

HW6

1. Given the five pairs of (x, y) values,

x : 0 1 6 3 5

y : 4 3 0 2 1

(a) Find the least squares estimates of slope and intercept, determine the best fitting straight line (use R program).

(b) Test $H_0: \beta_1 = 0$ versus $H_1: \beta_1 \neq 0$ with $\alpha = 0.05$.

(c) Obtain a 95% confidence interval for the fitted value given $x=1$.

(d) Calculate R-squared.

2. This is the R output of a linear regression model:

Call:

lm(formula = y ~ x)

Residuals:

Min	1Q	Median	3Q	Max
-2.7252	-1.2076	-0.3564	1.2183	2.8928

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	23.6409	16.4171	1.440	0.1754
x	0.6527	0.2416	2.702	0.0192 *

Signif. codes: 0 '****' 0.001 '***' 0.01 '**' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.779 on 12 degrees of freedom

Multiple R-squared: 0.3782, Adjusted R-squared: 0.3264

F-statistic: 7.3 on 1 and 12 DF, p-value: 0.01924

(a) What are the estimates of β_0 and β_1 ?

(b) Using $\alpha = 0.05$ to test on $H_0: \beta_1 = 0$ vs $H_1: \beta_1 \neq 0$. What is the conclusion?

(c) Compute the sum of squares error and sum of squares total for this model.

- (d) For $x = 70$, use the model to predict y and construct prediction interval with 95% confidence level.