

## Solution Problem Set III: Choosing Heuristics

1.

- $F = \{at(x, y), visited(x, y) \mid x, y \in \{0, \dots, m-1\}\}$
- $O = \{move(x, y, x', y'):$ 
  - Prec:  $at(x, y)$
  - Add:  $at(x', y'), visited(x', y')$
  - Del:  $at(x, y)$
- | for each adjacent  $(x, y)(x', y')$ , and  $(x', y') \notin W$  }
- $I = \{at(0,0), visited(0,0)\}$
- $G = \{visited(x,y) \mid (x,y) \in V\}$

2.

This is an open question, here we provide a few heuristic function examples. But do feel free to explore other heuristic function. More of this question are discussed for class or on LMS forum.

hints: Walls should also be taken under consideration. Manhattan distance is already an approximation for maze distance.

- $x$  and  $y$  are coordinates representing current location of agent, and  $V'$  are the coordinates that remain to be visited.
- a.  $h_g(s) = |V'|$  (goal-counting heuristic)
- b.  $h_c(s) = \min_{x_g, y_g \in V'} \text{Manhattan\_distance}(x, y, x_g, y_g)$   
(Manhattan distance to closest unvisited coordinate)
- c.  $h_f(s) = \max_{x_g, y_g \in V'} \text{Manhattan\_distance}(x, y, x_g, y_g)$   
(Manhattan distance to furthest unvisited coordinate)
- Both  $h_c(s)$  and  $h_f(s)$  are admissible and consistent,  $h_f(s)$  dominates  $h_c(s)$ .  $h_g(s)$  is an approximation for “pre-condition & delete relaxation” heuristic. The relaxation heuristic is admissible and consistent, but not its approximation.  $h_g(s)$  is admissible and consistent in this problem.
- All of them are in  $O(n)$
- A\*. Using the A\* from **slides** will guarantee find an optimal solution with an admissible heuristic.