



Lecture 5.

Convolutional Neural Network

Review

1. Limitation of Linear Classifier

- XOR Gate

2. Perceptron

- Perceptron = Linear Classifier
- Analogy to Neurons
- Building Block of the Neural Network

3. MLP

- MLP and the Neural Network
- The Universal Approximation Theorem
- Where Backpropagation becomes Important

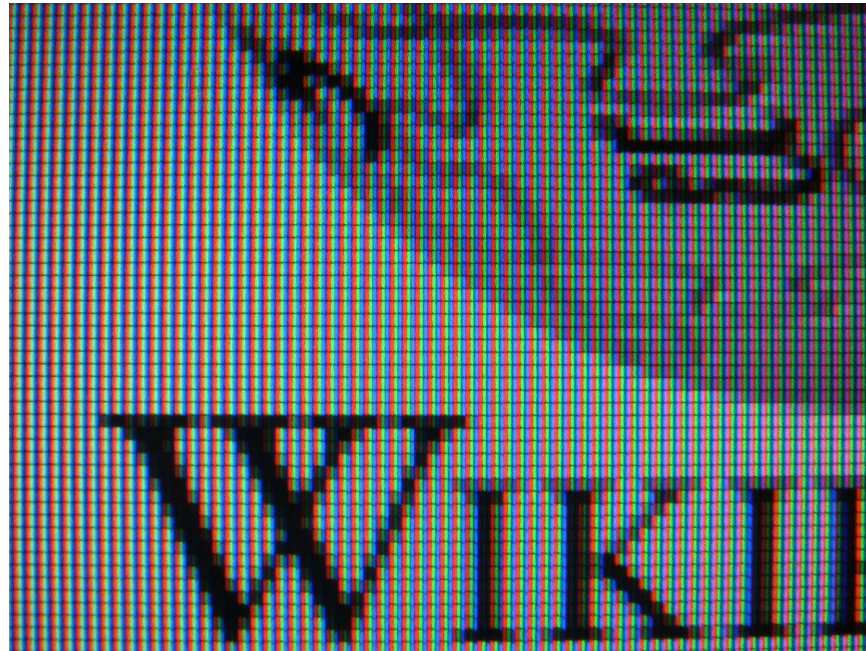
4. Limitations of MLP

Today's Contents

1. Back to Image Classification
2. Convolutional Neural Network

Back to Image Classification : Pixels

Image = Matrix of Pixels



Back to Image Classification : Pixels

What we see



What computer sees (grayscale)



$\mathbf{x} =$

(251, 181, 068, 041, 032, 071, 197,
196, 014, 132, 213, 187, 043, 041,
174, 011, 200, 254, 254, 232, 164,
202, 014, 012, 128, 242, 255, 255,
253, 212, 089, 005, 064, 196, 253,
255, 255, 251, 196, 030, 009, 165,
127, 162, 251, 254, 197, 009, 105,
062, 005, 100, 144, 097, 006, 170,
207, 083, 032, 051, 053, 134, 250)

Image from researchgate.net

Back to Image Classification : Pixels

RGB

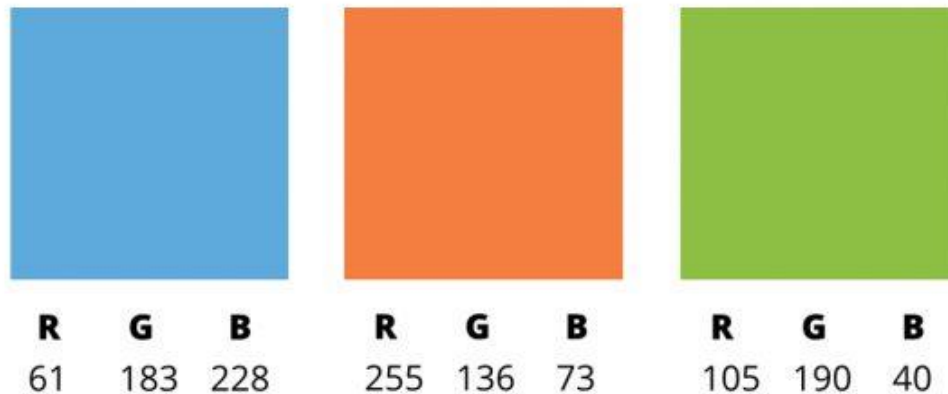


Image from <https://negliadesign.com/>

CIFAR-10

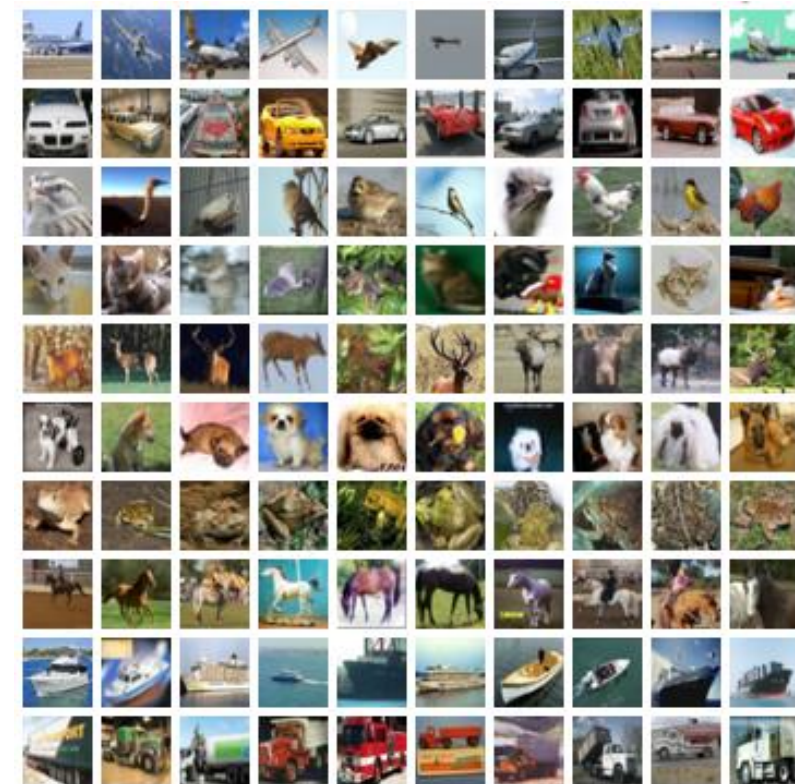
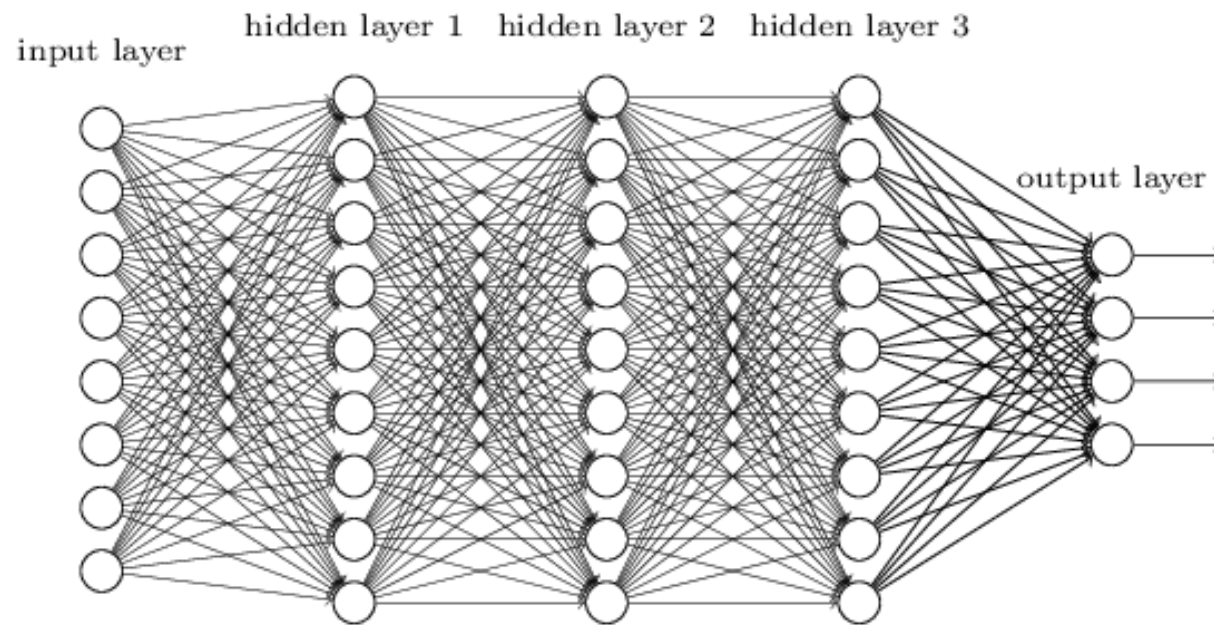


Image from <https://www.kaggle.com/>

Back to Image Classification : MLP

MLP



Back to Image Classification : MLP

Must Stretch Out Tensor into Vector

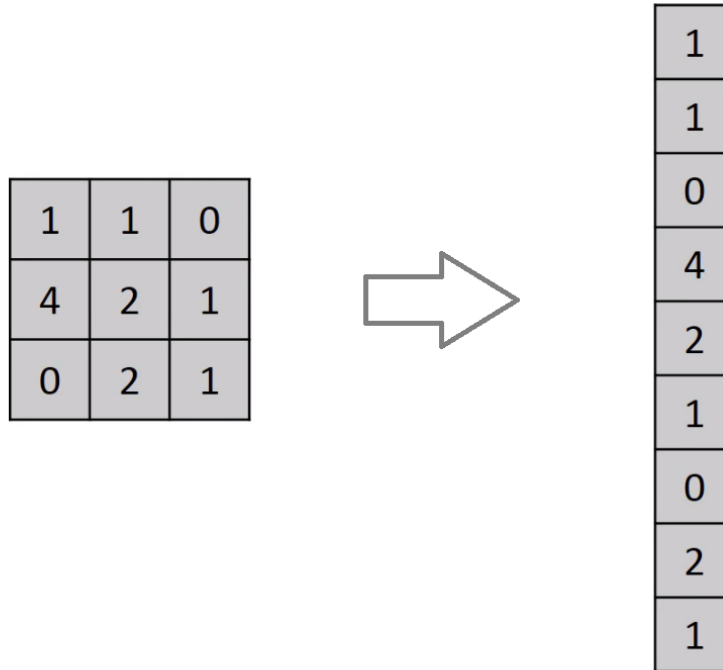


Image from <https://towardsdatascience.com>

Back to Image Classification : MLP

Worked well on MNIST

What about on CIFAR-10?

Back to Image Classification : MLP

However, MLPs are not appropriate for Image Classification...

1. Too many parameters required
2. Spatial structure is lost

Back to Image Classification : MLP

We want a model that,

1. Uses fewer parameters than MLPs
2. Preserves the spatial structure

Back to Image Classification : MLP

Recall The Universal Approximation Theorem...

"1개의 Hidden Layer를 가진 MLP로 어떤 함수도 근사할 수 있다."

However,

*"A feedforward network with a single layer is sufficient to represent any function,
But the layer may be infeasibly large and may fail to learn and generalize correctly."*

CNN : Idea

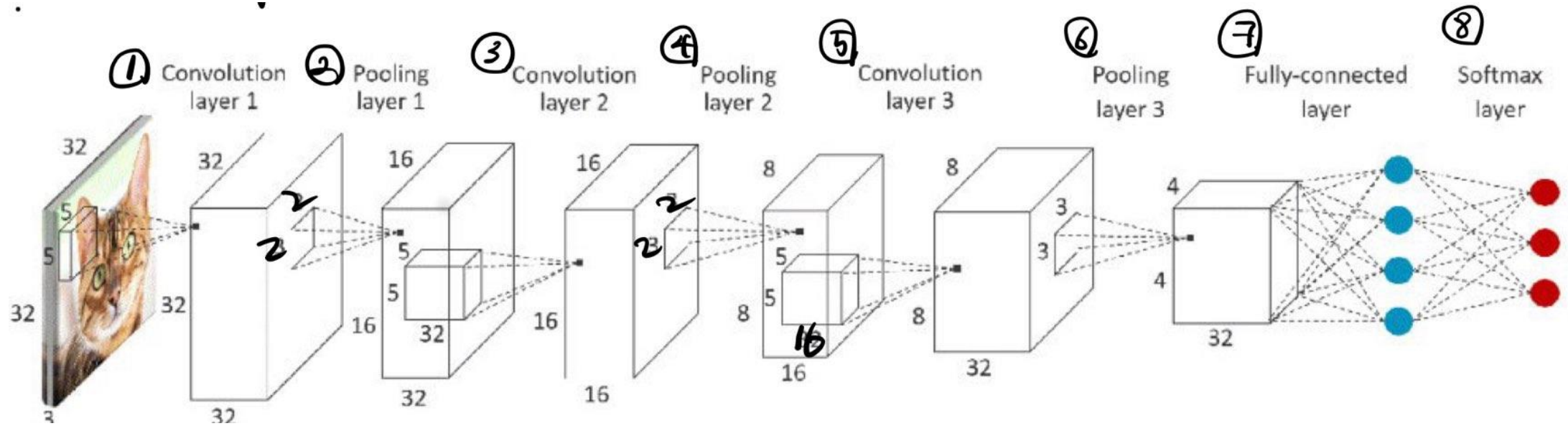
We want a model that,

1. Uses fewer parameters than MLPs
2. Preserves the spatial structure

Convolutional Neural Network to the rescue!!!

CNN : Idea

Image from <https://community.arm.com/>



What happened?!?!?!?

CNN : Idea

What happens during Tensor \rightarrow Tensor Mapping?

What are Convolution, Pooling, Fully-Connected Layers?

How does this Model extract features from spatial structure?

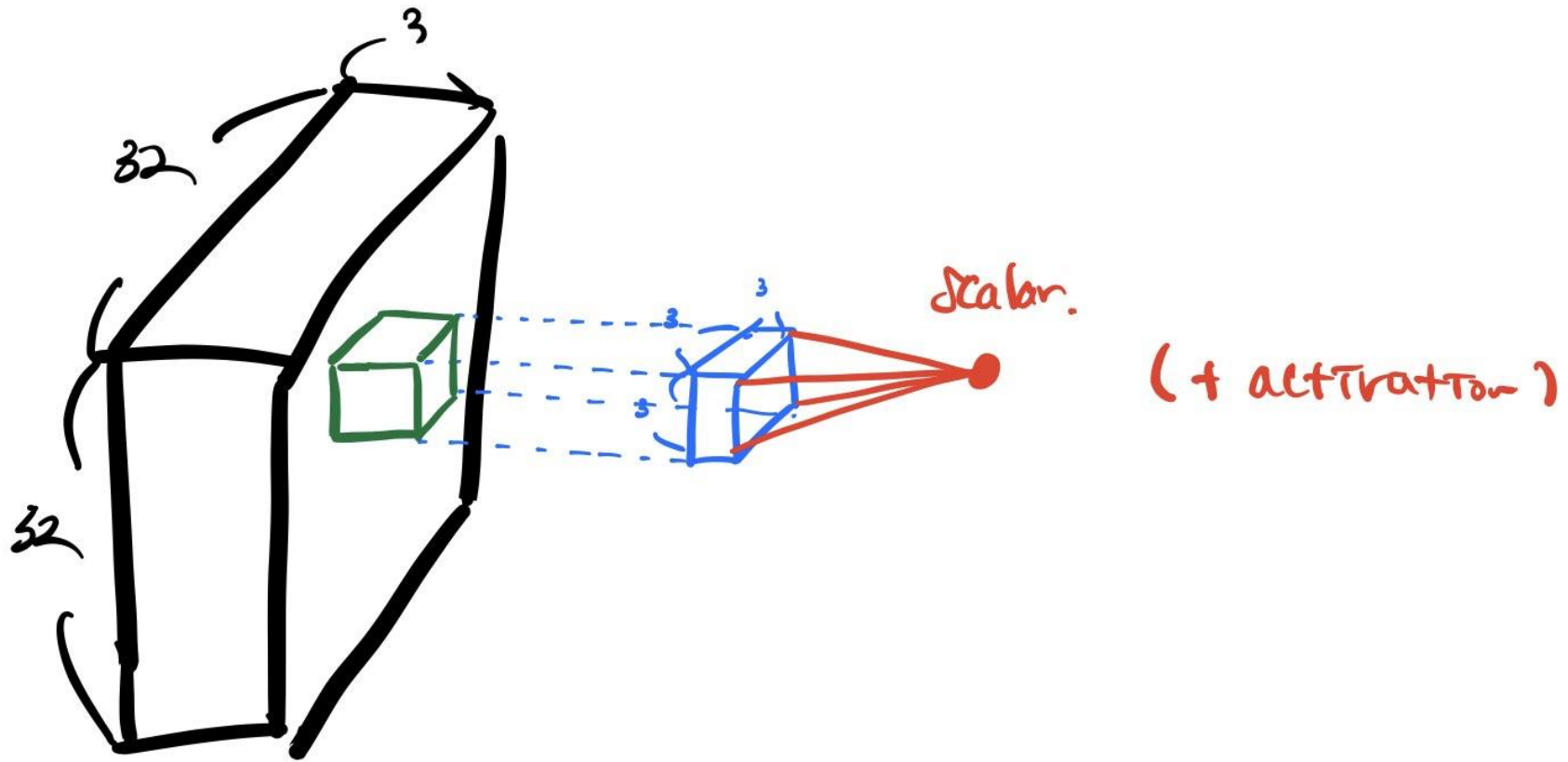
Does it use less parameters than the MLP?

CNN : Convolution

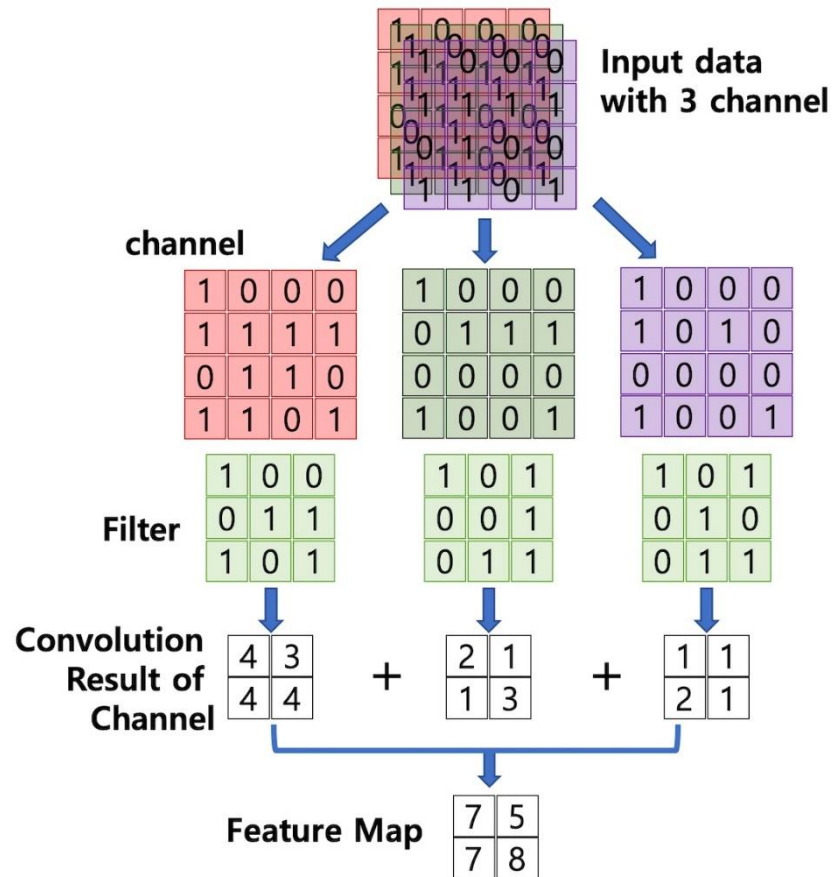
How do we map Tensor to Tensor, while preserving the spatial structure?

Apply **Filter** to small regions in the Tensor (Image)

CNN : Convolution



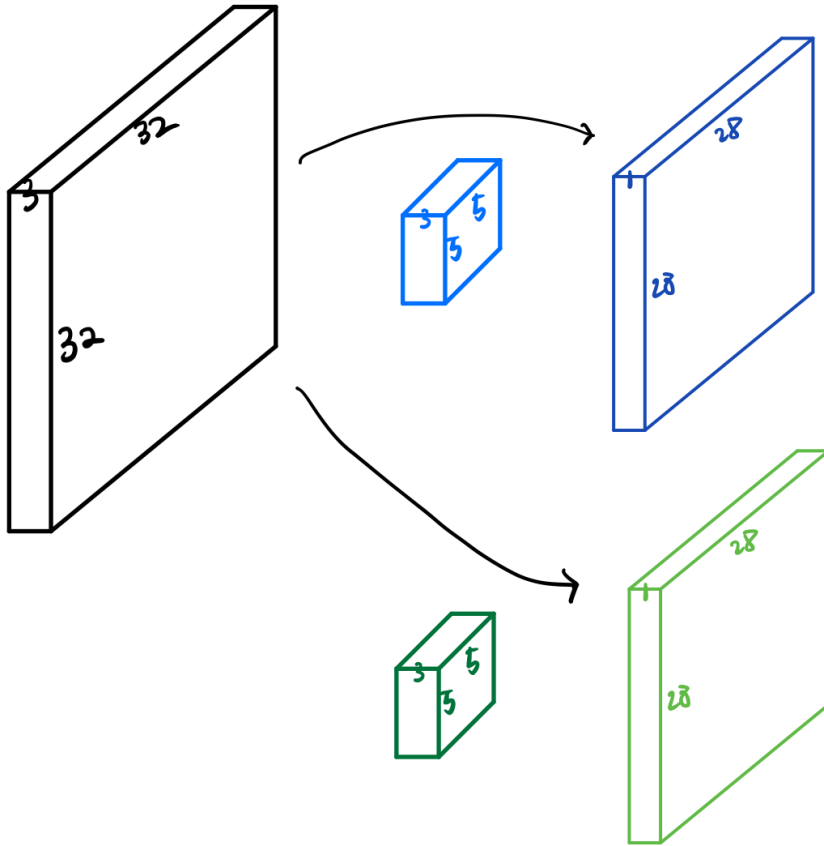
CNN : Convolution



While sliding over the tensor,
calculate the
sum of elementwise multiplication
This is called, **Convolution**

Image from taewan.kim/ppst/cnn

CNN : Convolution



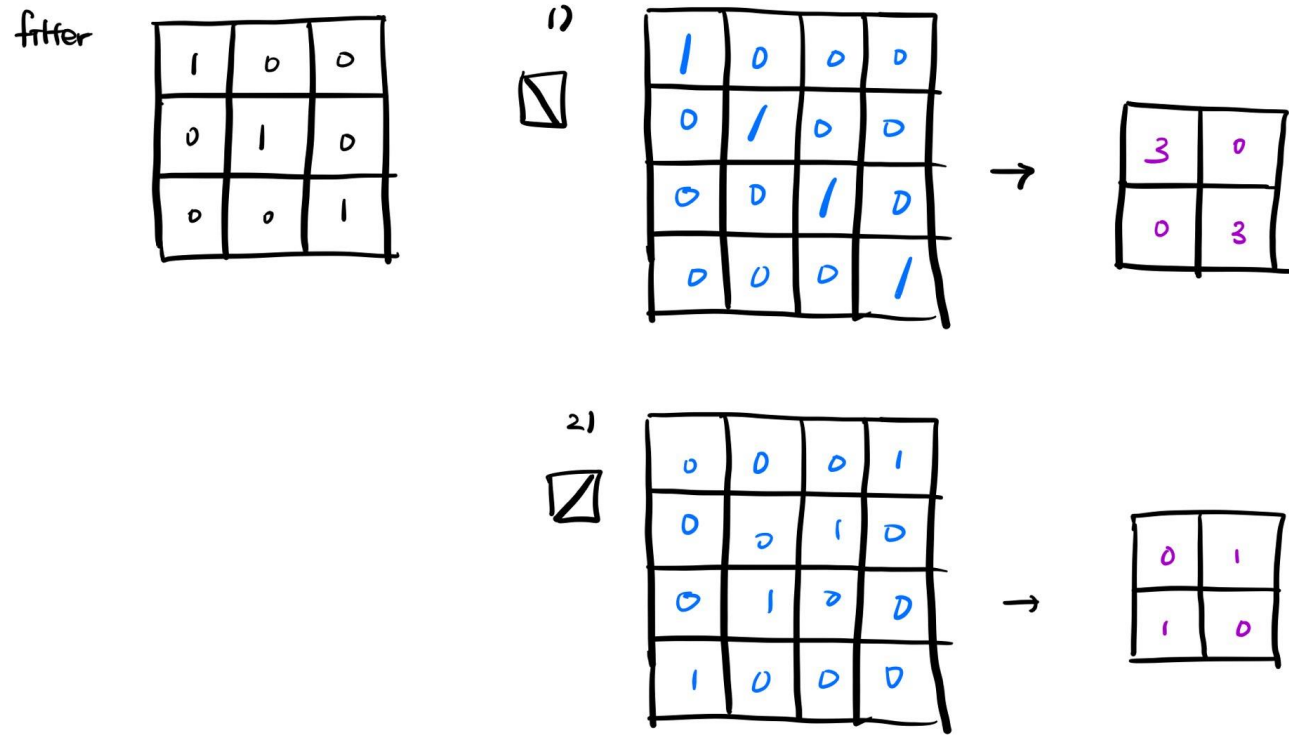
1 Filter = 1 Activation Map

CNN : Convolution

Then, how do filters extract features from the image,
while preserving the spatial structure?

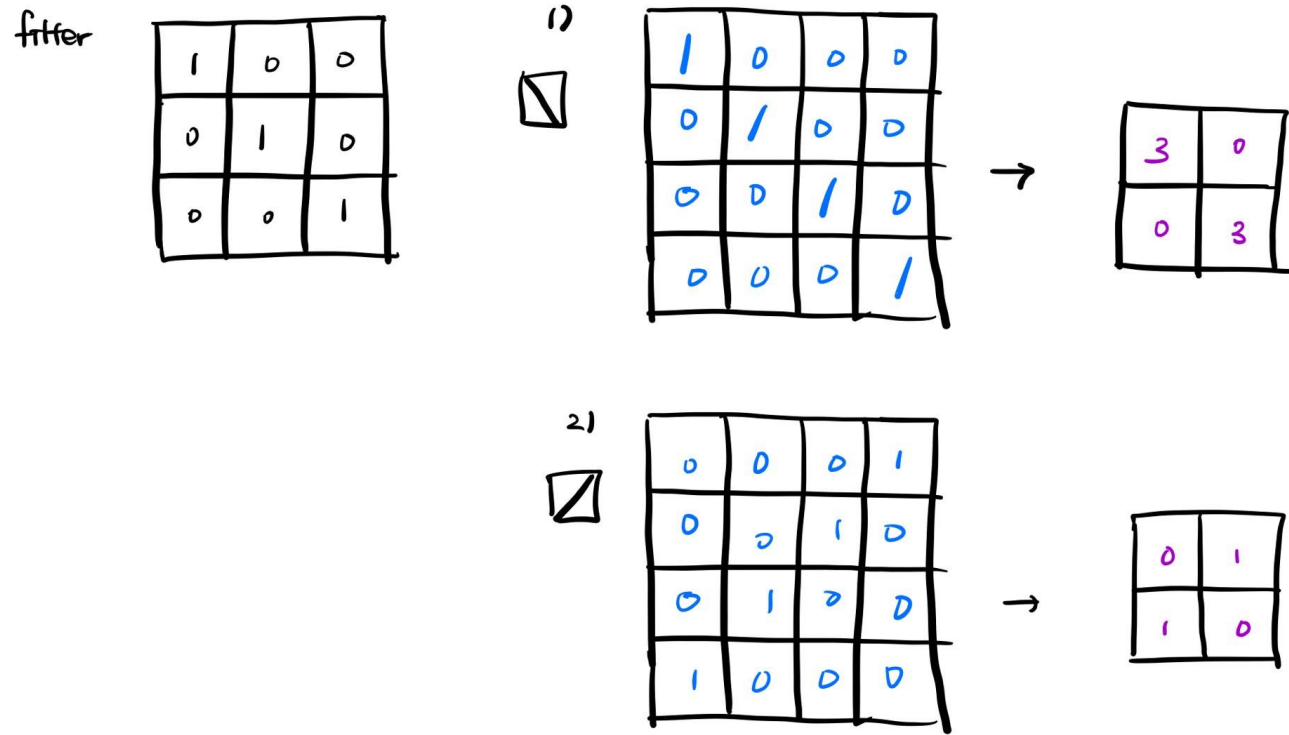
CNN : Convolution

For simplicity, assume White = 0 , Black = 1, and activation = RELU



CNN : Convolution

This filter focuses on the major diagonal... Other filters will focus on other features!



CNN : Convolution

Filters extract features from the spatial structure of the tensor

They are Parameters!!!

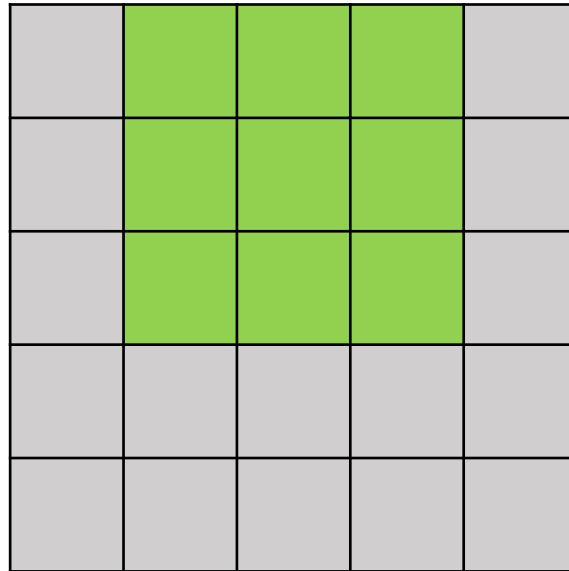
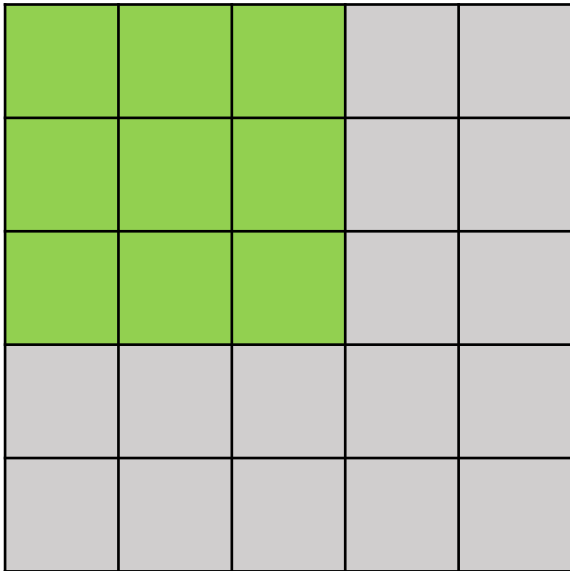
** So, they must be Updated via Backpropagation.

For more detail, read <https://becominghuman.ai/back-propagation-in-convolutional-neural-networks-intuition-and-code-714ef1c38199>

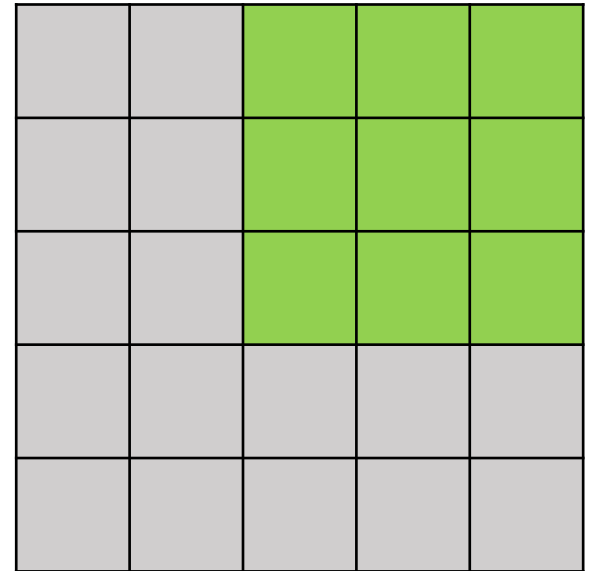
CNN : Convolution

How much does a filter move per slide? **Stride**

Stride 1



Stride 2



CNN : Convolution

$$O = \frac{I + 2Pa - F}{S} + 1$$

O = output size

N = input size

F = filter size

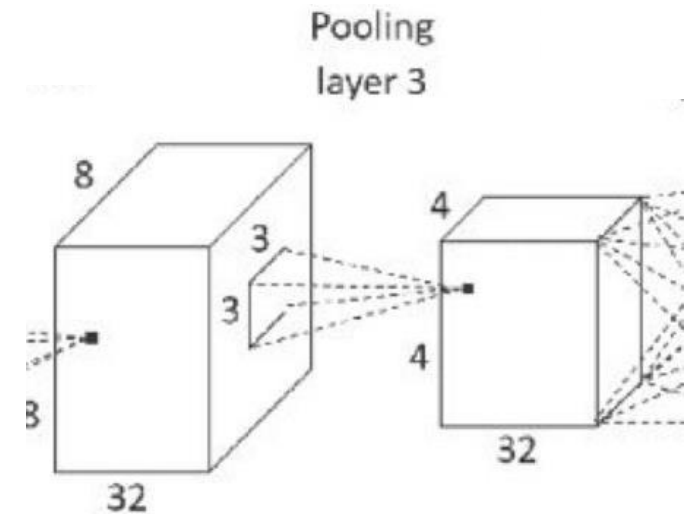
S = stride

Pa = padding size

CNN : Pooling

We want to reduce the dimension of the feature,

via **Pooling**



CNN : Pooling

Extract the representative value over a region...! No parameter involved!!!

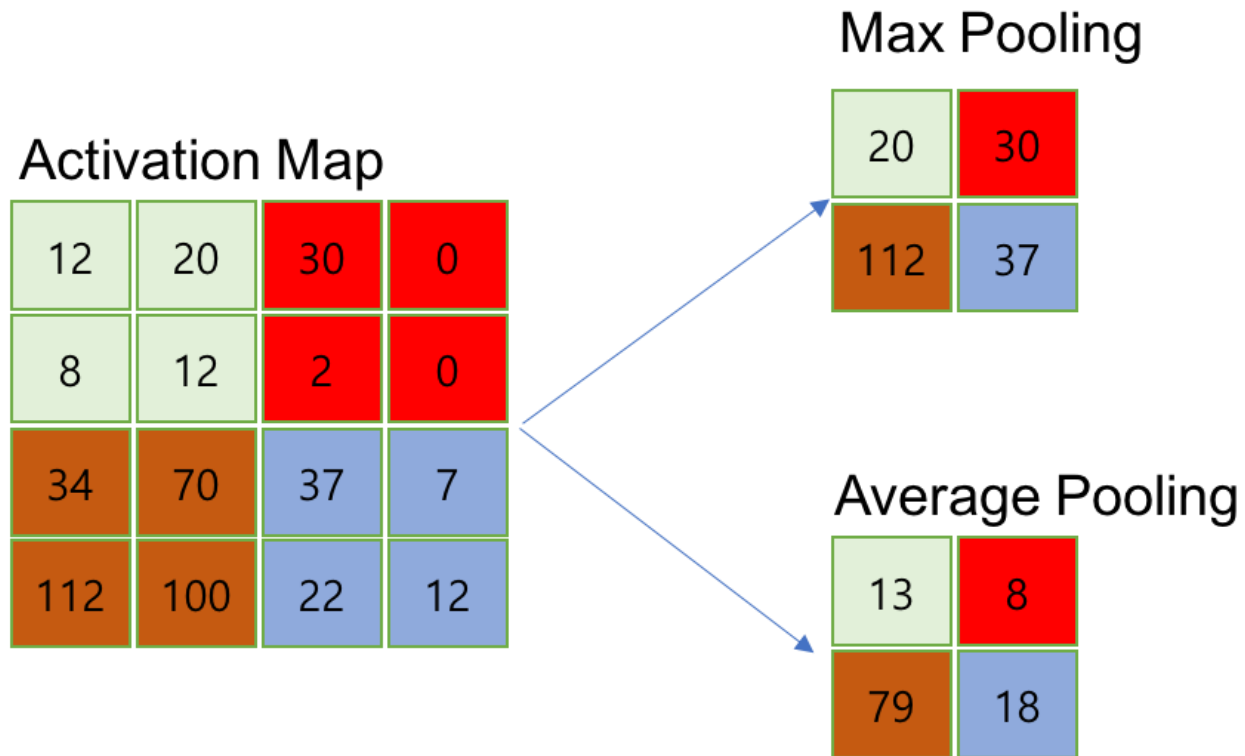


Image from taewan.kim/ppst/cnn

CNN : Pooling

$$O = \frac{I}{P_o}$$

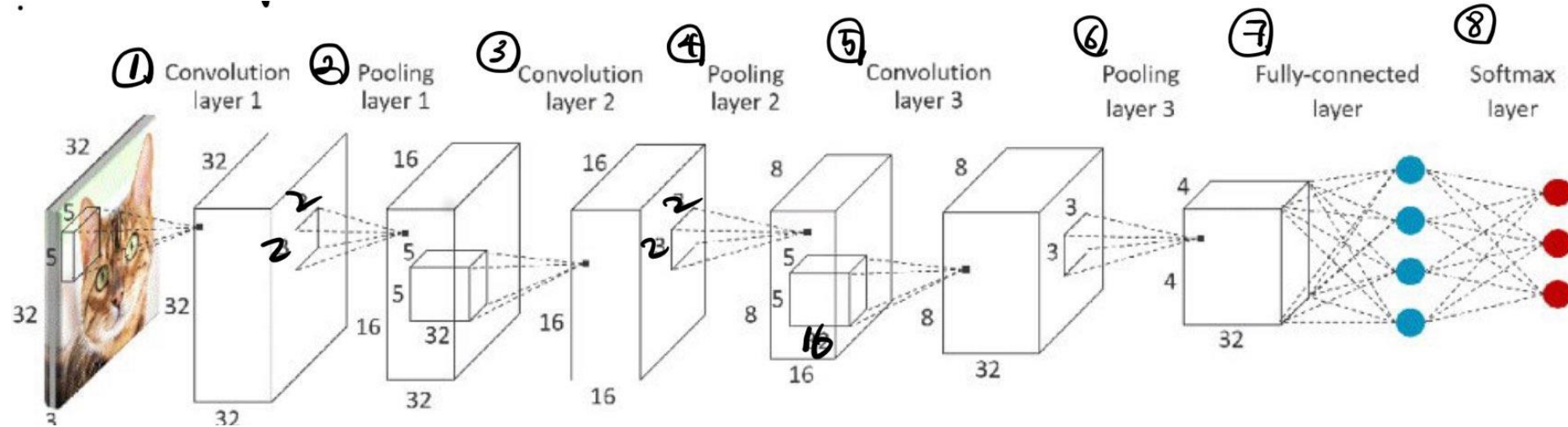
O = output size

I = input size

Po = pool size

** Generally, Pool Size = Pooling Stride

CNN : Fully-Connected Layer

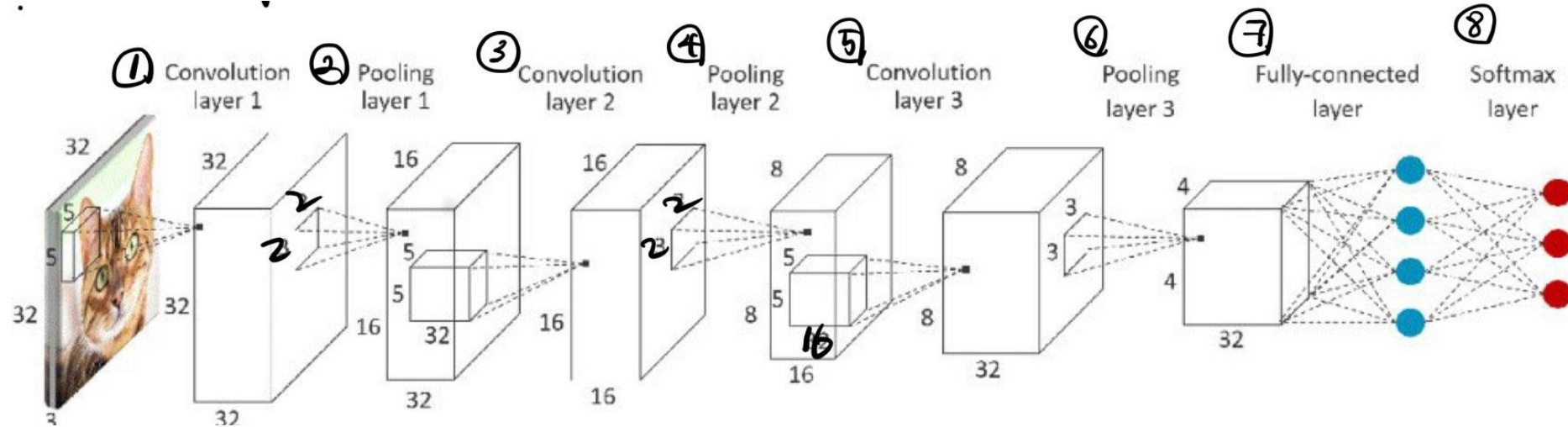


Extract features with **CONV Layers**

Then, reduce dimension with **POOL Layers**

Finally, flatten data and make classification via **FC(Fully-Connected) Layer**

CNN : Architecture



Extract features with **CONV Layers**

Then, reduce dimension with **POOL Layers**

Finally, flatten data and make classification via **FC(Fully-Connected) Layer**

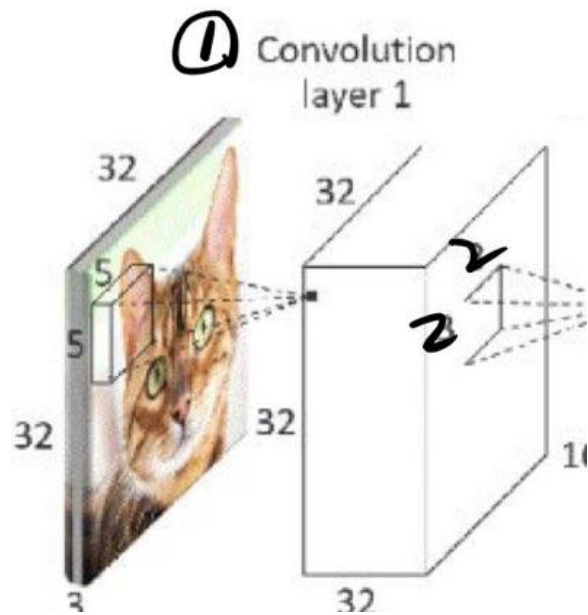
CNN : Architecture

Does it use less parameters than the MLP?

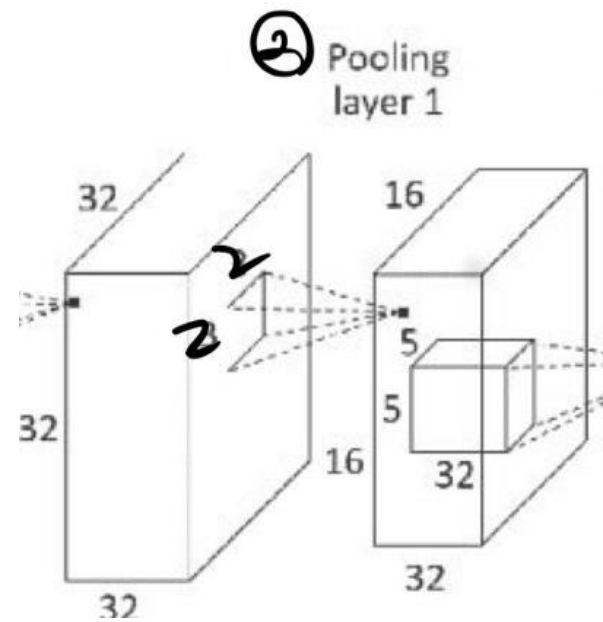
Let's follow the CNN Architecture and figure it out!!!

CNN : Architecture

CONV1

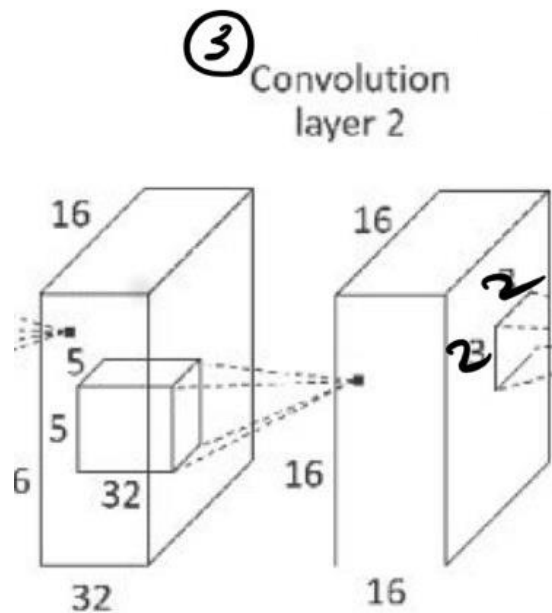


POOL1

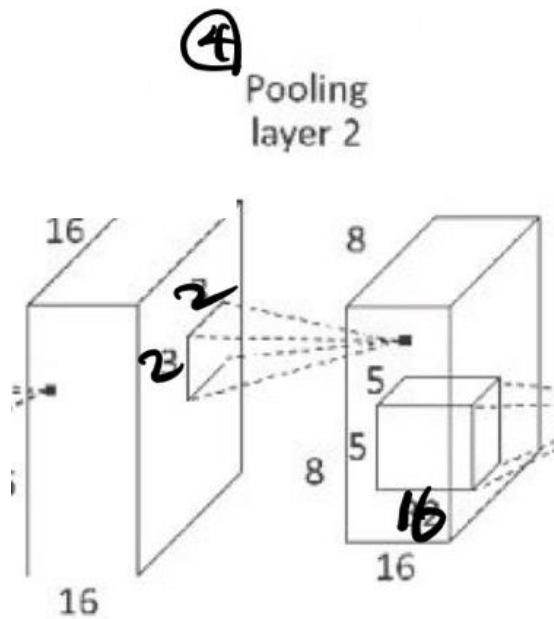


CNN : Architecture

CONV2

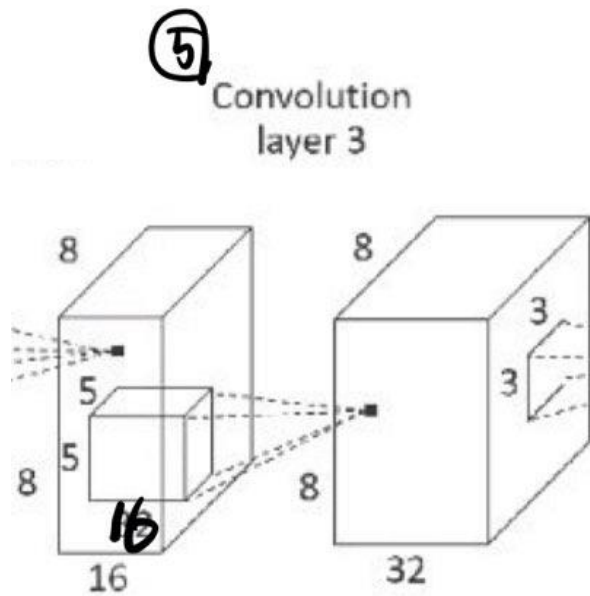


POOL2

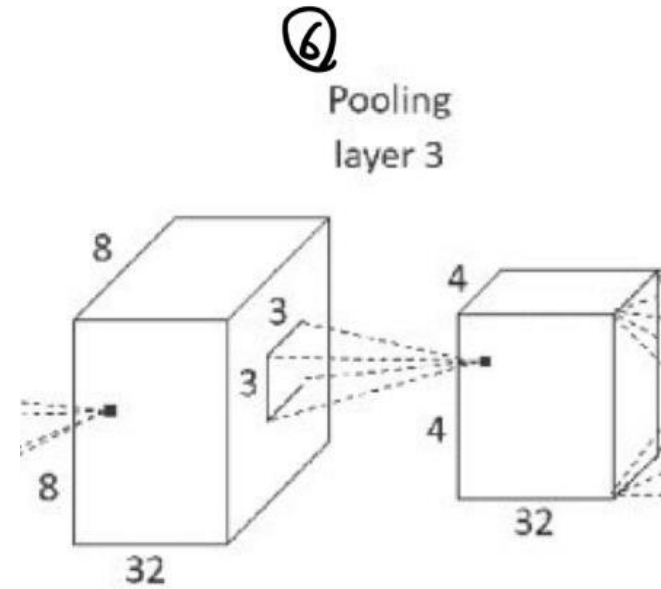


CNN : Architecture

CONV3

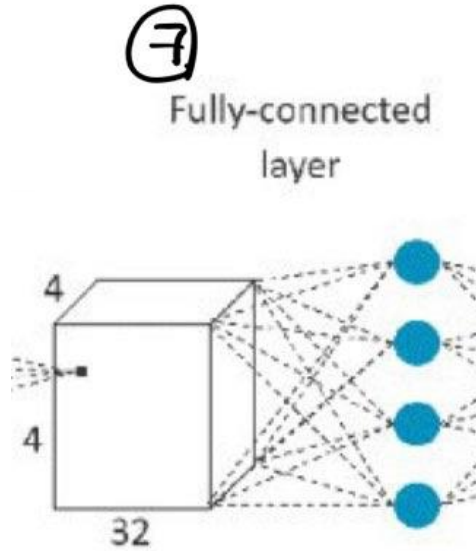


POOL3

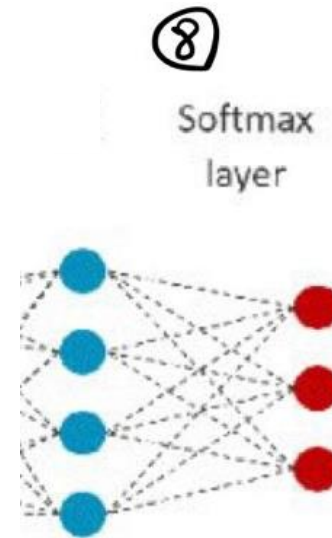


CNN : Architecture

FC



Softmax



CNN : Architecture

Total () Parameters were Used!

CNN : Architecture

However, if we used MLP instead, assuming CONV + POOL as one Hidden Layer,

$$32 * 32 * 3 \rightarrow 16 * 16 * 32 \rightarrow 8 * 8 * 16 \rightarrow 4 * 4 * 32 \rightarrow 10$$

Total () Parameters were Used!

CNN : Architecture

CNN uses much less Parameters than the MLP!!!

CNN : Performance

CIFAR-10

who is the best in CIFAR-10 ?



CIFAR-10 49 results collected

Units: accuracy %

Classify 32x32 colour images.

Result	Method	Venue	Details
96.53%	Fractional Max-Pooling	arXiv 2015	Details
95.59%	Striving for Simplicity: The All Convolutional Net	ICLR 2015	Details
94.16%	All you need is a good init	ICLR 2016	Details
94%	Lessons learned from manually classifying CIFAR-10	unpublished 2011	Details
93.95%	Generalizing Pooling Functions in Convolutional Neural Networks: Mixed, Gated, and Tree	AISTATS 2016	Details
93.72%	Spatially-sparse convolutional neural networks	arXiv 2014	
93.63%	Scalable Bayesian Optimization Using Deep Neural Networks	ICML 2015	
93.57%	Deep Residual Learning for Image Recognition	arXiv 2015	Details
93.45%	Fast and Accurate Deep Network Learning by Exponential Linear Units	arXiv 2015	Details
93.34%	Universum Prescription: Regularization using Unlabeled Data	arXiv 2015	
93.25%	Batch-normalized Maxout Network in Network	arXiv 2015	Details
93.13%	Competitive Multi-scale Convolution	arXiv 2015	
92.91%	Recurrent Convolutional Neural Network for Object Recognition	CVPR 2015	Details
92.49%	Learning Activation Functions to Improve Deep Neural Networks	ICLR 2015	Details

Classification Rankings :

[https://rodrigob.github.io/are we there yet/build/classification datasets results.html](https://rodrigob.github.io/are_we_there_yet/build/classification_datasets_results.html)

CNN : Performance



Review

We want a model that,

1. Uses fewer parameters than MLPs
2. Preserves the spatial information

Convolutional Neural Network to the rescue!!!

Preview on Next Lecture(s)

Limitations of MLP

1. Needs a lot of Labeled Data
2. Vanishing Gradient
3. Overfitting
4. Gets stuck in the Local Minima / Saddle Point

Preview on Next Lecture(s)

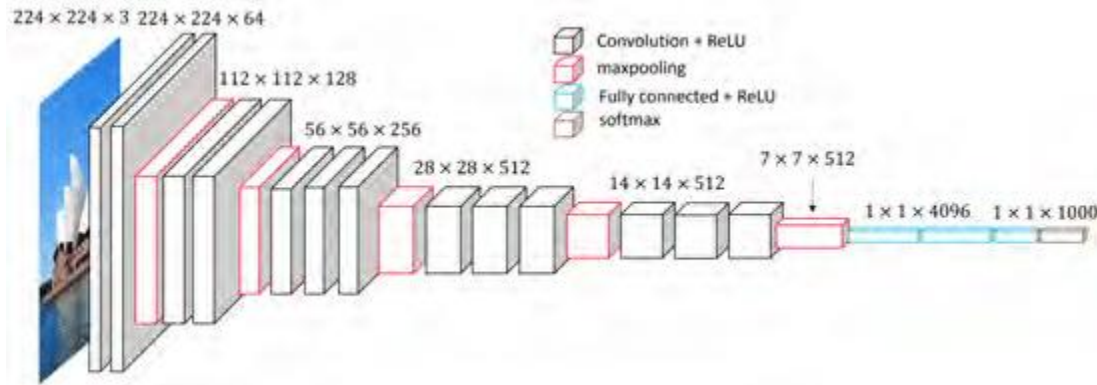


Image from researchgate.net

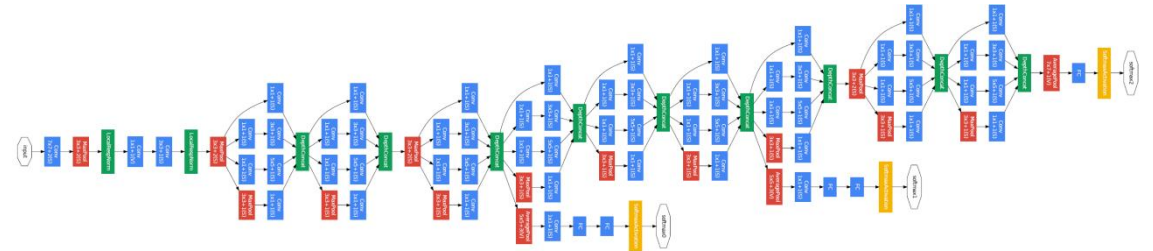


Image from medium.com