Chemistry 6491: Quantum Mechanics

Instructor

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Requirements and Grading Scheme

 $\begin{array}{lll} \text{Problem sets} & 25\% \\ \text{Math recitation} & 5\% \\ \text{First test} & 20\% \\ \text{Second test} & 20\% \\ \text{Final} & 30\% \end{array}$

Auditors are required to attend a minimum of 1/2 of the lectures. Pass/fail students are required to take both tests and the final and receive an overall passing grade.

Topics

In the list below, "S" denotes the primary textbook by Shankar. "S&O" denotes the optional supplementary book by Szabo & Ostlund (which covers more electronic structure theory, a topic we might touch on at the end if there is time, but it also has some good review of linear algebra in Chapter 1).

Unit I: Fundamentals of Quantum Mechanics

(A) Introduction to quantum mechanics: Scope and applicability of quantum mechanics The Schrödinger equation

(B) Linear vector spaces:

Definitions (S 1.1; S&O 1.1.1)

Inner and outer products (S 1.2; S&O 1.1.2-1.1.3)

Dual spaces and Dirac notation (S 1.3; S&O 1.1.4)

(C) Operators:

Basic operator rules (S 1.5-1.6)

Classes of operators: linear, hermitian, unitary, etc. (S 1.6; S&O 1.1.2)

Diagonalization and eigenvalue equations (S 1.8; S&O 1.1.6)

Change of basis (S 1.7; S pp 43-54; S&O 1.1.5)

The Propagator (S pp 43-54)

Functions of matrices (S 1.9; S&O 1.1.7)

Commutators; Campbell-Baker-Hausdorff theorem (notes)

Connection between functions and Dirac notation (S 1.10; S&O 1.2)

- (D) Postulates of QM (S Chapt 4)
- (E) Review of simple problems in 1D (S 5.1-5.2)
- (F) The classical limit: Ehrenfest's theorem (S Chapt 6)
- (G) Second quantization; example of harmonic oscillator (S Chapt 7) Application of Harmonic Oscillator to IR spectroscopy (handouts)

(H) Angular momentum (S Chapt 12):

Spherical harmonics (S 12.5)

Ladder operators (S 12.5)

Rigid rotator and Rotational spectroscopy

Central force problems (S 12.6)

Hydrogen atom (S Chapt 13)

Unit II: Approximate Methods

(A) Variational method:

Variational theorem (S 16.1)

Equivalence of Raleigh-Ritz procedure and diagonalization

(B) Time-independent perturbation theory (S 17.1-17.2)

Unit III: Advanced Fundamentals

- (A) Spin (S Chapt 14)
- (B) Addition of angular momenta (S Chapt 15)
- (C) Interaction of light with matter

Textbooks

1. R. Shankar, *Principles of Quantum Mechanics*, 2nd ed. (Plenum, New York, 1994). Intermediate-level physics book covering the pure quantum part, some lecture material drawn directly from here.

Other Books that may be Helpful

- 1. D. A. McQuarrie, *Quantum Chemistry* (University Science Books, Mill Valley, CA, 1983). Very readable introductory text.
- 2. A. Szabo and N. S. Ostlund, *Modern Quantum Chemistry*, *Introduction to Advanced Electronic Structure Theory*, 1st ed., revised (Dover, 1989). Short review of linear algebra and Dirac notation, and thorough introduction to Hartree–Fock theory.
- 3. I. N. Levine, *Quantum Chemistry*, 5th ed. (Prentice Hall, Englewood Cliffs, NJ, 2000). Covers most of the topics in this course at a slightly lower level.
- 4. G. Strang, *Linear Algebra and its Applications*, 3rd Ed., (Harcourt Brace Jovanovich, San Diego, 1988). Good intro to linear algebra.
- 5. E. Merzbacher, *Quantum Mechanics*, 3rd ed. (Wiley, New York, 1998). Advanced physics text.