How to Mimblewimble

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1 Introduction

This paper explains how Mimblewimble transactions look like, how they are generated, and how the ledger is constructed. It is a summary of parts of an article by Fuchsbauer et al. [1].

2 Transactions

2.1 Transaction structure

- A coin in Mimblewimble is of the form C = vH + rG, π so C is a (Pedersen) commitment to the value v, with randomness r and generators H and G. π is a range proof.
- In contrast to Bitcoin, there is no notion of addresses or scripts. Ownership
 of a coin is equivalent to the knowledge of its opening. The randomness r
 of the commitment now acts as the secret key for the coin.
- A transaction consists of $C = (C_1, ..., C_n)$ input coins and $C' = (C'_1, ..., C'_n)$ output coins.

A transaction is valid iff $\sum v'_i - \sum v_i = 0$, so we get the equation

$$\sum C' - \sum C = \sum v'_{i} * H + r'_{i} * G - \sum v_{i} * H + r_{i} * G$$

If we assume the transaction is valid we are left with the excess

$$E := (\sum r_i' - \sum r_i) * G$$

Knowledge of the opening of all coins and validity of the transaction implies knowledge of E.

However, directly revealing the opening of E would leak too much information. (An adversary knowing the openings for input coins and all but one output coin, could calculate that opening knowing the Excess)

Therefore we prove the knowledge of E by providing a signature which validates

for E as a public key.

Coinbase transactions additionally have a supply added to the excess

$$E := (\sum r_i' - \sum r_i) * G - s * H$$

Finally a Mimblewimble transactions consists of:

$$tx = (s, C, C', K)$$
 with $K = (\pi, E, \sigma)$

where s is the supply, C are input coins, C' output coins, K the so called Kernel consisting of π which are range proofs for the output coins, E which is a list of excess values and σ which are signatures.

2.2 Transaction merging

An essential property of the Mimblewimble protocol is that two transactions can easily be merged into one. Assume we have two transactions:

$$tx_0 = (s_0, C_0, C'_0, (\pi_0, E_0, \sigma_0))$$

$$tx_1 = (s_1, C_1, C_1', (\pi_1, E_1, \sigma_1))$$

Then the merged transaction simply is

$$tx_m = (s_0 + s_1, C_0 \mid\mid C_1, C_0' \mid\mid C_1', (\pi_0 \mid\mid \pi_1, (E_0, E_1), (\sigma_0, \sigma_1)))$$

Note that if the signature scheme supports merging of signatures such as the BLS signature scheme, the two signature can be replaced by one reducing the size of the transaction.

The merged transaction is valid iff the transactions it is composed of are valid.

2.2.1 Subset Problem

There is a subtle problem with the way transactions are merged in Mimblewimble. It is possible to reconstruct the constituent transactions in a merged transaction, which is problematic for privacy. Given a set of inputs, outputs and transactions kernels a subset of these will recombine to reconstruct a valid transaction. Given the two transactions:

$$tx_0 = (s_0, (C_1, C_2), (C_0'), (\pi_0, E_0, \sigma_0))$$

$$tx_1 = (s_1, (C_3), (C_1), (\pi_1, E_1, \sigma_1))$$

As described above we can aggregate the transaction to

$$tx_3 = (s_0 + s_1, (C_1, C_2, C_3), (C'_0, C'_1), (\pi_0 \mid\mid \pi_1, (E_0, E_1), (\sigma_0, \sigma_1)))$$

It is trivial to try all possible permutations to recover on of the transactions where it sums successfully to zero. And once we found this transaction, in this case everything remaining will be the second transaction which was merged.

This problem is mitigated (in Grin) by including a Kernel Offset with every transaction kernel. This is a blinding factor that needs to be added back to the kernel excess to verify the commitments sum to zero, such that

$$sum(C') - sum(C) = E + offset$$

Every time two transactions are merged the offsets are combined into one offset making it impossible to decompose it to the original offsets used in the seperate transactions and therefore impossible to recover the original transactions.

2.3 Cut through

Assume C appears as an output in tx_0 and as an input, in tx_1 , then we can erase C from the input and output list and the transaction will still be valid. Therefore every time a transaction spends an output, it is virtually forgotten, improving privacy and yielding in space savings.

2.4 Ledger

The Mimblewimble ledger itself is a transaction of the discussed form. Initially, the ledger starts empty, and transactions are added and aggregated recursively. Trivially only transactions which input coins are contained in the output coins of the ledger are valid.

- The supply of the ledger is the sum of the supplies of all transactions added so far. Therefore we can easily read the total circulating supply from the ledger.
- Due to cut through the input coin list of the ledger is always empty, and the output list is what is called UTXO set in Bitcoin.

3 Transaction creation protocol

3.1 Original protocol

- 1. Sender selects input coins C of total value $v \ge p$ (p is the value he wants to transfer to the receiver), creates change coins C' of total value v p and then sends C, C', the range proofs for C', plus the opening (-p, k) of $\sum C' \sum C$ to the receiver.
- 2. The receiver creates additional output coins C'' plus range proof of total value p with keys (k_i'') and computes a signature with secret key $k + \sum k_i''$ and finializes the transaction as

$$tx = (0, C, C' \mid\mid C'', (\pi, E = \sum C' + \sum C'' - \sum C, \sigma)$$

and publishes it to the ledger.

This protocol, however, turned out to be vulnerable. The receiver can spend the change coin C' by reverting the transaction, as he can compute valid range proofs and excess signatures. Doing this would give the sender his coin back, however as the sender might not have the keys for that coin anymore, the coins could be lost.

This problem was solved (in Grin) by making the signing process a two-party protocol. Now signature computation does not require the sender to send his share of the key to the receiver anymore.

3.2 Salvaged protocol

The authors of the paper [1] propose a slightly modified version of the protocol not vulnerable to this problem.

- 1. The sender constructs a full-fledged transaction spending his input coin C, creating change coins C', as well as a special output coin C = pH + kG and sends the tx and the opening (p,k) of the special coin to the receiver. (Note that, unlike in the previous case, k is now independent of the keys of the coins C and C'.)
- 2. The receiver now creates a second transaction tx' spending the special coin, creating its output coins C'' and aggregates tx and tx'. The receiver then publishes the merged transaction to the ledger.

The only drawback of this approach is that we two transactions kernels instead of just one, making the transaction slightly bigger.

References

[1] Georg Fuchsbauer, Michele Orrù, and Yannick Seurin. Aggregate cash systems: a cryptographic investigation of mimblewimble. In *Annual International Conference on the Theory and Applications of Cryptographic Techniques*, pages 657–689. Springer, 2019.