ISyE 7672 Convexity

Topics:

Convex sets: basics

Definitions, examples, elementary algebraic and topological properties

Main theorems

Caratheodory, Radon, Heeley

Separation

Krein-Milman

Theory of finite systems of linear inequalities

Theorem of the alternative

Structure of polyhedral sets

Theory of linear programming

Convex functions

Definitions, examples, sufficient conditions, elementary properties

Gradient inequality

Optimality conditions

Subgradients and Frenchal conjugacy

Convex Programming

Convex programs (usual and conic forms)

Lagrange and conic duality

Optimality conditions in convex programming

Saddle points: definitions, existence, interpretation