

Lec2_Models of Computation

Goal

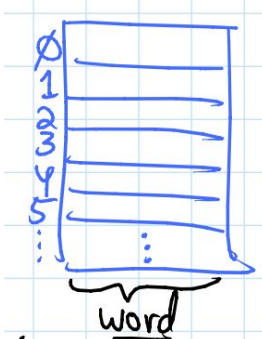

- What's an algorithm? What is time?
- Random Access Machine
- Pointer Machine
- Python Model
- Document Distance : Problem & Algorithms

What's an algorithm?

- Mathematical abstraction of computer program
- Computational procedure to solve a problem

Model of Computation

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Random Access Machine	Pointer Machine
 <p>Modeled by big array</p>	 <p>Dynamically allocated objects</p>

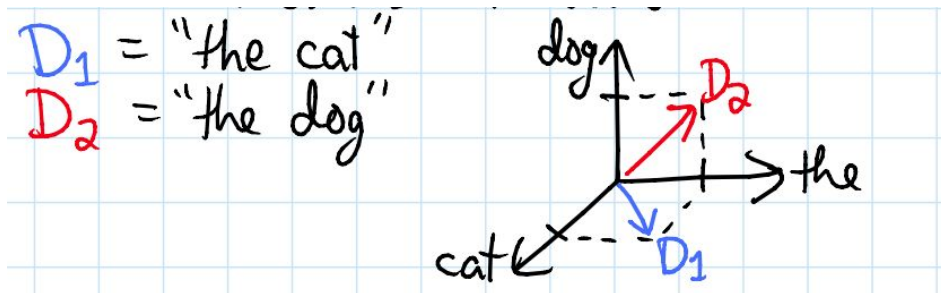
Python Model

1. List \rightarrow RAM
 - a. $L[i] = L[j] + 5 \rightarrow \Theta(1)$ time
 - b. $L.append(x) \rightarrow \Theta(1)$ time
 - c. $L = L1 + L2 \rightarrow \Theta(1 + L1 + L2)$ time

- d. $L1.\text{extend}(L2) \rightarrow \Theta(1+L2)$ time
- e. $\text{len}(L) \rightarrow \Theta(1)$ time
- f. $L.\text{sort}() \rightarrow \Theta(|L| \lg |L|)$ time
- 2. Object with $O(1)$ attributes \rightarrow Pointer machine
 - a. $x = x.\text{next} \rightarrow \Theta(1)$ time
- 3. dict
 - a. $D[\text{key}] = \text{val}$ (key in D) $\rightarrow \Theta(1)$ time
- 4. heap q
 - a. heappush & heappop $\rightarrow \Theta(\lg n)$ time
- 5. long
 - a. $x+y \rightarrow O(|x|+|y|)$ time
 - b. $x*y \rightarrow O((|x|+|y|)^{\lg 3})$ time

Document Distance Problem

- applications : find similar documents
- How to approach?
 - word = sequence of alphanumeric chars
 - document = sequence of words
 - Think of document D as **VECTOR**



- Distance : $d''(D1, D2) = (D1 \cdot D2) / (|D1| \cdot |D2|)$
- Geometric re-scaling $d(D1, D2) = \arccos(d''(D1, D2))$
- Distance Algorithm
 - Split each document into words
 - $\Theta(\text{Doc})$
 - Count word frequencies document
 - $\Theta(k \cdot \lg(k) \cdot |\text{word}|) \rightarrow k : \# \text{ words}$
 - Compute dot product
 - $O(|\text{doc}|)$

Code :
If words equal

```
        Total += count1 * count2
    If word1 <= word2
        Advance list 1
    else
        Advance list 2
    Repeat until either list done
```