

# Topic 5

## Network Layer

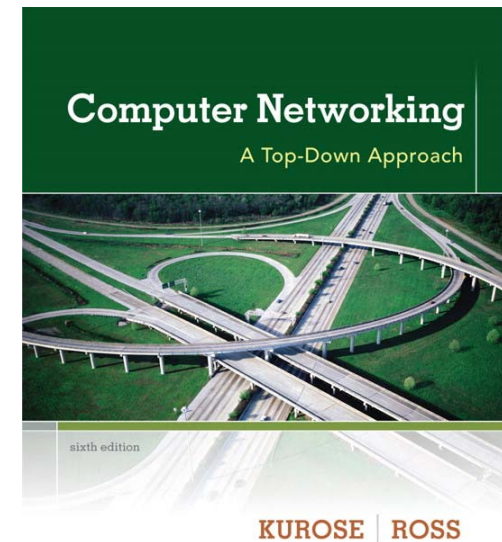
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**Computer  
Networking: A Top  
Down Approach**  
6<sup>th</sup> edition  
Jim Kurose, Keith Ross  
Addison-Wesley  
March 2012

# Topic 5: outline

## 5.1 introduction

## 5.2 what's inside a router

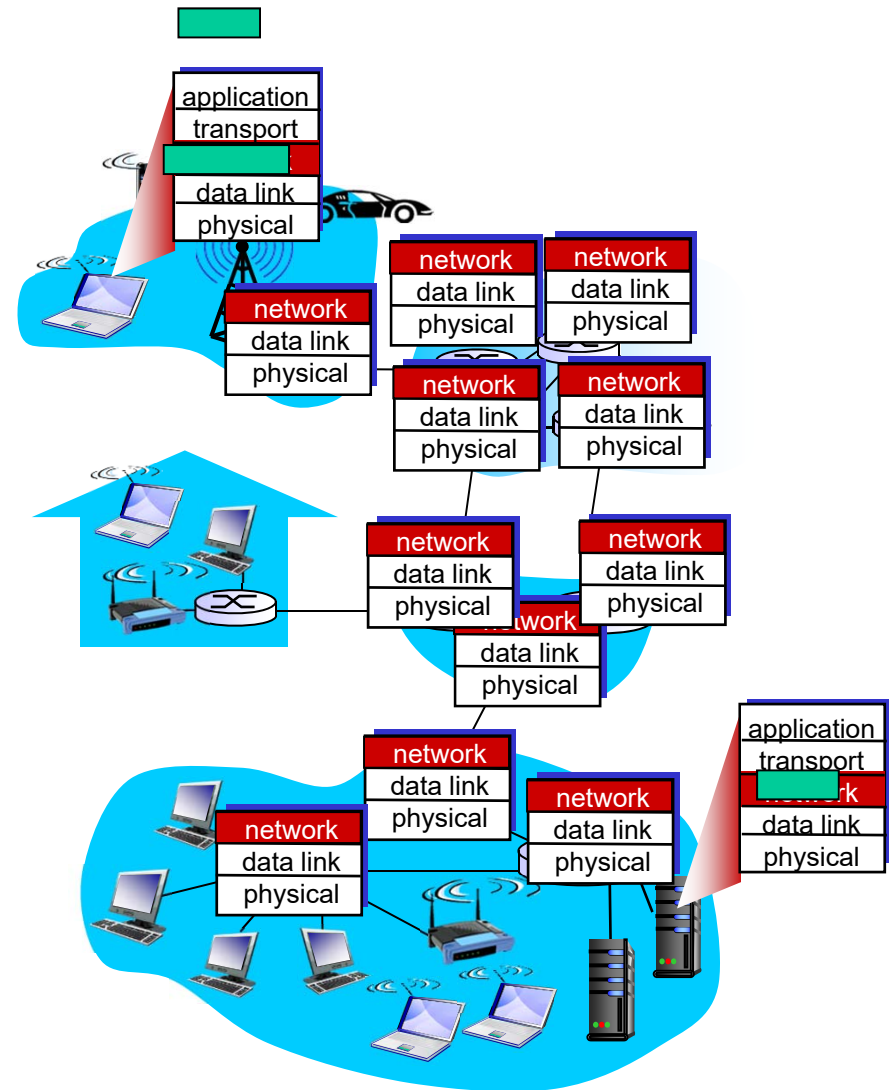
## 5.3 IP: Internet Protocol

- datagram format
- IPv4 addressing
- ICMP
- IPv6

## 5.4 routing algorithms

# Network layer

- ❖ transport segment from sending to receiving host
- ❖ on sending side encapsulates segments into datagrams
- ❖ on receiving side, delivers segments to transport layer
- ❖ network layer protocols in *every* host, router
- ❖ router examines header fields in all IP datagrams passing through it



# Two key network-layer functions

- ❖ *forwarding*: move packets from router's input to appropriate router output

- ❖ *routing*: determine route taken by packets from source to dest.

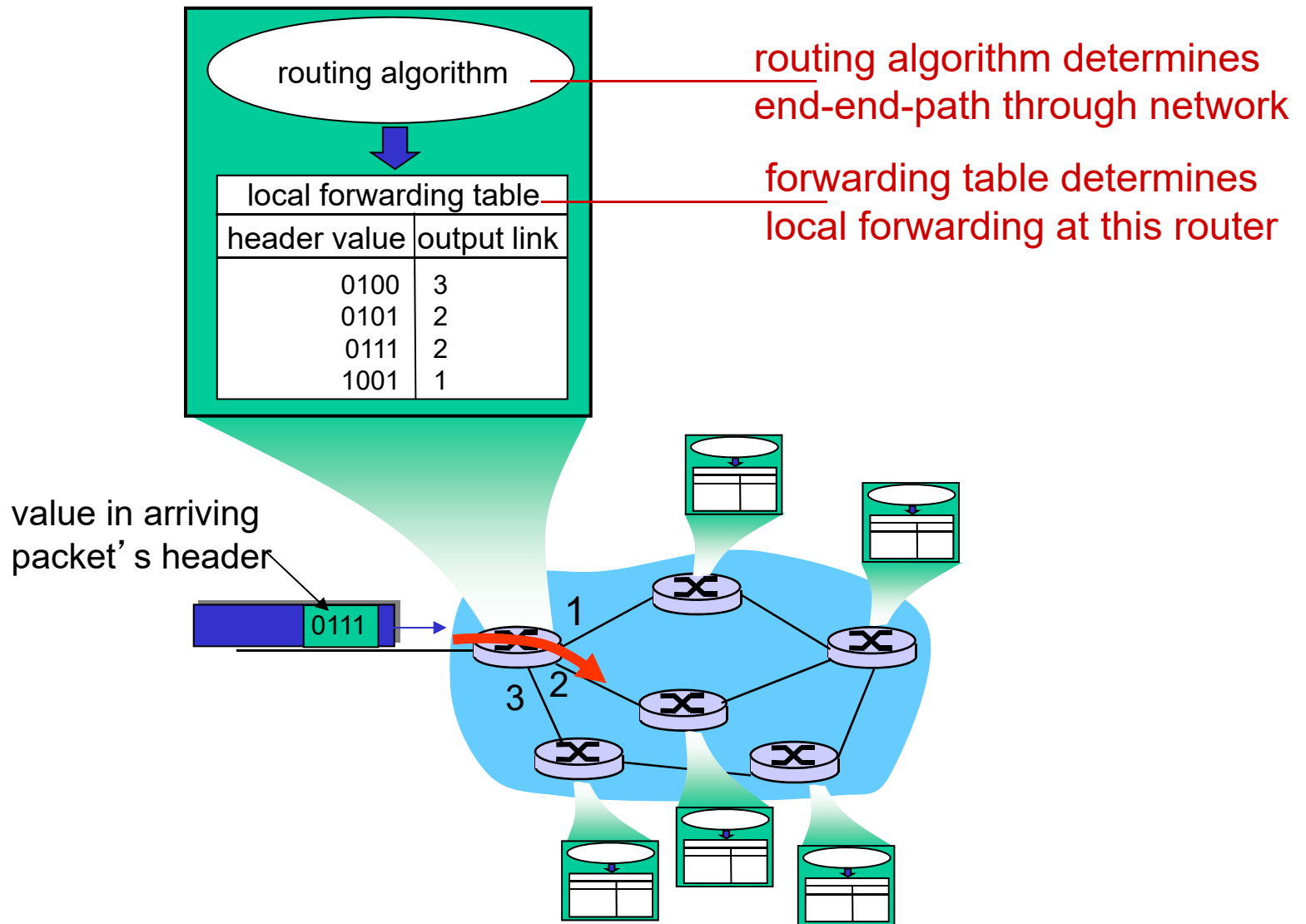
  - *routing algorithms*

*analogy:*

- ❖ *routing*: process of planning trip from source to dest

- ❖ *forwarding*: process of getting through single interchange

# Interplay between routing and forwarding



# Network service model

*Q:* What *service model* for “channel” transporting datagrams from sender to receiver?

*example services for individual datagrams:*

- ❖ guaranteed delivery
- ❖ guaranteed delivery with less than 40 msec delay

*example services for a flow of datagrams:*

- ❖ in-order datagram delivery
- ❖ guaranteed minimum bandwidth to flow
- ❖ restrictions on changes in inter-packet spacing

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5.1 introduction

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5.3 IP: Internet Protocol

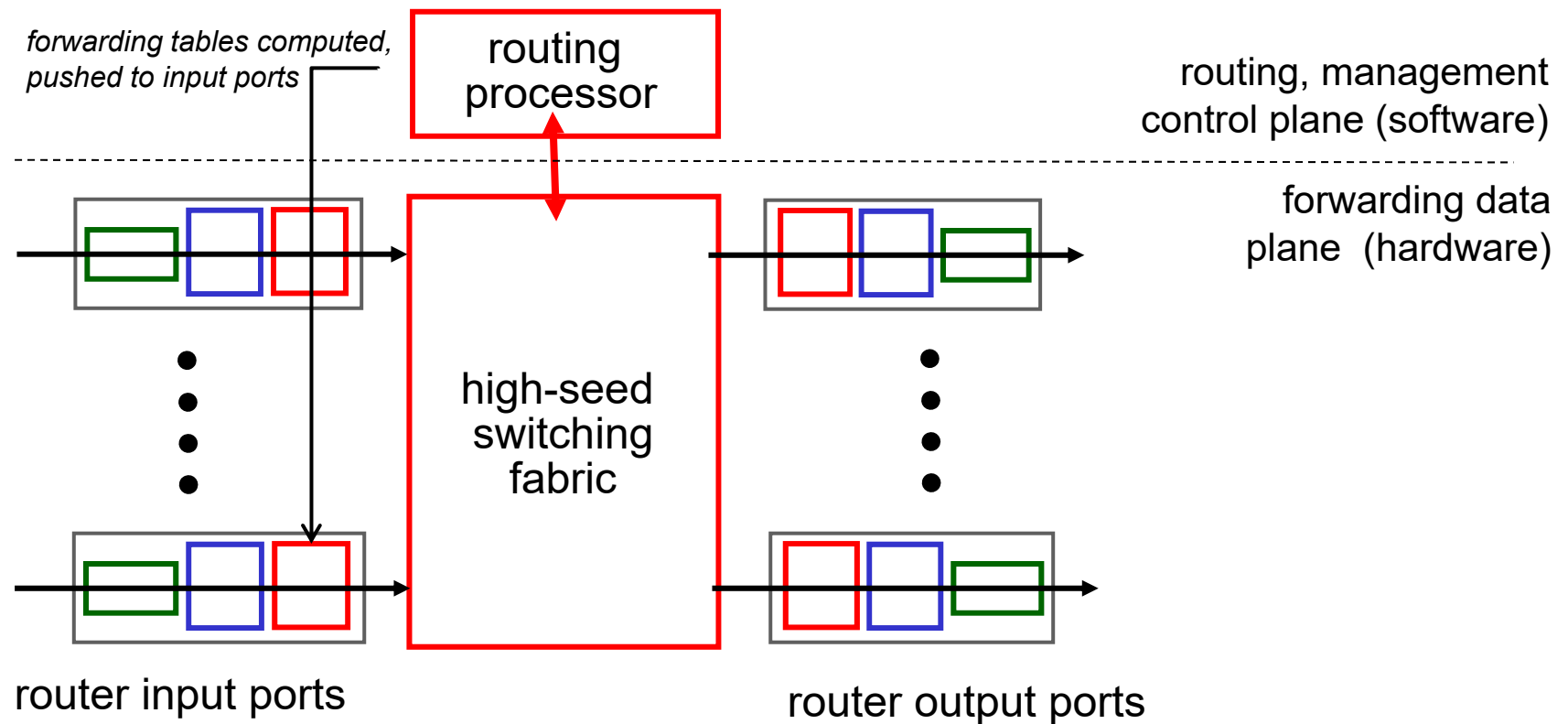
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5.4 routing algorithms

# Router architecture overview

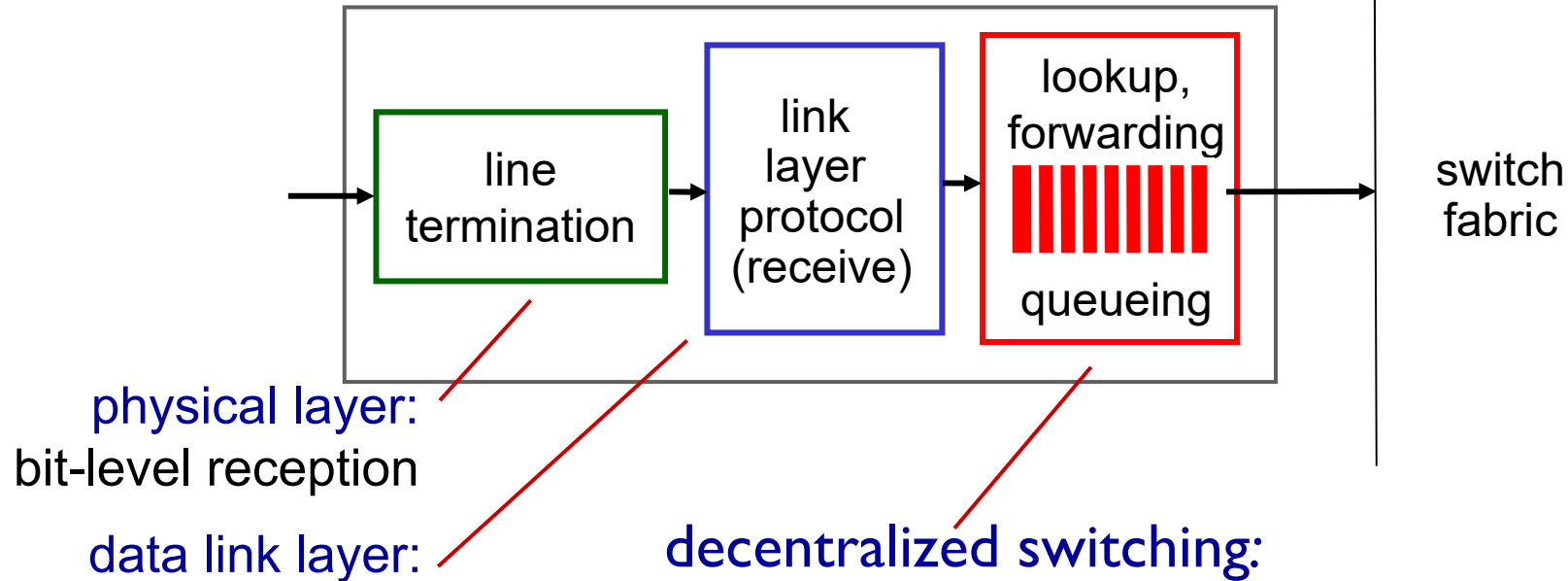
two key router functions:

- ❖ run routing algorithms/protocol
- ❖ *forwarding* datagrams from incoming to outgoing link





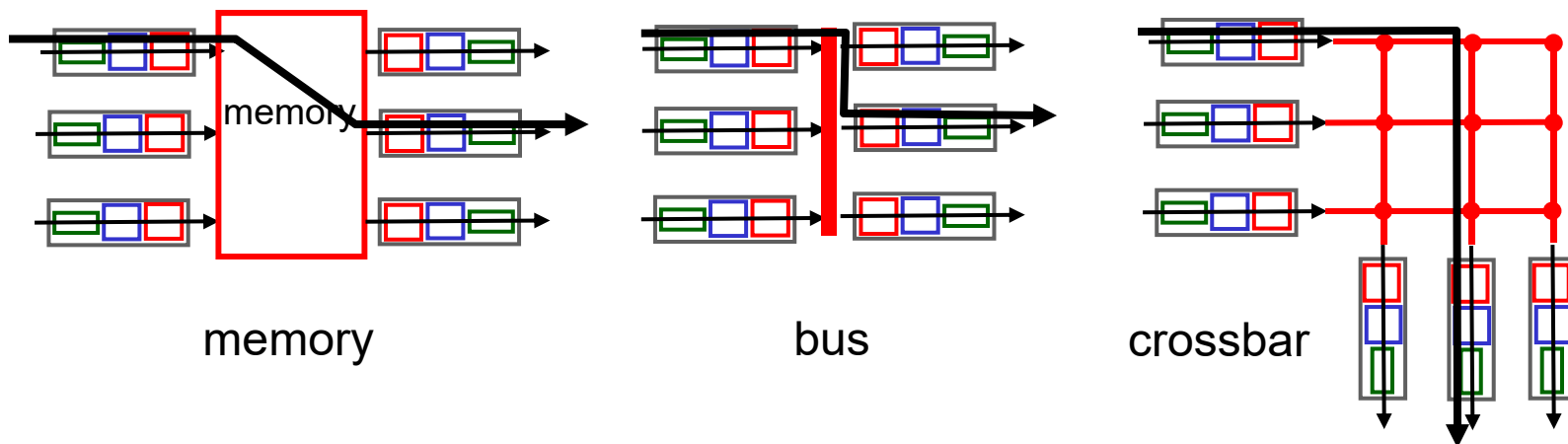
# Input port functions



- ❖ given datagram dest., lookup output port using forwarding table in input port memory (*“match plus action”*)
- ❖ goal: complete input port processing at ‘line speed’
- ❖ queueing: if datagrams arrive faster than forwarding rate into switch fabric

# Switching fabrics

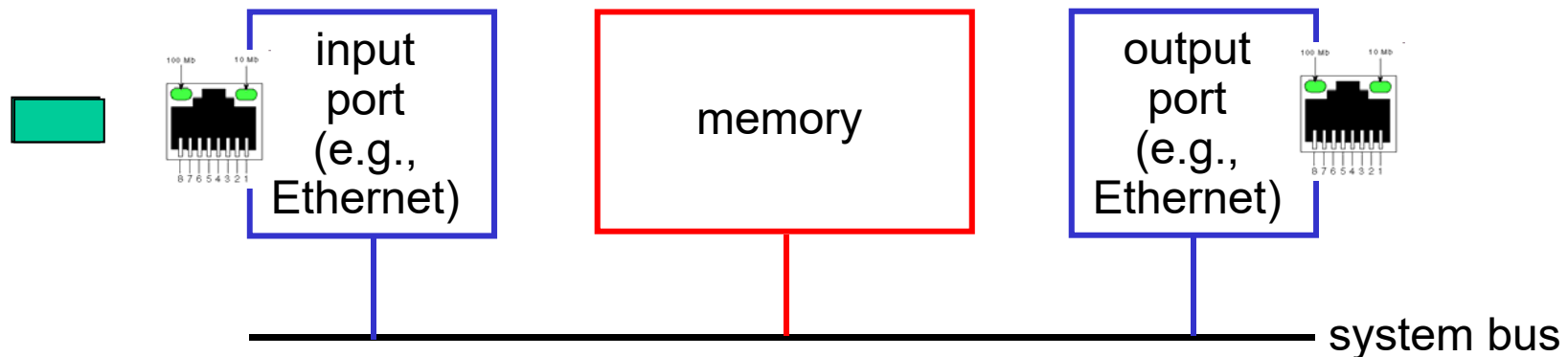
- ❖ transfer packet from input buffer to appropriate output buffer
- ❖ switching rate: rate at which packets can be transfer from inputs to outputs
  - often measured as multiple of input/output line rate
  - N inputs: switching rate N times line rate desirable
- ❖ three types of switching fabrics



# Switching via memory

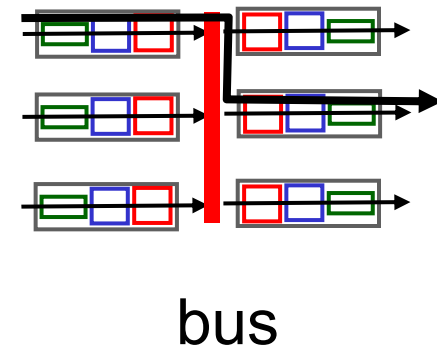
## *first generation routers:*

- ❖ traditional computers with switching under direct control of CPU
- ❖ packet copied to system's memory
- ❖ speed limited by memory bandwidth (2 bus crossings per datagram)



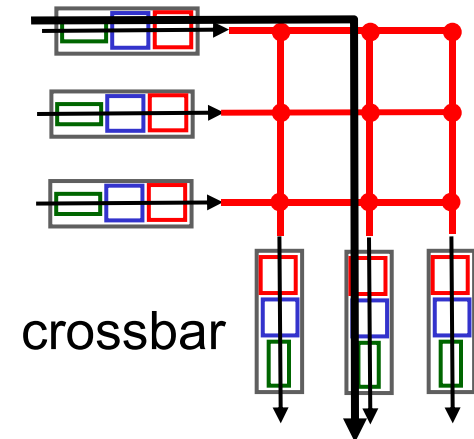
# Switching via a bus

- ❖ datagram from input port memory to output port memory via a shared bus
- ❖ *bus contention*: switching speed limited by bus bandwidth
- ❖ 32 Gbps bus, Cisco 5600: sufficient speed for access and enterprise routers

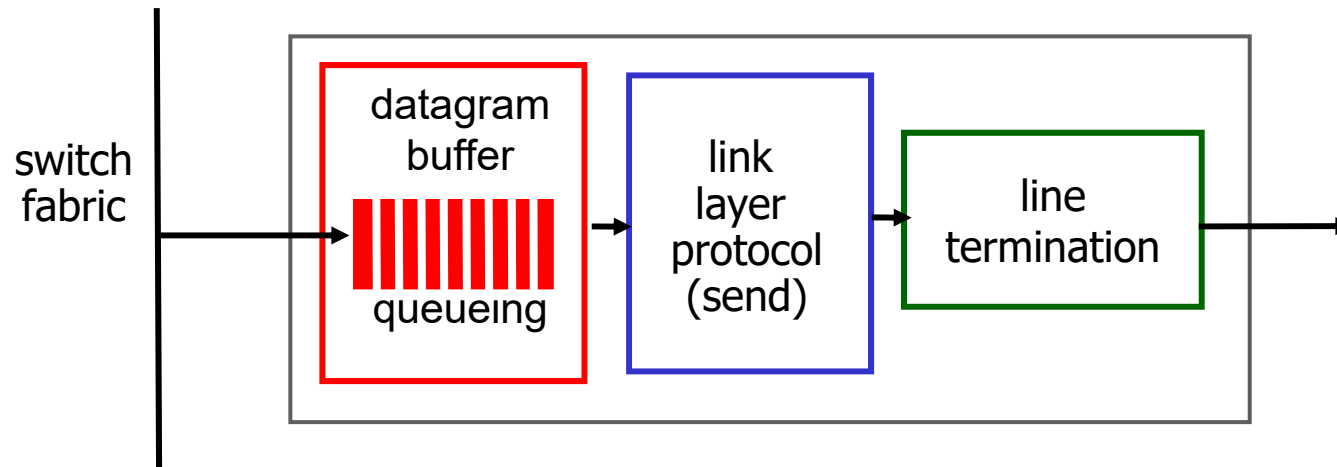


# Switching via interconnection network

- ❖ overcome bus bandwidth limitations
- ❖ banyan networks, crossbar, other interconnection nets initially developed to connect processors in multiprocessor
- ❖ advanced design: fragmenting datagram into fixed length cells, switch cells through the fabric.
- ❖ Cisco I2000: switches 60 Gbps through the interconnection network

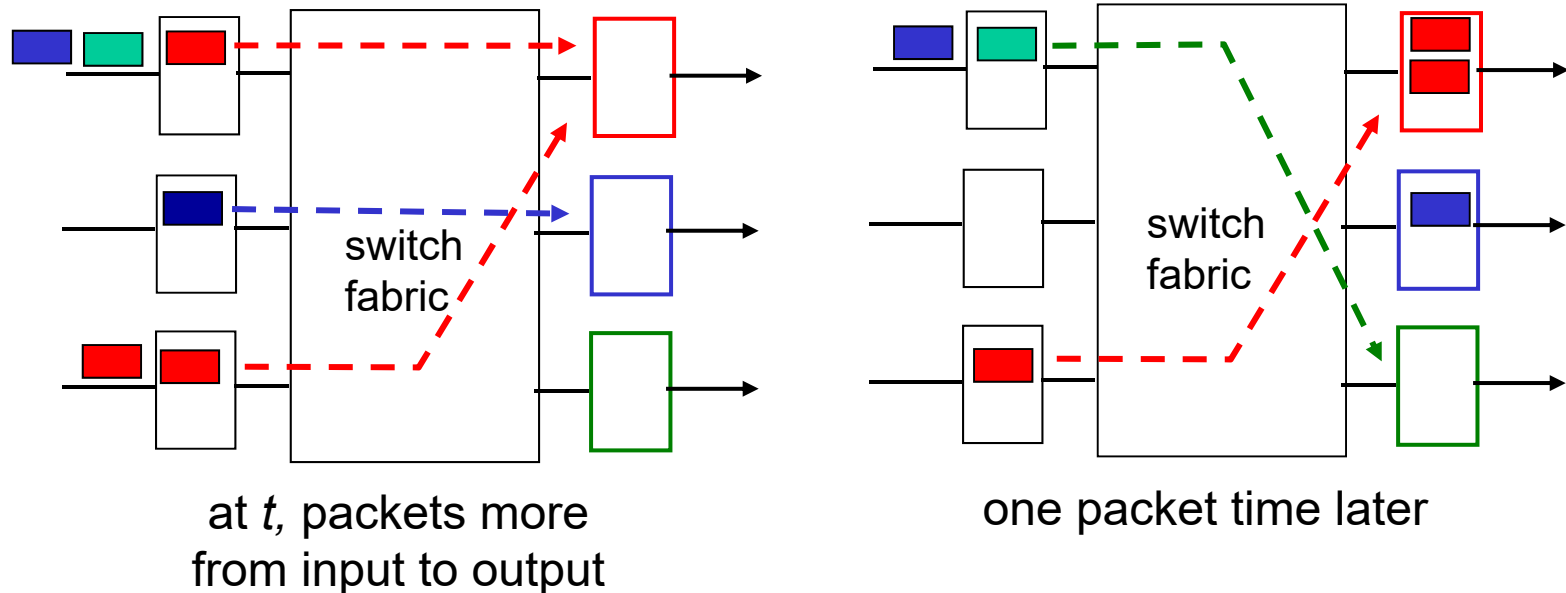


# Output ports



- ❖ *buffering* required from fabric faster rate  
Datagram (packets) can be lost due to congestion, lack of buffers
- ❖ *scheduling* datagrams  
Priority scheduling – who gets best performance, network neutrality

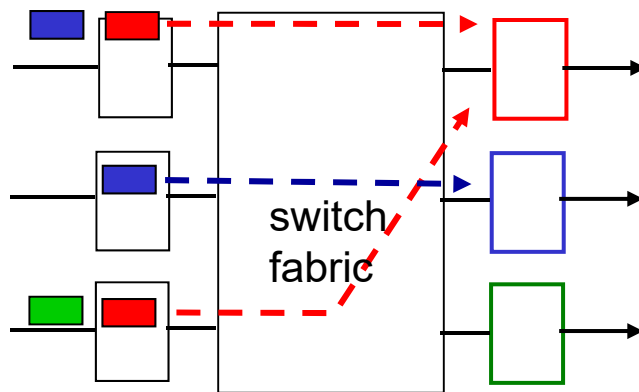
# Output port queueing



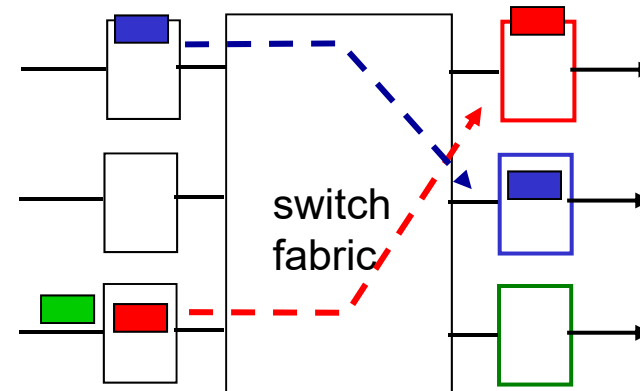
- ❖ buffering when arrival rate via switch exceeds output line speed
- ❖ *queueing (delay) and loss due to output port buffer overflow!*

# Input port queuing

- ❖ fabric slower than input ports combined -> queueing may occur at input queues
  - *queueing delay and loss due to input buffer overflow!*
- ❖ **Head-of-the-Line (HOL) blocking:** queued datagram at front of queue prevents others in queue from moving forward



output port contention:  
only one red datagram can be  
transferred.  
*lower red packet is blocked*



one packet time later:  
green packet  
experiences HOL  
blocking



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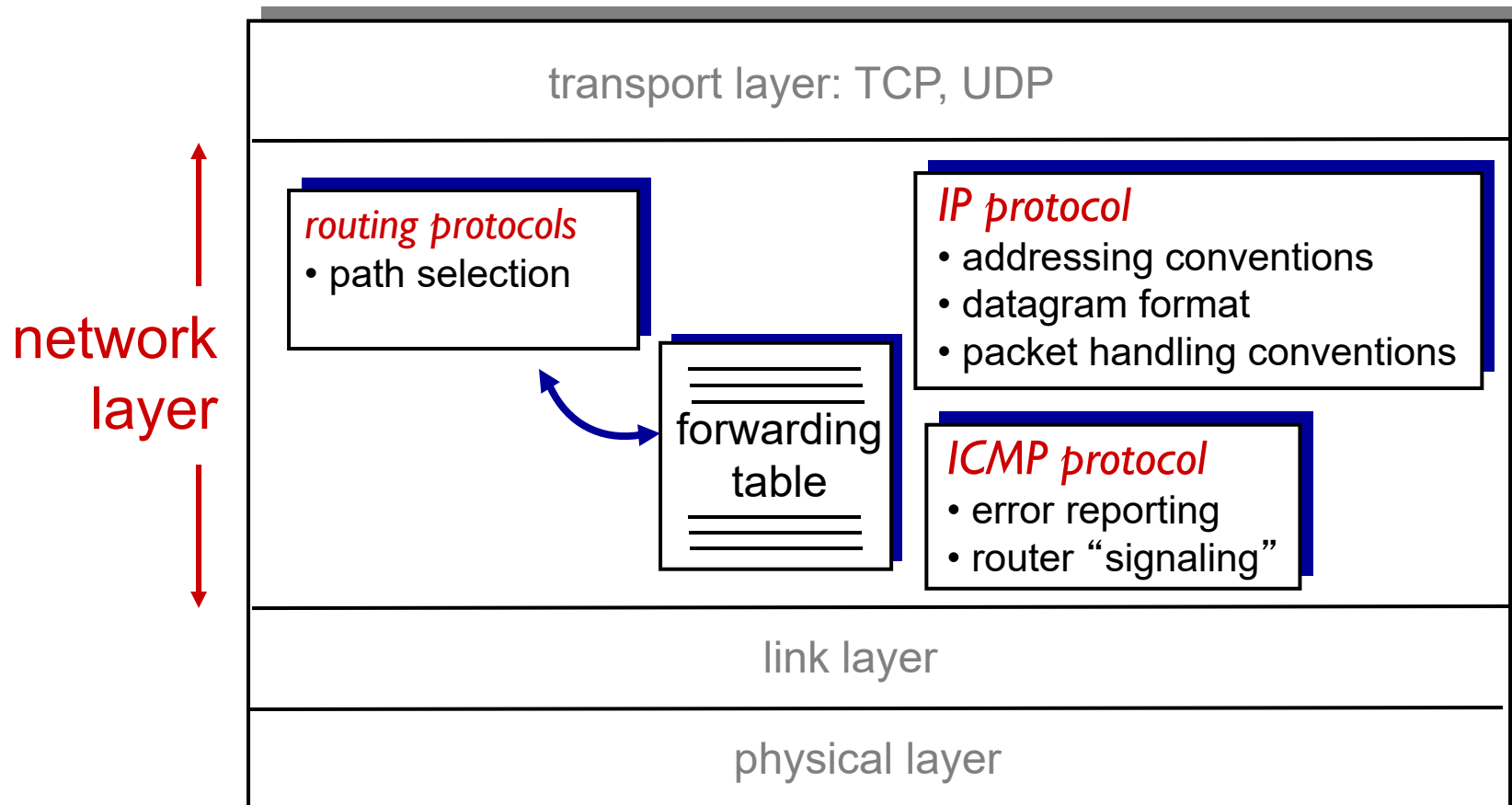
5.3 IP: Internet Protocol

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- IPv6

5.4 routing algorithms

# The Internet network layer

host, router network layer functions:



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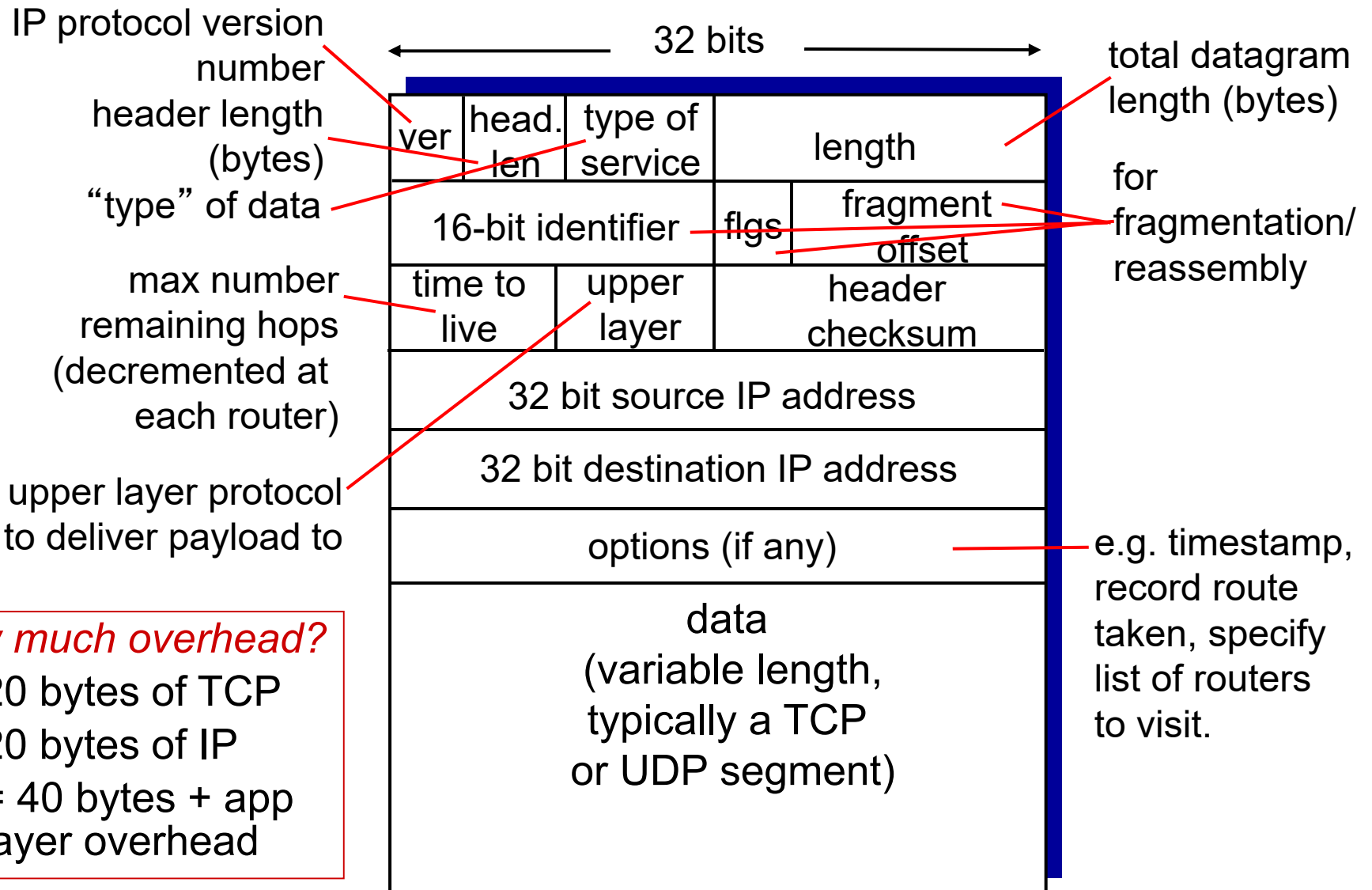
5.2 what's inside a router

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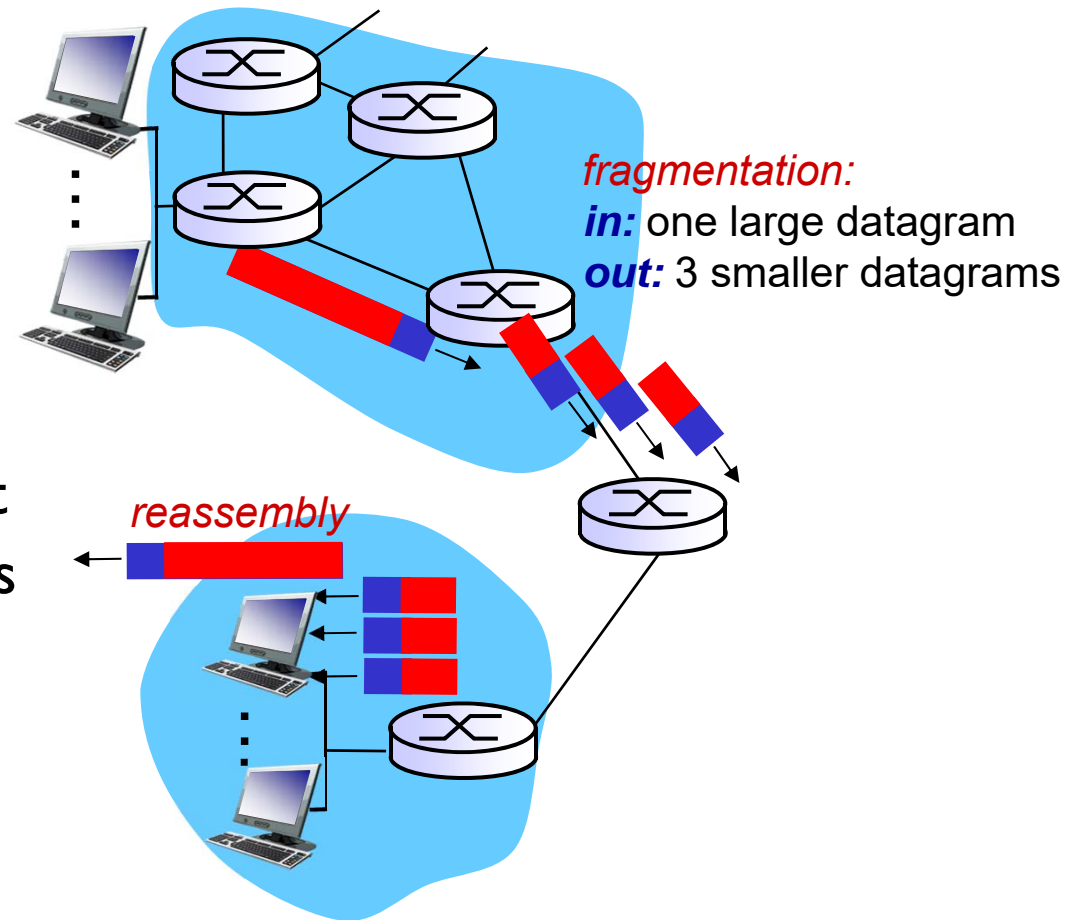
5.4 routing algorithms

# IP datagram format



# IP fragmentation, reassembly

- ❖ network links have MTU (max.transfer size) - largest possible link-level frame
  - different link types, different MTUs
- ❖ large IP datagram divided (“fragmented”) within net
  - one datagram becomes several datagrams
  - “reassembled” only at final destination
  - IP header bits used to identify, order related fragments



# IP fragmentation, reassembly

## *example:*

- ❖ 4000 byte datagram
- ❖ MTU = 1500 bytes

	length	ID	fragflag	offset	
	=4000	=x	=0	=0	

*one large datagram becomes  
several smaller datagrams*

1480 bytes in  
data field

offset =  
 $1480/8$

	length	ID	fragflag	offset	
	=1500	=x	=1	=0	

	length	ID	fragflag	offset	
	=1500	=x	=1	=185	

	length	ID	fragflag	offset	
	=1040	=x	=0	=370	

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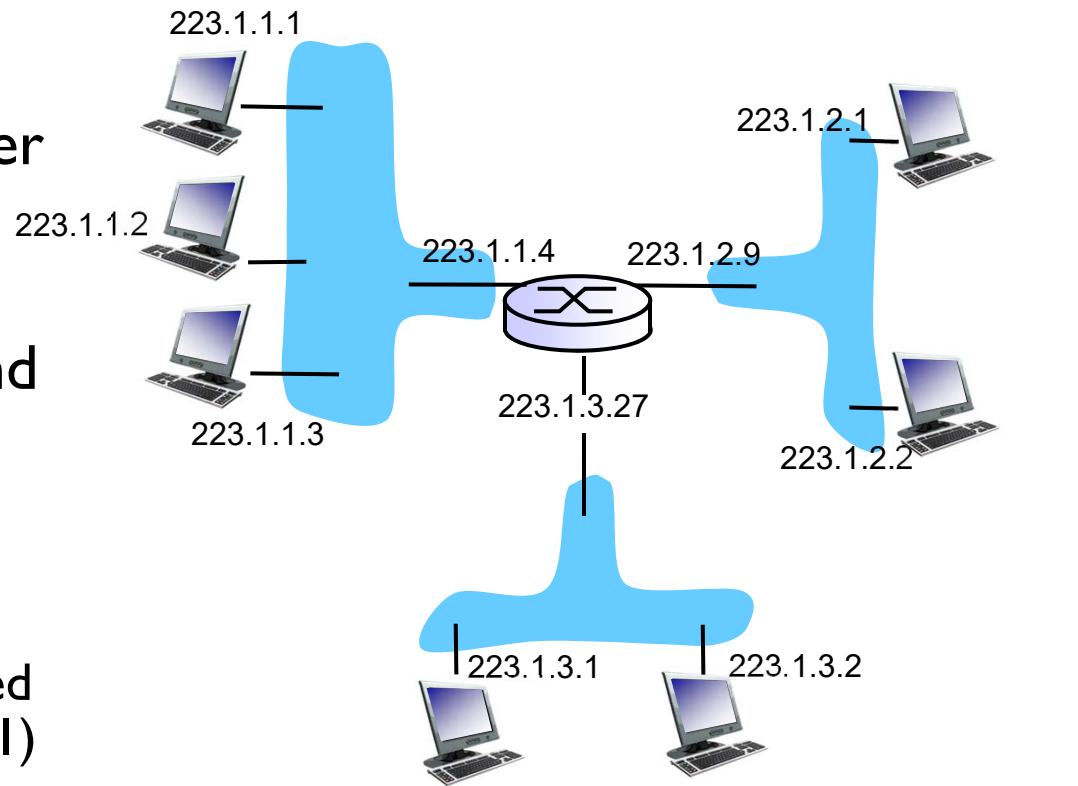
5.3 IP: Internet Protocol

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# IP addressing: introduction

- ❖ **IP address:** 32-bit identifier for host, router interface
- ❖ **interface:** connection between host/router and physical link
  - router's typically have multiple interfaces
  - host typically has one or two interfaces (e.g., wired Ethernet, wireless 802.11)
- ❖ **IP addresses associated with each interface**



$$223.1.1.1 = \underbrace{11011111}_{223} \underbrace{00000001}_1 \underbrace{00000001}_1 \underbrace{00000001}_1$$

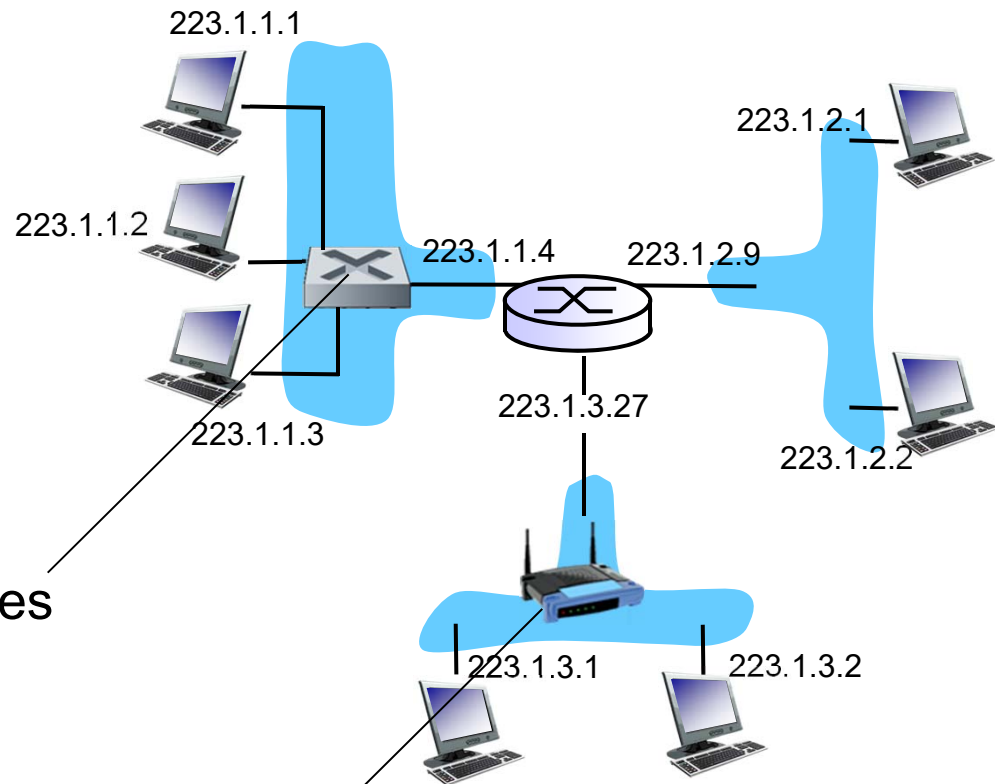


# IP addressing: introduction

*Q: how are interfaces actually connected?*

*A:* wired Ethernet interfaces connected by Ethernet switches

*For now:* don't need to worry about how one interface is connected to another (with no intervening router)



*A:* wireless WiFi interfaces connected by WiFi base station

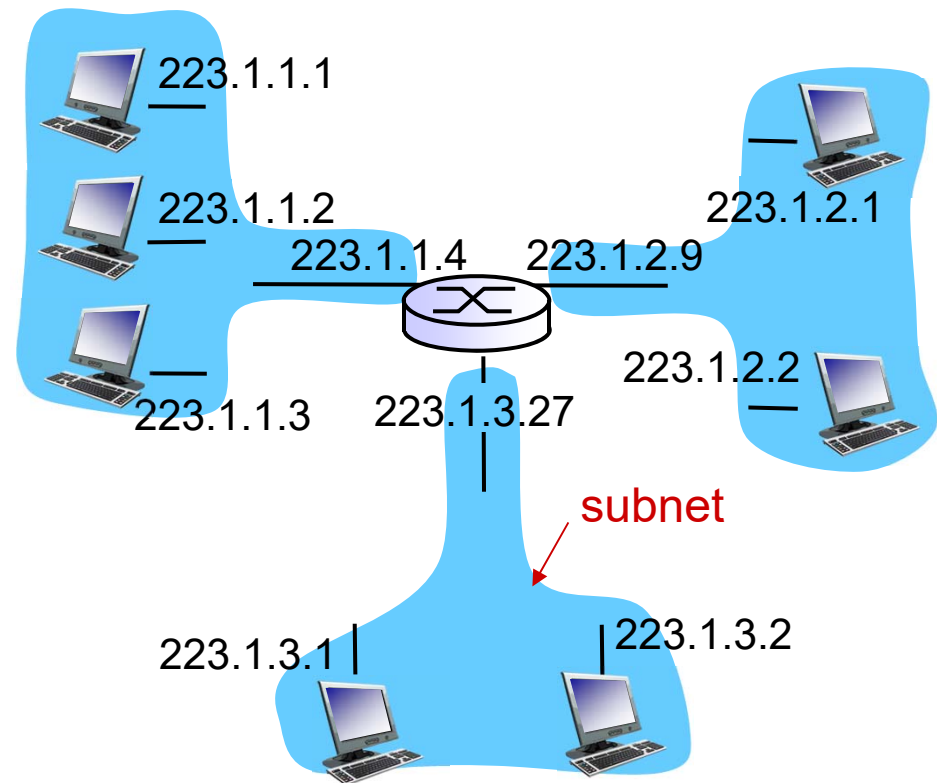
# Subnets

## ❖ IP address:

- subnet part - high order bits
- host part - low order bits

## ❖ *what 's a subnet ?*

- device interfaces with same subnet part of IP address
- can physically reach each other *without intervening router*

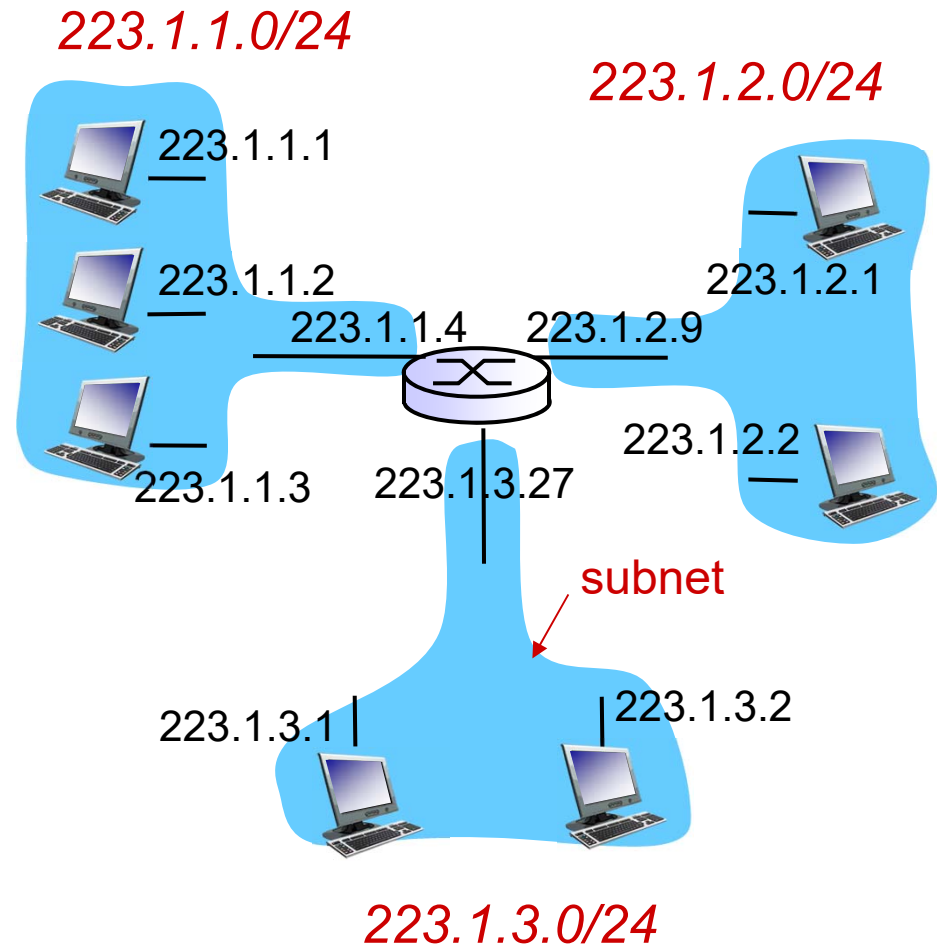


network consisting of 3 subnets

# Subnets

## *recipe*

- ❖ to determine the subnets, detach each interface from its host or router, creating islands of isolated networks
- ❖ each isolated network is called a *subnet*

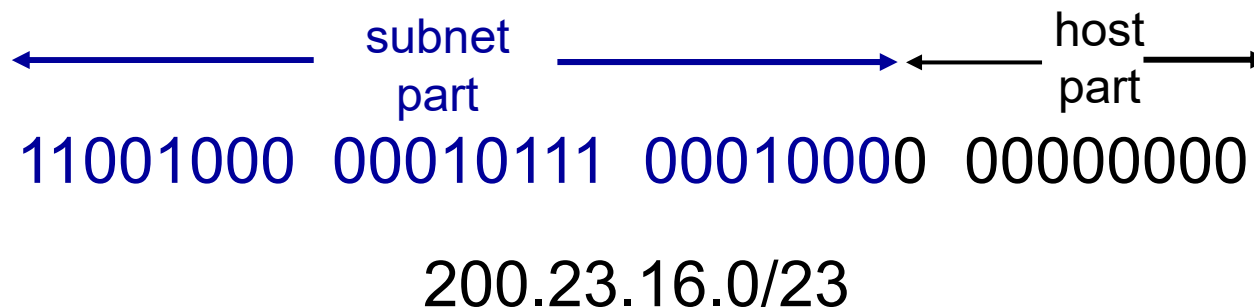


subnet mask: /24

# IP addressing: CIDR

## CIDR: Classless InterDomain Routing

- subnet portion of address of arbitrary length
- address format: **a.b.c.d/x**, where x is # bits in subnet portion of address



# IP addresses: how to get one?

**Q:** How does a *host* get IP address?

- ❖ hard-coded by system admin in a file
  - Windows: control-panel->network->configuration->tcp/ip->properties
  - UNIX: /etc/rc.config
- ❖ **DHCP: Dynamic Host Configuration Protocol:** dynamically get address from as server
  - “plug-and-play”

# DHCP: Dynamic Host Configuration Protocol

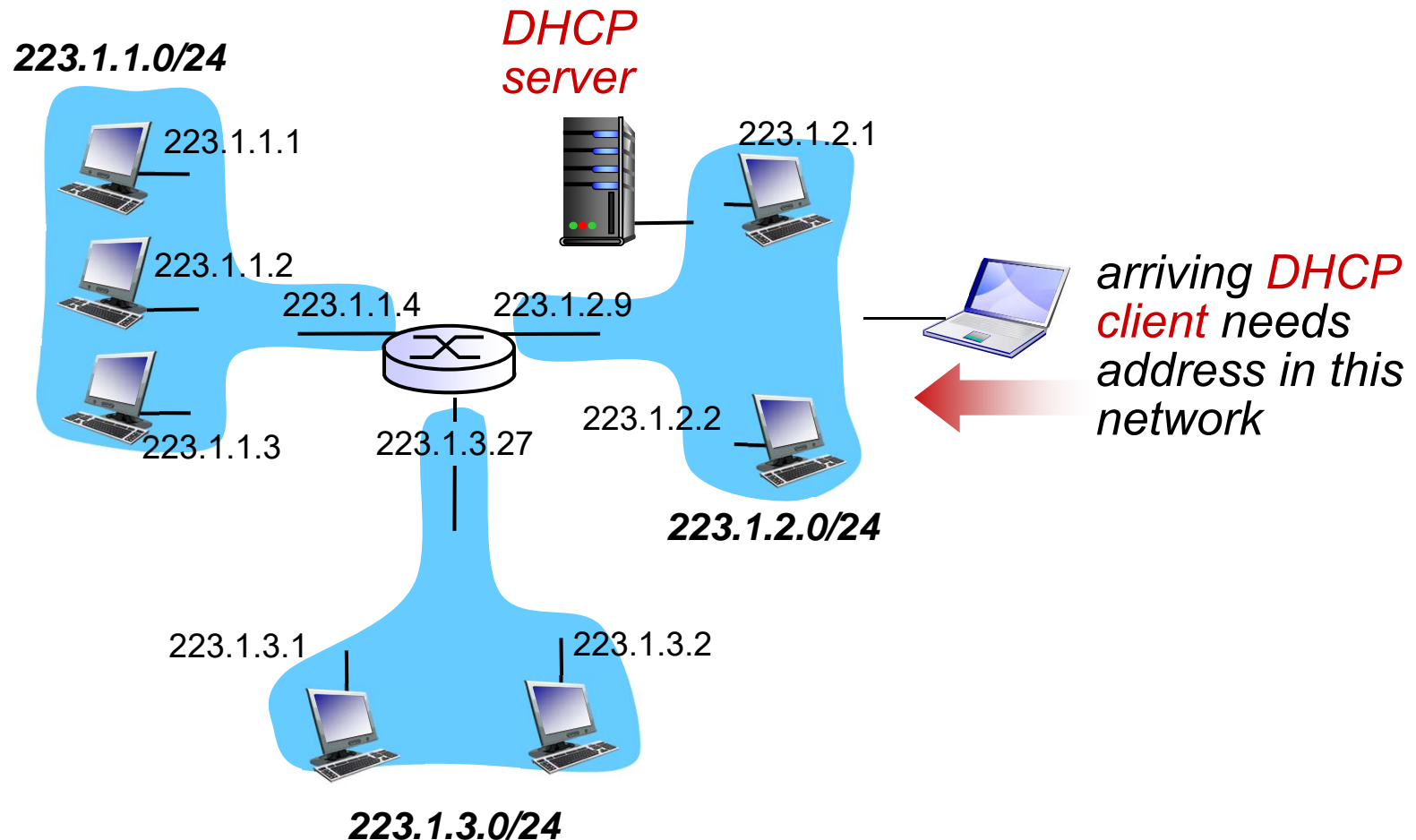
*goal:* allow host to *dynamically* obtain its IP address from network server when it joins network

- can renew its lease on address in use
- allows reuse of addresses (only hold address while connected/“on”)
- support for mobile users who want to join network (more shortly)

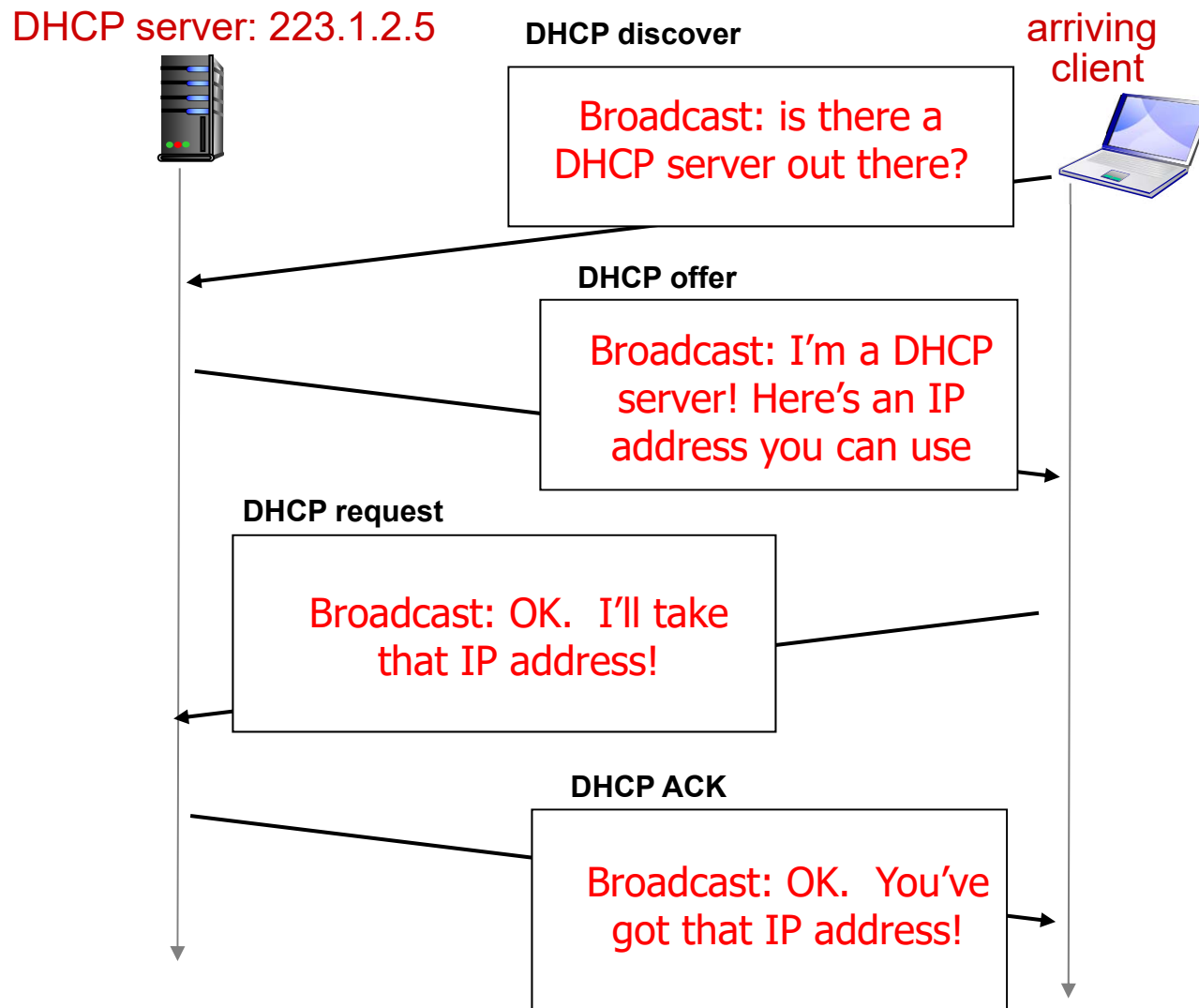
## *DHCP overview:*

- host broadcasts “DHCP discover” msg [optional]
- DHCP server responds with “DHCP offer” msg [optional]
- host requests IP address: “DHCP request” msg
- DHCP server sends address: “DHCP ack” msg

# DHCP client-server scenario



# DHCP client-server scenario



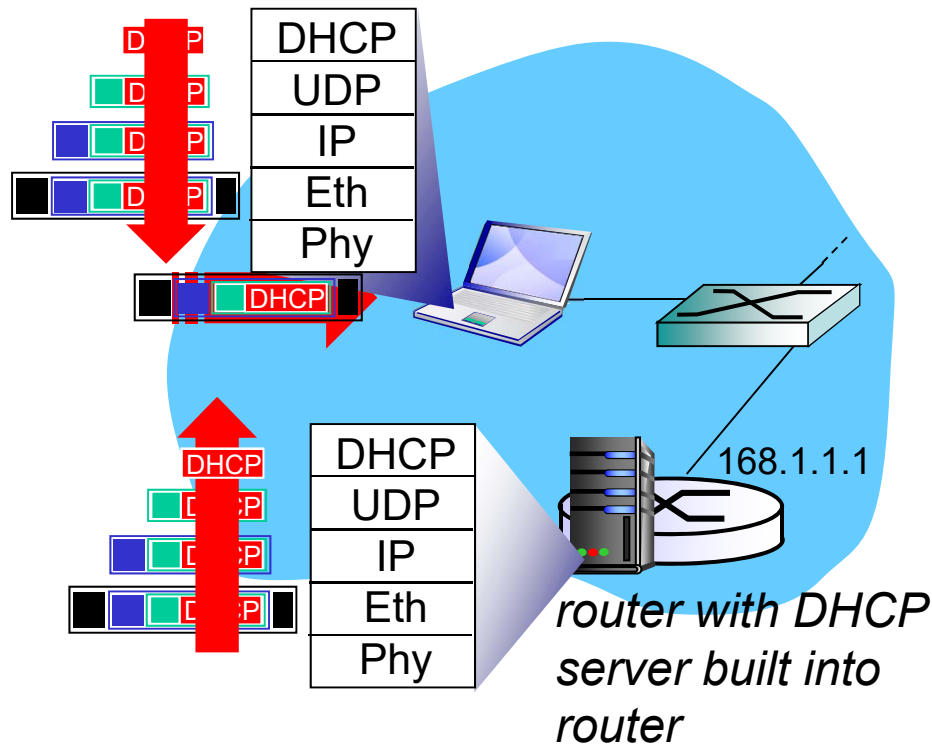


# DHCP: more than IP addresses

DHCP can return more than just allocated IP address on subnet:

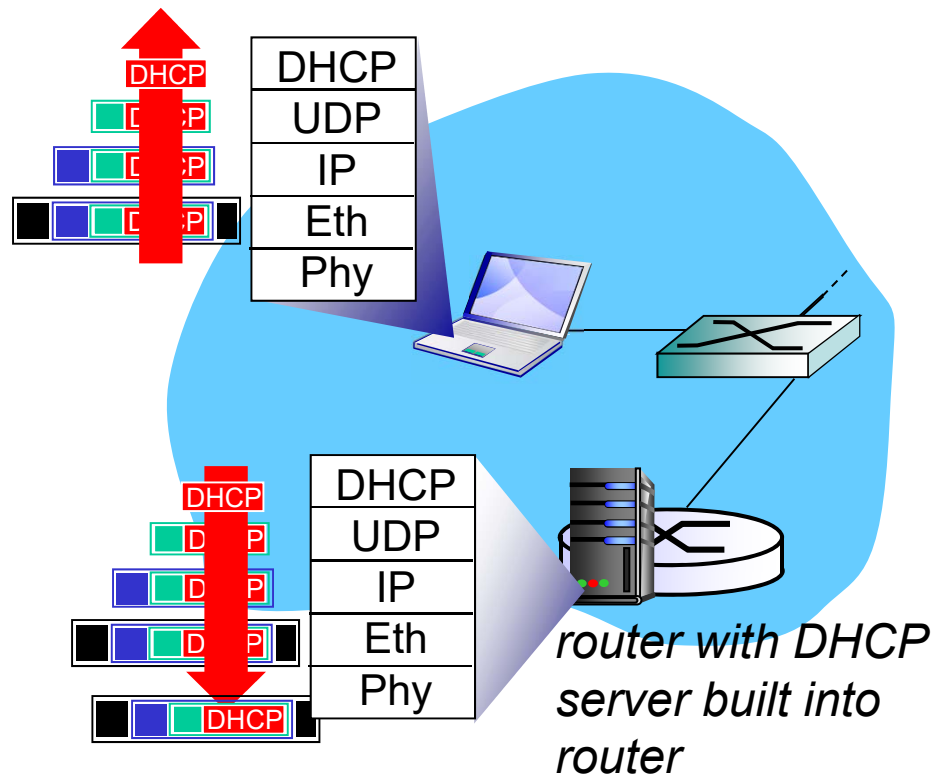
- address of first-hop router for client
- name and IP address of DNS sever
- network mask (indicating network versus host portion of address)

# DHCP: example



- ❖ connecting laptop needs its IP address, addr of first-hop router, addr of DNS server: use DHCP
- ❖ DHCP request encapsulated in UDP, encapsulated in IP, encapsulated in 802.1 Ethernet
- ❖ Ethernet frame broadcast (dest: FFFFFFFF) on LAN, received at router running DHCP server
- ❖ Ethernet demuxed to IP demuxed, UDP demuxed to DHCP

# DHCP: example



- ❖ DHCP server formulates DHCP ACK containing client's IP address, IP address of first-hop router for client, name & IP address of DNS server
- ❖ encapsulation of DHCP server, frame forwarded to client, demuxing up to DHCP at client
- ❖ client now knows its IP address, name and IP address of DNS server, IP address of its first-hop router

# DHCP: Wireshark output (home LAN)

Message type: **Boot Request (1)**

Hardware type: Ethernet

Hardware address length: 6

Hops: 0

**Transaction ID: 0x6b3a11b7**

Seconds elapsed: 0

Bootp flags: 0x0000 (Unicast)

Client IP address: 0.0.0.0 (0.0.0.0)

Your (client) IP address: 0.0.0.0 (0.0.0.0)

Next server IP address: 0.0.0.0 (0.0.0.0)

Relay agent IP address: 0.0.0.0 (0.0.0.0)

**Client MAC address: Wistron\_23:68:8a (00:16:d3:23:68:8a)**

Server host name not given

Boot file name not given

Magic cookie: (OK)

Option: (t=53,l=1) **DHCP Message Type = DHCP Request**

Option: (61) Client identifier

Length: 7; Value: 010016D323688A;

Hardware type: Ethernet

Client MAC address: Wistron\_23:68:8a (00:16:d3:23:68:8a)

Option: (t=50,l=4) Requested IP Address = 192.168.1.101

Option: (t=12,l=5) Host Name = "nomad"

**Option: (55) Parameter Request List**

Length: 11; Value: 010F03062C2E2F1F21F92B

**1 = Subnet Mask; 15 = Domain Name**

**3 = Router; 6 = Domain Name Server**

44 = NetBIOS over TCP/IP Name Server

.....

request

Message type: **Boot Reply (2)**

Hardware type: Ethernet

Hardware address length: 6

Hops: 0

**Transaction ID: 0x6b3a11b7**

Seconds elapsed: 0

Bootp flags: 0x0000 (Unicast)

**Client IP address: 192.168.1.101 (192.168.1.101)**

Your (client) IP address: 0.0.0.0 (0.0.0.0)

**Next server IP address: 192.168.1.1 (192.168.1.1)**

Relay agent IP address: 0.0.0.0 (0.0.0.0)

Client MAC address: Wistron\_23:68:8a (00:16:d3:23:68:8a)

Server host name not given

Boot file name not given

Magic cookie: (OK)

**Option: (t=53,l=1) DHCP Message Type = DHCP ACK**

**Option: (t=54,l=4) Server Identifier = 192.168.1.1**

**Option: (t=1,l=4) Subnet Mask = 255.255.255.0**

**Option: (t=3,l=4) Router = 192.168.1.1**

**Option: (6) Domain Name Server**

Length: 12; Value: 445747E2445749F244574092;

IP Address: 68.87.71.226;

IP Address: 68.87.73.242;

IP Address: 68.87.64.146

**Option: (t=15,l=20) Domain Name = "hsd1.ma.comcast.net."**

reply

# IP addresses: how to get one?

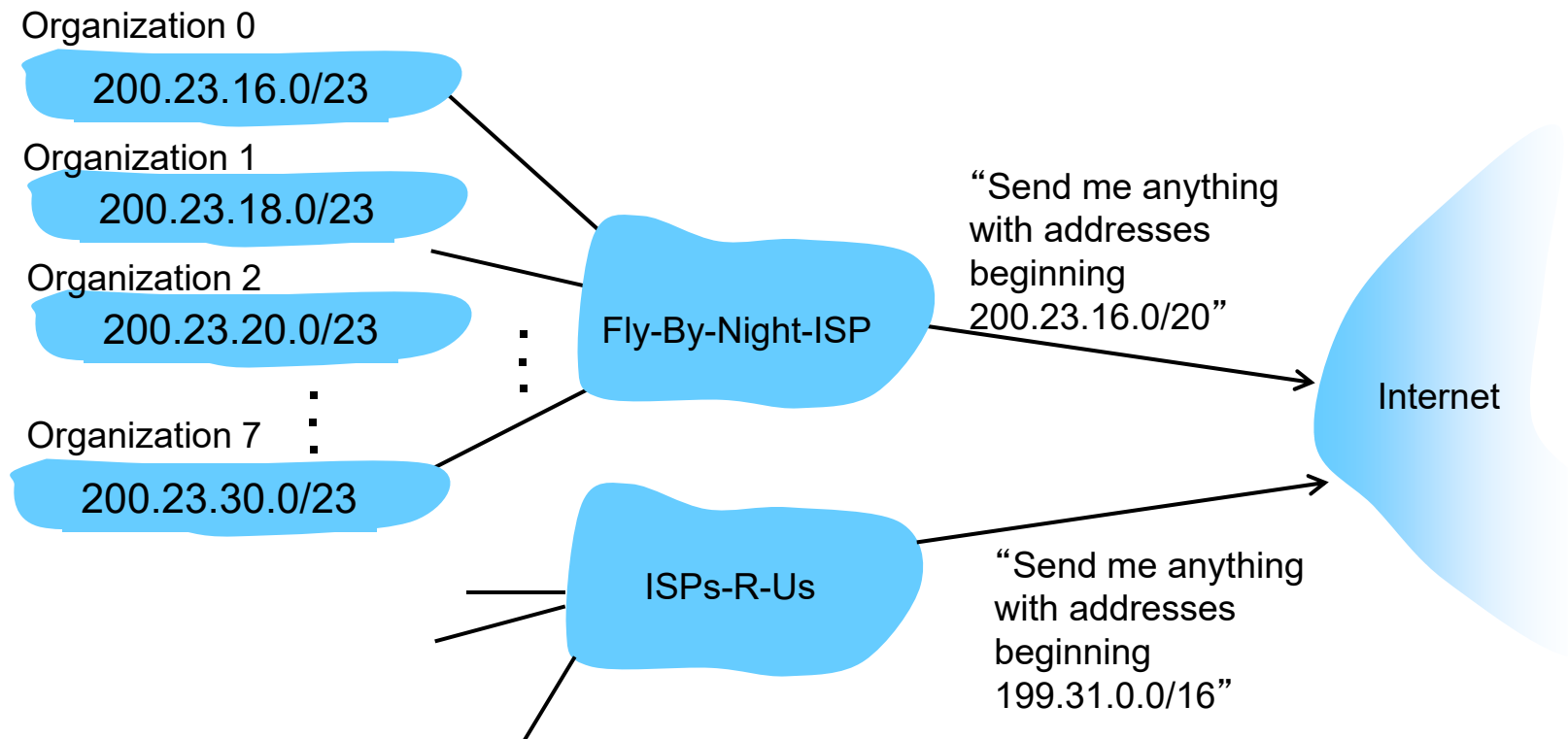
**Q:** how does *network* get subnet part of IP addr?

**A:** gets allocated portion of its provider ISP's address space

ISP's block	<u>11001000 00010111 00010000</u> 00000000	200.23.16.0/20
Organization 0	<u>11001000 00010111 00010000</u> 00000000	200.23.16.0/23
Organization 1	<u>11001000 00010111 00010010</u> 00000000	200.23.18.0/23
Organization 2	<u>11001000 00010111 00010100</u> 00000000	200.23.20.0/23
...	.....	....
Organization 7	<u>11001000 00010111 00011110</u> 00000000	200.23.30.0/23

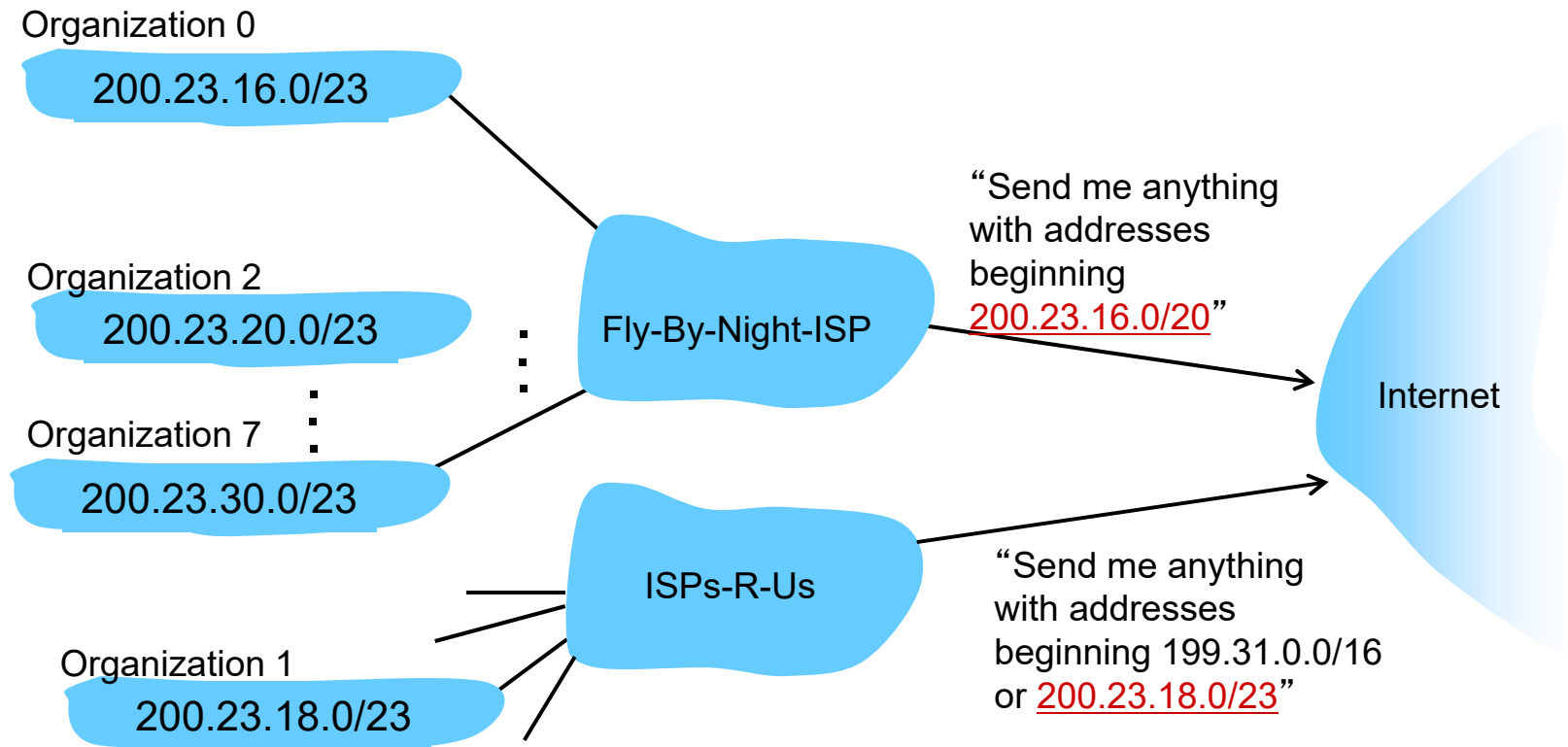
# Hierarchical addressing: route aggregation

hierarchical addressing allows efficient advertisement of routing information:



# Hierarchical addressing: more specific routes

ISPs-R-U has a more specific route to Organization 1



## IP addressing: the last word...

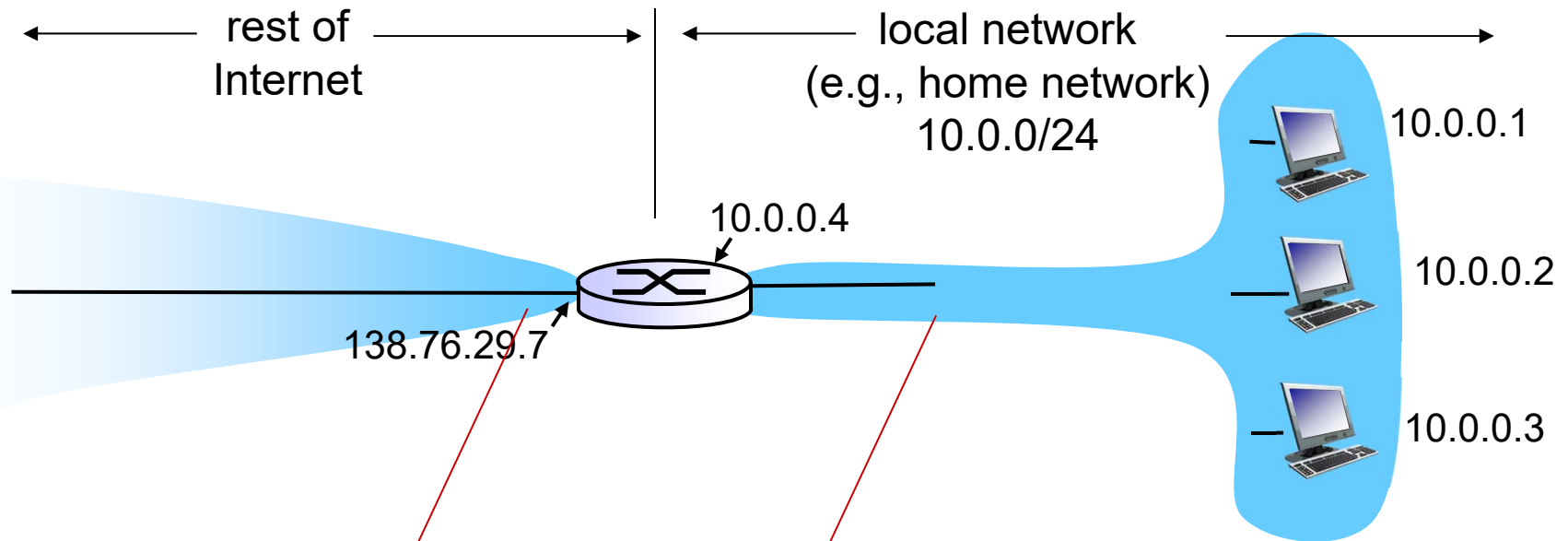
**Q:** how does an ISP get block of addresses?

**A:** **ICANN:** Internet Corporation for Assigned Names and Numbers <http://www.icann.org/>

- allocates addresses
- manages DNS
- assigns domain names, resolves disputes



# NAT: network address translation



*all* datagrams *leaving* local network have *same* single source NAT IP address: 138.76.29.7, different source port numbers

datagrams with source or destination in this network have 10.0.0/24 address for source, destination (as usual)

# NAT: network address translation

*motivation:* local network uses just one IP address as far as outside world is concerned:

- range of addresses not needed from ISP: just one IP address for all devices
- can change addresses of devices in local network without notifying outside world
- can change ISP without changing addresses of devices in local network
- devices inside local net not explicitly addressable, visible by outside world (a security plus)

# NAT: network address translation

*implementation:* NAT router must:

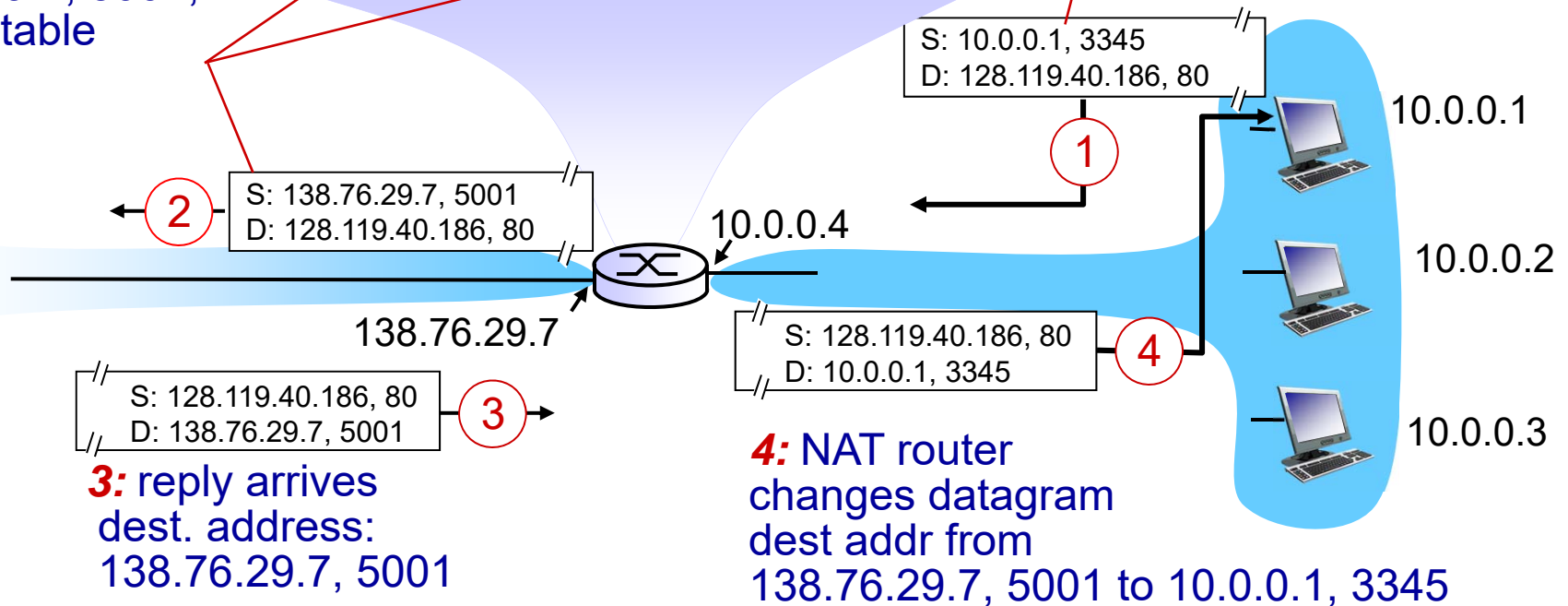
- *outgoing datagrams: replace* (source IP address, port #) of every outgoing datagram to (NAT IP address, new port #)  
... remote clients/servers will respond using (NAT IP address, new port #) as destination addr
- *remember (in NAT translation table)* every (source IP address, port #) to (NAT IP address, new port #) translation pair
- *incoming datagrams: replace* (NAT IP address, new port #) in dest fields of every incoming datagram with corresponding (source IP address, port #) stored in NAT table

# NAT: network address translation

**2:** NAT router changes datagram source addr from 10.0.0.1, 3345 to 138.76.29.7, 5001, updates table

NAT translation table	
WAN side addr	LAN side addr
138.76.29.7, 5001	10.0.0.1, 3345
.....	.....

**1:** host 10.0.0.1 sends datagram to 128.119.40.186, 80



# NAT: network address translation

- ❖ 16-bit port-number field:
  - 60,000 simultaneous connections with a single LAN-side address!
- ❖ NAT is controversial:
  - routers should only process up to layer 3
  - violates end-to-end argument
    - NAT possibility must be taken into account by app designers, e.g., P2P applications
  - address shortage should instead be solved by IPv6

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# ICMP: internet control message protocol

- ❖ used by hosts & routers to communicate network-level information

- error reporting:  
unreachable host, network, port, protocol
- echo request/reply (used by ping)

- ❖ network-layer “above” IP:
  - ICMP msgs carried in IP datagrams

- ❖ **ICMP message:** type, code plus first 8 bytes of IP datagram causing error

<u>Type</u>	<u>Code</u>	<u>description</u>
0	0	echo reply (ping)
3	0	dest. network unreachable
3	1	dest host unreachable
3	2	dest protocol unreachable
3	3	dest port unreachable
3	6	dest network unknown
3	7	dest host unknown
4	0	source quench (congestion control - not used)
8	0	echo request (ping)
9	0	route advertisement
10	0	router discovery
11	0	TTL expired
12	0	bad IP header

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# IPv6: motivation

- ❖ *initial motivation*: 32-bit address space soon to be completely allocated.
- ❖ additional motivation:
  - header format helps speed processing/forwarding
  - header changes to facilitate QoS

## *IPv6 datagram format:*

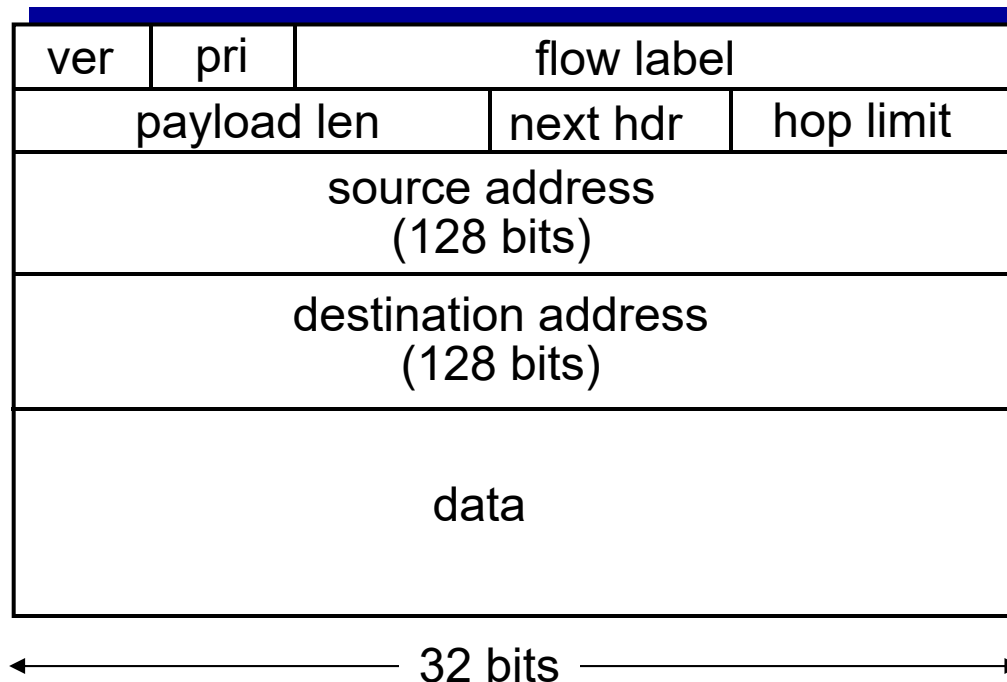
- fixed-length 40 byte header
- no fragmentation allowed

# IPv6 datagram format

*priority*: identify priority among datagrams in flow

*flow Label*: identify datagrams in same “flow.”

*next header*: identify upper layer protocol for data

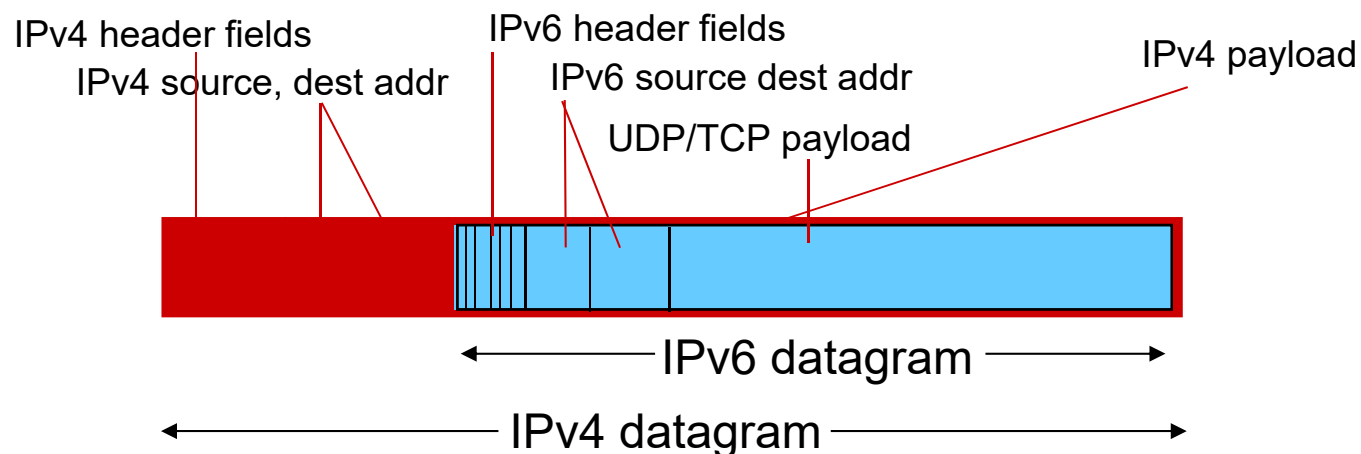


# Other changes from IPv4

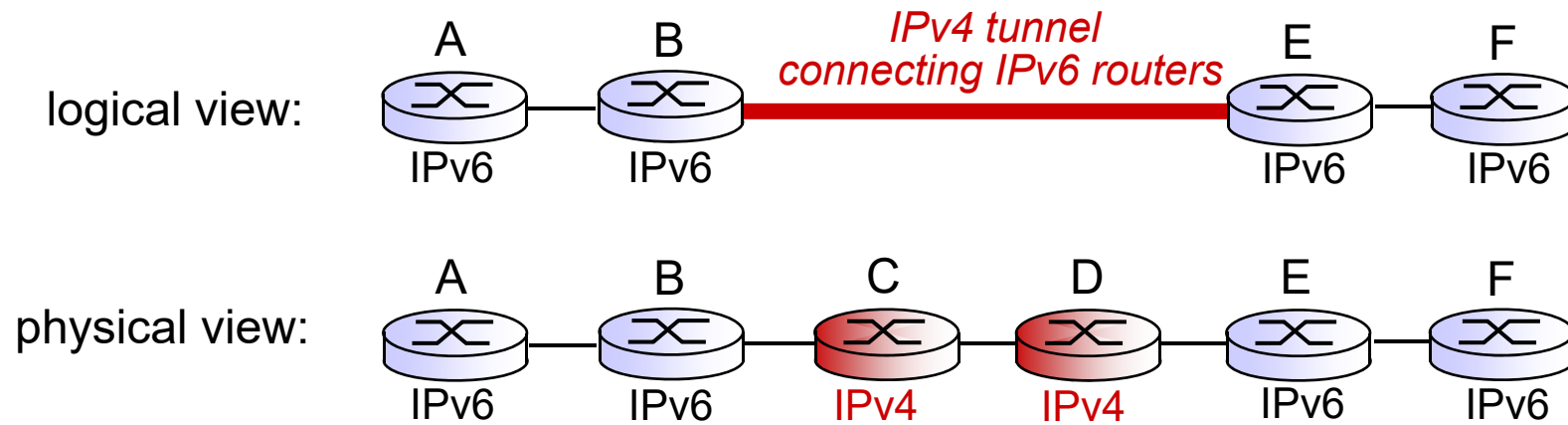
- ❖ *checksum*: removed entirely to reduce processing time at each hop
- ❖ *options*: allowed, but outside of header, indicated by “Next Header” field
- ❖ *ICMPv6*: new version of ICMP
  - additional message types, e.g. “Packet Too Big”
  - multicast group management functions

# Transition from IPv4 to IPv6

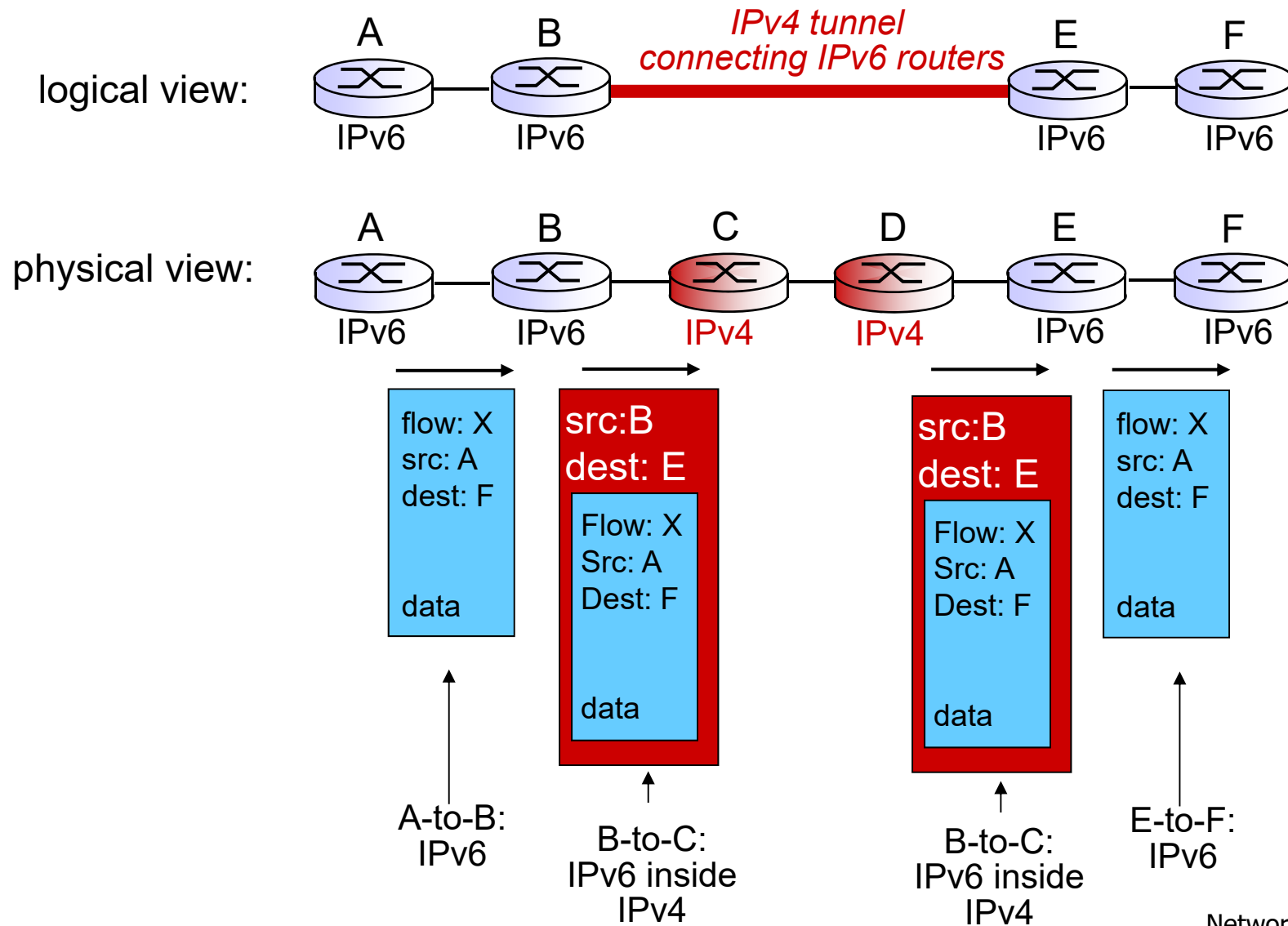
- ❖ not all routers can be upgraded simultaneously
  - no “flag days”
  - how will network operate with mixed IPv4 and IPv6 routers?
- ❖ *tunneling*: IPv6 datagram carried as *payload* in IPv4 datagram among IPv4 routers



# Tunneling



# Tunneling



# IPv6: adoption

- ❖ US National Institutes of Standards estimate [2013]:
  - ~3% of industry IP routers
  - ~11% of US gov't routers
- ❖ *Long (long!) time for deployment, use*
  - 20 years and counting!
  - think of application-level changes in last 20 years: WWW, Facebook, ...
  - *Why?*

# Topic 5: outline

5.1 introduction

5.2 what's inside a router

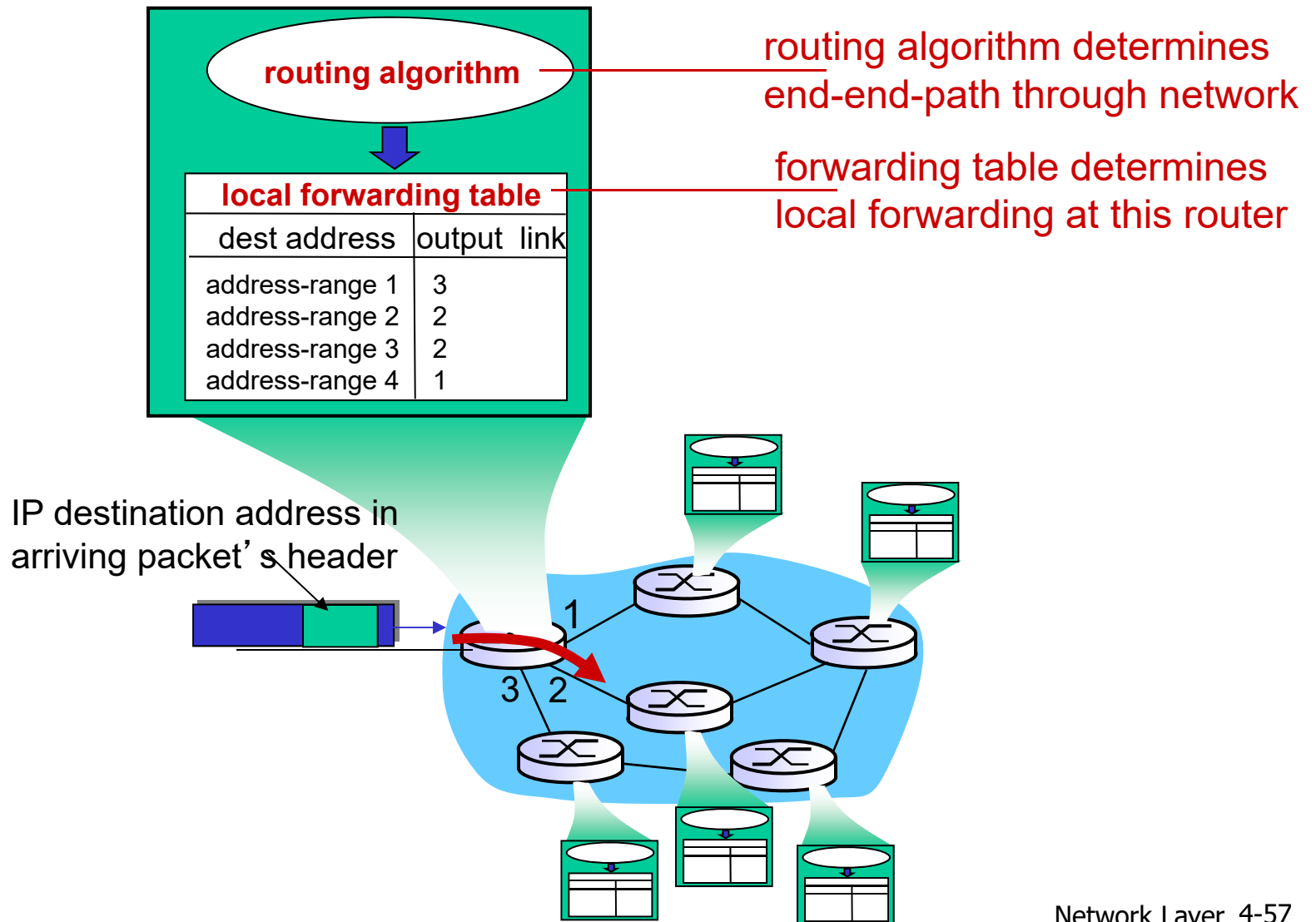
5.3 IP: Internet Protocol

- datagram format
- IPv4 addressing
- ICMP
- IPv6

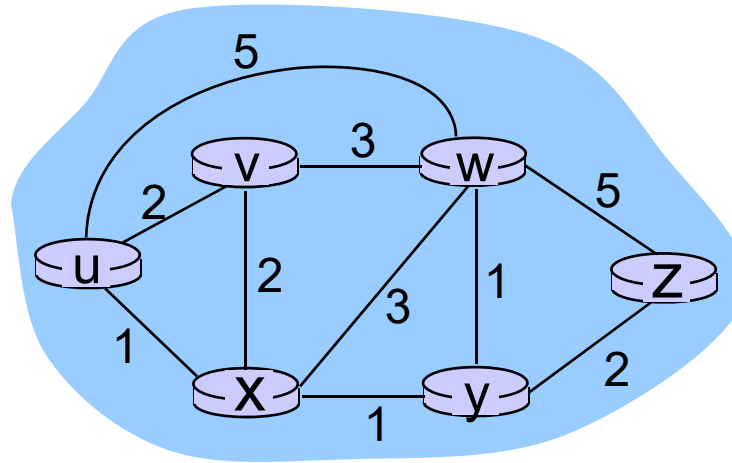
5.4 routing algorithms



# Interplay between routing, forwarding



# Graph abstraction

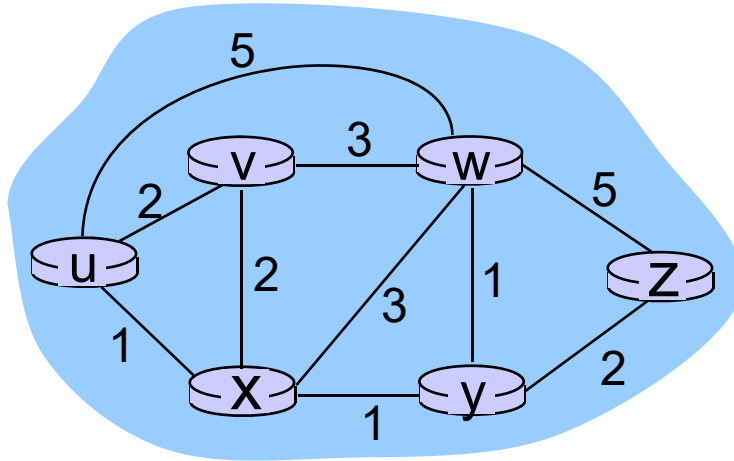


graph:  $G = (N, E)$

$N$  = set of routers =  $\{ u, v, w, x, y, z \}$

$E$  = set of links =  $\{ (u,v), (u,x), (v,x), (v,w), (x,w), (x,y), (w,y), (w,z), (y,z) \}$

# Graph abstraction: costs



$c(x, x') = \text{cost of link } (x, x')$   
e.g.,  $c(w, z) = 5$

cost could be related to delay,  
congestion level of the link, or  
inversely related to bandwidth

cost of path  $(x_1, x_2, x_3, \dots, x_p) = c(x_1, x_2) + c(x_2, x_3) + \dots + c(x_{p-1}, x_p)$

**key question:** what is the least-cost path between u and z ?  
**routing algorithm:** algorithm that finds that least cost path

# Routing algorithm classification

*Q: global or decentralized information?*

*global:*

- ❖ all routers have complete topology, link cost info
- ❖ “link state” algorithms

*decentralized:*

- ❖ router knows physically-connected neighbors, link costs to neighbors
- ❖ iterative process of computation, exchange of info with neighbors
- ❖ “distance vector” algorithms

# A Link-State Routing Algorithm

## *Dijkstra's algorithm*

- ❖ net topology, link costs known to all nodes
  - accomplished via “link state broadcast”
  - all nodes have same info
- ❖ computes least cost paths from one node (‘source’) to all other nodes
  - gives *forwarding table* for that node
- ❖ iterative: after k iterations, know least cost path to k dest.’s

## *notation:*

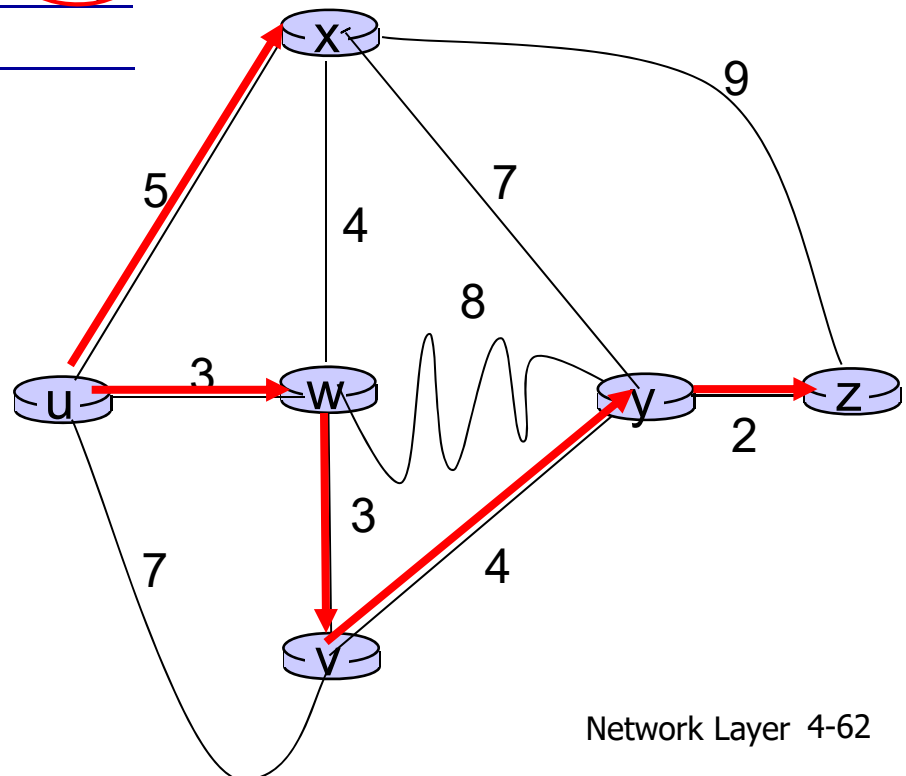
- ❖  $c(x,y)$ : link cost from node x to y;  $= \infty$  if not direct neighbors
- ❖  $D(v)$ : current value of cost of path from source to dest. v
- ❖  $p(v)$ : predecessor node along path from source to v
- ❖  $N'$ : set of nodes whose least cost path definitively known

# Dijkstra's algorithm: example

Step	N'	D( <b>v</b> ) p(v)	D( <b>w</b> ) p(w)	D( <b>x</b> ) p(x)	D( <b>y</b> ) p(y)	D( <b>z</b> ) p(z)
0	u	7,u	<b>3,u</b>	5,u	$\infty$	$\infty$
1	uw	6,w		<b>5,u</b>	11,w	$\infty$
2	uwx	<b>6,w</b>			11,w	14,x
3	uwxv				<b>10,v</b>	14,x
4	uwxvy					<b>12,y</b>
5	uwxvyz					

## notes:

- ❖ construct shortest path tree by tracing predecessor nodes
- ❖ ties can exist (can be broken arbitrarily)



# Dijkstra's Algorithm

1 **Initialization:**

2  $N' = \{u\}$

3 for all nodes  $v$

4 if  $v$  adjacent to  $u$

5 then  $D(v) = c(u,v)$

6 else  $D(v) = \infty$

7

8 **Loop**

9 find  $w$  not in  $N'$  such that  $D(w)$  is a minimum

10 add  $w$  to  $N'$

11 update  $D(v)$  for all  $v$  adjacent to  $w$  and not in  $N'$  :

12  **$D(v) = \min( D(v), D(w) + c(w,v) )$**

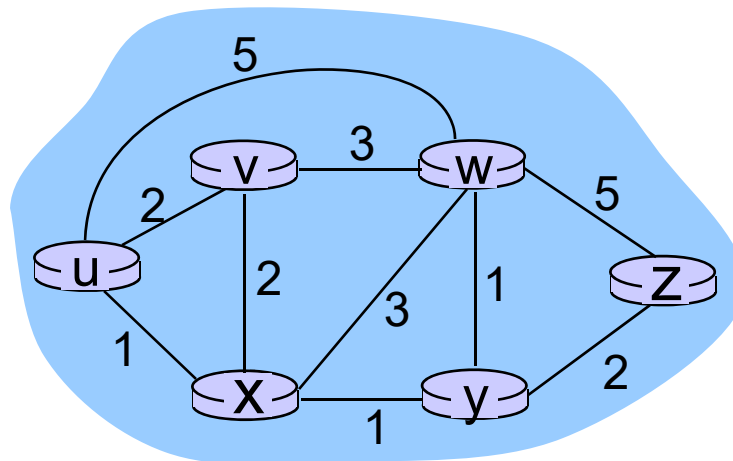
13 /\* new cost to  $v$  is either old cost to  $v$  or known

14 shortest path cost to  $w$  plus cost from  $w$  to  $v$  \*/

15 **until all nodes in  $N'$**

# Dijkstra's algorithm: another example

Step	N'	D(v),p(v)	D(w),p(w)	D(x),p(x)	D(y),p(y)	D(z),p(z)
0	u	2,u	5,u	1,u	$\infty$	$\infty$
1	ux	2,u	4,x		2,x	$\infty$
2	uxy	2,u	3,y			4,y
3	uxyv		3,y			4,y
4	uxyvw					4,y
5	uxyvwz					





# Distance vector algorithm

*Bellman-Ford equation (dynamic programming)*

let

$d_x(y) :=$  cost of least-cost path from  $x$  to  $y$

then

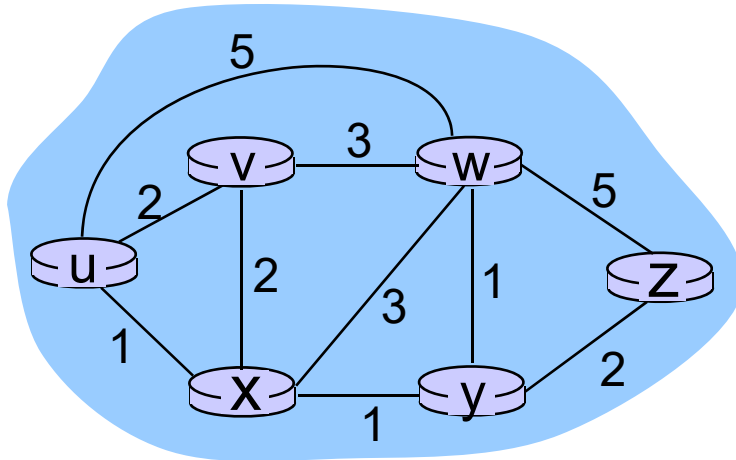
$$d_x(y) = \min_v \{ c(x,v) + d_v(y) \}$$

cost from neighbor  $v$  to destination  $y$

cost to neighbor  $v$

$\min$  taken over all neighbors  $v$  of  $x$

# Bellman-Ford example



clearly,  $d_v(z) = 5$ ,  $d_x(z) = 3$ ,  $d_w(z) = 3$

B-F equation says:

$$\begin{aligned} d_u(z) &= \min \{ c(u,v) + d_v(z), \\ &\quad c(u,x) + d_x(z), \\ &\quad c(u,w) + d_w(z) \} \\ &= \min \{ 2 + 5, \\ &\quad 1 + 3, \\ &\quad 5 + 3 \} = 4 \end{aligned}$$

node achieving minimum is next  
hop in shortest path, used in forwarding table

# Distance vector algorithm

- ❖  $D_x(y)$  = estimate of least cost from x to y
  - x maintains distance vector  $\mathbf{D}_x = [D_x(y): y \in N]$
- ❖ node x:
  - knows cost to each neighbor v:  $c(x,v)$
  - maintains its neighbors' distance vectors. For each neighbor v, x maintains  $\mathbf{D}_v = [D_v(y): y \in N]$

# Distance vector algorithm

## *key idea:*

- ❖ from time-to-time, each node sends its own distance vector estimate to neighbors
- ❖ when  $x$  receives new DV estimate from neighbor, it updates its own DV using B-F equation:

$$D_x(y) \leftarrow \min_v \{c(x,v) + D_v(y)\} \text{ for each node } y \in N$$

- ❖ under minor, natural conditions, the estimate  $D_x(y)$  converge to the actual least cost  $d_x(y)$

# Distance vector algorithm

## *iterative, asynchronous:*

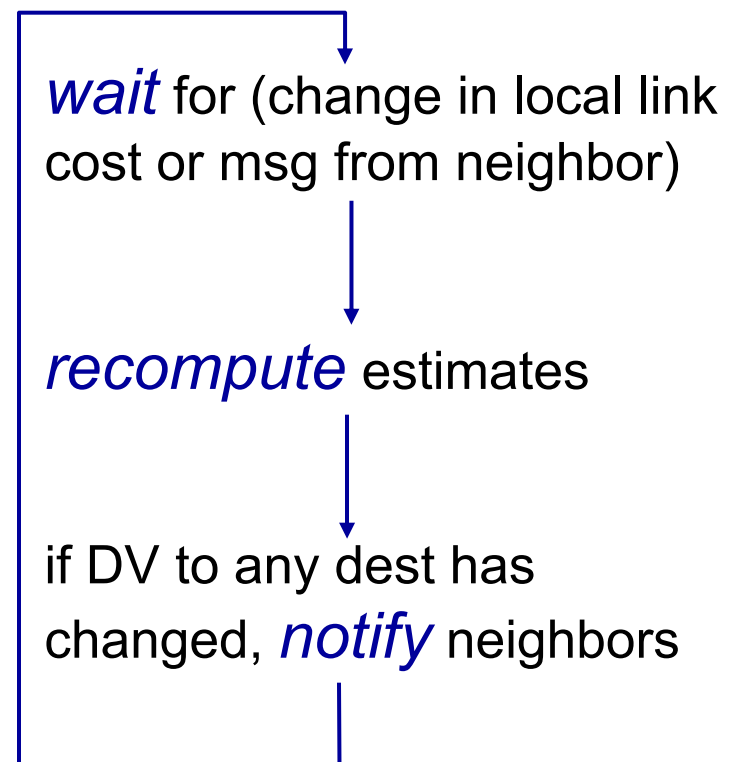
each local iteration  
caused by:

- ❖ local link cost change
- ❖ DV update message from neighbor

## *distributed:*

- ❖ each node notifies neighbors *only* when its DV changes
  - neighbors then notify their neighbors if necessary

## *each node:*



$$D_x(y) = \min\{c(x,y) + D_y(y), c(x,z) + D_z(y)\}$$

$$= \min\{2+0, 7+1\} = 2$$

$$D_x(z) = \min\{c(x,y) + D_y(z), c(x,z) + D_z(z)\}$$

$$= \min\{2+1, 7+0\} = 3$$

**node x  
table**

		cost to		
		x	y	z
from	x	0	2	7
	y	∞	∞	∞
	z	∞	∞	∞

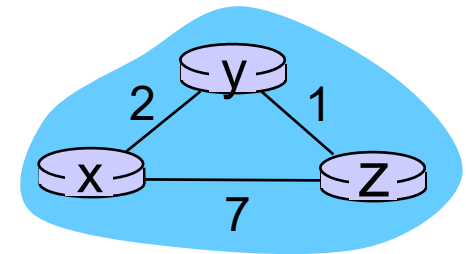
**node y  
table**

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	2	0	1
	z	∞	∞	∞

**node z  
table**

		cost to		
		x	y	z
from	x	∞	∞	∞
	y	∞	∞	∞
	z	7	1	0

		cost to		
		x	y	z
from	x	0	2	3
	y	2	0	1
	z	7	1	0



time

$$D_x(y) = \min\{c(x,y) + D_y(y), c(x,z) + D_z(y)\}$$

$$= \min\{2+0, 7+1\} = 2$$

$$D_x(z) = \min\{c(x,y) + D_y(z), c(x,z) + D_z(z)\}$$

$$= \min\{2+1, 7+0\} = 3$$

**node x  
table**

from \ cost to			
	x	y	z
x	0	2	7
y	∞	∞	∞
z	∞	∞	∞

**node y  
table**

from \ cost to			
	x	y	z
x	∞	∞	∞
y	2	0	1
z	∞	∞	∞

**node z  
table**

from \ cost to			
	x	y	z
x	∞	∞	∞
y	∞	∞	∞
z	7	1	0

from \ cost to			
	x	y	z
x	0	2	3
y	2	0	1
z	7	1	0

from \ cost to			
	x	y	z
x	0	2	7
y	2	0	1
z	7	1	0

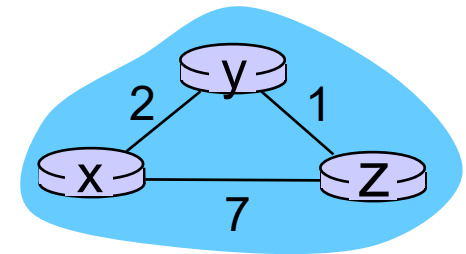
from \ cost to			
	x	y	z
x	0	2	7
y	2	0	1
z	3	1	0

from \ cost to			
	x	y	z
x	0	2	3
y	2	0	1
z	3	1	0

from \ cost to			
	x	y	z
x	0	2	3
y	2	0	1
z	3	1	0

from \ cost to			
	x	y	z
x	0	2	3
y	2	0	1
z	3	1	0

time →



# Comparison of LS and DV algorithms

## *message complexity*

- ❖ **LS:** with  $n$  nodes,  $E$  links,  $O(nE)$  msgs sent
- ❖ **DV:** exchange between neighbors only

**robustness:** what happens if router malfunctions?

## *LS:*

- node can advertise incorrect *link* cost
- each node computes only its own table

## *DV:*

- DV node can advertise incorrect *path* cost
- each node's table used by others
  - error propagate thru network



# 5 Pirates Puzzle

5 pirates of different ages have a treasure of 100 gold coins.

On their ship, they decide to split the coins using this scheme:

The oldest pirate proposes how to share the coins, and ALL pirates (including the oldest) vote for or against it.

If 50% or more of the pirates vote for it, then the coins will be shared that way. Otherwise, the pirate proposing the scheme will be thrown overboard, and the process is repeated with the pirates that remain.

Assume that all 5 pirates are intelligent, rational, greedy, and do not wish to die, (and are rather good at math for pirates). If you were the oldest pirate, how do you propose?



**Richard E. Bellman**

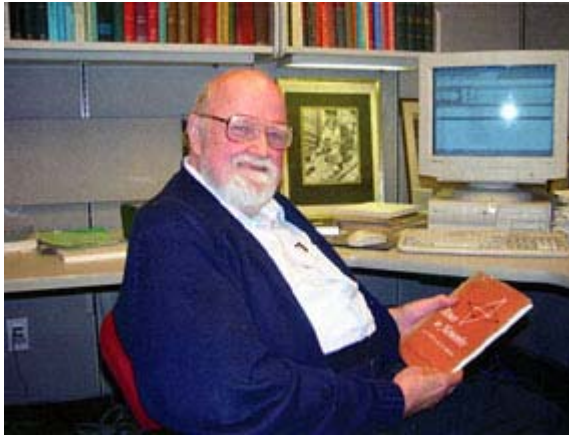


1920 - 1984

Mathematics and Control theory

Ph.D at Princeton

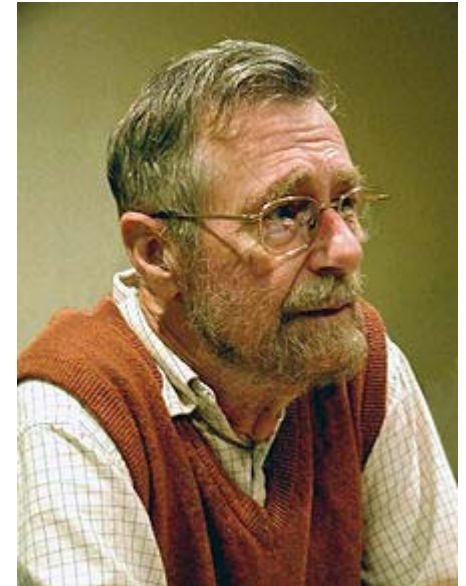
**Lester R. Ford Jr.**



1927 - 2017

Mathematics

**Edsger W. Dijkstra**



1930 - 2002

Computing science

Theoretical  
computer science

Turing Award  
(1972)