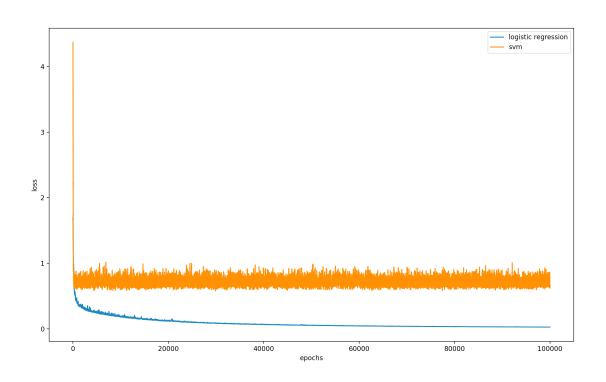
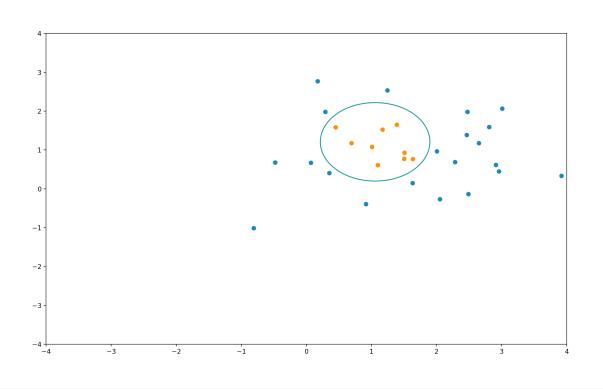
PIRP2







```
Proposition) - log 1/ is a strongly convex function (*)
  tin: Rt-R=-logn, WLOG, choose 12 KM, from IR
     Since J_1, J_2 \Rightarrow \eta J_1 + (1-\eta) J_2 \in \mathbb{R}^+, \forall \eta \in (0,1), \mathbb{R}^+ is canvex.
 f''(x) = \frac{1}{x^2} 70 \Rightarrow f(x) is strictly increasing function ... (1)
 g(e)= £t(m) + (1-t) t(m) - t(tn+ (1-tm2), g: I°17→ R
g(t) = t(t(),)-t(tx,+(1+1)) - (+t)(f(tx,+(1+1))-t0))
                  = t((-t)(1,-1,2) t'(c,) - ((-t) t(1,-1,2) t'(c,), = c,6 (tx,+(1+6),2,1,), = c, € (1, tx,+(1+6),2), by MUTL(1)
               = f(/t) (x-1/2) (f((,) - f((,)) = f(/t) (x-2) (c,-c) f"((3), = f((3), (3) & (2, (1) by MVT & (1)
 .. g(t) >0 for te (91).
 O_{KL} = \sum_{i=1}^{\infty} P_{i}(l_{i} + \sum_{j=1}^{K}) , \sum_{i=1}^{\infty} P_{i} = 1, \sum_{i=1}^{\infty} P_{i}
                      = \frac{1}{2} \int_{a}^{b} \left( - \log \frac{g_{x}}{g_{x}} \right)
```

$$P(N = -l_{2}) \times r.v. \quad s.t. \quad f(x = \frac{8a}{p_{1}}) = p_{1}, \quad \psi_{1}$$

Then,
$$D_{FL} = E[Y(X)] \ge Y(E[X]) = Y(\frac{x}{e^{-2}}) = Y(1) = 0$$

PS.

Let) X be r.u. s.e. $f(X=\frac{2i}{p_i})=p_i$, $\forall i$. Since, $p\neq f_i$, X isn't constant r.u. $Y(M) \triangleq -l=g \mathcal{N}$ is strictly convex function. ASW, $D_{KL} = E[Y(M)] \neq Q(E[X)) = 0$ *

```
to (x)= U = ( axtb) = = = u, e(a, x+b,)
   a, b, u e RP, be R3P
 i) Vafo(1/2 6 (a)Hb)
 : Jufo(1)= 5 (an+b)
ii) the for = or (a)+b) 0 (= diag(or (a)+b)) u
1) = 0 ( = 0 ( sin bi)) = Un sian bi)
     6 (OHb) ER, UERP => 0 is well-defined.
     (S'(\alpha)Hb))_i = S'(\alpha)_i + V_i)_i \quad (u)_i = V_i
    \left( \text{C}_{(\alpha)}(\mu, \mu) \text{OM} \right)^2 = \text{C}_{(\alpha)}(\mu, \mu, \mu) \text{OM} = \frac{3p^2}{3p^2} = \left( \frac{1}{4} \text{OM} \right)^2
Jing (σ'(0)+4)) U = 5 diag(σ'(0)+4)); U; ∈(β)
    (diag (6'(a)+b)); = ( = diag (6'(0)+b)); ( b); = 6'(0)+b) (1; = (6'(0)+b) (0);
     : Toto(1)= = (a)+4) OU = diag( = (a)+6) IV
 iii) To fo(x)= (5(0)+6)04)1 = diag(5(0)+6) ux
 1) Dato = Da fuj or ograb) = Aui or (ainti)
```

Tuto(N= (6(an+6)0U)) = (6(an+6)0(un)) (:7 is scala)

X

= diag(6'(a)+6)) (1) (:: (iil-2)

(2) asw

