

Assignment 4, Part 1, Specification

Bilal Jaffry

April 9, 2018

The purpose of this software design exercise is to design and implement a functional version of the solitaire card game played using a deck of cards. This documentation shows the complete specification for implementation and subsequent testing.

Card ADT Module

Module

Card

Uses

N/A

Syntax

Exported Constants

numOfRanks = 13

numOfSuits = 4

Exported Types

Card = ?

RANK = {ACE, TWO, THREE, FOUR, FIVE, SIX, SEVEN, EIGHT, NINE, TEN, JACK, QUEEN, KING}

SUIT = {SPADE, HEART, CLUB, DIAMOND}

Exported Access Programs

Routine name	In	Out	Exceptions
Card	SUIT, RANK	Card	
getRank		RANK	
getSuit		SUIT	
setRank	RANK		
setSuit	SUIT		

Semantics

State Variables

st : SUIT

rnk : RANK

State Invariant

None

Assumptions

The constructor `Card` is called for each object before instance before any other access routine is called for that object. The constructor cannot be called on an existing object.

Access Routine Semantics

`Card(s, r):`

- transition: $st, rnk := s, r$
- output: $out := self$
- exception: None

`getRank():`

- output: $out := rnk$
- exception: None

`getSuit():`

- output: $out := st$
- exception: None

`setRank(r):`

- transition: $rnk := r$
- exception: None

`setSuit(s):`

- transition: $st := s$
- exception: None

Deck ADT Module

Template Module

Deck

Uses

Card from CardADT.

Syntax

Exported Constants

MAX_CARDS = 52

Exported Types

Deck = ?

Exported Access Programs

Routine name	In	Out	Exceptions
Deck		Deck	
dealCard		Card	outside_bounds
shuffleDeck			

Semantics

State Variables

numCard: \mathbb{Z}

deckOfCards: seq of Card

State Invariant

None

Assumptions

The constructor Deck is called for each object instance before any other access routine is called for that object. The constructor cannot be called on an existing object.

Access Routine Semantics

Deck():

- transition: $\forall(i : \mathbb{N} | i \in MAX_CARDS : deckOfCards[i] = Card)$
- output: $out := self$
- exception: None

dealCard():

- transition: $numCard = numCard + 1$
- output: $out := deckOfCards[numCard]$
- exception: $(numCard > MAX_CARDS \mid numCard < 0) \implies outside_bounds()$

shuffleDeck():

- transition: $\forall(i : \mathbb{N} | i \in MAX_CARDS - 1 : swap(deckOfCards(i), deckOfCards(i+1)))$
- exception: None

Local Functions

swap: $Card \times Card \rightarrow None$

swap (a, b): Takes two cards and swaps them around. $\equiv (a = b, b = a)$

Board Module

Template Module

Board

Uses

Deck from DeckADT and Card from CardADT.

Syntax

Exported Constants

```
NUM_OF_FREECELLS = 4;  
NUM_OF_HOMECELLS = 4;  
NUM_OF_GAMECELLS = 8;
```

Exported Types

Board = ?

Exported Access Programs

Routine name	In	Out	Exceptions
Board		Board	
moveGameToGame	$\mathbb{Z}, \mathbb{Z}, \mathbb{Z}$		invalid_move(),outside_bounds()
moveGameToHome	\mathbb{Z}, \mathbb{Z}		invalid_card(),invalid_move(),empty_outsid
moveGameToFree	\mathbb{Z}, \mathbb{Z}		invalid_move(),outside_bounds()
moveFreeToGame	\mathbb{Z}, \mathbb{Z}		invalid_move(),empty_outside_bounds()
moveFreeToHome	\mathbb{Z}, \mathbb{Z}		invalid_card(),invalid_move(),empty_cells()
WinGame		\mathbb{B}	
isEmptyGameCell	\mathbb{Z}	\mathbb{B}	outside_bounds()
isEmptyHomeCell	\mathbb{Z}	\mathbb{B}	outside_bounds()
isEmptyFreeCell	\mathbb{Z}	\mathbb{B}	outside_bounds()
suitMatch	SUIT, SUIT	\mathbb{B}	
rankMatch	RANK, RANK	\mathbb{B}	
getGameCells		seq of (seq of Card)	empty_cells()
getFreeCells		seq of Card	empty_cells()
getHomeCells		seq of (seq of Card)	empty_cells()
setGameCells	Card, \mathbb{Z}		outside_bounds()

Semantics

State Variables

HomeCells: seq of (seq of Card)

FreeCells: seq of Card

GameCells: seq of (seq of Card)

dck: Deck

win: \mathbb{B}

emptyFreeCell: seq of \mathbb{B}

State Invariant

None

Assumptions

The constructor Board is called for each object instance before any other access routine is called for that object. The constructor cannot be called on an existing object.

Access Routine Semantics

Board():

- transition: $|HomeCells|, |GameCells|, |FreeCells|, win :=$
NUM_OF_HOMECELLS, NUM_OF_FREECELLS, NUM_OF_GAMECELLS,
FALSE
- transition: $dck.shuffleDeck(), \forall(i : \mathbb{N} | i \in MAX_CARDS: (\forall(j : \mathbb{N} | j \in NUM_OF_GAMECELLS:$
 $GameCells[j] = dck.dealCard())))$
- output: $out := self$
- exception: None

moveGameToGame(numOfCards, col1, col2):

- transition:
 $\forall (i : \mathbb{N} | i \in numOfCards: GameCells[col2][|GameCells[col2]|-1] = GameCells[col1][|GameCells[col1]|-1])$
- exception: $(numOfCards > availableMoves(col2)) \vee (\neg isEmptyGameCell(col1))$
 \vee
 $(\neg rankMatch(GameCells[col1][|GameCells[col1]|-1].getRank(), GameCells[col2][|GameCells[col2]|-1].getRank()))$
 \vee
 $(\neg suitMatch(GameCells[col2][|GameCells[col2]|-1].getSuit(), (GameCells[col1][|GameCells[col1]|-1].getSuit())) \implies invalid_move()$
- exception: $(\neg validCol(col1) \vee \neg validCol(col2)) \implies outside_bounds()$

moveGameToHome(gameCol, homeCol):

- transition: $HomeCells[homeCol][|HomeCells[homeCol]| - 1]$
 $= GameCells[gameCol][|GameCells[gameCol]| - 1]$
- exception:
 $\neg(isEmptyGameCell(gameCol) \wedge validGameCol(gameCol) \wedge validHomeCol(homeCol)) \implies$
 $empty_outside_bounds()$

exception:

$\neg \text{rankMatch}(\text{GameCells}[\text{gameCol}][|\text{GameCells}[\text{gameCol}| - 1].\text{getRank}(),$
 $\text{HomeCells}[\text{homeCol}][|\text{HomeCells}[\text{homeCol}| - 1].\text{getRank}())$
 \vee
 $\neg \text{suitMatch}(\text{GameCells}[\text{gameCol}][|\text{GameCells}[\text{gameCol}| - 1].\text{getSuit}(),$
 $\text{HomeCells}[\text{homeCol}][|\text{HomeCells}[\text{homeCol}| - 1].\text{getSuit}()) \implies \text{invalid_move}()$

`moveGameToFree(gameCol, freeCol):`

- transition:

$\text{FreeCells}[\text{freeCol}], \text{emptyFreeCell}[\text{freeCol}] :=$
 $\text{GameCells}[\text{gameCol}][|\text{GameCells}[\text{gameCol}| - 1], \text{emptyFreeCell}[\text{freeCol}] = \text{FALSE}$

- exception: $\neg \text{emptyFreeCell}[\text{freeCol}] \vee \text{isEmptyGameCell}(\text{gameCol}) \implies \text{invalid_move}()$

`moveFreeToGame(freeCol, gameCol):`

- transition:

$\text{GameCells}[\text{gameCol}][|\text{GameCells}[\text{gameCol}| - 1], \text{emptyFreeCell}[\text{freeCol}] :=$
 $\text{FreeCells}[\text{freeCol}], \text{TRUE}$

- exception:
 $\neg \text{rankMatch}(\text{GameCells}[\text{gameCol}][|\text{GameCells}[\text{gameCol}| - 1].\text{getRank}(),$
 $\text{FreeCells}[\text{freeCol}].\text{getRank}())$
 \vee
 $\neg \text{suitMatch}(\text{FreeCells}[\text{freeCol}].\text{getSuit}(),$
 $\text{GameCells}[\text{gameCol}][|\text{GameCells}[\text{gameCol}| - 1].\text{getSuit}()) \implies \text{invalid_move}()$

exception: $\text{isEmptyFreeCell}(\text{freeCol}) \vee \neg \text{validGameCol}(\text{gameCol}) \vee \neg \text{validFreeCol}(\text{freeCol})$
 $\implies \text{empty_outside_cells}()$

`moveFreeToHome(freeCol, homeCol):`

- transition:

$\text{HomeCells}[\text{homeCol}][|\text{HomeCells}[\text{homeCol}| - 1], \text{emptyFreeCell}[\text{freeCol}] :=$
 $\text{FreeCells}[\text{freeCol}], \text{emptyFreeCell}[\text{freeCol}] = \text{TRUE}$

- exception: $\text{isEmptyFreeCell}(\text{gameCol}) \implies \text{empty_cells}()$

exception:

$\neg \text{rankMatch}(\text{FreeCells}[\text{freeCol}].\text{getRank}(),$
 $\text{HomeCells}[\text{homeCol}][|\text{HomeCells}[\text{homeCol}|-1].\text{getRank}()])$
 \vee
 $\neg \text{suitMatch}(\text{FreeCells}[\text{freeCol}].\text{getSuit}(),$
 $\text{HomeCells}[\text{homeCol}][|\text{HomeCells}[\text{homeCol}|-1].\text{getSuit}()]) \implies \text{invalid_move}()$

$\text{isEmptyGameCell}(\text{col})$:

- output: $\text{out} := \text{GameCells}[\text{col}].\text{empty}()$
- exception: $\neg (0 \leq \text{col} < \text{NUM_OF_GAMECELLS}) \implies \text{outside_bounds}()$

$\text{isEmptyHomeCell}(\text{col})$:

- output: $\text{out} := \text{HomeCells}[\text{col}].\text{empty}()$
- exception: $\neg (0 \leq \text{col} < \text{NUM_OF_HOMECCELLS}) \implies \text{outside_bounds}()$

$\text{isEmptyFreeCell}(\text{col})$:

- output: $\text{out} := \text{emptyFreeCell}[\text{col}]$
- exception: $\neg (0 \leq \text{col} < \text{NUM_OF_FREECELLS}) \implies \text{outside_bounds}()$

$\text{getGameCells}()$:

- output: $\text{out} := \text{GameCells}$
- exception: $\text{GameCells}.\text{empty}() \implies \text{empty_cells}()$

$\text{getHomeCells}()$:

- output: $\text{out} := \text{HomeCells}$
- exception: $\text{HomeCells}.\text{empty}() \implies \text{empty_cells}()$

$\text{getFreeCells}()$:

- output: $\text{out} := \text{FreeCells}$

- exception: $\text{FreeCells.empty}() \implies \text{empty_cells}()$

$\text{setGameCells}(a, i)$:

- transition: $\text{GameCells}[i] \parallel \langle a \rangle$
- exception: $\neg \text{validGameCol}(i) \implies \text{outside_bounds}()$

$\text{rankMatch}(a, b)$:

- output: $a - b \equiv 1$
- exception: None

$\text{suitMatch}(a, b)$:

- output: $(a + 3 \equiv b) \vee (a - 3 \equiv b) \vee (a + 1 \equiv b) \vee (a - 1 \equiv b)$
- exception: None

$\text{WinGame}()$:

- output: $+(i : \mathbb{N} \mid i \in \text{NUM_OF_HOMECELLS} \wedge |\text{HomeCells}[i]| \equiv \text{numOfRanks}: 1) \equiv \text{NUM_OF_HOMECELLS}$
- exception: None

Local Functions

$\text{validGameCol}: \mathbb{Z} \rightarrow \mathbb{B}$

$\text{validGameCol}(\text{gameCol}) \equiv 0 \leq \text{gameCol} \leq (\text{NUM_OF_GAMECELLS})$

$\text{validFreeCol}: \mathbb{Z} \rightarrow \mathbb{B}$

$\text{validFreeCol}(\text{freeCol}) \equiv 0 \leq \text{freeCol} \leq (\text{NUM_OF_FREECELLS})$

$\text{validGameCol}: \mathbb{Z} \rightarrow \mathbb{B}$

$\text{validHomeCol}(\text{homeCol}) \equiv 0 \leq \text{homeCol} \leq (\text{NUM_OF_HOMECELLS})$

$\text{availableMoves} \mathbb{Z} \rightarrow \mathbb{Z}$

$\text{availableMoves}(\text{targetCol}) \equiv$

$\text{freeSpots} = +(i : \mathbb{N} \mid i \in \text{NUM_OF_FREECELLS} \wedge \text{isEmptyFreeCell}(i) : 1)$

$\text{gameSpots} = +(j : \mathbb{N} \mid j \in \text{NUM_OF_GAMECELLS} \wedge \text{isEmptyGameCell}(j) : 1)$

$\vee -(k : \mathbb{N} \mid k = \text{targetCol} : -1)$

$\implies \text{availableMoves} = \text{freeSpots} \times 2^{\text{gameSpots}}$