# **ELEC 4700: Assignment 2**- Finite Difference Method

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### Part 1

Use the Finite Difference Method to solve for the electrostatic potential in the rectangular region L x W using  $del^2 V = 0$ 

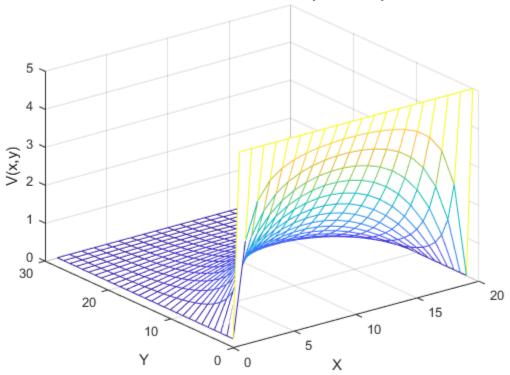
# Part 1: a)

```
V = V0 @ x = 0, V = 0 @ x = L \text{ and } V = 0 @ y = 0, y = W
% The Finite Difference Method will be used to solve Laplace's
 equation in
% 2D space to determine the effect of an electrostatic potential. The
% matrix form GV = F will be used to solve the equation.
clear all; clc;
% Inputs
W = 20;
L = 1.5*W;
nx = L;
ny = W;
V0 = 5;
G = sparse(nx*ny);
B = zeros(nx*ny,1);
% Surface map
sMap = zeros(nx,ny);
for i = 1:nx
    for j = 1:ny
       n = j + (i-1)*ny;
```

```
if i == 1 % left
           G(n,:) = 0;
           G(n,n) = 1;
           B(n) = V0;
       elseif i == nx % right
           G(n,:) = 0;
           G(n,n) = 1;
           B(n,1) = 0;
       elseif j == 1 % bottom
           G(n,:) = 0;
           G(n,n) = 1;
           B(n,1) = 0;
       elseif j == ny % top
           G(n,:) = 0;
           G(n,n) = 1;
           B(n,1) = 0;
       else
           nxm = j + (i-2)*ny;
           nxp = j + (i)*ny;
           nym = j-1 + (i-1)*ny;
           nyp = j+1 + (i-1)*ny;
           G(n,n) = -4;
           G(n, nxm) = 1;
           G(n, nxp) = 1;
           G(n, nym) = 1;
           G(n, nyp) = 1;
       end
    end
end
phi_vec = G\backslash B;
% Map values back to Surface Map
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny;
        sMap(i,j) = phi_vec(n);
    end
end
figure(1)
mesh(sMap);
xlabel("X");
ylabel("Y");
zlabel("V(x,y)");
title("Finite Difference Solution of Laplace's Equation");
```

- % As stated in the boundary conditions, the potential of V0 is located on
- % the left side of the surface and OV is located on the right boundary. The
- % top and bottom boundaries are left open. The electrostatic potential
- % gradually decreases as away from the left side of VO.





# **Part 1: b)**

```
V = V0 @ x = 0, x = L and V = 0 @ y = 0, y = W
clear all; clc;
% Inputs
W = 20;
L = 30;

nx = L;
ny = W;

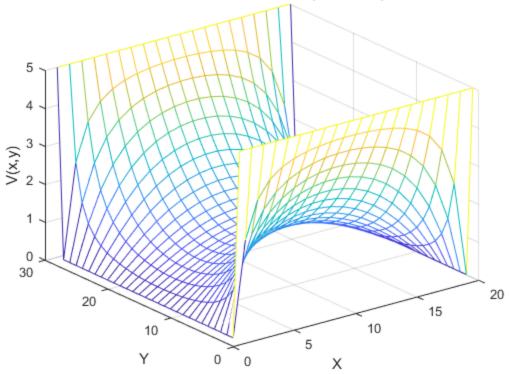
V0 = 5;

G = sparse(nx*ny);
B = zeros(nx*ny,1);
% Surface map
```

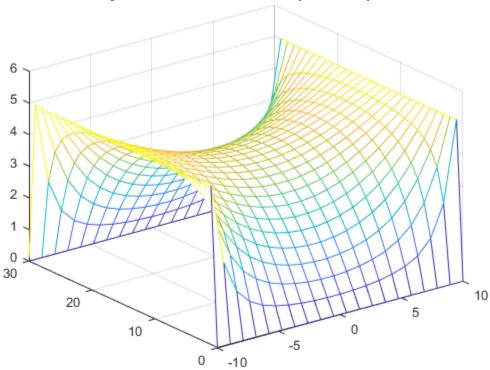
```
sMap = zeros(nx,ny);
for i = 1:nx
    for j = 1:ny
       n = j + (i-1)*ny;
       if i == 1 % left
           G(n,:) = 0;
           G(n,n) = 1;
           B(n) = V0;
       elseif i == nx % right
           G(n,:) = 0;
           G(n,n) = 1;
           B(n,1) = V0;
       elseif j == 1 % bottom
           G(n,:) = 0;
           G(n,n) = 1;
           B(n,1) = 0;
       elseif j == ny % top
           G(n,:) = 0;
           G(n,n) = 1;
           B(n,1) = 0;
       else
           nxm = j + (i-2)*ny;
           nxp = j + (i)*ny;
           nym = j-1 + (i-1)*ny;
           nyp = j+1 + (i-1)*ny;
           G(n,n) = -4;
           G(n, nxm) = 1;
           G(n, nxp) = 1;
           G(n, nym) = 1;
           G(n, nyp) = 1;
       end
    end
end
phi_vec = G\backslash B;
% Map values back to Surface Map
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny;
        sMap(i,j) = phi_vec(n);
    end
end
figure(2)
mesh(sMap);
```

```
xlabel("X");
ylabel("Y");
zlabel("V(x,y)");
title("Finite Difference Solution of Laplace's Equation");
% Similar to the plot above, this plot features the right side of the
% surface with a potential of VO.
% Analytical Series Solution
sMap2=zeros(L,W);
a = 30;
b=10;
x=linspace(-10,10,20);
y=linspace(0,L,L);
[xx,yy] = meshgrid(x,y);
figure(3)
for n=1:2:600
             sMap2 = (sMap2 + (cosh(n*pi*xx/a)).*sin(n*pi*yy/a))./(n*cosh(n*pi*b/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).*sin(n*pi*yy/a)).
a)));
            mesh(x,y,(4*V0/pi)*sMap2)
            title("Analytical Series Solution of Laplace's Equation")
            pause(0.01)
end
% The above plot is obtained from solving the analytic series solution
% Laplace's equation. Due to the memory constraints of MATLAB, the n
% variable is only capable of reaching a value of around 600. Anthing
% greater than this value, the solution becomes inaccurate. To obtain
% perfect accuracy, the series must be evaluated to infinity.
  Therefore the
% numeric solution is prefered.
```





## Analytical Series Solution of Laplace's Equation

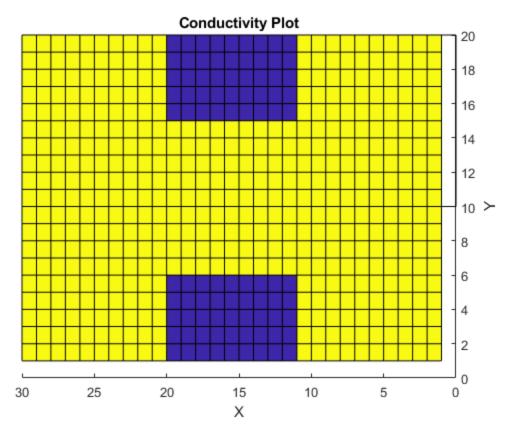


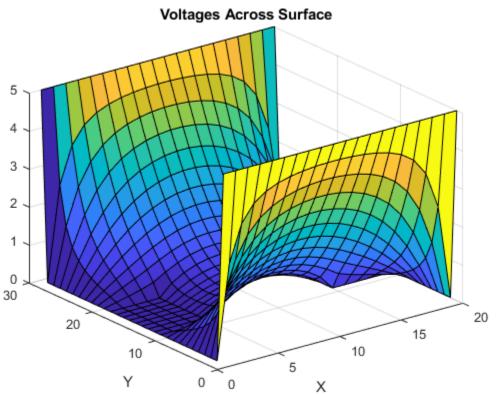
# **Part 2: a)**

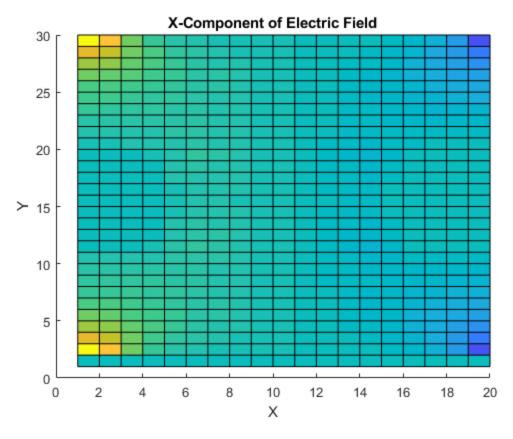
```
% Similar to Part 1, this part describes the current flow in a 2D
 surface
% with a highly resistive barrier.
clear all; clc;
%Inputs
W = 20;
L = 1.5*W;
nx = L;
ny = W;
V0 = 5;
sig1 = 1;
sig2 = 1e-2;
Wb = 6;
Lb = 10;
top_box = [(nx/2) - (Lb/2) \ 0 \ Lb \ Wb];
bottom_box = [(nx/2)-(Lb/2) ny-Wb Lb Wb];
% Populate sigma matrix
sigma = ones(nx,ny);
for i=1:nx
    for j=1:ny
        if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) \mid \mid j > bottom_box(2))
            sigma(i,j) = sig2;
        end
    end
end
% Conductivity Plot
figure(4)
rectangle('Position',top_box)
rectangle('Position',bottom_box)
surface(sigma)
camroll(90)
title('Conductivity Plot')
xlabel('Y')
ylabel('X')
% Construct G Matrix
G = sparse(nx*ny);
B = zeros(nx*ny,1);
for i=1:nx
    for j=1:ny
```

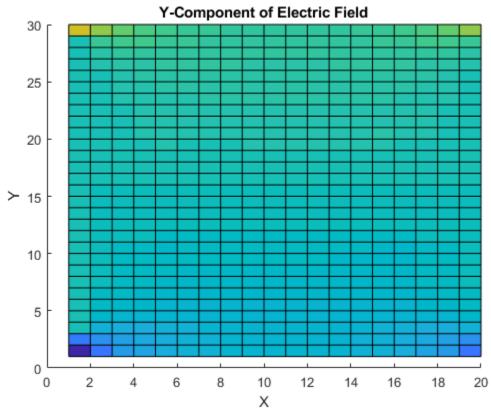
```
n = j + (i-1)*ny; % Node mapping
        if i == 1 % Left
            G(n,:) = 0;
            G(n,n) = 1;
            B(n) = V0;
        elseif i == nx % Right
            G(n,:) = 0;
            G(n,n) = 1;
            B(n,1) = V0;
        elseif j == 1 % Bottom
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        elseif j == ny % Top
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        else % Not along any boundary
            if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) || j > bottom_box(2))) % Inside box
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig2;
                G(n, nxp) = sig2;
                G(n, nym) = sig2;
                G(n, nyp) = sig2;
            else
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig1;
                G(n, nxp) = sig1;
                G(n, nym) = sig1;
                G(n, nyp) = sig1;
            end
        end
    end
end
phi\_vec = G\backslash B;
```

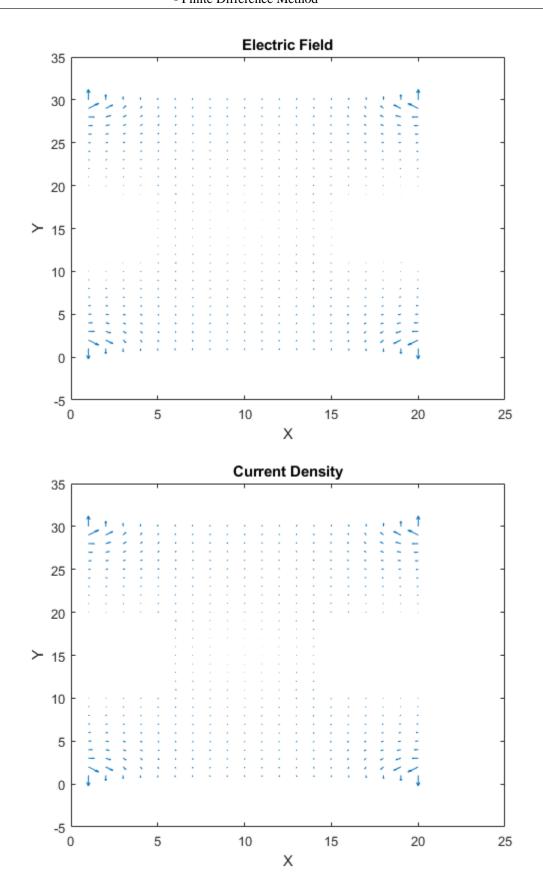
```
sMap3 = zeros(nx,ny);
% Map voltages back on to surface map
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny;
        sMap3(i,j) = phi_vec(n);
    end
end
figure(5)
surf(sMap3)
title('Voltages Across Surface')
xlabel('X');
ylabel('Y');
% Electric Field
[Ex, Ey] = gradient(sMap3);
figure(6)
surface(Ex)
title('X-Component of Electric Field')
xlabel('X');
ylabel('Y');
figure(7)
surface(Ey)
title('Y-Component of Electric Field')
xlabel('X');
ylabel('Y');
figure(8)
quiver(Ex,Ey)
title('Electric Field')
xlabel('X');
ylabel('Y');
% Current Density
Jx = Ex.*sigma;
Jy = Ey.*sigma;
figure(9)
quiver(Jx,Jy)
title('Current Density')
xlabel('X');
ylabel('Y');
```











## **Part 2: c)**

Create different bottle necks (4) and graph current mesh

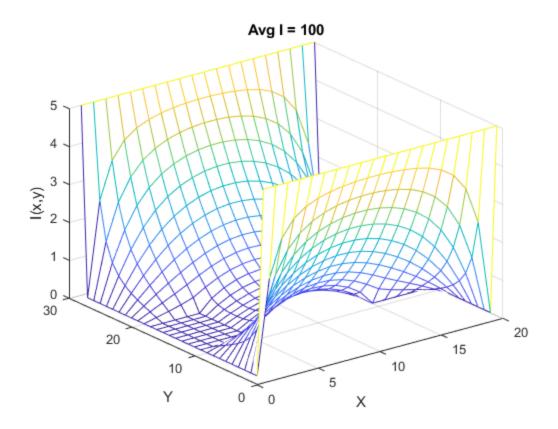
```
% Current in Bottle Neck
R = sigma;
for i=1:nx
    for j=1:ny
        if sigma(i,j) == sig2
            R(i,j) = 1/sig2;
        end
    end
end
current = sMap3./R;
C0 = sum(current(1,:));
C1 = sum(current(L,:));
C = (C0 + C1)/2;
figure(10)
mesh(current);
xlabel('X');
ylabel('Y');
zlabel('I(x,y)');
title(['Avg I = ', num2str(C)]);
% Adjust bottle neck
Wb = 8;
Lb = 10;
top_box = [(nx/2)-(Lb/2) \ 0 \ Lb \ Wb];
bottom_box = [(nx/2)-(Lb/2) ny-Wb Lb Wb];
% Populate sigma matrix
sigma = ones(nx,ny);
for i=1:nx
    for j=1:ny
        if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) \mid \mid j > bottom_box(2))
            sigma(i,j) = sig2;
        end
    end
end
% Construct G Matrix
G = sparse(nx*ny);
B = zeros(nx*ny,1);
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny; % Node mapping
        if i == 1 % Left
            G(n,:) = 0;
```

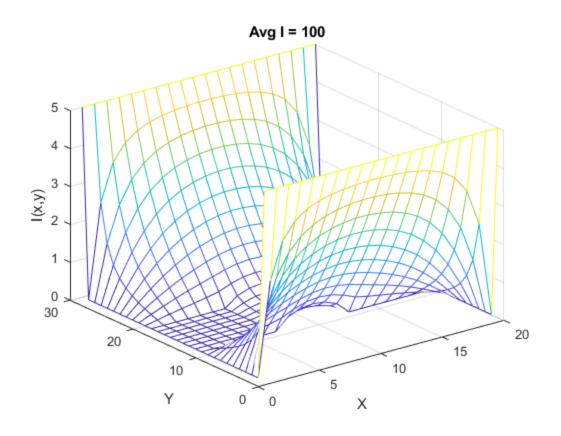
```
G(n,n) = 1;
            B(n) = V0;
        elseif i == nx % Right
            G(n,:) = 0;
            G(n,n) = 1;
            B(n,1) = V0;
        elseif j == 1 % Bottom
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        elseif j == ny % Top
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        else % Not along any boundary
            if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) || j > bottom_box(2))) % Inside box
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig2;
                G(n, nxp) = siq2;
                G(n, nym) = sig2;
                G(n, nyp) = sig2;
            else
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig1;
                G(n, nxp) = sig1;
                G(n, nym) = sig1;
                G(n, nyp) = sig1;
            end
        end
    end
end
phi_vec = G\backslash B;
sMap4 = zeros(nx,ny);
% Map voltages back on to surface map
for i=1:nx
```

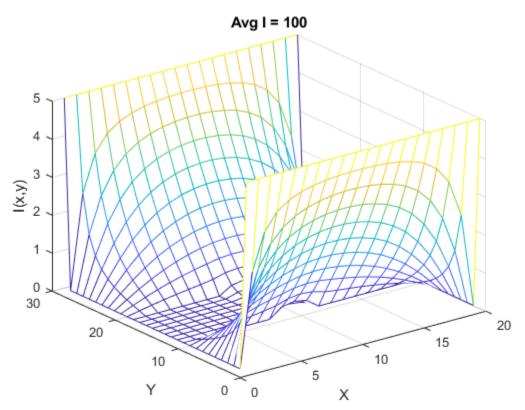
```
for j=1:ny
        n = j + (i-1)*ny;
        sMap4(i,j) = phi_vec(n);
    end
end
R = sigma;
for i=1:nx
    for j=1:ny
        if sigma(i,j) == sig2
            R(i,j) = 1/sig2;
        end
    end
end
current = sMap4./R;
figure(11)
mesh(current);
xlabel('X');
ylabel('Y');
zlabel('I(x,y)');
title(['Avg I = ', num2str(C)]);
% Adjust bottle neck
Wb = 9;
Lb = 10;
top\_box = [(nx/2)-(Lb/2) \ 0 \ Lb \ Wb];
bottom_box = [(nx/2)-(Lb/2) ny-Wb Lb Wb];
% Populate sigma matrix
sigma = ones(nx,ny);
for i=1:nx
    for j=1:ny
        if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
bottom_box(4) \mid \mid j > bottom_box(2))
            sigma(i,j) = sig2;
        end
    end
end
% Construct G Matrix
G = sparse(nx*ny);
B = zeros(nx*ny,1);
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny; % Node mapping
        if i == 1 % Left
            G(n,:) = 0;
            G(n,n) = 1;
            B(n) = V0;
```

```
elseif i == nx % Right
            G(n,:) = 0;
            G(n,n) = 1;
            B(n,1) = V0;
        elseif j == 1 % Bottom
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        elseif j == ny % Top
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        else % Not along any boundary
            if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) || j > bottom_box(2))) % Inside box
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = siq2;
                G(n, nxp) = sig2;
                G(n, nym) = sig2;
                G(n, nyp) = sig2;
            else
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = siq1;
                G(n, nxp) = sig1;
                G(n, nym) = sig1;
                G(n, nyp) = sig1;
            end
        end
    end
end
phi\_vec = G\backslash B;
sMap5 = zeros(nx,ny);
% Map voltages back on to surface map
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny;
        sMap5(i,j) = phi\_vec(n);
```

```
end
end
R = sigma;
for i=1:nx
    for j=1:ny
        if sigma(i,j) == sig2
            R(i,j) = 1/sig2;
        end
    end
end
current = sMap5./R;
figure(12)
mesh(current);
xlabel('X');
ylabel('Y');
zlabel('I(x,y)');
title(['Avg I = ', num2str(C)]);
% Decreasing the width of the bottleneck seems to have no affect on
the
% total current in the surface, as each iteration of different
bottleneck
% width produces the same total current.
```







## **Part 2: d)**

Change sigma, calculate current, graph mesh current

```
% Adjust bottle neck
Wb = 5;
Lb = 10;
top_box = [(nx/2)-(Lb/2) \ 0 \ Lb \ Wb];
bottom_box = [(nx/2)-(Lb/2) ny-Wb Lb Wb];
% Populate sigma matrix
sigma = ones(nx,ny);
sig2 = 1e-3;
sig1 = 1;
for i=1:nx
    for j=1:ny
        if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
bottom_box(4) || j > bottom_box(2)))
            sigma(i,j) = sig2;
        end
    end
end
% Construct G Matrix
G = sparse(nx*ny);
B = zeros(nx*ny,1);
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny; % Node mapping
        if i == 1 % Left
            G(n,:) = 0;
            G(n,n) = 1;
            B(n) = V0;
        elseif i == nx % Right
            G(n,:) = 0;
            G(n,n) = 1;
            B(n,1) = V0;
        elseif j == 1 % Bottom
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        elseif j == ny % Top
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        else % Not along any boundary
```

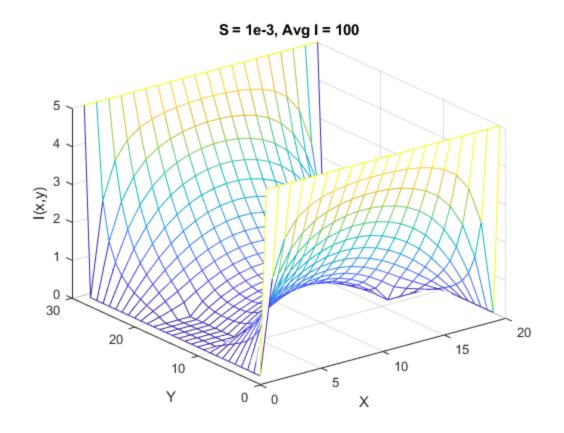
```
if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) || j > bottom_box(2))) % Inside box
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig2;
                G(n, nxp) = sig2;
                G(n, nym) = sig2;
                G(n, nyp) = sig2;
            else
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig1;
                G(n, nxp) = sig1;
                G(n, nym) = sig1;
                G(n, nyp) = sig1;
            end
        end
    end
end
phi\_vec = G\backslash B;
sMap5 = zeros(nx,ny);
% Map voltages back on to surface map
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny;
        sMap5(i,j) = phi_vec(n);
    end
end
R = sigma;
for i=1:nx
    for j=1:ny
        if sigma(i,j) == sig2
            R(i,j) = 1/sig2;
        end
    end
end
current = sMap5./R;
figure(13)
mesh(current);
xlabel('X');
```

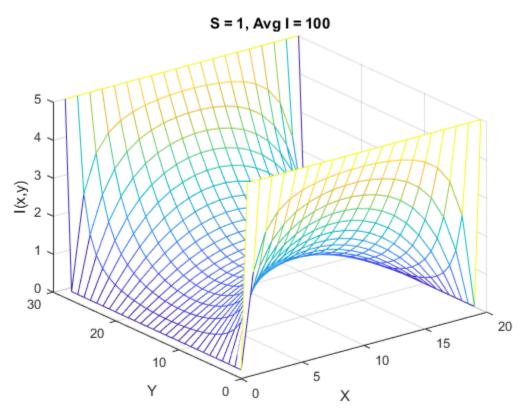
```
ylabel('Y');
zlabel('I(x,y)');
title(['S = 1e-3, Avg I = ', num2str(C)]);
% Populate sigma matrix
sigma = ones(nx,ny);
sig2 = 1;
sig1 = 1;
for i=1:nx
    for j=1:ny
        if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
bottom_box(4) || j > bottom_box(2)))
            sigma(i,j) = sig2;
        end
    end
end
% Construct G Matrix
G = sparse(nx*ny);
B = zeros(nx*ny,1);
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny; % Node mapping
        if i == 1 % Left
            G(n,:) = 0;
            G(n,n) = 1;
            B(n) = V0;
        elseif i == nx % Right
            G(n,:) = 0;
            G(n,n) = 1;
            B(n,1) = V0;
        elseif j == 1 % Bottom
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        elseif j == ny % Top
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        else % Not along any boundary
            if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) || j > bottom_box(2))) % Inside box
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
```

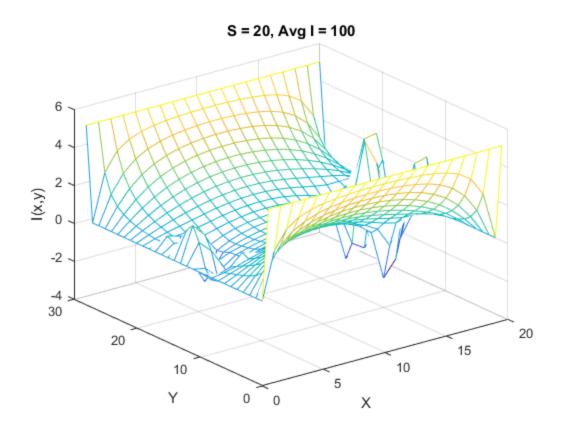
```
G(n,n) = -4;
                G(n, nxm) = sig2;
                G(n, nxp) = sig2;
                G(n, nym) = sig2;
                G(n, nyp) = sig2;
            else
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig1;
                G(n, nxp) = sig1;
                G(n, nym) = sig1;
                G(n, nyp) = sig1;
            end
        end
    end
end
phi\_vec = G\backslash B;
sMap5 = zeros(nx,ny);
% Map voltages back on to surface map
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny;
        sMap5(i,j) = phi_vec(n);
    end
end
R = sigma;
for i=1:nx
    for j=1:ny
        if sigma(i,j) == sig2
            R(i,j) = 1/sig2;
        end
    end
end
current = sMap5./R;
figure(14)
mesh(current);
xlabel('X');
ylabel('Y');
zlabel('I(x,y)');
title(['S = 1, Avg I = ', num2str(C)]);
% Populate sigma matrix
sigma = ones(nx,ny);
sig2 = 2;
sig1 = 1;
```

```
for i=1:nx
    for j=1:ny
        if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) \mid j > bottom_box(2))
            sigma(i,j) = sig2;
        end
    end
end
% Construct G Matrix
G = sparse(nx*ny);
B = zeros(nx*ny,1);
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny; % Node mapping
        if i == 1 % Left
            G(n,:) = 0;
            G(n,n) = 1;
            B(n) = V0;
        elseif i == nx % Right
            G(n,:) = 0;
            G(n,n) = 1;
            B(n,1) = V0;
        elseif j == 1 % Bottom
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        elseif j == ny % Top
                G(n,:) = 0;
                G(n,n) = 1;
                B(n,1) = 0;
        else % Not along any boundary
            if (i > top_box(1) && i < top_box(1)+top_box(3) && (j <</pre>
 bottom_box(4) || j > bottom_box(2))) % Inside box
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
                nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = siq2;
                G(n, nxp) = sig2;
                G(n, nym) = sig2;
                G(n, nyp) = sig2;
                nxm = j + (i-2)*ny;
                nxp = j + (i)*ny;
```

```
nym = j-1 + (i-1)*ny;
                nyp = j+1 + (i-1)*ny;
                G(n,n) = -4;
                G(n, nxm) = sig1;
                G(n, nxp) = sig1;
                G(n, nym) = sig1;
                G(n, nyp) = sig1;
            end
        end
    end
end
phi vec = G\backslash B;
sMap5 = zeros(nx,ny);
% Map voltages back on to surface map
for i=1:nx
    for j=1:ny
        n = j + (i-1)*ny;
        sMap5(i,j) = phi_vec(n);
    end
end
R = sigma;
for i=1:nx
    for j=1:ny
        if sigma(i,j) == sig2
            R(i,j) = 1/sig2;
        end
    end
end
current = sMap5./R;
figure(15)
mesh(current);
xlabel('X');
ylabel('Y');
zlabel('I(x,y)');
title(['S = 20, Avg I = ', num2str(C)]);
% Increasing the conductivity in the barrier region increases the
total
% current in that region. However, in every iteration of different
% conductivity values, the average current does not change.
```







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