

# Homework 2

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## Bisection ; steps

For a gamma density  $f$  with  $\alpha = 2$  and  $\beta = 2$ ,

1. Solve  $G(\lambda) = F(b_\lambda) - F(a_\lambda) - \alpha = 0$  and  $g(b_\lambda) = g(a_\lambda) = 0$  where  $g(x) = f(x) - \lambda$ .
2. Set  $a, b$  and  $c = \frac{a+b}{2}$ .
3. If  $\text{sign}\{g(b) - g(a)\}g(c) < 0$  then  $a \leftarrow c$ , else  $b \leftarrow c$ .

```
rm(list = ls())
# Function for solving  $g(x) = 0$ 
solveg <- function(g, a, b, l, iter.max = 100, eps = 1e-7) {
  for (i in 1:iter.max) {
    c <- (a + b)/2
    if (sign(g(b, l) - g(a, l)) * g(c, l) < 0) {
      a <- c
    } else {
      b <- c
    }
    if (abs(b - a) < eps) {
      break
    }
  }
}
```

```

    return(a)
  }
  g <- function(x, l) dgamma(x, 2, 1/2) - l
  print(x0 <- solveg(g, 0, 2, .1))

```

```
## [1] 0.5183422
```

```
dgamma(x0, 2, 1/2) # Equals lambda!
```

```
## [1] 0.1
```

```

out.f <- function(alp = 0.9, iter.max = 100, eps = 1e-10) {
  a <- 1e-10 ; b <- dgamma(2, 2, 1/2) - 1e-10
  # a, b <- minimum and maximum of lambda.
  for (i in 1:iter.max) {
    c <- (a + b)/2
    a.lam <- solveg(g, 0, 2, c)
    b.lam <- solveg(g, 2, 1e7, c)
    if (pgamma(b.lam, 2, 1/2) - pgamma(a.lam, 2, 1/2) - alp
        b <- c
    } else {
      a <- c
    }
    if (abs(b - a) < eps) break
  }
  return(c(a.lam, b.lam))
}
dgamma(out.f(), 2, 1/2) # lambda

```

```
## [1] 0.0385381 0.0385381
```

```
pgamma(out.f()[2], 2, 1/2) - pgamma(out.f()[1], 2, 1/2) # alp
```

```
## [1] 0.9
```