

## Problem Set VIII: Reinforcement Learning

Recall the following description from Problem Set VII:

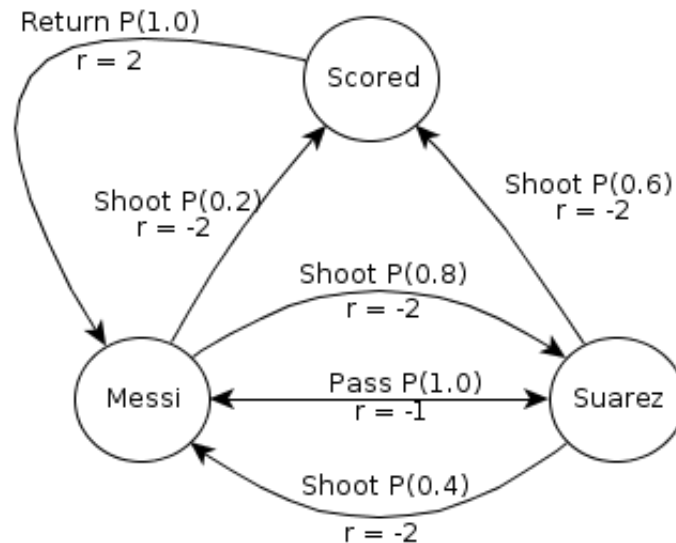
Consider two football-playing robots: Messi and Suarez.

They play a simple two-player cooperate game of football, and you need to write a controller for them. Each player can pass the ball or can shoot at goal.

The football game can be modelled as a discounted-reward MDP with three states: *Messi*, *Suarez* (denoting who has the ball), and *Scored* (denoting that a goal has been scored); and the following action descriptions:

- If Messi shoots, he has 0.2 chance of scoring a goal and a 0.8 chance of the ball going to Suarez. Shooting towards the goal incurs a cost of 2 (or a reward of -2).
- If Suarez shoots, he has 0.6 chance of scoring a goal and a 0.4 chance of the ball going to Messi. Shooting towards the goal incurs a cost of 2 (or a reward of -2).
- If either player passes, the ball will reach its intended target with a probability of 1.0. Passing the ball incurs a cost 1 (or a reward of -1).
- If a goal is scored, the only action is to return the ball to Messi, which has a probability of 1.0 and has a reward of 2. Thus the reward for scoring is modelled by giving a reward of 2 when *leaving* the goal state.

The following diagram shows the transition probabilities and rewards:



### Tasks

1. What is the difference between Sarsa and Q-learning?
2. Assume the following Q-table, which is learnt after several episodes:

State	Action		
	Pass	Shoot	Return
Messi	-0.4	-0.8	–
Suarez	-0.7	-0.2	–
Scored	–	–	1.2

In the next step of the episode, from the state ‘Suarez’, Suarez passes the ball to Messi. Show the Q-learning update for this action using a discount factor  $\gamma = 0.9$  and learning rate  $\alpha = 0.4$ .

**Note:** As this is a reinforcement learning problem, assume that the transition probabilities are not accessible to your algorithm.

3. Consider again being in the state ‘Suarez’, Suarez passes the ball to Messi and then Messi decides to shoot. Show the SARSA update for the Pass action using a discount factor  $\gamma = 0.9$  and learning rate  $\alpha = 0.4$  and assuming  $a'$  (the next action to be execute) is Shoot. Compare to the Q-learning update. What is different?

## Additional Tasks for Personal Study

To improve your understanding of reinforcement learning and how to work with Q functions, pick up from where you left of last week and complete the *fourth* question of Project 3 at <http://ai.berkeley.edu/reinforcement.html#Q4>. You should already have all the necessary files to complete this task.

**Hints** In order to help you complete the task, here are some useful hints:

1. The functions that you need to change:
  - a) computeValueFromQValues
  - b) getQValue
  - c) computeActionFromQValues.
2. The files you need to take a look:
  - a) util.py (Counter())
  - b) featureExtractors.py
3. How to test your code:
  - a) python gridworld.py -a q -k 5 -m (to get your agent to learn via keyboard input)
  - b) python autograder.py -q q4 (testing by autograde)