

Meta-Learning

EECE695D: Efficient ML Systems

Spring 2025

Recap

- **Goal.** Efficient Training
- **How?** Use “experience” gained from previous training episodes
- **Last Class.** Continual Learning
 - Multiple tasks, shown sequentially
 - Goal. Preserve knowledge on seen tasks, to perform well on **seen tasks**
- **Today.** Use it for **unseen tasks?**

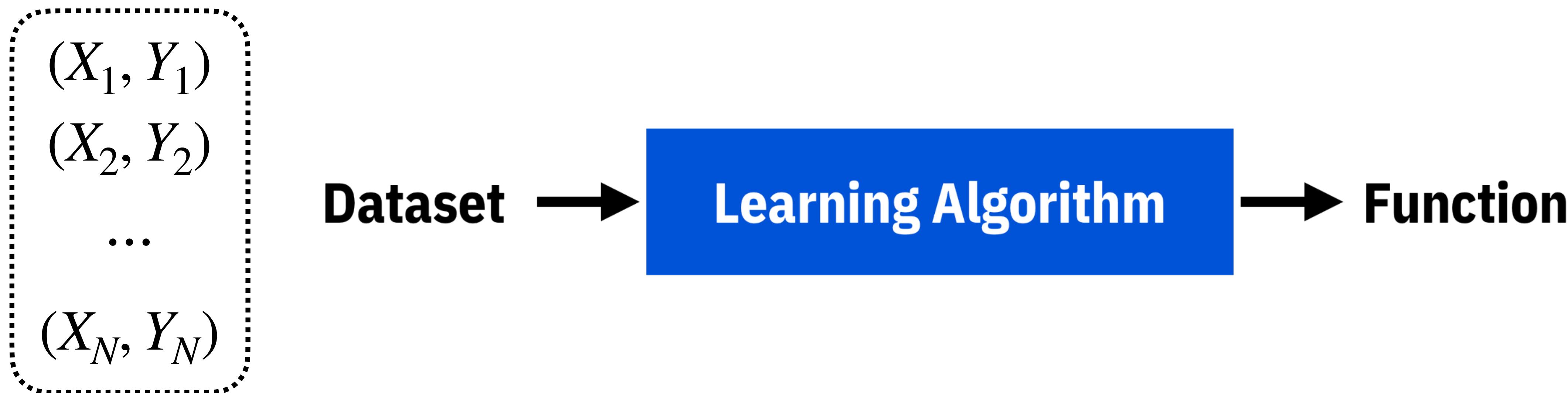
Basic idea

Idea

- Gains **experience** over multiple learning episodes
 - Covering a distribution of related tasks
- **Goal.** Improve its performance on **future learning tasks**
 - Has two names
 - “Learning to learn”
 - “Meta-learning”

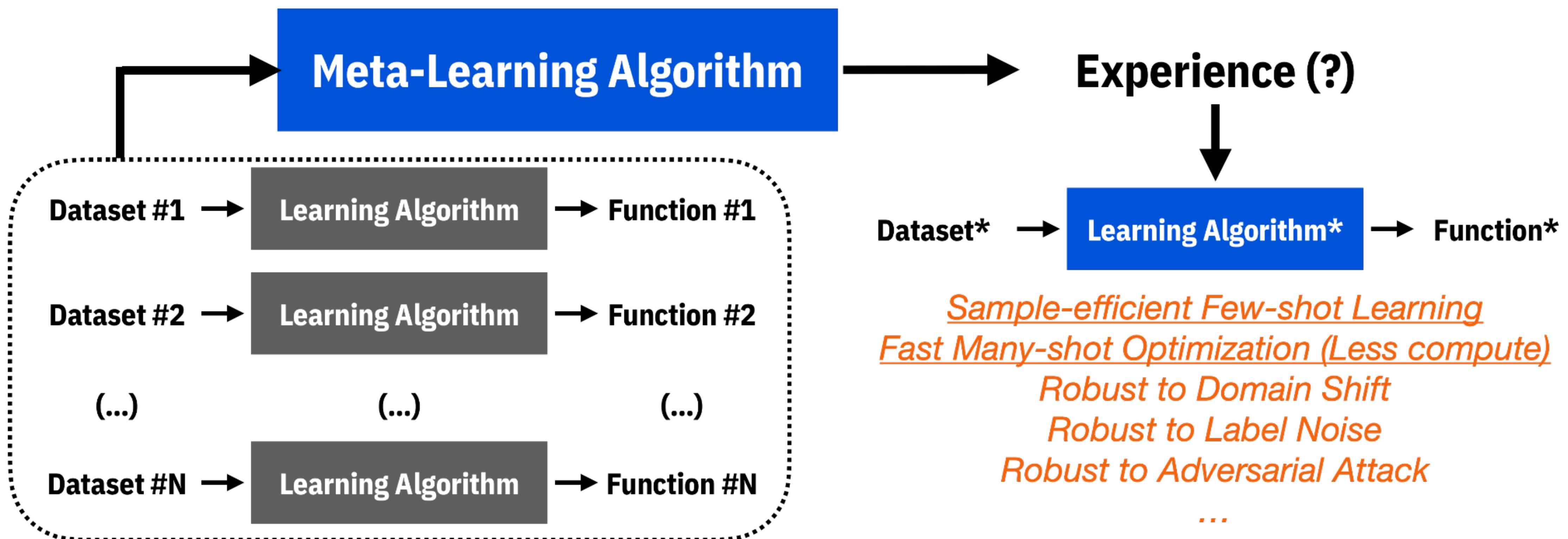
Learning

- **Given.** A **dataset** drawn from a distribution (i.e., training data)
- **Goal.** Find a **model** (function) that works well on the dataset
 - Should work well on **new data** drawn from the distribution (i.e., test data)



“Meta”-Learning

- **Given.** A “task” set drawn from a distribution
- **Goal.** Find a “meta-model” (experience) that works well on the task set
 - Should work well on new “task” drawn from the distribution



Formalism

- We have a set of tasks drawn from an unknown distribution

$$T_1, \dots, T_m \sim P_{\text{task}}$$

- Each task consist of a triplet

$$T_i = (D_i^t, D_i^v, L_i)$$

- D_i^t, D_i^v : Training (support) / Validation (query) set of task i
- L_i : Loss function
 - $L_i(\theta, \omega, D_i^v)$ is the loss of model param θ on dataset D_i^v , when we have transferred the **meta-knowledge** ω

Formalism

- **Training.** Fit the model parameter θ on each task:

$$\theta_i^*(\omega) = \arg \min_{\theta} L_i(\theta, \omega, D_i^t)$$

- **Meta-Training.** Minimize the average task-wise losses:

$$\min_{\omega} \sum_{i=1}^m L_i(\theta_i^*(\omega), \omega, D_i^v)$$

- Note. We care about the validation loss, evaluated after per-task fitting

Formalism

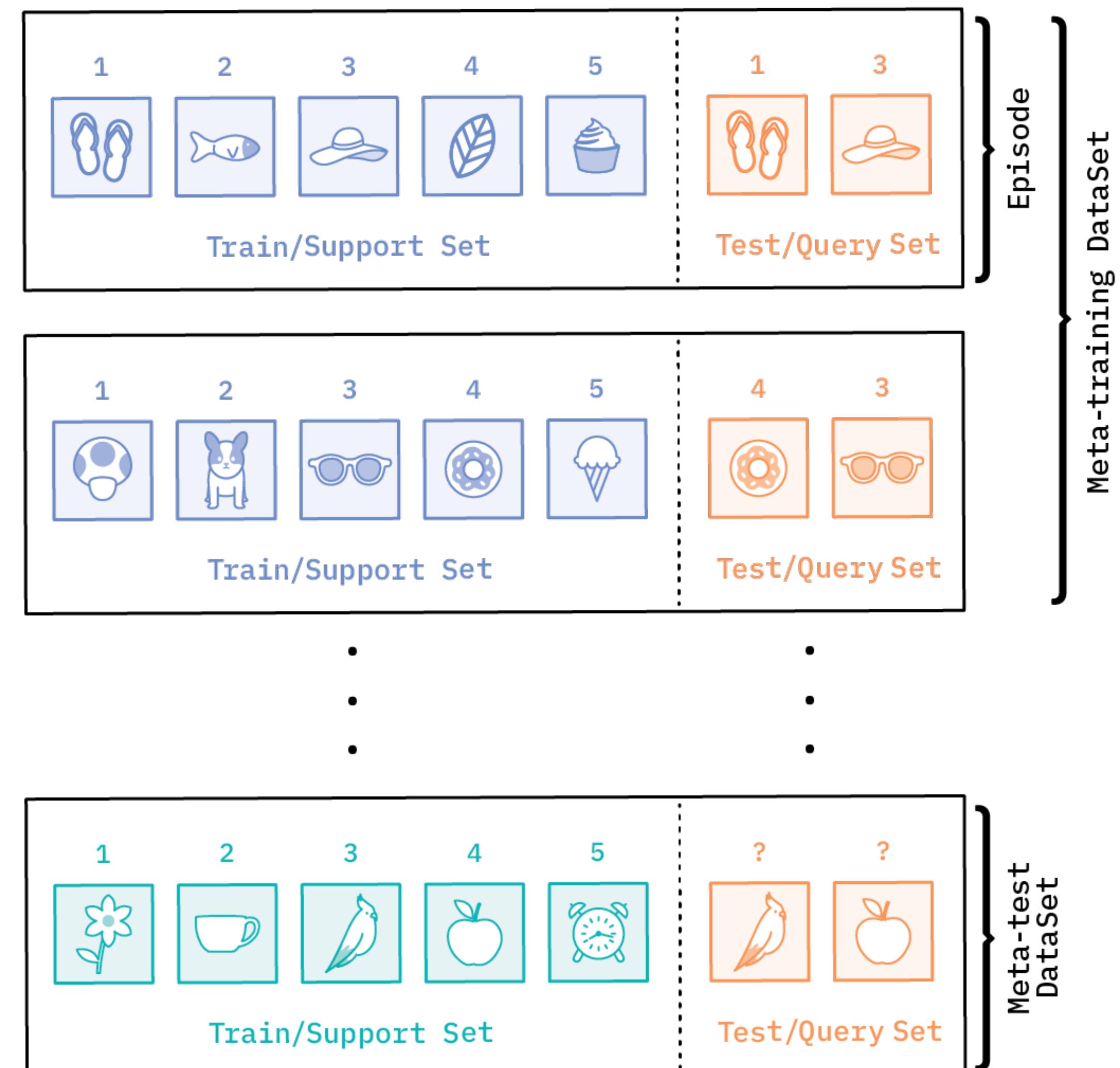
- **Question.** Which **meta-knowledge** ω can we transfer?
 - Initial Parameters, Optimizer, Hyperparameters, Black-box Model, Embedding (Metric), Modules, Instance Weights, Exploration Policy, Attention, Architecture, Noise Generator, Curriculum, Dataset, Environment, Loss/Reward, Data Augmentation, (...)
- Today we'll cover the most popular ideas

Example task

- As a running example, we consider **few-shot classification**

- Each task is a k -class classification
 - For each class, we have few samples (e.g., n samples)
 - Classes differ from task to task
- At (meta-)test, we receive another k -class classification problem with n training samples for each class.

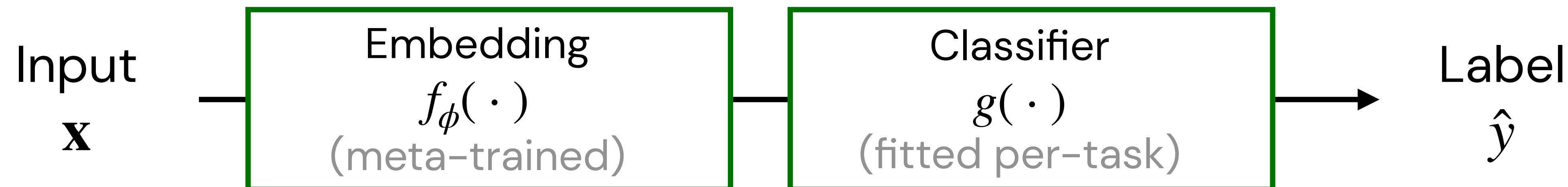
(called k -way, n -shot classification)



Algorithms

Metric-based: ProtoNet

- **Idea.** Learn a **feature-space metric** that works well for future tasks
 - That is, train an **embedding function** $f_\phi(\cdot)$ so that classification based on the latent features $f_\phi(\mathbf{x})$ can be done accurately
 - Meta-knowledge ω . Embedding function $f_\phi(\cdot)$
 - Model parameter θ . Metric-based classifier $g(\cdot)$
(will be explained shortly)

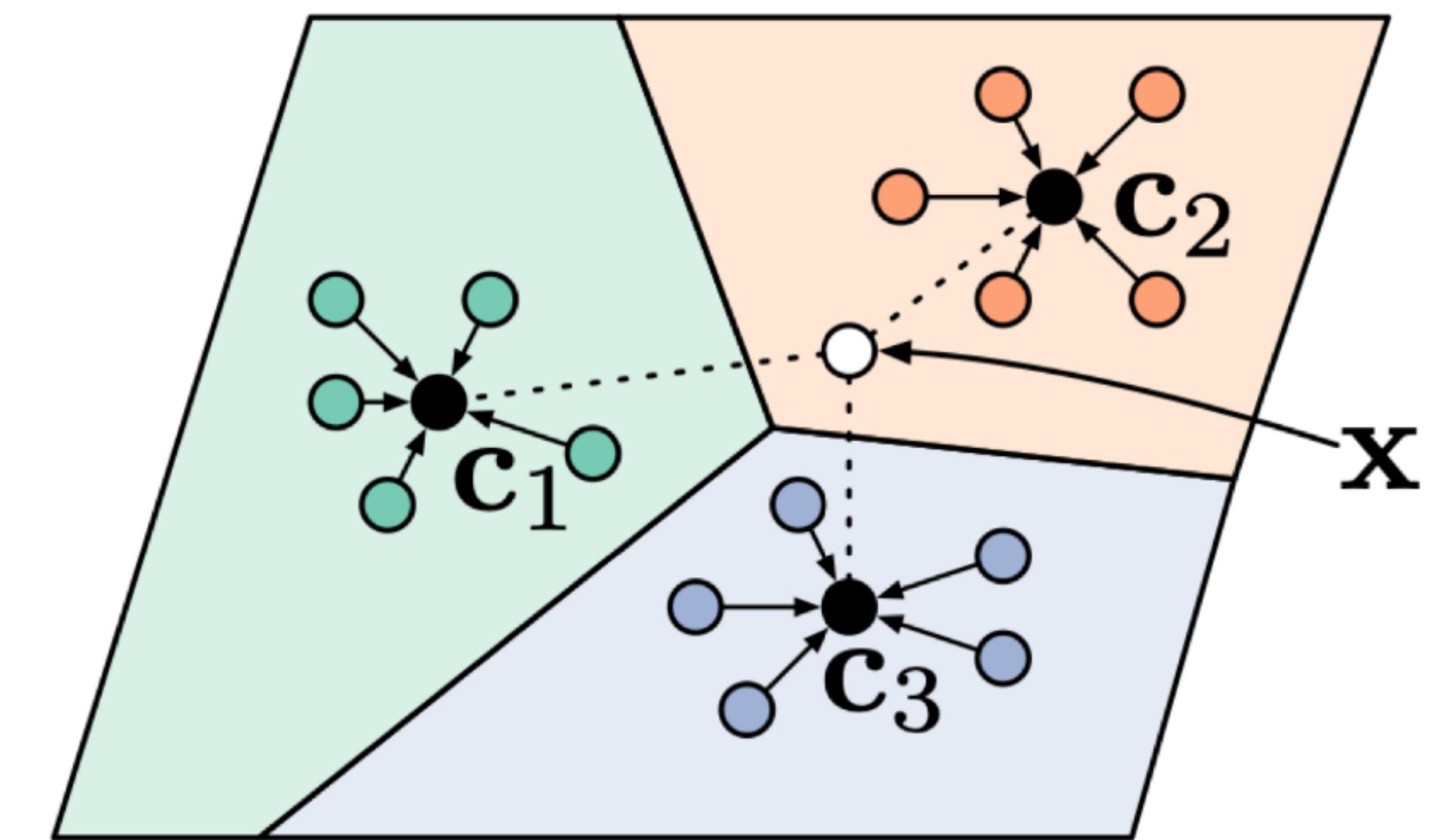


Metric-based: ProtoNet

- **Classifier.** Prototype Classifiers
 - **Prototype features** are defined for each class, as the mean embedding

$$\mathbf{c}_k = \frac{1}{|S_k|} \sum_{(\mathbf{x}_i, y_i) \in S_k} f_\phi(\mathbf{x}_i)$$

- Perform the softmax classification
- $$p_\phi(y = k | \mathbf{x}) = \frac{\exp(-d(f_\phi(\mathbf{x}), \mathbf{c}_k))}{\sum_{k'} \exp(-d(f_\phi(\mathbf{x}), \mathbf{c}_{k'}))}$$
- No training needed; not many samples needed



Metric-based: ProtoNet

- **Meta-Training.** Find ϕ which minimizes classification loss on each task:
 - i.e., average of the per-task losses, where the loss for task j is:

$$\sum_{(\mathbf{x}_i, y_i) \in D_j^v} -\log p_\phi(y = y_i | \mathbf{x}_i)$$

- Note. We use validation samples
- Note. Prototypes \mathbf{c}_k also depend on ϕ

Metric-based: ProtoNet

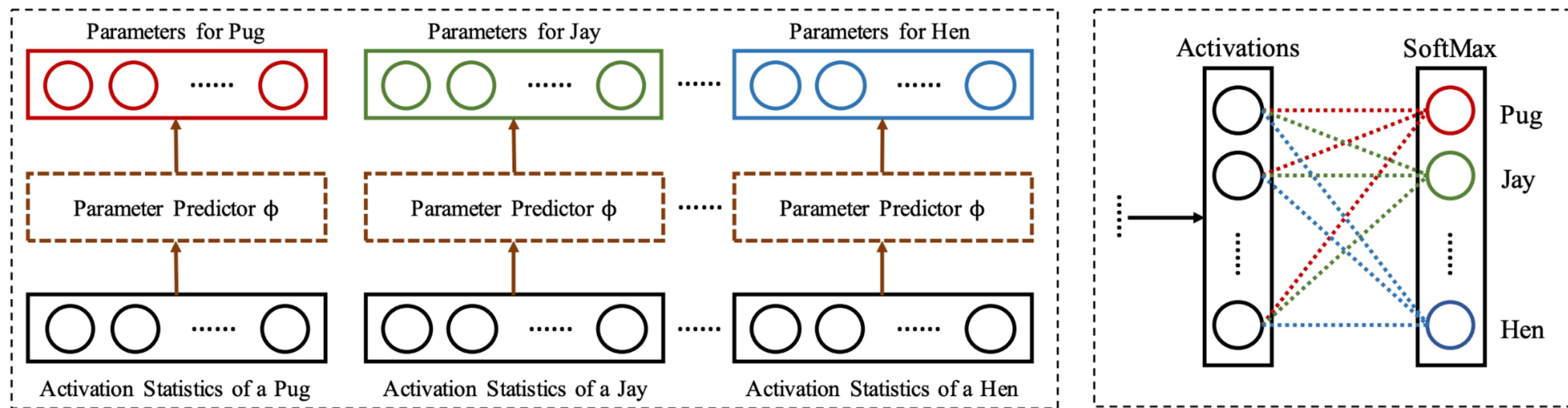
- **Algorithm.** Take an **episode-based** approach:
 - Iterate over:
 - Randomly draw a task (or tasks, if RAM permits)
 - Compute prototypes with the training split
 - Compute loss on validation split
 - Update features for several SGD steps
 - Gradients through both prototypes & validation samples

Metric-based: ProtoNet

- **Pros.** Zero adaptation cost
- **Cons.**
 - No flexibility
 - Given f_ϕ , we cannot improve much even with many test samples
 - Meta-training cost is large
 - Feature map is usually large
 - Gradients flow through both support & query samples

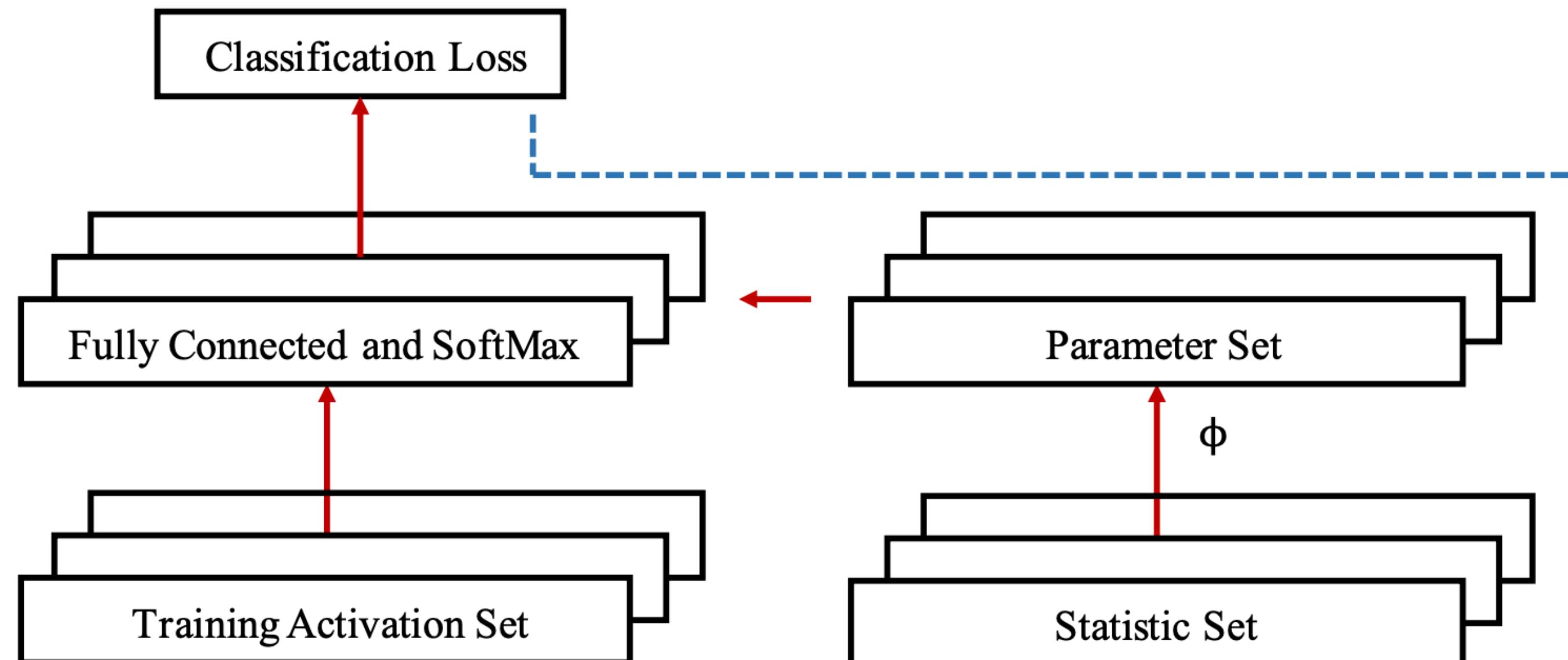
Model-based: Parameter Prediction

- **Idea.** Train a model which predict **classifier weights** for each class, based on the activation statistics of a pre-trained feature map
 - Meta-knowledge ω . Weight prediction model
 - Model parameter θ . The predicted weights



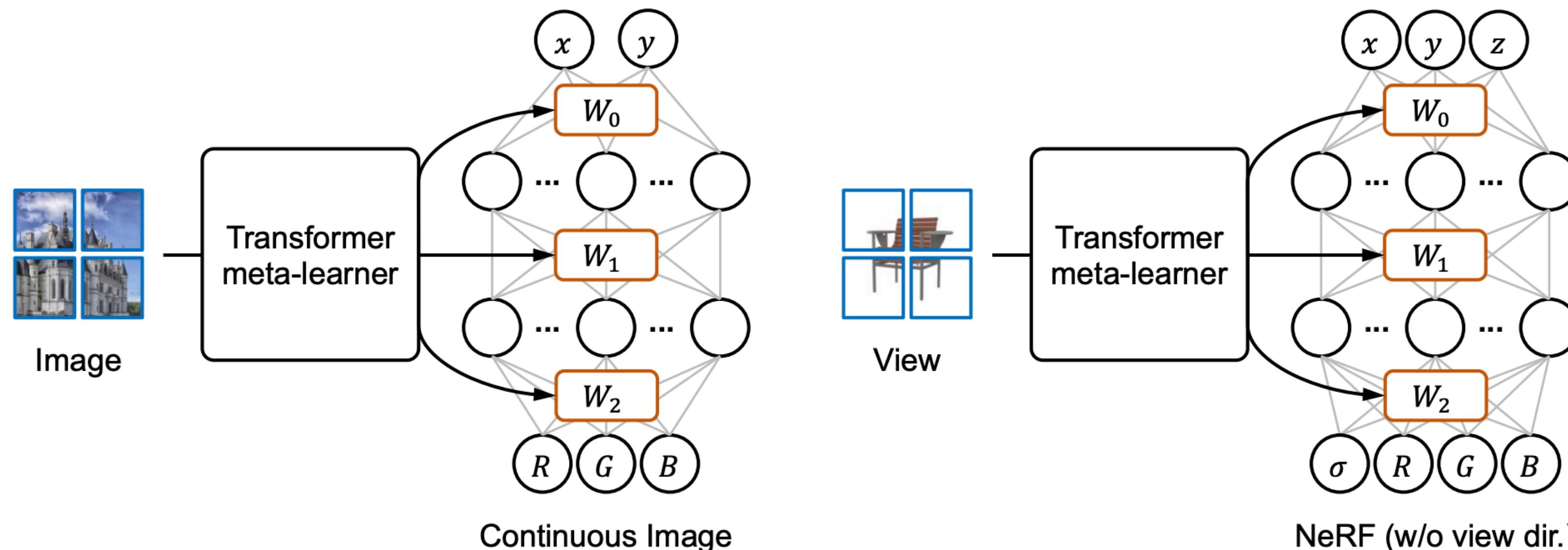
Model-based: Parameter Prediction

- **Meta-Training.** Similar to ProtoNet, but update the weight predictors not feature maps
 - Gradient on parameter predictors flows through the support samples only
 - Small-scale, and query samples do not affect the parameter predictor



Model-based: Parameter Prediction

- This approach is quite popular in NeRF / 3DGS literature
 - All layer weights are predicted, from the given image/views
 - Sometimes a “modulation” added or multiplied to the base model
 - Requires a very large meta-learner, sometimes

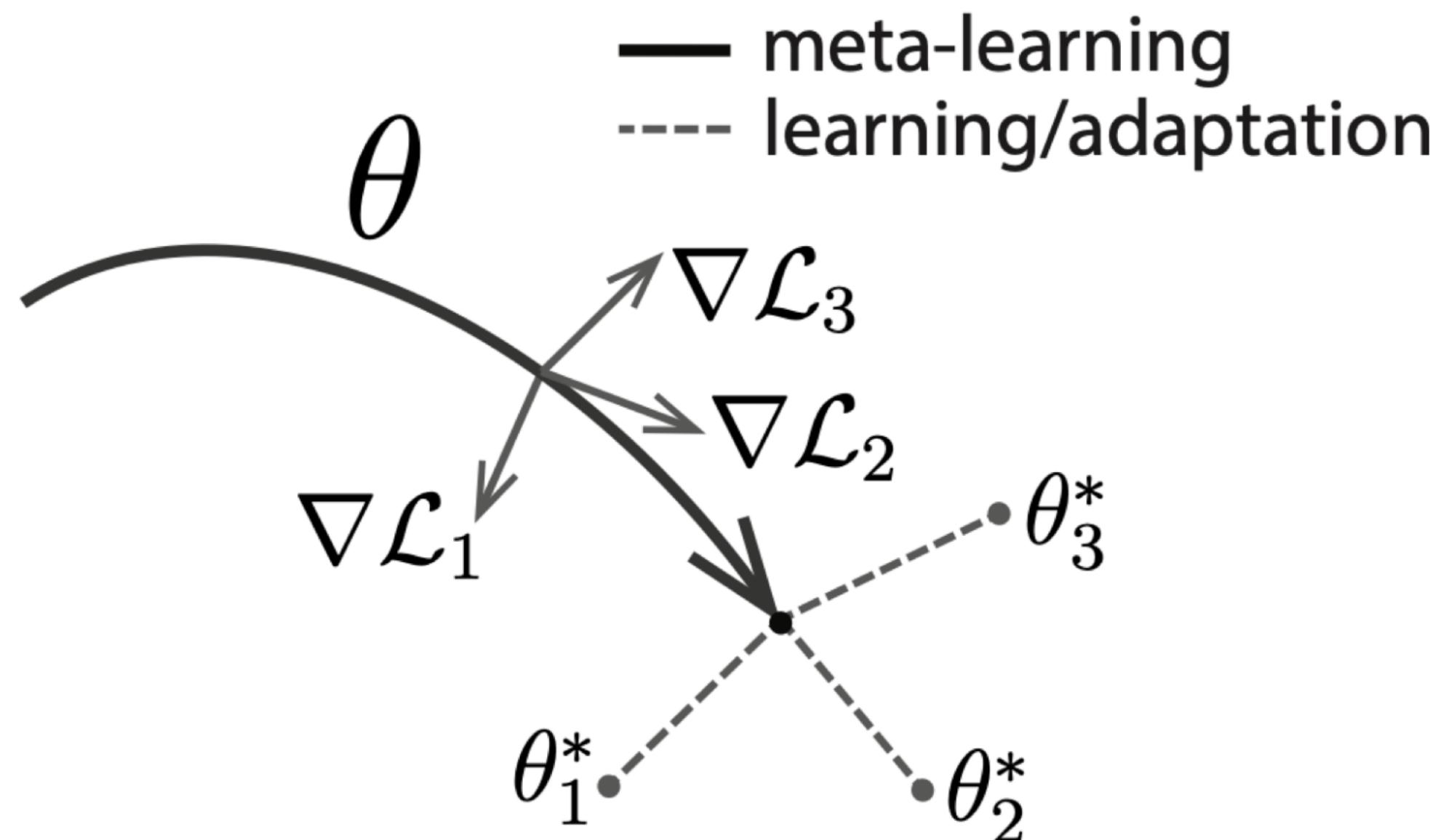


Model-based: Parameter Prediction

- **Pros.** Potentially reduced computational cost
 - Can play with the model size
- **Cons.** Still, suffers from restricted expressive power
 - On unseen data, limited capacity to adapt further

Optimization-based: MAML

- **Idea.** Train a **good initialization** from which the model can adapt rapidly to each task within a small number of SGD steps
 - Meta-knowledge ω . Initial parameters θ_0
 - Model parameter θ . Model weights $\theta_i = \theta_0 + \Delta\theta_i$



Optimization-based: MAML

- **Meta-Training.** We iterate over a double loop:

- Initialize θ

- **OUTER LOOP:**

- Sample a batch of task $1, \dots, t$

- **INNER LOOP:** For each $i \in \{1, \dots, t\}$

- Generate task-adapted parameters with SGD

$$\theta'_i(\theta) = \theta - \alpha \nabla_{\theta} L(\theta, D_i^t)$$

- Update θ (pre-adaption) to minimize val loss

$$\theta \leftarrow \theta - \beta \nabla_{\theta} \sum L_i(\theta'_i(\theta), D_i^v)$$

- Return the converged parameter

Optimization-based: MAML

- **Pros.** Improved adaptivity – just train further!
- **Cons.** Much **memory** required (need to track multiple versions of model)
 - Many memory-light variants: iMAML, 1st-order MAML, Reptile
 - Still, long-horizon meta-learning is not satisfactory with these (i.e., many steps in the inner loop)

Algorithm 2 Reptile, batched version

```
Initialize  $\theta$ 
for iteration = 1, 2, ... do
    Sample tasks  $\tau_1, \tau_2, \dots, \tau_n$ 
    for  $i = 1, 2, \dots, n$  do
        Compute  $W_i = \text{SGD}(L_{\tau_i}, \theta, k)$ 
    end for
    Update  $\theta \leftarrow \theta + \beta \frac{1}{n} \sum_{i=1}^n (W_i - \theta)$ 
end for
```

Learned Optimizers

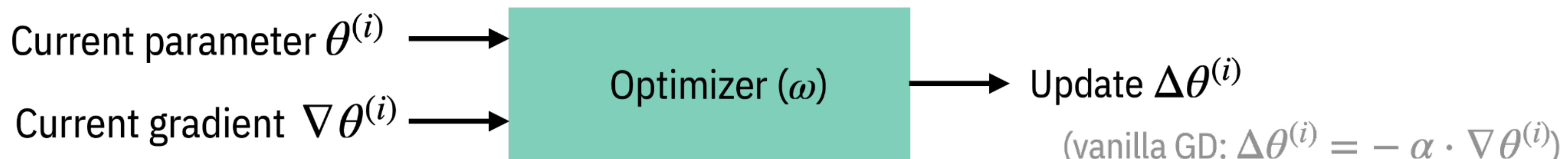
- **Idea.** Learn an **optimizer** to replace SGD
 - **Motivation.** Adam works extremely well
 - Is it optimal?
 - How do we remove the need for hyperparameter tuning?

Algorithm 1: Adam, our proposed algorithm for stochastic optimization. See section 2 for details, and for a slightly more efficient (but less clear) order of computation. g_t^2 indicates the elementwise square $g_t \odot g_t$. Good default settings for the tested machine learning problems are $\alpha = 0.001$, $\beta_1 = 0.9$, $\beta_2 = 0.999$ and $\epsilon = 10^{-8}$. All operations on vectors are element-wise. With β_1^t and β_2^t we denote β_1 and β_2 to the power t .

```
Require:  $\alpha$ : Stepsize  
Require:  $\beta_1, \beta_2 \in [0, 1]$ : Exponential decay rates for the moment estimates  
Require:  $f(\theta)$ : Stochastic objective function with parameters  $\theta$   
Require:  $\theta_0$ : Initial parameter vector  
     $m_0 \leftarrow 0$  (Initialize 1st moment vector)  
     $v_0 \leftarrow 0$  (Initialize 2nd moment vector)  
     $t \leftarrow 0$  (Initialize timestep)  
    while  $\theta_t$  not converged do  
         $t \leftarrow t + 1$   
         $g_t \leftarrow \nabla_{\theta} f_t(\theta_{t-1})$  (Get gradients w.r.t. stochastic objective at timestep  $t$ )  
         $m_t \leftarrow \beta_1 \cdot m_{t-1} + (1 - \beta_1) \cdot g_t$  (Update biased first moment estimate)  
         $v_t \leftarrow \beta_2 \cdot v_{t-1} + (1 - \beta_2) \cdot g_t^2$  (Update biased second raw moment estimate)  
         $\hat{m}_t \leftarrow m_t / (1 - \beta_1^t)$  (Compute bias-corrected first moment estimate)  
         $\hat{v}_t \leftarrow v_t / (1 - \beta_2^t)$  (Compute bias-corrected second raw moment estimate)  
         $\theta_t \leftarrow \theta_{t-1} - \alpha \cdot \hat{m}_t / (\sqrt{\hat{v}_t} + \epsilon)$  (Update parameters)  
    end while  
    return  $\theta_t$  (Resulting parameters)
```

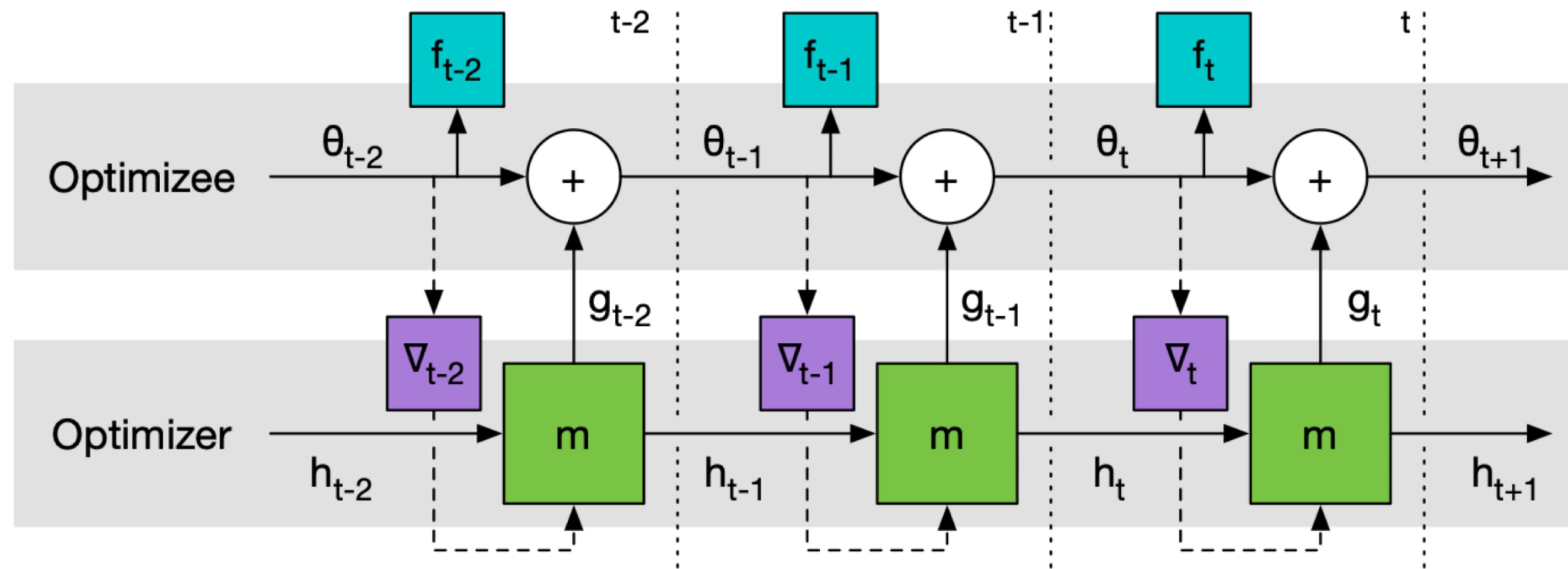
Learned Optimizers

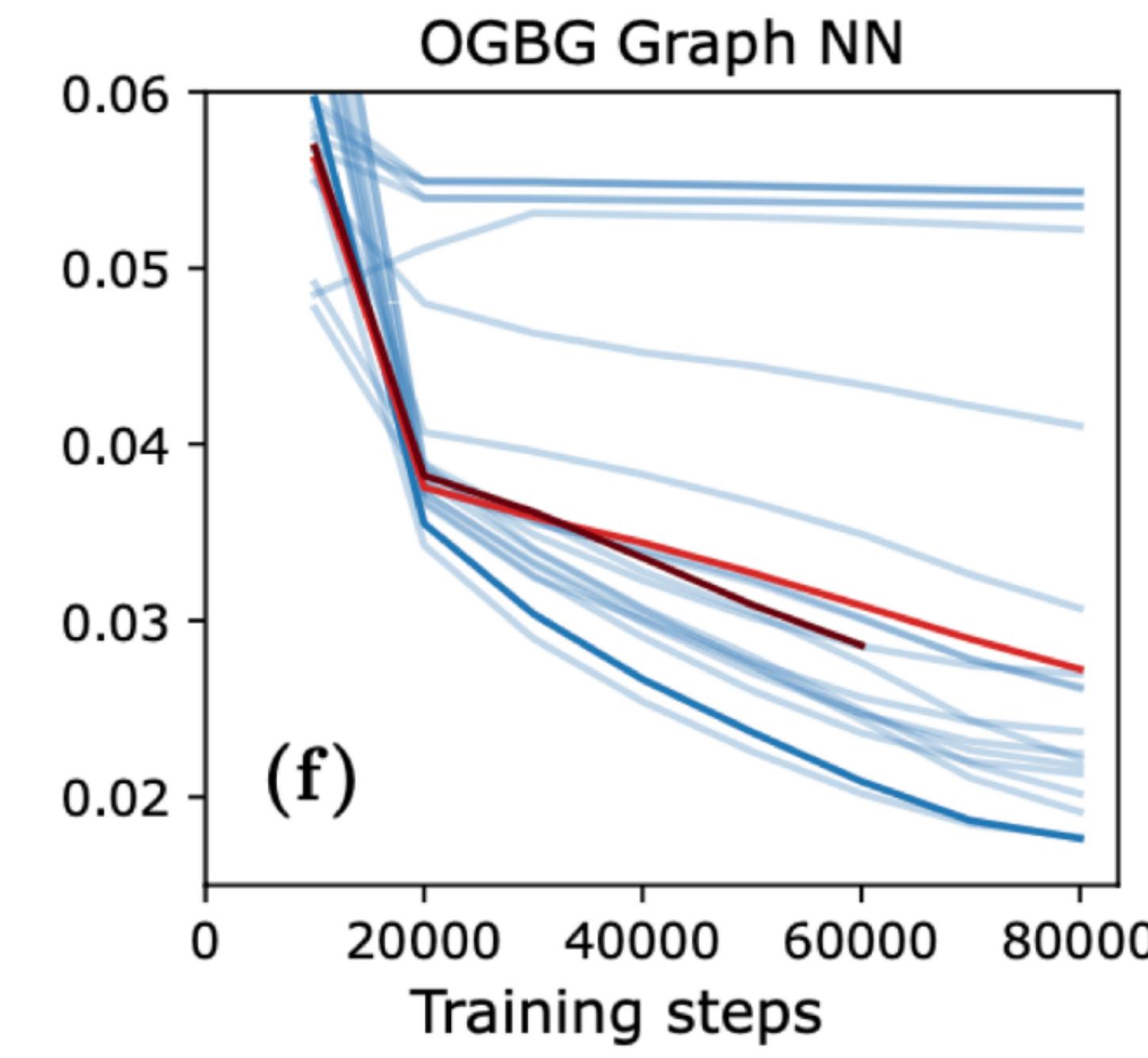
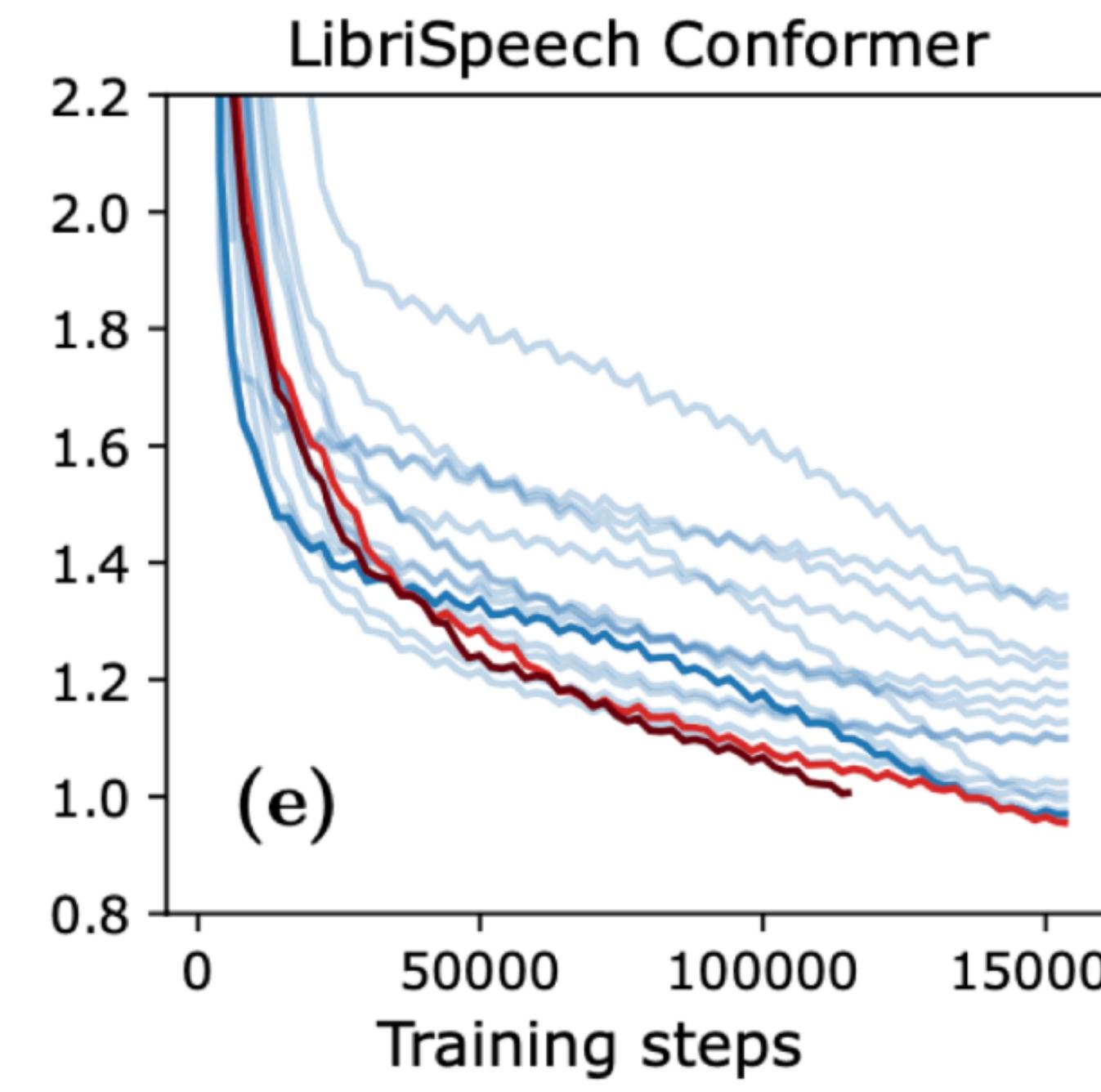
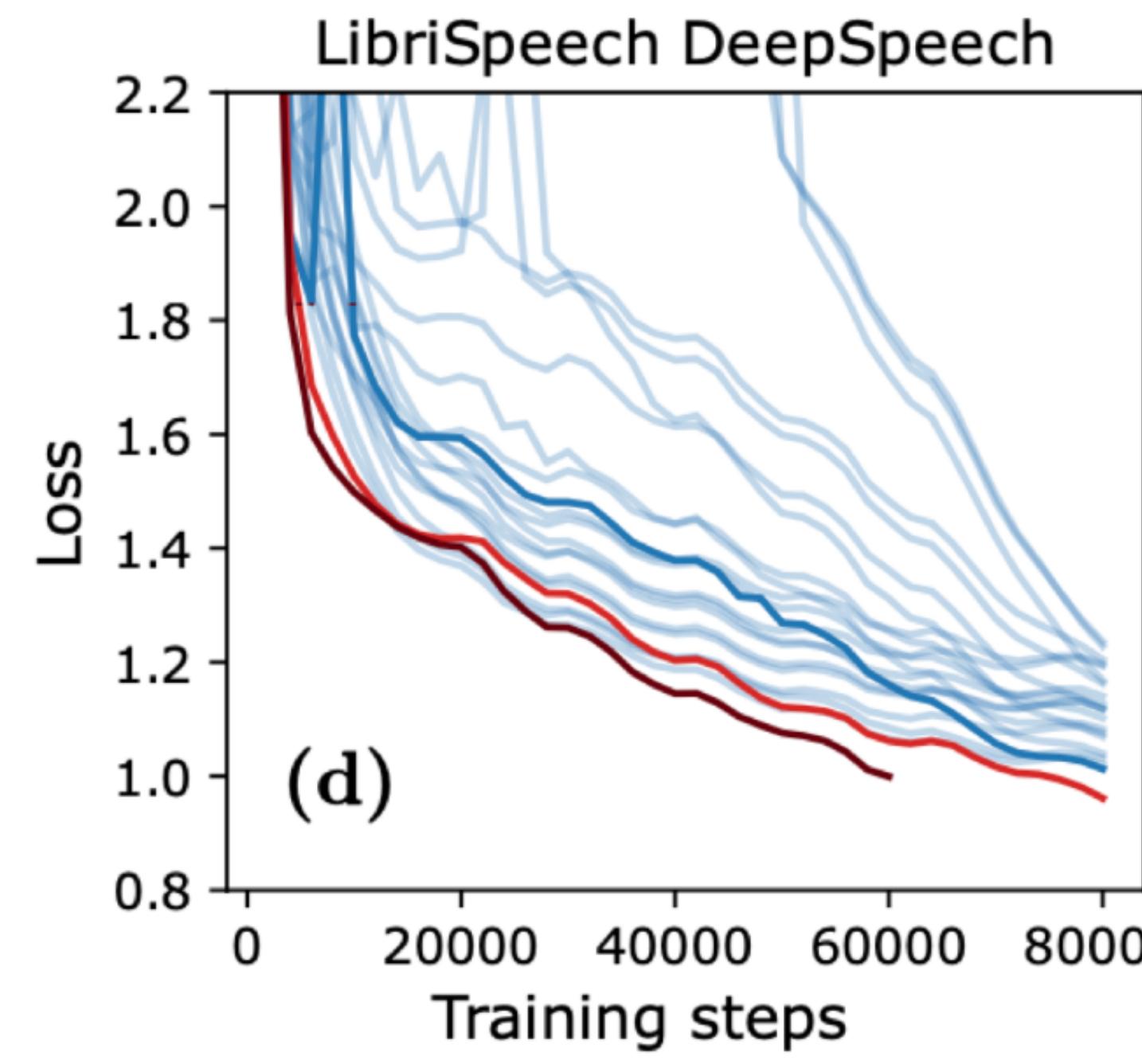
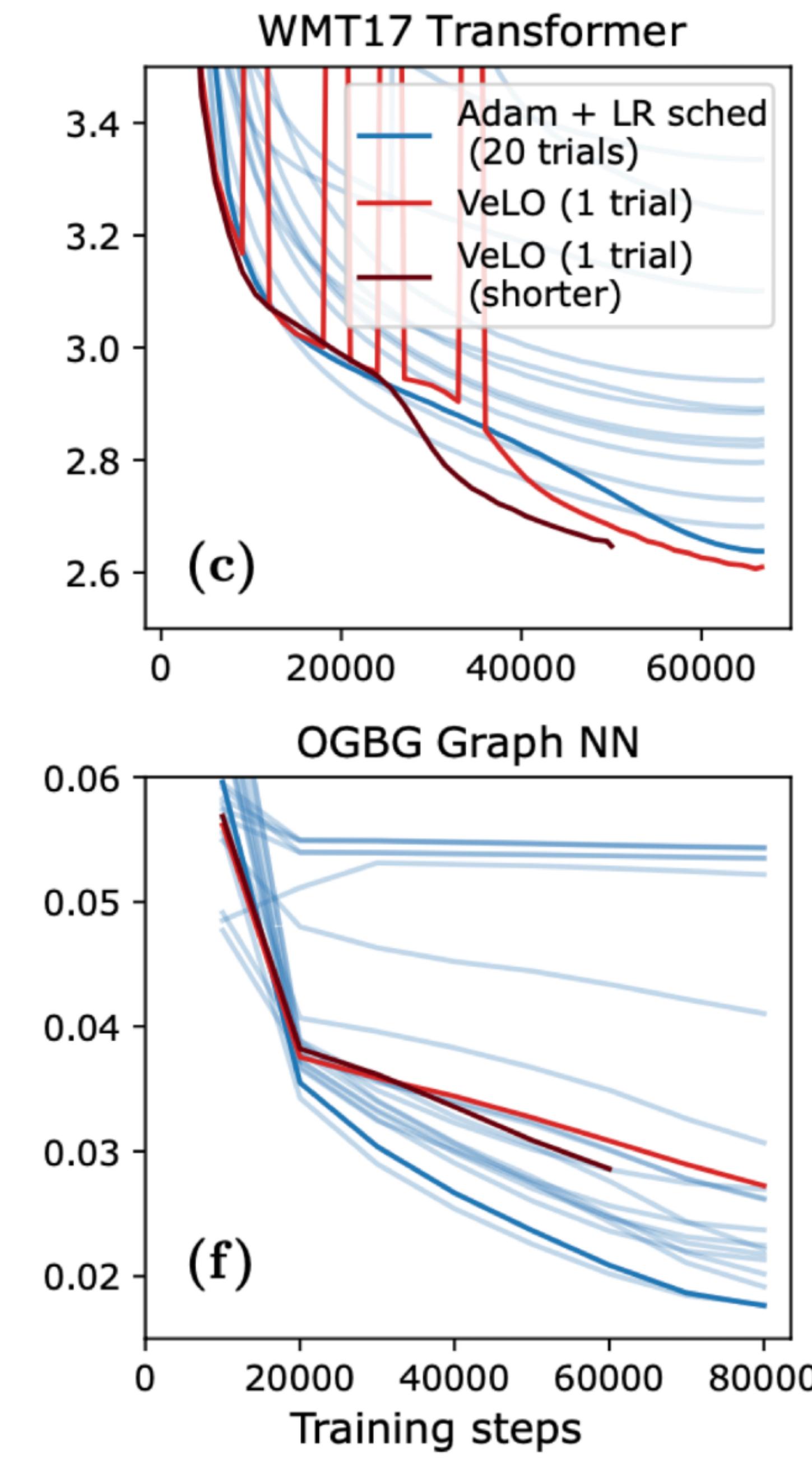
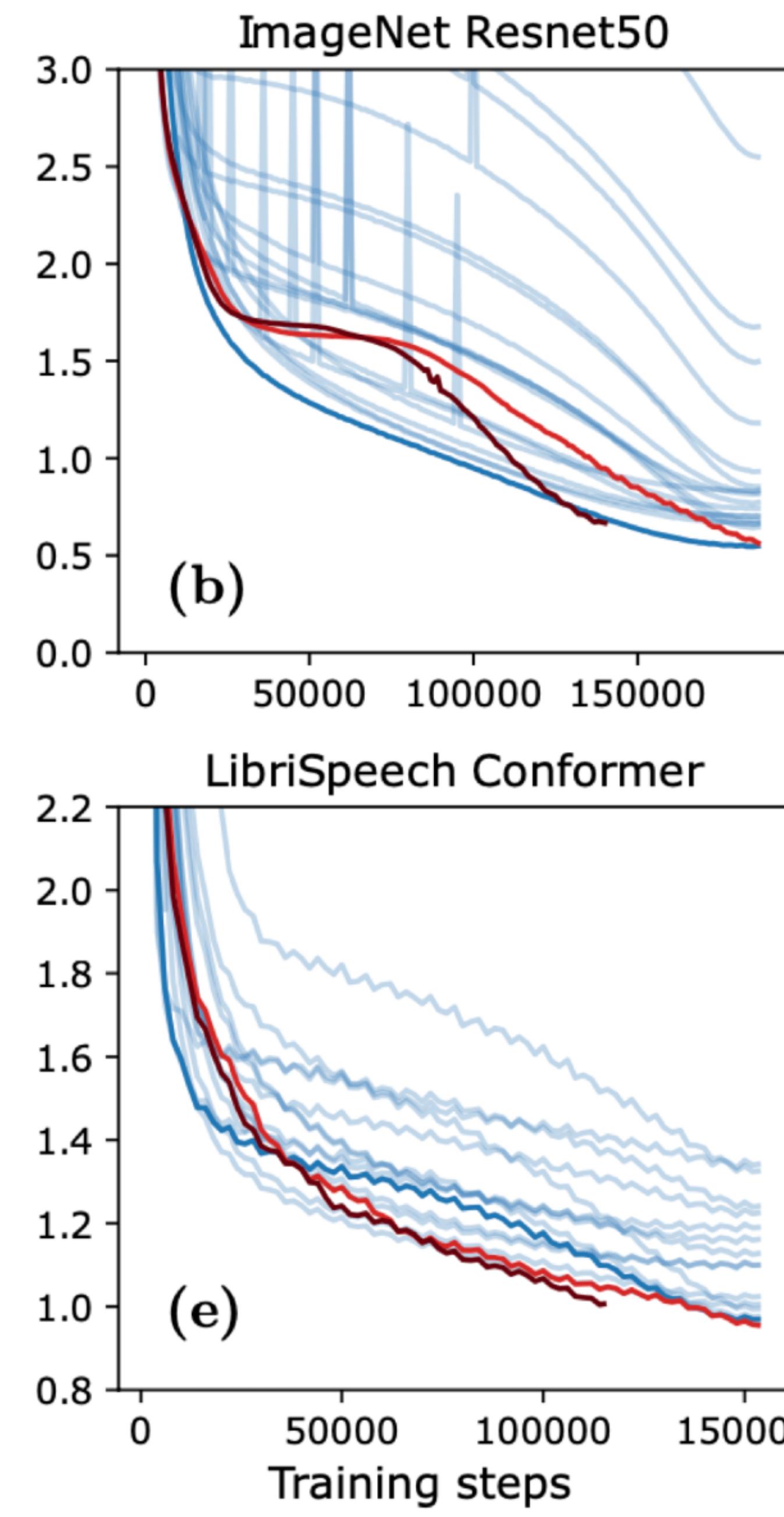
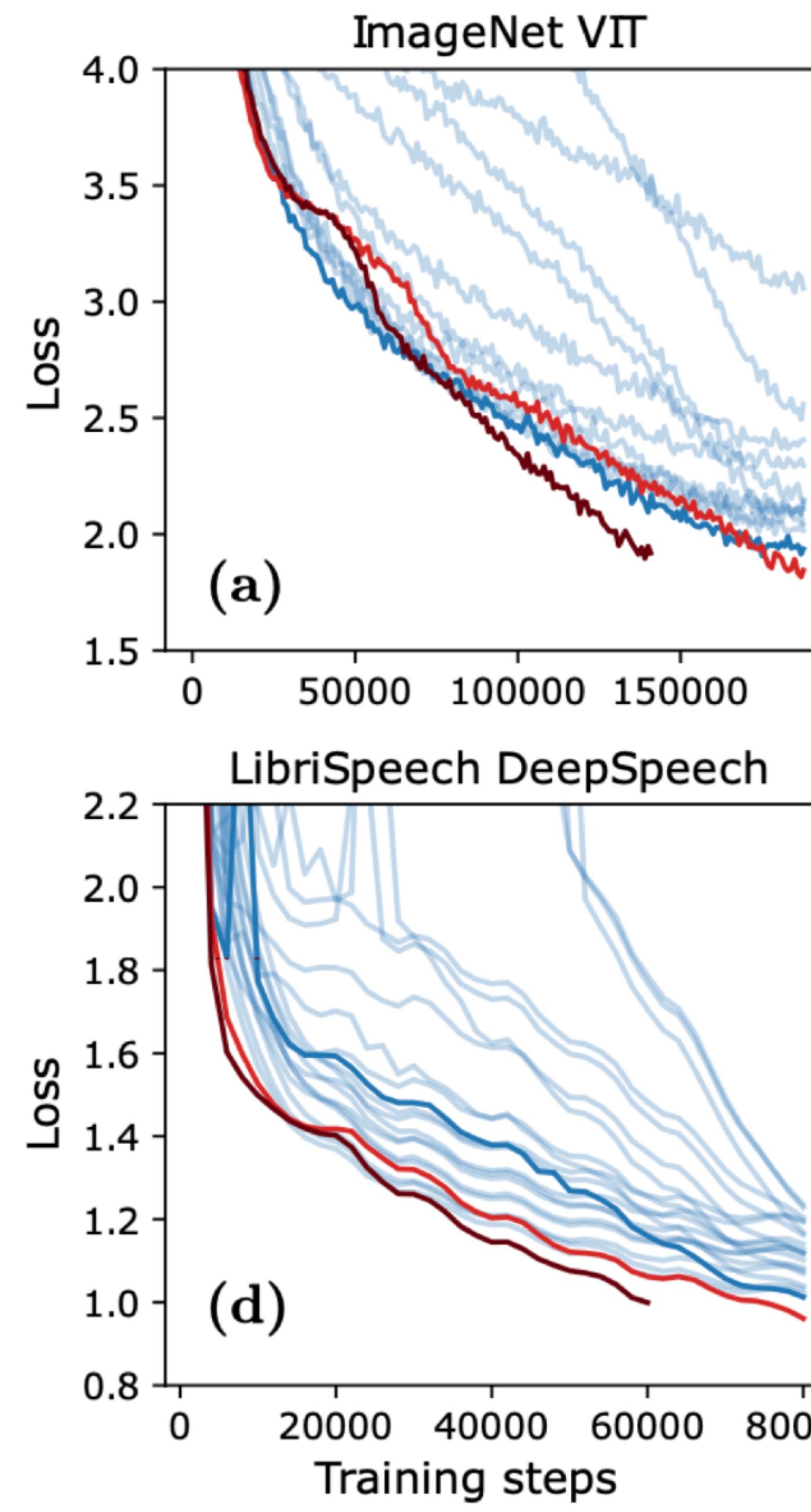
- **Question.** How do we parameterize the optimizer?
- **Answer.** View it as a black box that takes **current param & gradient** as input, and the **actual update** as an output
 - **Challenge.** Need to be able to express the **momentum**
 - **Challenge.** Need to be able to optimize **various-sized tensors / models**



Learned Optimizers

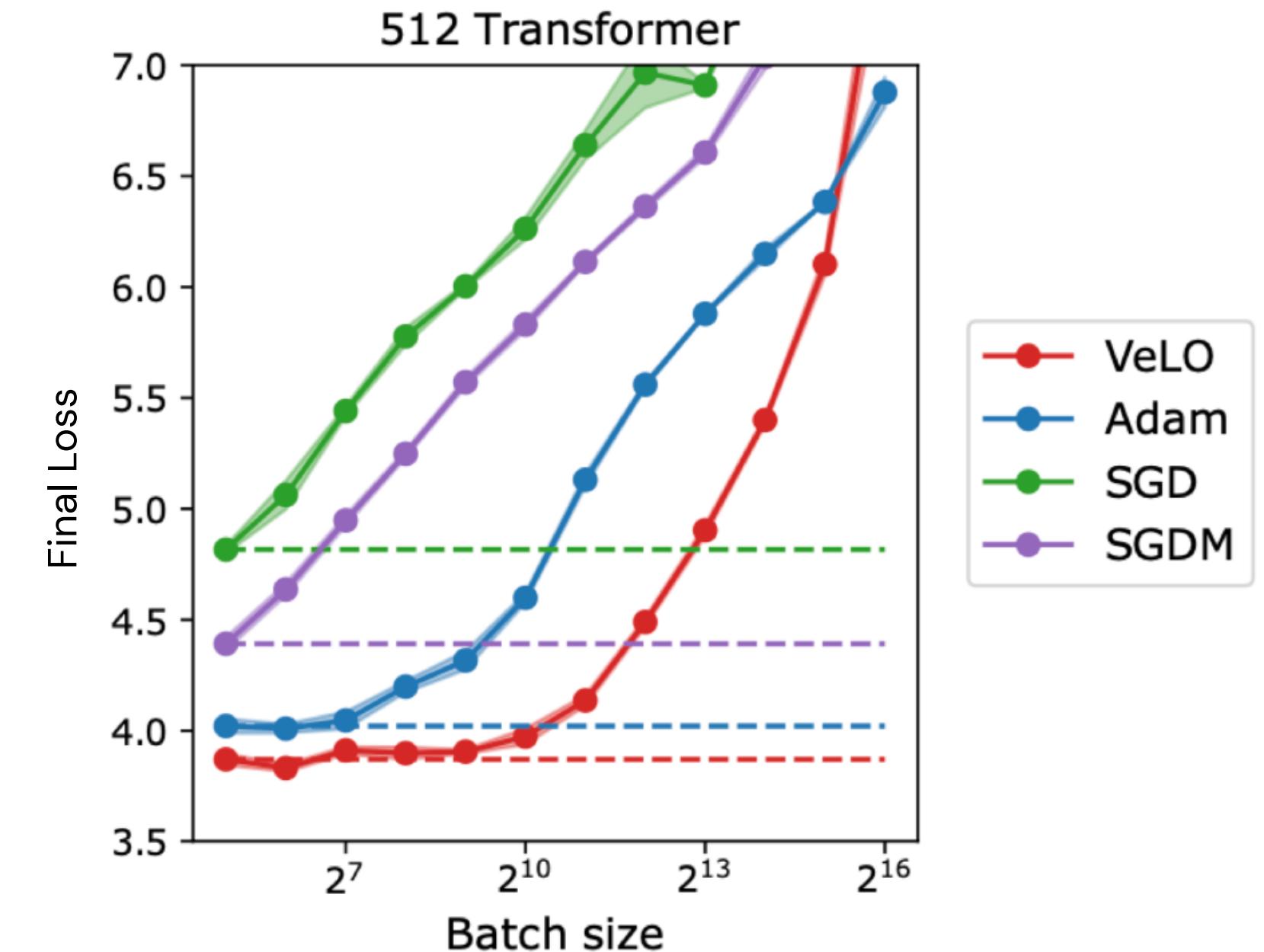
- We use LSTM-based models
 - **Momentum.** “States” can keep track of past gradients
 - **Tensor size.** Sequential prediction, coordinate-by-coordinate





Learned Optimizers

- **Pros.**
 - Less need to tune optimizers
 - Can handle larger batch sizes
 - Accelerate training!
- **Cons.**
 - Does not scale up to large models / long training / RL
 - No actual speedup (more compute)



Other topics:
Test-time adaptation

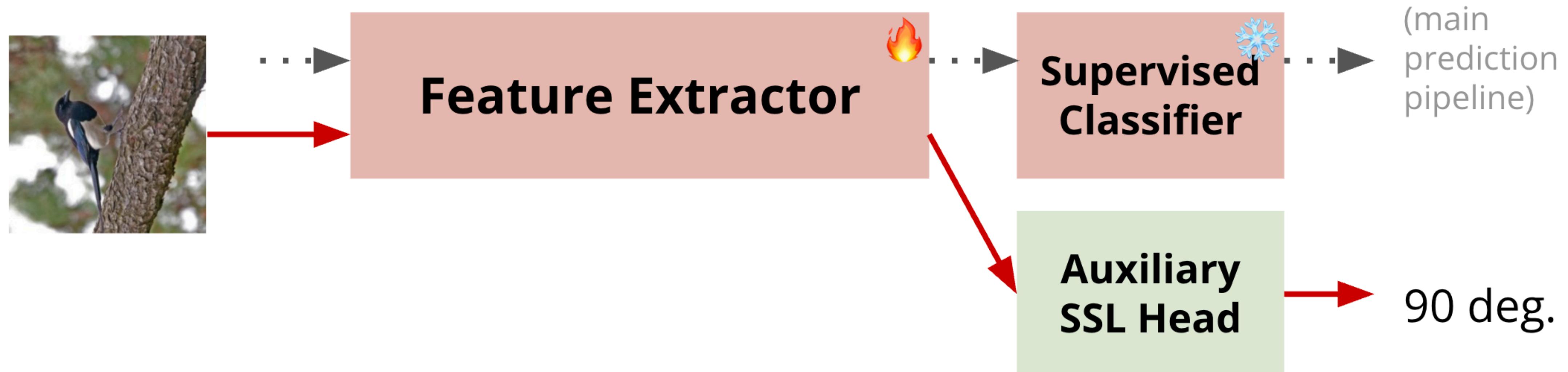
Test-Time Training / Adaptation

- **Idea.** Perform additional adaptation on given task at test time
 - Unlike meta-learning, use only the **(a batch of) unlabeled data**
 - Roughly two categories:
 - Test-Time Training. Can utilize some source data
 - Fully Test-Time Adaptation. No access to source data

setting	source data	target data	train loss	test loss
fine-tuning	-	x^t, y^t	$L(x^t, y^t)$	-
domain adaptation	x^s, y^s	x^t	$L(x^s, y^s) + L(x^s, x^t)$	-
test-time training	x^s, y^s	x^t	$L(x^s, y^s) + L(x^s)$	$L(x^t)$
fully test-time adaptation	-	x^t	-	$L(x^t)$

Test-Time Training / Adaptation

- Example. Test-Time Training (2019)
 - Fine-tune the feature map using a self-supervised learning task
 - Uses **rotation-prediction** task
 - Needs altering the orig. model to be trained using SL + SSL loss jointly



Test-Time Training / Adaptation

- Example. TENT (2021)
 - If we have a good model, maybe our predictor is **mostly correct**:
 - Thus, reinforce current predictions:
 - Use a **batch of data** to minimize **prediction entropy**
 - Tunes only scaling&shifting in BatchNorm layers

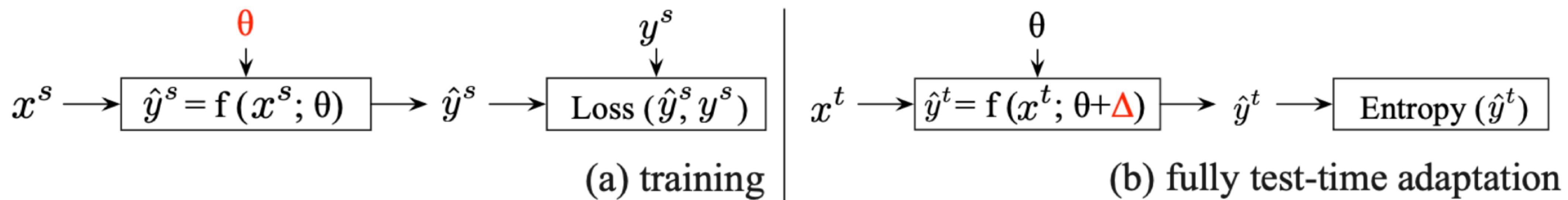


Figure 3: Method overview. Tent does not alter training (a), but minimizes the entropy of predictions during testing (b) over a constrained modulation Δ , given the parameters θ and target data x^t .

Wrapping up

- Transferring knowledge from a task to task:
 - Continual Learning
 - Meta-Learning
 - Test-time Adaptation
- **Next week.** A bit more on training efficiency

That's it for today

