also build the Merkle tree with its transactions and be added in a blockchain.

1.2.3 Block header

A block header is a summary of the block, it's like its metadata. A block header contains six fields:

version	The block's version	4 bytes
hashPrevBlock	The previous block's hash	32 bytes
hashMerkleRoot	The Merkle root representing all transactions in the block (see 1.2.4)	32 bytes
time	The Unix time at which the block header was hashed	4 bytes
target	This is a shortened version of the target (see 1.3.1)	4 bytes
nonce	A random number	4 bytes

We'll see later that block headers are used for mining (see 1.3).

C++ code As we've just seen, a block header contains all the fields mentioned: version, previous block hash, Merkle root, time, target and the nonce.

```
class BlockHeader {
private:
    //Attributes
    string version = "20000000"; //Version of the block (from Bloc #573513 of Bitcoin blockchain)
    string hashPrevBlock; //hash of the previous block
    string hashMerkleRoot; //merkle root
    string time; //time
    string target; //expected target for the hash
    string nonce; //random number
}
```

The version is always the same in our simulation because it won't affect mining. In the real world, the version helps to decode the block. A block header can set a nonce and compute its hash (by applying SHA256 twice).

1.2.4 Merkle root

As we've just seen, one of the block header fields is a Merkle root. Conceptually, it represents a fingerprint of the transactions' list and concretely it's just a hash.

The blockchain uses Merkle trees for two reasons :

- To have a lightweight representation of the transactions because it results in only a hash.
- To be able to check if a transaction exists in a block without knowing all transactions in this block.

Merkle trees use a hash function, for blockchains, they use the same function than mining, which is SHA256(SHA256(.)).

The main advantage of this technology is the speed and the ease to verify if a transaction belongs to a block. We don't need to know all transactions of the block and we don't even need to reveal any data from the transactions but only their hashes.

For example, if we want to check if the transaction 3 belongs to the block in our previous figure. We have to know its hash (Hash 3), Hash 4, Hash 12 and Hash 56 (see 1.4). With those hashes, we can reconstruct the Merkle root. If it's the same, this means that the transaction 3 belongs to the block and that no transaction has been modified so the whole block is correct.

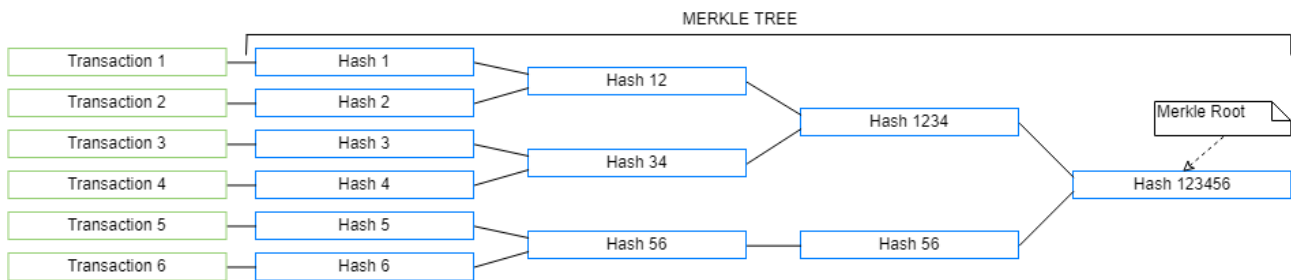


Figure 1.4: A Merkle tree

C++ code We've created a class to build the Merkle tree from a vector of string and to return the Merkle root.

```
class MerkleTree {
private:
    static string hashOperation(string str); //Hash operation to build the merkle tree
public:
    static string getMerkleRoot(vector<string> transactions); //Compute the merkle tree of the given transactions
}
```

1.2.5 The network

With all the concepts presented above, we can create a transaction, add it in a block, which will be mined thanks to its block header. Now, let's see how the nodes in the network secure the blockchain together.

The strength of the blockchain lies in its network because each node keeps a complete or partial copy of the blockchain. To keep the network updated, the nodes constantly share information between them. Typically, to broadcast a new transaction or a newly mined block :

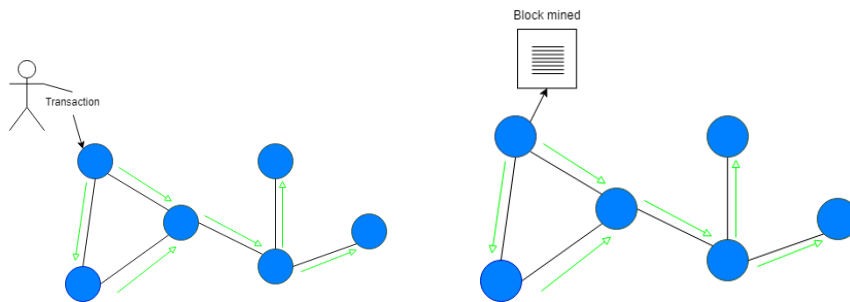


Figure 1.5: Communication inside the network

Then, each node updates its version of the blockchain. Now, one can wonder what happens if a node receives two different mined blocks at the same time?

The node will fork the blockchain and have two versions of it and he will keep accepting blocks for both chains. As long as they have the same length, the node will choose to work on one of the chains but if one chain becomes longer, the node will keep it and forget the other one.

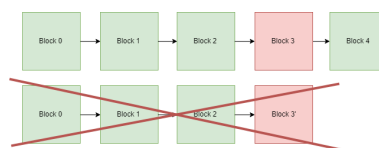


Figure 1.6: Fork chains

The blockchain is always the longest chain created because it's the one that has required more mining work. This means that to have control over the blockchain, an attacker should have the majority of the computational

power (at least 51%).

C++ code As we said, the network is composed of miners so we implement miners as an object with the following fields:

- An ID
- A vector of string to describe his mempool.
- A vector of blockchains to describe his versions of blockchains including forks.

```
class Miner {  
  
private:  
    int id; //Miner's ID  
    vector<string> memPool; //List of transactions  
    vector<Blockchain*> blockchains; //Blockchains (sorted by length)  
}
```

A miner can fill a new block with transactions from his mempool, mine a block and add a block to one of his blockchains.

Miners also have some functions to communicate through the network. For example, to serialize and deserialize blockchains (because only serializable objects can be sent in the network) or to handle a block the miner received.

Finally, blockchains are represented as linked lists with basic operations like adding a block or consult the last block.

```
class Blockchain {  
  
private:  
    Block* head; //The head of the blockchain, i.e the last mined block  
    int blockID = -1; //Block ID of the more recent block  
}
```

1.2.6 Bitcoin Block example

Bitcoin blockchain is public, we can follow the evolution on web sites like www.blockchain.com ([2]). We can see the fields we described and some other details, for example:

Summary	
Height	573522 (Main chain)
Hash	0000000000000000021d691b53c5fd815f3c87b2681ba0d5410245769515ad1
Previous Block	0000000000000000000016b35a6ede34250eb4ab437c19a3890cd233d4e01dc7f3
Next Blocks	000000000000000000001fd325c4ad75768248fc8b38c3239ad86d03db7702ed40
Time	2019-04-27 21:19:37
Difficulty	6,353,030,562,983.98
Bits	388779537
Number Of Transactions	2824
Output Total	1,060.84986755 BTC
Estimated Transaction Volume	260.30901865 BTC
Size	1148.763 KB
Version	0x20000000
Merkle Root	e33ebb8eee10f32cb071b4d0d6f11f0e69fa2a033532d80c7b6458c7fccb821e
Nonce	2454731301
Block Reward	12.5 BTC
Transaction Fees	0.10361587 BTC

Figure 1.7: Example of a Bitcoin block

More precisely, hash functions, like SHA256, hold three properties:

1. Pre-image resistance: knowing y_1 , it's difficult to find x_1 such that $h(x_1) = y_1$.
2. Second pre-image resistance: knowing x_1 , it's difficult to find x_2 such that $h(x_1) = h(x_2)$.
3. Collision resistance: it's difficult to find pairs (x_1, x_2) such that $h(x_1) = h(x_2)$.

1.4 Blockchain applications

Now that we've understood the principles of blockchains, we may wonder what are the main uses nowadays.

Why people use blockchains instead of other security methods? We can suggest a few reasons to answer this question (see [3]) :

- Blockchains are fast, secure and transparent. Moreover, history has proven its robustness since no attacks resulted from a weakness inside the blockchain itself.
- In general, people have a great opinion of it: 84% think it provided more security than other methods.
- One can estimate around 70% cost savings on business operation and 30 - 50 % on compliance.

What are the main blockchain applications? In the few last years, we've seen a lot of new blockchains being launched in different fields. We can have a look at some of them (see [4])

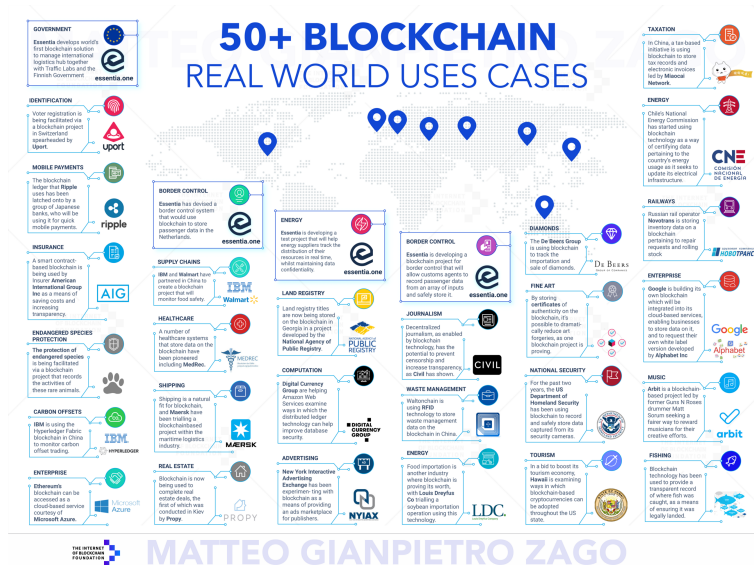


Figure 1.8: Blockchain uses in the world (see [Link to medium.com](#))

We see that blockchains may be used by governments for taxation and border controls, in the energy field and social field for insurance and healthcare.

We can take the example of Uport who created a platform based on Ethereum blockchain to register residents' ID (see [5]). They collaborated with the city of Zug (Switzerland) to allow residents to access eServices like online voting.

The first step for a Zug citizen is to create his digital identity on the Uport platform. He will have to fill a form with his data and to visit one of the Zug offices in person to cross-check his digital identity. Then, he will get his credentials to access Zug eServices.

The city of Zug planned to develop its service of online voting in Spring 2018 using this new technology. Eventually, blockchains could facilitate a lot the interactions between people and governments.

Chapter 2

Blockchain simulation

As explained in the previous chapter, we've created classes to represent some features related to blockchains. Thus, we can instantiate miners, blocks, block headers and blockchains.

2.1 Sequential code

Then, the first version of the code is about making these objects to work together. This is a sequential version where, in the end, we have one miner able to create blocks, mine them and build his blockchain.

When the job is done, we display the state of the blockchain:

```
Block mined !!!
Block mined !!!
Block mined !!!
Block mined !!!
Block mined !!!
Block id : 498ee2102e...
      ^
      |
      | prev : 00005c598b24cd0d779fe3736bb939309be53bdd4c2720fccc6e7c3041c26ad3
      | target : 0000696f40000000000000000000000000000000000000000000000000000000
      |
      |
Block id : 5c598b24cd...
      ^
      |
      | prev : 00004bf3e1ab280434b8775bd1476415d19850cba39d76fb98cd1b6e8722be43
      | target : 0000696f40000000000000000000000000000000000000000000000000000000
      |
      |
Block id : 4bf3e1ab28...
      ^
      |
      | prev : 000063ffc09dfb29fb27119b731efcd7d71763d436d059516ea9845eb21df4aba
      | target : 0000696f40000000000000000000000000000000000000000000000000000000
      |
      |
Block id : 63ffc09dfb...
      ^
      |
      | prev : 00002afbd9585a3ccff4154bde28990344610e0f5a5042e6a7d4b8a57b833f68
      | target : 0000696f40000000000000000000000000000000000000000000000000000000
      |
      |
Block id : 2afbd9585a...
      ^
      |
      | prev : 71c6818d7b0f63728222fe1d39be96e1027bb901fac8a2ed8e59993098bef0e7
      | target : 0000696f40000000000000000000000000000000000000000000000000000000
      |
      |
Block 0 : 71c6818d7b...
```

Figure 2.1: Example of execution

We don't concentrate further in the analysis because the objective is to parallelize this code.

2.2 Parallel code

Transactions management As we mentioned, transaction management is simplified. So we decide to generate transactions with our specific generator and to communicate these transactions to all the miners.

Thus, the first challenge is to generate and broadcast transactions. We arbitrary choose the miner 0 to generate the transactions, then he will serialize and broadcast them to the other miners.

At the same time, we manage the reception of these transactions by the others miners. They deserialize them and push them to their mempool.

Communication through the network The most important challenge is to make the miners communicate about blocks they discovered. To do so, we created the following algorithm:

Algorithm 1 Communication between miners

```
while the mempool isn't empty do
  We fill a new block with transactions from the mempool
  while No message received && no block mined do
    We try to mine the block
    if Block mined then
      We write related information into a log file
      We broadcast the block mined
    end if
    We check for messages
    if Block received then
      Block reception algorithm (see below)
    else if Blockchain received then
      We add the blockchain to ours
      We sort our chains to work on the longest
    else if Blockchain request received then
      We send back the requested blockchain
    end if
  end while
end while
```

Algorithm 2 Block reception

```
for All our blockchains do
  if The new block is the next one then
    We add it at the end
  else if The new block is the last one then
    We do nothing
  else
    for All blocks in the chain do
      if The new block and the current one are the same then
        We sent back this chain
      else if The new block is the next of the current one then
        We create a forked chain including the new block
        We sort our chains
        We send our version of the chain
      end if
    end for
  end if
end for
```

2.2.1 Extra features

Tests It's important to regularly test our code, especially to check if the communications are complete because this kind of error is quite hard to detect. There are some dedicated libraries to test our code but, in our case, we used a direct way by implementing controls to test our functions and print the results so we can check the correctness of our system.

We can test sending and receiving a block, a blockchain or an empty blockchain. This increases our confidence in the code robustness.

Frequency estimation We've seen that the computational power of a miner is important because the higher his computational power the faster it will mine. Then, we created a code to estimate the frequency of a miner.

To estimate the frequency, we use the instruction RDTSC (Read Time Stamp Counter) which reads the value of the register TSC. This register counts the number of cycles since the last reset. So we use the following algorithm to compute the number of cycles in 1 second:

Algorithm 3 Frequency estimation

```
int nbCycle = rdtsc()
Wait for 1 second
frequency = rdtsc() - nbCycle
```

Logs All along the code, we write information in the log files to help analyze the blockchain at the end. For example:

- [freq] 2.4225 → Indicates the miner computational power in GHz.
- [Tue Jul 23 17:40:48 2019] 3fd2146979 26027 → Indicates the miner has mined a block with the exact time, the block ID and the duration in milliseconds.
- [nbChains] 1 → Indicates the number of forked chains the miner has made.
- [i] 47a9270fb6 → Indicates the beginning of the ith chain and its first block.

```
[freq] 2.4225
[Tue Jul 23 17:40:48 2019] 3fd2146979 26027
[Tue Jul 23 17:42:48 2019] 34e26d6493 145406
[Tue Jul 23 17:43:50 2019] 1d73180563 207477
[Tue Jul 23 17:44:55 2019] 5ed3889ceb 272771
[Tue Jul 23 17:46:30 2019] 253a7f3b44 367423
[nbChains] 1
[0] 47a9270fb6
253a7f3b44
4eee424737
36845c7579
67611329fc
```

Figure 2.2: Example of a log file

We also write a general log file with the following data:

- [nbTransactions] 1000 → Indicates the number of transactions.
- [nbProc] 20 → Indicates the number of miners.
- [difficulty] 3 → Indicates the difficulty for the target (i.e. the number of zeros required at the beginning of the hash).
- [finalTime] 389194 → Indicates how long it took to complete the execution in milliseconds.

2.3 Results

Reading the logs

1. We read the file with the general data: nbProc, nbTransactions, difficulty.
2. We read the file of each miner to get his frequency, the block mined and the blockchains.
3. From the longest chain, we determine which miner has won a reward.
4. We extract the data to display the timeline of the longest blockchain.
5. We extract the times where the blocks were mined to compute statistics.

In the end, we display a table summing up the rewards and the forks of each miner, another table with statistics about the time needed to mine blocks and a timeline of the blockchain 10 blocks by 10 blocks.

The following results were produced on the Geneva University cluster with a target starting with 5 zeros.

Analysis of the rewards and forks table This table is interesting in two points:

1. To analyze if the frequency and the number of rewards are correlated. The more a miner has computational power, the faster it should mine.

In our case, all miners have the same frequency because they were all located on the same node of the cluster.

2. To observe the number of forks because this number is directly linked to the number of messages. If the number of forks is low, it means the consensus was obtained straight forward. On the other hand, if this number is high, it means the miners exchanged a lot of messages and probably wasted time on mining blocks which were finally not in the longest chain.

In our case, we see the number of forks is 1 for all miners so it means that our algorithm is efficient.

Name	Freq	Rewards	Forks
'Proc 1'	2.1949	0	1
'Proc 2'	2.1949	5	1
'Proc 3'	2.1949	0	1
'Proc 4'	2.1949	1	1
'Proc 5'	2.1949	0	1
'Proc 6'	2.1949	0	1
'Proc 7'	2.1949	0	1
'Proc 8'	2.1949	2	1
'Proc 9'	2.1949	1	1
'Proc 10'	2.1949	0	1
'Proc 11'	2.1949	0	1
'Proc 12'	2.1949	4	1
'Proc 13'	2.1949	1	1
'Proc 14'	2.1949	0	1
'Proc 15'	2.1949	1	1
'Proc 16'	2.1949	0	1
'Proc 17'	2.1949	1	1
'Proc 18'	2.1949	0	1
'Proc 19'	2.1949	0	1
'Proc 20'	2.1949	4	1

Figure 2.3: Rewards won by the miners

Analysis of the statistics table We can observe that the range is quite wide, from ≈ 9 minutes to 7 seconds, it means that some miners mined a block very quickly whereas some others took more time. This is because we choose the nonce in a uniform distribution so it's completely possible to obtain a right nonce after a few tries only.

We can also note that the average time to mine a block is around 1 minute and 48 seconds, it's an arbitrary choice compared to the 10 minutes for the original blockchain.

Unit	Minimum	Maximum	Range	Mean	Median
'seconds'	7.302	535.63	528.33	113.97	65.103

Figure 2.4: Statistics about the time needed to mine a block

Analysis of the timeline We want to see the evolution in time of the longest chain produced by our system. We display the blocks, 10 by 10, according to the time they were mined.

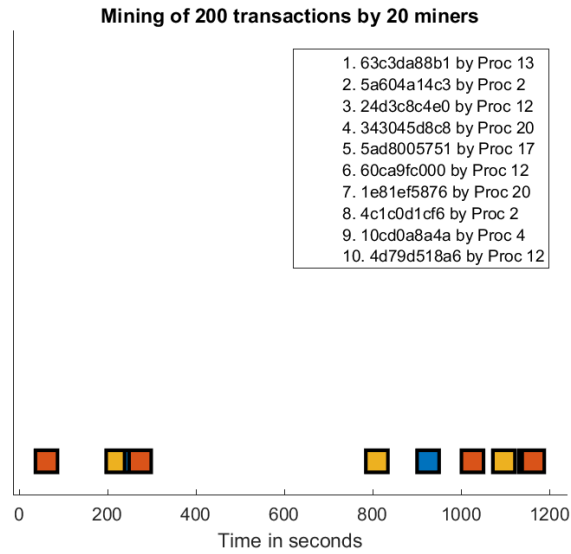


Figure 2.5: Timeline for the 10 first blocks

2.4 Can we improve our model?

Here are some ideas to improve our simulation:

- The possibility to choose the network structure. To do so, we could use an adjacency matrix:

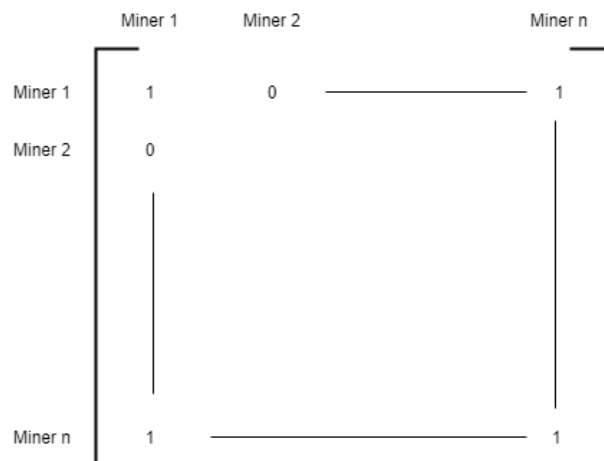


Figure 2.6: Example of an adjacency matrix

An adjacency matrix is symmetrical and 1 in the position (i, j) indicates that the miner i and j are neighbors. For example, in the figure above, the miner 1 and n are neighbors but not the miner 1 and 2.

With this method, we could try several network structures and analyze their influence on the mining process.

- The possibility to create pools. We could create a function which defines if a miner belongs to a pool or not:

$$isInPool(miner) = \begin{cases} 0, & \text{if the miner doesn't belong to a pool} \\ i > 0, & \text{if the miner belongs to the pool } i \end{cases}$$

Then, when a miner successfully mined a block, we share the reward with the pool if he belongs to one. With the method, we could try to implement the 51% attack.

- Implementing the selfish mining attack. We've implemented the finite state machine which models this attack but we could also try to implement this algorithm for real to observe the results match.

Chapter 3

Breaking mining if SHA256 is compromised

We know that mining is based on SHA256 so, in this part, we'll see different techniques (inspired by [1]) to defeat traditional mining if SHA256 is broken.

3.1 Pre-image with fixed Merkle root

First, we analyze the probability for an attacker with a pre-image oracle to break mining, i.e. to get a high probability of solving the PoW before the other nodes in the network.

If we suppose we can have a pre-image oracle for SHA256, then we will be able to build an oracle for $H_M(x) = SHA256(SHA256(x))$ by applying the first oracle twice.

3.1.1 Input set of H_M

As explained before, a miner applies the hashing operation $H_M(x)$ to the block header. A classic miner only controls the value of the nonce but an attacker will try to control more.

The version, the previous block's hash and the Merkle root are fixed fields.

For the time field, the system allows a range of 7200 seconds around the current time. So, over the 32 bits dedicated to this field, an attacker will be able to control about 13 bits.

For the target, the protocol will check if the target value is at most the one defined by the consensus of the network, this means the attacker can control about 28 bits.

For the nonce, like any miner, the attacker can control the 32 bits allowed to it.

The block header's size is $4 + 32 + 32 + 4 + 4 + 4 = 80$ bytes = 640 bits.

An attacker can control $b = 13 + 28 + 32 = 73$ bits on the input value, which means he has 2^b possibilities to call the hash function H_M .

3.1.2 Output set of H_M

The result of H_M is a hash from SHA256, so it has a length of $n = 256$ bits and there are 2^n possibilities of outputs.

Then, in order to fulfill the condition given by the target, the hash needs to start with a specific number of zeros, let's note d zeros.

In reality, matching with the coefficient may require more effort (see A for more details).

This means that there are 2^{n-d} hashes lower than the target.

3.1.3 Probability of breaking mining

By calling H_M , one has a probability of $\frac{2^{n-d}}{2^n}$ to get a valid hash.

That way, we can get the number of correct pre-images i.e in the input set, how many inputs will end as a correct hash.

$$proba_of_correct_hash \times \#possible_inputs = \frac{2^{n-d}}{2^n} \times 2^b = 2^{b-d} \quad (3.1)$$

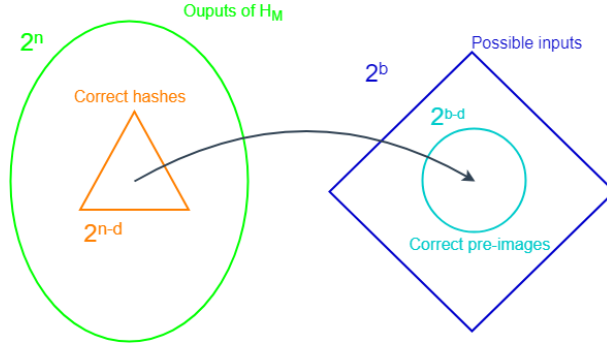


Figure 3.1: Probability of getting a correct pre-image

In his attack attempt, the attacker queries the pre-image oracle for specific target hashes. So he will choose a correct hash (triangle set) and hope that the output is one of the correct pre-images. This is the probability that he gets an accepted pre-image.

$$\frac{\#pre-images}{\#accepted_outputs} = \frac{2^{b-d}}{2^{n-d}} = 2^{b-n} \quad (3.2)$$

Then, to get the real probability of success, we need to add a constraint on the number of queries allowed to the attacker. Because, otherwise, the attack won't be faster than traditional mining. So let's consider the attacker can query the oracle 2^a times.

$$P_{success} = 2^a \times 2^{b-n} = 2^{a+b-n} \quad (3.3)$$

Finally, we can estimate this probability of success. Let's take $a = 80$ so the attacker has 2^{80} tries (above this value, he may need more than 10 minutes to complete his attack). So, we have $P_{success} = 2^{80+73-256} = 2^{-103} \approx 10^{-32}$, which is completely negligible.

Then, we can conclude that having a simple pre-image oracle doesn't help to break mining.

3.2 Pre-image with variable Merkle root

3.2.1 Random Merkle root

In the previous section, we've assumed that the Merkle root is a fixed field because we've supposed that the list of transactions was also fixed.

But an adversary could try to work backward, to choose a random Merkle root and to try to reconstruct the Merkle tree leading to semantically valid transactions. By contrast with the previous method, the transactions are created by the attacker himself. However, even without figuring out any probabilities, we can conclude that this method is infeasible. That's because the reconstructed transactions will have to contain valid outputs and valid signatures.

3.2.2 Coin base transactions

However, there is an exception for the previous remark based on two observations. First, the system doesn't have a constraint about the number of transactions in a block and second, each block has a coinbase transaction, which creates money as a reward for the miner.

An attacker could create a block with only a coinbase transaction. These transactions have a fixed prefix and suffix and they have a length-variable field up to 100 bytes, scriptSig.

Then, the attacker can create a valid block by finding a valid Merkle root: $h(a||x||b) = T$, where x is the Merkle root, T is the target and a and b are the prefix and suffix of the block header. Finally, he'll have to solve: $h(b||y||d) = x$, where y is the scriptSig and b and d are the prefix and suffix of the coinbase transaction. So the Merkle root match with a valid transaction. ($||$ means concatenation)

Both predictions will have a pre-image with high probability but if not, the attacker can try with another target or with different lengths for the scriptSig. Nevertheless, his probability of success is very high.

3.3 Bounded pre-image oracle

3.3.1 Construction of the oracle

In reality, a hash function breakage can imply more powerful tools than a simple pre-image oracle. To cover this possibility, we can construct a general oracle (see [1]).

This oracle takes as input : $(a, b, y_l, y_h, i, s) = (prefix, suffix, target_low, target_high, position, length)$. It will return x_i such that : $y_l \leq h(a||x_i||b) \leq y_h$ or none (if there is no pre-image).

In other words, the prefix, suffix and length of the pre-image are fixed, this allows us to have control over the format of the pre-image and, in our context, to fix some fields of the block header. The value will be between a target range, this will help us satisfy the condition given by the target.

The position of the pre-image is also specified, this means the same x_i is returned on each call and a call on j will return $x_j \neq x_i$.

Technically, the suffix is added to keep a symmetry but it's not needed for our attack. Moreover, in reality, this is usually the hardest part of the oracle to setup.

3.3.2 Attacks against mining

An attacker with access to our bounded oracle can simply call for $(headerBeginning, none, 0^{256}, target, 0, 32)$.

For recall, the target is 256 bits long, the block header is 32 bits and the headerBeginning is the beginning of the block header until the nonce. This will return a pre-image of 32 bits with the first fields of the block header and a correct nonce such that the hash is under the target value.

This kind of attack will completely break mining, which allows the attacker to create deep forks and then, reverse transactions or double-spend.

3.4 Second pre-image and collision

We've seen in the previous section vulnerabilities linked to pre-images. Let's have a look at second pre-images and collisions.

3.4.1 Attacks on blocks

Second pre-image Let's recall the theory about second pre-images: for a specific hash given by a specific input, a second pre-image oracle allow us to find another input giving the same hash.

In our context, one could want to replace a block by a new block with the same hash to maintain the blockchain valid, this way one could completely modify the blockchain.

However, this is concretely infeasible because more than just the hash, the new block has to be valid in terms of transactions. This means the transactions have correct inputs and correct signatures, the probability that the new block respects these constraints is almost zero.

Collision For collisions, the idea would be to create several blocks with the same hash and to insert them in the network. This would allow an attacker to be able to fork the chain and possibly double-spend or steal coins. However, following the same remark we did for second pre-images, the probability to create valid blocks is negligible.

To conclude, collisions and second pre-images are irrelevant to break mining.

3.4.2 Merkle roots

As recall the hash function H_M is also in Merkle trees, then one could alter already mined blocks by changing transactions but with the same Merkle root.

Blocks inside the blockchain This idea would be to change the transactions in a block by getting a Merkle root with the same hash. As we expose before, the probability of getting valid transactions is very low. So the nodes will reject the modified block.

New added blocks However, the situation is different if the adversary focuses on the last block. The attacker can create a new block with different transactions but the same Merkle root. Even if, this newly created block is invalid, the attacker can send it to the network and this may cause the nodes to reject both blocks or even to accept the invalid block.

This attack was done in July 2015 ([6]), nodes were accepting invalid blocks and then, validating wrong transactions. Nowadays, a new version of the protocol has been released and these problems are solved.

The adversary can also double-spend coins by creating a new block with conflicting transactions according to the valid block using a collision or second pre-image oracle. Then, he can transmit both blocks in the network, this will fork the blockchain and may fool the vendor.

3.5 Conclusion

3.5.1 Consequences summary

We can sum up the different consequences of breakages on SHA256.

<u>Breakage</u>	<u>Consequences</u>
Pre-image	Complete breakage of the blockchain
Bounded pre-image	Complete breakage of the blockchain
Second pre-image	Double spending, steal coins
Collision	Double spending, steal coins

3.5.2 Contingency plans

All the attacks presented above are based on potential SHA256 vulnerabilities. We cannot guarantee that SHA256 will stay safe forever. However, we can notice it was created in 2001 and no significant weaknesses have been discovered yet so we can conclude SHA256 is quite robust (see a StackExchange conversation about SHA256 security, [7]).

In case SHA256 is broken, Bitcoin has a contingency plan (see [8]).

As we've seen this situation would be dramatic, an attacker could compromise the whole system, this includes the alert system.

The plan in this situation is to ask the users to shut down their clients and to hardcode the public keys of all addresses that have unspent outputs. Then, these keys will be used when a new version of the blockchain is released.

The code for all of this should be prepared but, in reality, this is not the case because, even if the consequences would be severe, the risk is very low.

Chapter 4

Attacks using mining weaknesses

In the previous chapter, we've seen that mining is based on SHA256 and we've analyzed the consequences if SHA256 is broken. In this chapter, we'll try to find some weaknesses in mining and use them to fool the process.

4.1 Double-spending

One of the very famous technic to trick a seller is called double-spending. As explained in [9], a double-spending attack is used by a buyer to foul the seller, following the next steps :

1. The buyer A broadcasts a transaction AB in the network where he pays seller B.
2. The buyer A creates another block with a transaction \overline{AB} which invalidates transaction AB.
3. The buyer A secretly mines a branch on this new block.
4. The buyer A waits that seller B sends his product.
5. Once the buyer's branch is long enough, he broadcasts it which will deny transaction AB.

With this method, the attacker uses his bitcoin twice, that's why it's called double-spending.

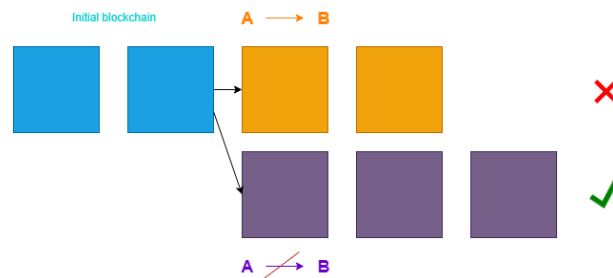


Figure 4.1: Double-spending - The longest chain will be the purple one which invalidates the bitcoins sent to B while the seller has already sent his product

4.2 51% attack

4.2.1 What is it?

The main difficulty to achieve this attack is to be able to build a longer chain to invalidate the transaction which gives bitcoins to the seller. One possible solution is the 51% attack.

The 51% attack has always been an important concern about blockchains' security. The main idea is that an attacker will control the majority of the computational power, i.e. at least 51%.

The ability of someone controlling a majority of the network hash rate to revise transaction history and prevent new transactions from confirming. (Bitcoin glossary [10])

In other words, an adversary with at least 51% of the network will be able :

- To prevent some users to do transactions, by systematically denying their transactions. Because the attacker controls the majority of the network, even if some nodes confirm the user's transaction, it will never be part of the longest chain.
- To reverse his transactions, this is double-spending.

4.2.2 Is it possible to implement it?

For Bitcoin To set a 51% attack up, an attacker needs to gather enough mining computers to get more than 50% of the computational power of the actual network.

Moreover, the attacker will have to supply enough electrical power to run those computers.

Now, the real question is how much will it cost. We can try to estimate the cost for Bitcoin (see [11]).

First, buying specialized computers for mining will cost about \$2.4 million and \$250 million in infrastructure to install these computers and the equipment needed (like ventilation).

Then, to power this structure, one will need around 30 Terawatts of electricity per year. For example, Morocco consumed 29 Terawatts in 2017 and Switzerland consumed 63 Terawatts the same year. All this electricity will cost around \$2 million by day.

To sum up, a 51% attack against Bitcoin will cost \$1.4 billion. This makes the attack almost impossible due to this huge cost, even for a large state-sponsored organization, it will be very complicated to set up this attack.

What about other blockchains? We've studied the feasibility of Bitcoin which is one of the most famous blockchains nowadays and its network is now very large. But one can wonder if the threat is more important with smaller blockchains.

Indeed, the cost for a 51% attack decreases for smaller coins. However, for every serious blockchain, there are still thousands or millions of nodes and anyways, it would more profitable to mine honestly and win coins through rewards.

On [Crypto51](#), we can observe the cost to make a 51% attack on different cryptocurrencies.

Name	Symbol	Market Cap	Algorithm	Hash Rate	1h Attack Cost	NiceHash-able
Bitcoin	BTC	\$208.66 B	SHA-256	71,147 PH/s	\$1,104,830	0%
Ethereum	ETH	\$31.62 B	Ethash	157 TH/s	\$160,091	6%
Litecoin	LTC	\$7.81 B	Scrypt	468 TH/s	\$77,561	3%
BitcoinCashABC	BCH	\$7.45 B	SHA-256	2,543 PH/s	\$39,483	3%
BitcoinSV	BSV	\$3.59 B	SHA-256	923 PH/s	\$14,338	7%
Monero	XMR	\$1.50 B	CryptoNightR	342 MH/s	\$6,884	5%
Dash	DASH	\$1.41 B	X11	5 PH/s	\$6,598	6%
EthereumClassic	ETC	\$867.77 M	Ethash	7 TH/s	\$7,622	119%
Zcash	ZEC	\$712.02 M	Equihash	5 GH/s	\$19,835	6%
BitcoinGold	BTG	\$466.69 M	Zhash	4 MH/s	\$1,964	26%

Figure 4.2: Crypto51

Then, the probability remains low especially for the biggest blockchains. However, it can still happen (see [12]). For example, EthereumClassic was attacked in January 2019 and it lost almost \$1.1 million in one day.

Preventing this attack can be very complicated but there are still some ideas :

- Merging mining. Smaller cryptocurrencies can use mining power of larger ones so they become less vulnerable.
- Penalizing delayed blocks. The attacker mines blocks secretly and broadcasts them lately, a penalty will reduce the benefit of the attack.

- A detection algorithm for the 49% left. Once the attack is detected, the 49% left can try to acquire more power to stop the attack.

4.3 Selfish mining

In the previous section, we've considered an attack to trick vendors by taking advantage of the system. Now, we will study a method to trick the system itself.

As we mentioned before, a node wins a reward when he successfully mines a block and adds it in the blockchain, the node earns the rewards as long as his block is in the blockchain.

We will present the method of selfish mining, where miners try to increase their rewards allowed for mining (see [13]).

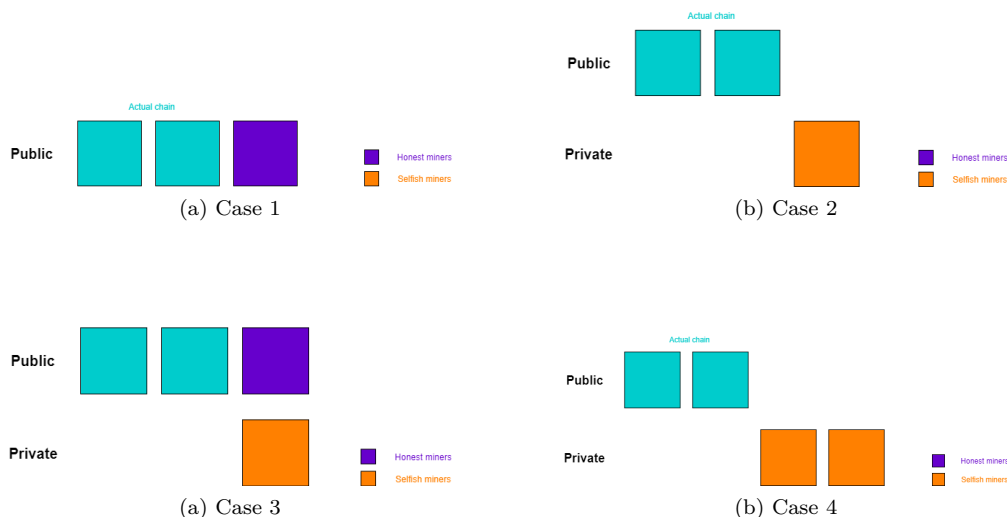
4.3.1 What is it?

First, let's suppose that all the computational power is divided into two groups: the first group follows the selfish mining strategy and the second group follow the classic mining strategy.

The main idea of selfish mining is to mine secretly blocks in advance so the miners create a longer chain than the others. Then, at the right time, they reveal their chain which will become the new longest chain, so they win the rewards and waste the work of the other miners.

Let's see in details how this strategy works, there are four important cases:

- Case 1: The honest miners find a new block on the public chain, the selfish miners will just adopt the new chain.
- Case 2: The selfish miners find a new block on the public chain, they will keep this block secret and then, there are two possibilities (Case 3 or 4).
- Case 3: The selfish miners have secretly one block in advance but the honest miners find a new block first and broadcast it, in that case, the selfish miners broadcast their secret block immediately. Since two blocks are broadcast almost at the same time, miners will have to choose which block they mine after. All the selfish miners will mine after their block, and the honest miners will mine on the first they receive. Let's note γ the proportion of honest miners who mine after the selfish miners' block.
- Case 4: The selfish miners have secretly one block in advance and they find a new one, so they keep this new block secret. Then, they will try to keep two blocks or more in advance the longest time possible. If they only have one block left, they publish their secret chain.



4.3.2 Is it feasible?

As we've just seen, this strategy is based on the fact that the selfish miners succeed in mining blocks ahead of the honest miners. To do so, it's obvious that their combined computational power will affect their chance of success, let's note α the computational power of the selfish miners.

As described in [13], we can represent the selfish mining algorithm with a finite state machine.

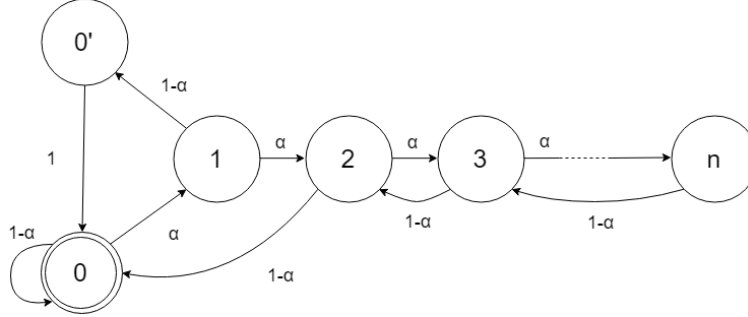


Figure 4.3: Selfish mining finite state machine

In this machine, the initial state is the state 0 and it corresponds to case 1. The state 1 corresponds to case 2, the state 0' to case 3 and the states 2 and more correspond to case 4.

We can compute the probabilities of this state machine, we note p_i the probability of being in state i . From these probabilities, we can compute the rewards the selfish and honest miners will win.

We can find more explanations about the formulas in this appendix B.

$$r_honest = p_0.(1 - \alpha).1 + p_{0'}.\gamma.(1 - \alpha).1 + p_{0'}.(1 - \gamma)(1 - \alpha).2$$

$$r_selfish = p_{0'}.\gamma.(1 - \alpha).1 + p_{0'}.\alpha.2 + p_2.(1 - \alpha).2 + P[i > 2].(1 - \alpha).1$$

Table 4.1: Revenue won by the honest and selfish miners according to α and γ

We can implement this finite state machine and try some values of α and γ .

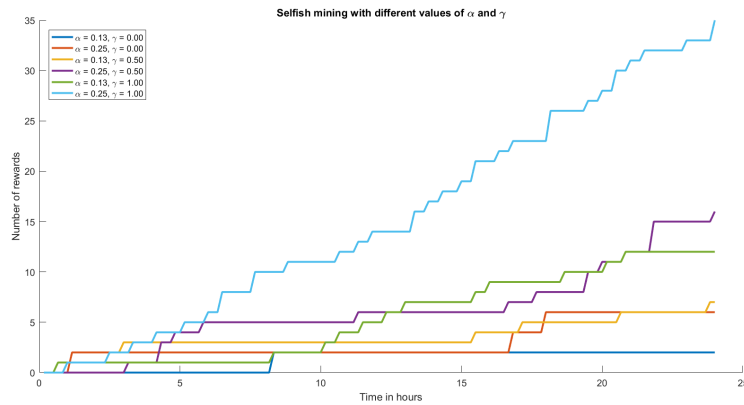
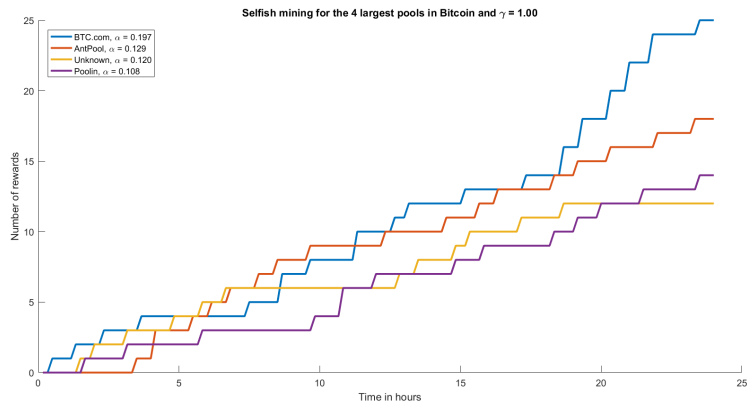
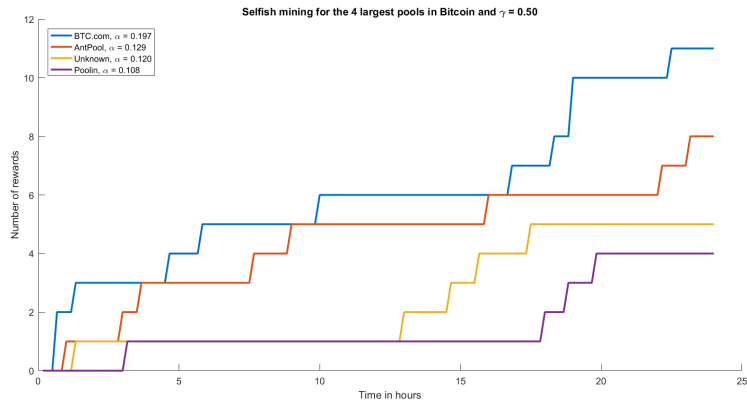
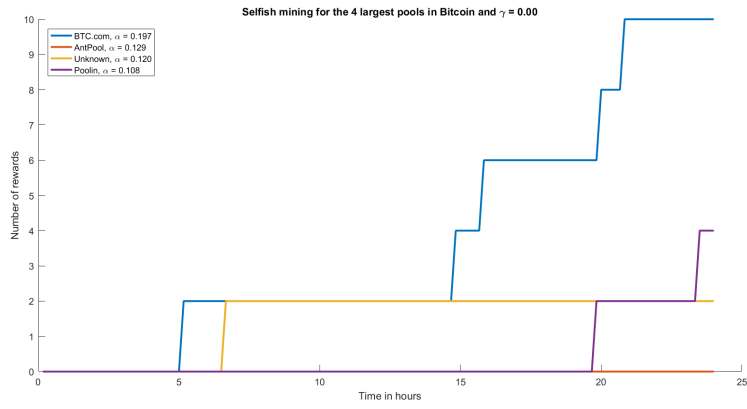


Figure 4.4: Rewards according to different α and γ

We see that γ and α are linked because the more γ increases the more the pool size α needs to increase to win the same reward. Let's try several values of γ with the hash rates of the four largest pools in Bitcoin network (see [14]).



We can see that the pools will be able to win more if they can propagate their blocks fast enough, i.e. if γ is high enough.

Now, we need to know if it's worth the effort against the honest mining, to do so we can analyze the link between α and γ in the formulas for the revenues (Table 4.1) as it was done in [13].

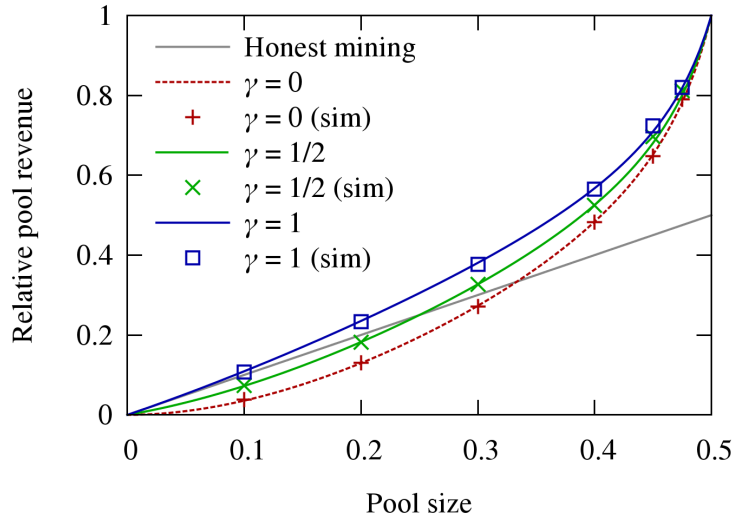


Figure 4.5: Revenue of the selfish miners for different values of α and γ

This figure shows the importance of γ . With a high γ , the pool will propagate its blocks to the whole network very quickly so the selfish mining strategy will be efficient.

However, with a low γ , the honest miners will propagate their blocks quickly. If we take the extreme case of $\gamma = 0$, we'll need a pool with around 35% of the mining power. For Bitcoin, the largest pool has 19.7% of hash rate (see [14]) so it seems secured for low γ .

In Bitcoin, the protocol doesn't ensure that γ , which represents the propagation rate of the pools' miners, will stay low. This is because when an honest miner has several chains of the same length, he will choose to mine the first block he receives. Then, a pool can perform a Sybil attack, they use virtual miners who won't mine but when they detect that the honest miners have mined a new block, they propagate the pool's block so it will be broadcasted faster and increase γ .

A solution to this problem would be to change the protocol and force the miners to choose randomly between chains of the same length. This would lead to $\gamma = 1/2$ and it would require a pool with 25% of hash rate, which is hard to achieve in practice.

Chapter 5

Quantum computing and blockchains' security

Since the 1990s, quantum computing has become an important field of research in computer science. In 1998, we've seen the first quantum computer with 3 qubits and since then a lot of improvements and researches have been done to build a stable quantum computer.

Let's anticipate the possible apogee of the quantum era and study how it could affect blockchains' security.

5.1 What is Quantum computing?

Quantum computing differs from classical computing by the way it stores and manipulates information.

Let's have a quick reminder of how a classic computer works.

They use bits to represent data, a bit can be either 0 or 1. Those two states are represented through an electrical signal.

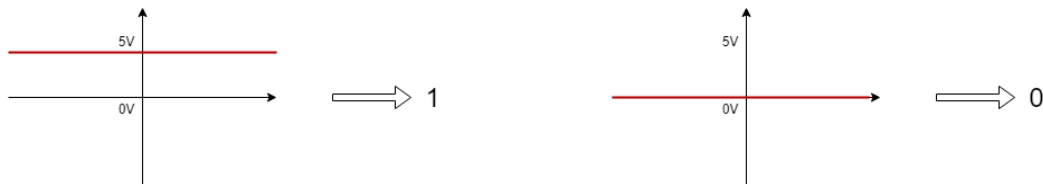


Figure 5.1: Coding of a bit

We process these signals with transistors to make logical gates, this is the basics of processors and computer architecture. To represent complex data, we create registers made of several bits. For example, a n-bits register can represent 2^n values/states.

Now, what about quantum computing? (see [15]) As the name suggests, this new technology is based on quantum physics, the big difference with classic computers is that there aren't bits anymore but qubits or quantum bits.

These qubits are not binary, either 0 or 1, but they exist in a superposition of 0 and 1. This is the superposition principle, we can understand it as probabilities so we commonly describe a qubit with the following formula:

$$|x\rangle = \alpha \cdot |0\rangle + \beta \cdot |1\rangle \quad (5.1)$$

where α is the probability for 0 and β is the probability for 1.

Mathematically, we can interpret these different states as coexisting but physically they're not, this is because quantum physics is not deterministic but probabilistic so we can't measure it precisely.

It's important to highlight that a quantum computer isn't an evolution of classic computers like clusters can be. A whole new technology is involved in heading to a new way of representing and manipulating data.

We won't go too far in the details about quantum physics and qubits but we can investigate two interesting questions.

How do we physically build a qubit? There are different possibilities to build a qubit, we need to use a two-level system, a system where a quantum superposition can exist. For example, we could use photons and light polarization, where we measure how much the light is vertically or horizontally polarized.

One famous method is to use spins of the electrons (see [16]) where we measure the spin angular momentum to describe the quantum state of the electron. This spin can be affected by the magnetic field around the particle.

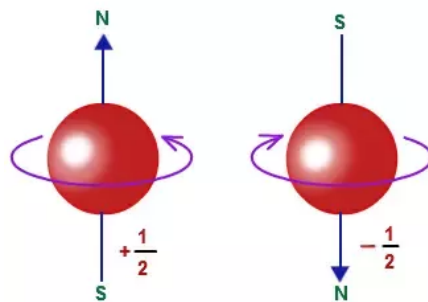


Figure 5.2: Electron spin from [17]

These methods are more complicated than electric signals for classic bits, it's harder to keep the quantum bits stable. Researches are working on the stability of qubits to build bigger computers.

How can we recover the state from a qubit? Quantum computers follow a rule called "Wave function collapse", which says that a superposed state can't be known entirely, we can only measure it and so reduce it to one value.

This means that even if we have a 2^n superposed state, we will reduce it to one result. Then a quantum computer can be used only for specific problems with specifically designed algorithms like Grover algorithm.

To conclude, a quantum computer will always be less polyvalent than its classical equivalent but it can be so much powerful for some specific problems. For example, it can be used for prime factorization, Peter Shor a scientist from Bell's lab found a quantum algorithm that could solve this problem.

5.2 Is quantum computing a treat to blockchains' security?

Now that we have a better idea of how a quantum computer works, let's try to figure out how to hack the mining process with a quantum computer (see [18]).

For recall, the goal of mining is to find a nonce so the hash is lower than a specific target. The nonce is a 4-bytes value, so to use quantum computers to solve this problem, we'll need 4 qubits or 32 qubits. A block header is 80 bytes so we'll append the 4 qubits to 76 regular bytes and we'll get a 256 bits result.

Nowadays, quantum computers are not as easy to program as classic computers because quantum computers don't use the same logic gates so we'll need to build the circuit corresponding to our algorithm.

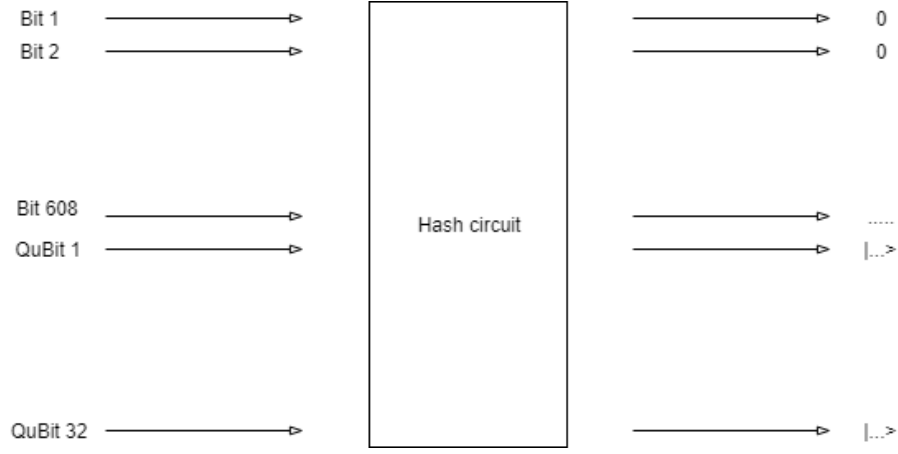


Figure 5.3: Circuit to build to hack mining

But here we have a problem, with a quantum computer, it's quite easy to find the final hash lower than the target but, due to the wave function collapse, we can't find which value of the nonce gave this output but it's exactly what we're looking for.

With the qubits, we can simultaneously have all the hashes with all the possible values of the nonce. To find the right ones, we could loop through all the solutions but it won't be faster than traditional mining so it's back to square one.

5.2.1 Grover algorithm

A solution to this problem is Grover algorithm (see [19]) which reduces the complexity to search in N values from $\mathcal{O}(N)$ to $\mathcal{O}(\sqrt{N})$.

The goal is to find a solution in a list of N values, the solution is defined by a function f where:

$$f(x) = \begin{cases} 1, & \text{if it's the solution} \\ 0, & \text{otherwise} \end{cases}$$

We have a list of N values so the numbers can be described this way:

$$\langle \Psi | = c_0 \cdot \langle 00...0 | + c_1 \cdot \langle 00...1 | + \dots + c_{N-1} \cdot \langle 11...1 | = \sum_{i=0}^{N-1} c_i \cdot \langle i | \quad (5.2)$$

where $\sum_{i=0}^{N-1} |c_i|^2 = 1$.

Grover algorithm follows these steps:

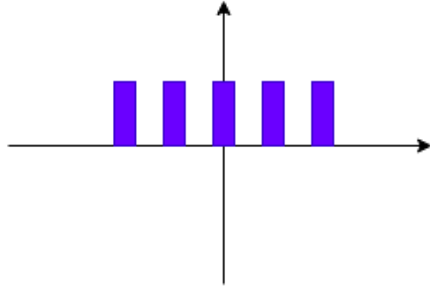
1. It creates a uniform superposition over all states:

$$\langle \Psi |_{initial} = \frac{1}{\sqrt{N}} \sum_{i=0}^{N-1} \langle i |$$

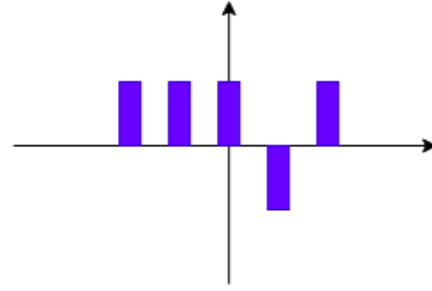
(We would like $\langle \Psi |_{final} = \epsilon \cdot \langle 00...0 | + \dots + (1 - \epsilon) \cdot \langle solution | + \dots + \epsilon \cdot \langle 11...1 |$)

2. It applies an operator to inverse the phase of the solutions.
3. It applies an operator to increase and decrease magnitudes, it corresponds to a mirror of magnitudes around their mean.
4. It repeats the two last steps $\approx \frac{\pi}{4} \sqrt{N}$

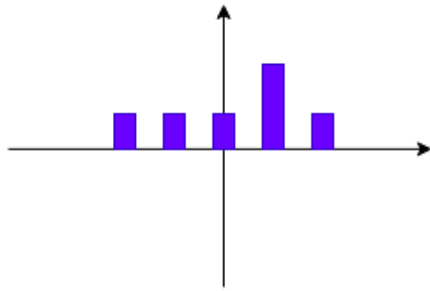
Next some schemes to illustrate the steps:



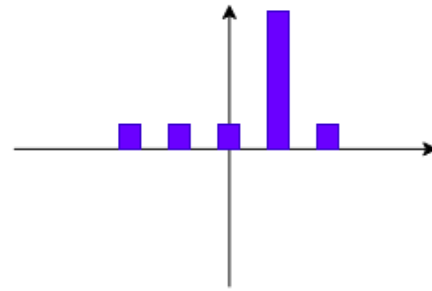
(a) Step 1



(b) Step 2



(a) Step 3



(b) Step 4 (after all iterations)

Now, with this algorithm, we can reduce the complexity to $\mathcal{O}(\sqrt{N})$. In our case, we have 32 qubits so there are $N = 2^{32}$ possible values then we have to search in $\sqrt{N} = \sqrt{2^{32}} = 2^{16} = 65,536$.

With this method, we have a theoretical solution to hack mining with a quantum computer, so it proves that quantum computing could be a real treat to blockchains security. It will depend on the evolution in the quantum field and the researches to improve the performances and stability of quantum computers.

5.3 How close are we to build a quantum computer?

We've just seen that quantum computing can be a serious threat to blockchains' security and cryptography in general. Now, we can wonder where are we in building a quantum computer?

As we mentioned, quantum computers come up with a physical challenge because qubits aren't stable (see [20]). Actually, there are different ways to implement a qubit but they are very sensitive to noise like temperature change or electrical fluctuation. A solution is to keep the circuits very cold, around the absolute zero (-273 degrees Celsius) but it involves large infrastructures.

So for now, there is still a need in research to put together large numbers of qubits (from a thousand to millions) but to keep it a reasonable size.

Then, when can we hope to see the first 'real' quantum computers? According to the recent improvements we made, we may think we're close to the apogee, but in fact, history has shown us that researches and advances take time.

Some had even predicted quantum computers before 2019 but with the work left to do, 10 years seems to be a reasonable estimation.

5.4 Do we have a contingency plan?

Let's have a look to the future and put ourselves in the quantum apogee. Actually, in parallel with the researches to develop quantum computing, some have found new algorithms and techniques to strengthen cryptography against quantum computers.

This new field of research is called post-quantum cryptography and some algorithms could be used to secure blockchains. In the actual version of the blockchain, we'll face two issues against a quantum computer:

- Signature breakage: because RSA algorithm used for signing transactions will be broken. An easy solution is to change the public / private key of the sender at each transaction, this is already a recommended practice.
- As we mentioned, mining will be in danger. A solution will be to change the proof of work to be quantum resistant (see [21]). Here are the basic properties we want for proof of work:
 1. An adjustable difficulty according to the network computational power.
 2. The PoW is difficult to find but easy to verify.
 3. No advantage for quantum computers to find the PoW faster than a classical computer.

Points 1 et 2 are already accomplished by the actual PoW. To satisfy point 3, an alternative is to base the difficulty to find the PoW not on computational power but memory.

For example, we could use Momentum, a memory intensive proof of work based on finding birthday collisions (see [22]).

Chapter 6

Conclusion

In this work, we've studied blockchains operation, then we focused our analysis on the mining process and we implemented a blockchain simulator to analyze and understand this process better. Our analysis was divided in three main chapters:

First, as mining is based on SHA256, we studied the threats involved in case SHA256 is compromised. However, the probabilities of such a situation are low and there are contingency plans to counter the problem.

Then, we've studied the robustness of the system by exploring some techniques like selfish mining or how to double-spend coins. Like the previous argument, the probabilities of success are low and would involve a lot of resources like computers, electrical power, ...

Finally, we tried to have a step ahead by looking at quantum technology. We discovered that it could represent an important threat to mining and blockchains' security. The challenge, to take advantage of this technology, is now to build a stable and powerful enough quantum computer and it may require a decade to reach this point.

To conclude on the security of the mining process, the different threats that we've studied are quite unlikely or not ready yet to be set up. Moreover, the security measures like the contingency plans allow us to trust this technology and explain its growing popularity.

Appendix A

Complements about the target

What does it imply to consider that the hash starts with d zeros?

To simplify the analysis, we can assume that the condition of having a hash lower than the target is equivalent to start by d zeros, where d is $256 - \text{exponent_length}$.

The "real" condition is harder to fulfill so how much work does it require if we only fulfill the second condition? Let's suppose we find a hash starting with d zeros:

$0...0a_1a_2a_3a_4a_5a_60...0$

and we have the following target:

$0...0c_1c_2c_3c_4c_5c_60...0$

There are 3 possibilities:

- $a_1 < c_1$: then the condition is fulfilled.
- $a_1 = c_1$: we look at the next the bit and we are in the same situation for c_2 , same for c_3 , ..., c_5 .
- $a_1 > c_1$: we need a more bit of effort to satisfy the condition.

For a_6 , if $a_6 = c_6$, we also need one more bit of effort to satisfy the condition. Finally, whatever the situation, we need only one more bit of effort.

Appendix B

Explanations about the revenues

In the chapter about selfish mining, we've calculated the revenues of the honest and selfish miners.

$$r_honest = p_0.(1 - \alpha).1 + p_{0'}.\gamma.(1 - \alpha).1 + p_{0'}.(1 - \gamma)(1 - \alpha).2$$

$$r_selfish = p_{0'}.\gamma.(1 - \alpha).1 + p_{0'}.\alpha.2 + p_2.(1 - \alpha).2 + P[i > 2].(1 - \alpha).1$$

Table B.1: Revenue won by the honest and selfish miners according to α and γ

Here are more explanations about these formulas:

$p_0.(1 - \alpha).1$	The honest miners find a block on the actual chain, they win 1 reward.
$p_{0'}.\gamma.(1 - \alpha).1$	The selfish and honest miners broadcast a block at the same time, then the honest miners find the next block after the selfish miners' one, the honest and selfish miners win both 1 reward.
$p_{0'}.(1 - \gamma)(1 - \alpha).2$	The selfish and honest miners broadcast a block at the same time, then the honest miners find the next block after their own one, so they win 2 rewards.
$p_{0'}.\gamma.(1 - \alpha).1$	The selfish and honest miners broadcast a block at the same time, then the honest miners find the next block after the selfish miners' one, the honest and selfish miners win both 1 reward.
$p_{0'}.\alpha.2$	The selfish and honest miners have both found a block, but the selfish miners find their next block first, they publish both blocks and they win 2 rewards.
$p_2.(1 - \alpha).2$	The selfish miners had a lead of two blocks but the honest miners find one, so the selfish miners publish their two blocks and they win 2 rewards.
$P[i > 2].(1 - \alpha).1$	Each time the selfish miners increase their lead above 2 blocks, they win 1 reward.

Table B.2: Explanations for the revenue of honest miners and selfish miners

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