PREPARE FOR TVCG 1

Nonobtuse remeshing with a guaranteed angle bound

Abstract—Quality meshing is an important problem in geometric modeling, visualization and scientific computing. In this paper, we propose a 3D triangular remeshing method with a *guaranteed* angle bound of $[30^{\circ}, 90^{\circ}]$. Given a original 2-manifold, open or closed, a rough approximate mesh with the proposed angle bound is first generated. This is achieved by a novel extension of the classical marching cubes algorithm. Next, an iterative constrained optimization, along with constrained Laplacian smoothing, decimation, and subdivision, is performed to arrive at a close approximation of the original mesh.

Index Terms—Remeshing, non-obtuse meshes, marching cube, deform-to-fit.



1 Introduction

The most commonly used shape representation is triangular mesh. Efficient rendering, finite element analysis, and geometry processing such as compression, smoothing and deformation benefit form high quality meshes. Thus, a lot remeshing methods have been proposed to improve the mesh quality [1], both in terms of geometry [2], [3] and connectivity [4], [5].

In terms of geometry quality, it is desirable for the triangular mesh to have no small angles and/or no larger angles, depending on the targeted applications [6]. For example, an essential condition of the accuracy of finite element solutions on triangular meshes is that the angle of any triangle, independent of its size, should not be small. This is called the minimum angle condition. Furthermore, both small and large angles can cause poor condition of the stiffness matrix [6]. For some applications, nonobtuse mesh, in which every angle is no larger than 90°, are desirable. Nonobtuse meshes result in more efficient and more accurate geodesic distances computation by fast marching method [7]. Also, nonobtusity ensures the well-known cotangent weights of discrete Laplace-Beltrami operator would be positive [8].

Thus, there have been lots of works on 2D triangulation with angle bounds and remeshing of curved surfaces with angle quality criterion. Chew develops a refinement scheme to ensure an angle bound of $[30^{\circ}, 120^{\circ}]$ based on constrained Delaunay triangulation [9]. Bern et al. propose an $O(nlog^2n)$ nonobtuse triangulating algorithm [10]. Cheng and Shi [11] use restricted union of balls to generate an ε -smapling of a surface and extract a mesh form the Delaunay triangulation of the samples points, where a lower angle bound of 30° can be obtained. A survey on

nonobtuse simplicial partitions is given in [12]. A novel obtuse triangle suppression method is proposed in [13] based on centroidal Voronoi tessellation.

In this paper, we extend our nonobtuse remeshing work [14] to the angle bound of $[30^{\circ}, 90^{\circ}]$. Furthermore, our method can preserve the sharp feature during the process of remeshing.

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2 CONCLUSION

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APPENDIX A PROOF OF THE FIRST ZONKLAR EQUATION

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APPENDIX B

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