Direct Tests of Black Hole Accretion Rate Prescriptions: I. Bondi Accretion at Different Scales

James Agostino, 1 Ming-Yi Lin, 1 Natasha Jones, 1 Anne M. Medling, 1 Loreto Barcos-Muñoz, 2,3 Daniel Anglés-Alcázar, 4 Claudio Ricci, 5,6 George C. Privon, 7,8,9 Vivian U, 10 Paul Torrey, 11,12,13 Philip F. Hopkins, 14 and Claire Max 4 ¹Ritter Astrophysical Research Center and Department of Physics & Astronomy, University of Toledo, Toledo, OH 43606, USA ² National Radio Astronomy Observatory, 520 Edgemont Road, Charlottesville, VA, 22903, USA ³Department of Astronomy, University of Virginia, 530 McCormick Road, Charlottesville, VA, 22903, USA 4PLACEHOLDER ⁵ Instituto de Estudios Astrofísicos, Facultad de Ingeniería y Ciencias, Universidad Diego Portales, Avenida Ejercito Libertador 441, Santiago, Chile 10 ⁶Kavli Institute for Astronomy and Astrophysics, Peking University, Beijing 100871, China 11 ⁷ National Radio Astronomy Observatory, 520 Edgemont Road, Charlottesville, VA 22903 12 ⁸ Department of Astronomy, University of Florida, P.O. Box 112055, Gainesville, FL 32611, USA 13 Department of Astronomy, University of Virginia, 530 McCormick Road, Charlottesville, VA 22904, USA 14 ¹⁰4129 Frederick Reines Hall, Department of Physics and Astronomy, University of California, Irvine, CA 92697, 15 USA16 ¹¹Department of Astronomy, University of Virginia, 530 McCormick Road, Charlottesville, VA 22904 17 ¹² Virginia Institute for Theoretical Astronomy, University of Virginia, Charlottesville, VA 22904, USA 18

13 The NSF-Simons AI Institute for Cosmic Origins, USA

¹⁴IPAC, California Institute of Technology, 1200 East California Boulevard, Pasadena, CA 91125, USA

ABSTRACT

We present spatially resolved parsec-scale measurements of nuclear conditions (gas density and kinetic temperature) relevant for black hole accretion rate predictions in the Seyfert 2 galaxy, NGC 1068. We inject these parameters into the prescription for a Bondi-like accretion model, then compare the resulting accretion rate prediction to the empirical accretion rate derived from hard X-ray observations. Cosmological simulations have spatial resolution ranging between, from ~10 pc to on order kpc, and so for reasonable comparison we test these accretion rate predictions in pixel-sized radial steps out to 500 pc. Compared to warm H_2 gas, CO gas is the dominant mass carrier close to the SMBH. We find that the Bondi accretion rate (\dot{M}_{Bondi}) of cold molecular gas alone (measured using CO) overestimates the true accretion rate by up to 4 dex in a small aperture ($r\lesssim6$ pc) around the black hole, but that it performs much better on large ($r\gtrsim300$ pc) scales. These results are the first in a series of direct tests of accretion rate prescriptions, and they suggest that using a Bondi accretion formalism to model supermassive black hole accretion in Seyfert 2 galaxies may lead to overestimated accretion rates depending on the resolution of the simulation.

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Supermassive black holes (SMBHs), despite their small gravitational radius of the sphere

⁴⁰ of influence (1~100 pc), are thought to be a hold key piece of the connection between pc and key key scales of galaxy evolution. Observations of galaxies with active galactic nuclei (AGN) have shown both directly and indirectly that AGN have can inject energy into their surrounding environments, which can ultimately quench or in some cases trigger star formation (see Fabian 2012 for a review).

Active galactic nuclei do not only interact 50 with the central part of galaxies, they may 51 also significantly impact several global prop-52 erties of galaxies and their surrounding inter-53 galactic media, allowing us to indirectly infer 54 their influence on those observables. Relation-55 ships between black hole mass and global galaxy 56 properties, like the velocity dispersion of stars 57 in the galactic bulge, have been well-calibrated 58 and show tight correlations (see Kormendy & 59 Ho 2013; McConnell & Ma 2013 for reviews). 60 These correlations suggest that AGN radiative 61 feedback, which in part depends on black hole 62 mass, may leave an imprint on bulge stellar ve-63 locity dispersion (see Ferrarese & Merritt 2000; 64 Gebhardt et al. 2000 for seminal studies). Star 65 formation in massive halos is suppressed (e.g. in 66 Behroozi et al. 2013; Torrey et al. 2014), which 67 could be caused by heating of the interstellar 68 medium (ISM) from AGN feedback. In the high 69 energy regime, a discrepancy is found between 70 the observed and expected correlations between 71 X-ray luminosities and temperatures of gas in 72 the intra-cluster medium (called the L_X -T re-73 lation, see Mushotzky 1984; Markevitch 1998). 74 This discrepancy suggests that gas in the intra-75 cluster medium evolves differently from dark 76 matter; energetics input by host AGN could be 77 a factor as to why.

Indirect cases of the impact of AGN feedback 79 on galaxy formation histories are only made 80 more intriguing by direct evidence of AGN feed-81 back. Since more than 100 years ago (M87; Cur-82 tis 1918) radio jets powered by a central SMBH si have been seen to extend up to ~0.9 Mpc outside from their host galaxies (e.g. Centaurus A; Burns et al. 1983). Outflows driven by these SMBHs have been observed in the process of depleting the ISM at outflow rates of 700 M_☉ yr⁻¹ (e.g. in Mrk 231; Feruglio et al. 2010). Our pilot galaxy for this study, NGC 1068, has a complex and well studied AGN-driven outflow that also impacts the ISM on sub-kpc scales (e.g. Wilson & Ulvestad 1983; Müller-Sánchez et al. 2011; García-Burillo et al. 2014; Saito et al. 2022; Hviding et al. 2023; Holden & Tadhunter 2023; Gallimore & Impellizzeri 2023; Mutie et al. 2024; Hagiwara et al. 2024).

The energy output of an AGN is driven by 98 mass accretion onto its accretion disk, fueled 99 by inflows in the nuclei of galaxies. This gas then accelerates to speeds of up to > 0.1c in 101 the accretion disk, and that disk can power ra-102 diative outflows. The direct observational feed-103 back can be classified as two mechanisms: radia-104 tive (quasar mode) or kinematic (radio mode) 105 (Fabian 2012). In the quasar mode, occurring when the black hole accretes mass quickly, pho-107 tons from the accretion disk couple to the ISM, 108 transferring momentum in a powerful jet. In ra-109 dio mode, accretion onto the disk is slower, and 110 the primary feedback mechanism is in the form 111 of collimated radio jets that typically appear 112 narrower than quasar-mode jets (see Cielo et al. 113 2018 for a simulated comparison between the 114 feedback of the two modes). Both modes can 115 drive outflows, but the guasar-mode is thought 116 to start the quenching process (the spatial ex-117 tent of which grows over time) and then the 118 radio-mode maintains that quenched state (see Fabian 2012 and Morganti 2017 for reviews).

As simulations of galaxy evolution have been informed by increasingly detailed observations, theorists have begun to study the physical mechanisms that drive AGN feedback and how that feedback impacts the simulated host galaxies. Dubois et al. (2013a) (see also Dubois et al.

 126 2013b; Taylor & Kobayashi 2015) examined how 127 AGN jets impact cold gas and transform blue, 128 disky galaxies into red ellipticals. Building on 129 these studies, Rosas-Guevara et al. (2015), who 130 simulated accretion in galaxies of varied halo 131 mass, find that in galaxies with 131 above 132 $^{1011.5}$ 15 15 15 15 15 15 15 15 15 15 15 of cosmological simulations in which they couple 15 15 AGN feedback to different phases of the ISM. 15 They find, in part, that energy output from the 15 AGN as feedback must couple with both the 15 cold and hot phases in order to avoid excessive 15

As is seen in both observations and simula-142 tions, global galaxy properties can be affected 143 by accretion-dependent feedback. Theorists 144 have attempted to model the physical processes 145 causing those properties to change. Williamson 146 et al. (2020) perform radiation hydrodynamics 147 modeling of the 1-100 pc scales in a nuclear re-148 gion of a simulated AGN host. They demon-149 strate that increasingly polar winds are pro-150 duced when anisotropic radiation from the AGN 151 shifts the mass distribution of the outflow orig-152 inating from the AGN. Meenakshi et al. (2022) 153 simulated the direct interaction between AGN 154 jet-induced outflows on 2 kpc scale and the ISM and found shocked emission fronts in the ISM 156 that could be responsible for stunting star formation. On r < 1 pc scale, Wada et al. (2023) 158 were able to induce radiation-driven dusty out-159 flows which impact the ISM as they continue on 160 their outward paths. Tying the small and large 161 scales together has been an ongoing challenge. Due to computational constraints, large-scale 163 cosmological simulations that can model hun-164 dreds of Mpc³ at a time are not able to directly 165 resolve the physical processes that drive gas ac-166 cretion at <<1 pc scales where accretion takes 167 place, and so sub-grid prescriptions for black 168 hole accretion and its subsequent feedback must be adopted.¹ The 'sub-grid' is defined as the rei70 gion below the gridded resolution of the simui71 lation. Unfortunately, there is no unified model i72 for these sub-grid physics, and different studi73 ies use different accretion prescriptions. The i74 most commonly applied prescription is the one i75 described in (Bondi 1952), often referred to as i76 Bondi accretion. The equation follows the form:

$$\dot{M}_{Bondi} = \frac{4\pi G^2 M_{BH}^2 \rho}{\left(c_s^2 + v_{rel}^2\right)^{3/2}}$$
 (1)

where G is the gravitational constant, M_{BH} is the mass of the black hole, ρ is the gas density, 180 c_s is the sound speed, and v_{rel}^2 is the relative 181 velocity of the gas. In the pure Bondi case, the 182 gas is assumed to be stationary relative to the 183 galactic potential, so v_{rel}^2 is zero. This model is 184 theoretically predicated on gas free-falling onto 185 the SMBH once it reaches the Bondi radius, $_{186}$ R_{Bondi} = 2GM_{BH} $/c_s^2$. The Bondi radius is where 187 the escape velocity of the SMBH (based on its 188 mass) equals the sound speed of the gas in the 189 nuclear region. The physical scale of the Bondi 190 radius is typically on order 0.1-300 pc if we as- $_{\rm 191}$ sume $\rm c_{\rm s}$ of 400 km $\rm s^{-1}$ and SMBH mass range 192 of $10^6 \sim 10^9 \, \mathrm{M}_{\odot}$. Some large scale cosmo-193 logical simulation suites use a pure Bondi pre-194 scription to account for SMBH accretion, like 195 MassiveBlack-II (Khandai et al. 2015), EAGLE 196 (Schaye et al. 2015), and IllustrisTNG (Wein-197 berger et al. 2017; Pillepich et al. 2018a). Physically, the issue with the Bondi accre-199 tion formalism is that it ignores both the angu-200 lar momentum of the gas and interactions due

201 to self-gravity between gas particles, which is

202 only appropriate in the case of hot, virialized 203 gas (Hobbs et al. 2012). Recent studies have

204 shown that gas and other accreting material still

Although there is also much variation in AGN feedback prescriptions, this program will focus on discussing the accretion rate prescriptions, on which all feedback depends.

has angular momentum inside what may be the Bondi radius, particularly in gas-rich mergers or galaxies with Seyfert AGN (e.g. in Davies et al. 2013; Medling et al. 2014; Lin et al. 2016), and so Bondi accretion timescales may be much shorter than in reality where angular momentum delays accretion.

To account for this problem, some large-213 scale cosmological simulation suites apply ac-214 cretion physics by using modified versions of 215 Bondi accretion. The prescription in the *Il*-216 lustris (the predecessor to IllustrisTNG; Vo-217 gelsberger et al. 2013; Genel et al. 2014) and 218 Magneticum Pathfinder hydrodynamical simu-219 lation suites (Hirschmann et al. 2014; Bocquet 220 et al. 2016; Dolag et al. 2016) modify Bondi 221 by multiplying Equation 1 by a constant (unit-222 less) 'boost' factor α (following the prescription 223 of Springel et al. 2005; Di Matteo et al. 2005; 224 Springel & Hernquist 2005). The boost factor 225 is used to account for the volume average of the 226 Bondi-rates for both the cold and hot phases 227 in the simulations and typically has a value = 228 100. Another large-scale cosmological model, ₂₂₉ Horizon-AGN (Dubois et al. 2016), uses an α 230 similar to *Illustris* and *Magneticum*, but instead 231 of a constant value, their boost factor (following 232 the prescription from Booth & Schaye 2009) de-233 pends on density of the gas. Another approach, 234 used by the large-scale *Romulus* suite (Tremmel 235 et al. 2017) is to adjust the Bondi accretion rate 236 depending on the motion of the simulated gas 237 particles. In Romulus, if the smallest relative 238 velocity (which they equate to v_{bulk}, the bulk 239 motion of the gas) of the gas particle closest to 240 the SMBH is faster than the rotational veloc-241 ity of the gas, they replace the relative velocity $_{242}$ of the SMBH with v_{bulk} and multiply the Bondi ²⁴³ rate by a boost factor dependent on gas density. Bondi or Bondi-like accretion prescriptions 245 are the most commonly used, but theorists have 246 also designed accretion prescriptions with very 247 different underlying physics. One large-scale

simulation ([100 h^{-1} Mpc]³ volume) suite that ²⁴⁹ in part uses one of these prescriptions is SIMBA 250 (Davé et al. 2019a). In SIMBA, pure Bondi 251 accretion is still applied for hot gas accretion 252 where, as we mentioned, it is most appropri-253 ate. But, they then apply a torque-limited ac-254 cretion formalism for the cold gas where insta-255 bilities in the disk drive mass inflow (Hopkins 256 & Quataert 2011; Anglés-Alcázar et al. 2017). ²⁵⁷ Understanding if and in which cases different 258 sub-grid prescriptions are accurately estimating 259 accretion rates onto the black holes of galaxies 260 is critically important to cosmological simula-261 tions. Without an accurate prescription for ac-262 cretion over time, simulations cannot accurately 263 implement the impact of AGN feedback, and as 264 such may have incorrect outcomes with regards 265 to galaxy formation and evolution.

Observationally testing how black hole accre-267 tion rate prescriptions perform has only be-268 come possible in recent times. In this study, 269 we directly measure the parameters that go into 270 Bondi accretion, $\rho_{\rm gas}$ and c_s , on physical scales 271 ranging from 2-170 pc. We then plug these mea-272 sured parameters into the pure Bondi accretion 273 prescription as a function of radius to mimic 274 what a simulation at that resolution would es-275 timate for the black hole accretion rate. Fi-276 nally we test these predicted Bondi accretion 277 rates against empirically derived accretion rates 278 using hard (14-195 keV) X-ray data from the 279 The Burst Alert Telescope (BAT) AGN Spec-280 troscopic Survey (BASS) survey (Ricci et al. 281 2017). The BAT instrument (Barthelmy et al. $282\ 2005$; Krimm et al. 2013) on Swift (Gehrels et al. 283 2004) is a hard X-ray detector that surveys the 284 entire sky, reporting X-ray sources to within 1-4 285 arcmin accuracy.

In this work, we use cosmological parameters of $H_0=70~{\rm km~s^{-1}~Mpc^{-1}},~\Omega_m=0.28,~{\rm and}$ $\Omega_{\Lambda}=0.72$ (Hinshaw et al. 2009). To calculate spatial scales and luminosity distance to NGC

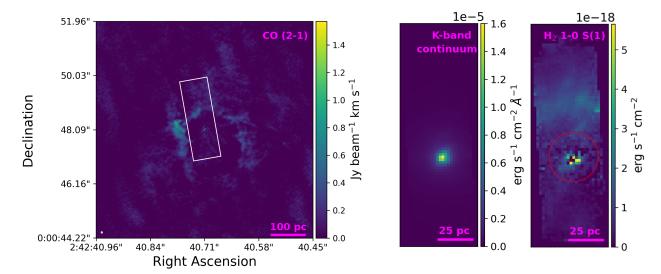


Figure 1. Nuclear region of NGC 1068 in the CO(2-1) flux (left, from ALMA), $2.2\mu m$ continuum (middle), and the continuum subtracted rovibrational H₂ 1-0 S(1) transition (right), described in Section 2. The CO(2-1) moment 0 map is masked below $3\times rms$ and the white box in the CO(2-1) moment map represents the field of view of the NIR data. The very small, white ellipse in the bottom left represents the beam size of the ALMA data (41×30 mas). All three images show flux peaks at the AGN's location and both the CO and H₂ maps have enhanced emission in the CND ring. The red circle in the H₂ 1-0 S(1) moment map represents the aperture in which T_{Kin} is calculated in Figure 3.

²⁹⁰ 1068 we use Ned Wright's Cosmology Calcula-²⁹¹ tor (Wright 2006).

2. NGC 1068 OBSERVATIONS

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For NGC 1068, we made use of <3 pc scale resolution both in the near infrared (NIR) with Keck/OSIRIS+AO (adaptive optics; PI Medling), and in the sub-mm with ALMA archival data (PI García-Burillo).

2.1. Keck/OSIRIS K-band Integral Field Spectroscopy

The first of two sets of data we are using to this project is a set of high resolution integral field unit (IFU) Keck/OSIRIS+AO (OH-303 Suppressing InfraRed Imaging Spectrograph, Larkin et al. 2006) integrations, for which we mosaic all frames into a single data cube. These observations were taken with the Kbb filter (broad-band K between 1.965 - 2.381 μ m) with the 35 mas pixel⁻¹ plate scale on 2018 December 28th, 2019 January 22nd, and 2019 October 7th for a total exposure time of 6120 seconds

311 (51 frames, 120 seconds each). Weather im-312 pacted observations on 2019 October 7th, dur-313 ing which the laser guiding system was also not 314 working. We used the galaxy nucleus as the 315 natural guide star in NGS mode, and as the 316 tip/tilt star in LGS mode. AO corrections in 317 those frames without the laser produced larger 318 point spread functions with full-width at half-319 maximum (FWHM) values between 3 and 5 $_{320}$ pixels compared to ~ 2 with the laser on other 321 nights. We reduced the Keck/OSIRIS+AO ob-322 servations using the OSIRIS Data Reduction ³²³ Pipeline (OSIRISDRP, Lyke et al. 2017; Lockhart et al. 2019) version 4.2.0, which we use to 325 extract a spectrum for each spatial pixel, assem-326 ble the spectra into a cube, and mosaic the 51 327 total frames together to form the final image, 328 which has a 0.17" point spread function (PSF) 329 FWHM. Flux calibration was applied for each 330 night before final mosaicking.

The resulting mosaic reveals a strong K-Band continuum (particularly near the AGN) and

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333 H_2 1-0 rovibrational emission (S(0), λ_{rest} = 334 2.2235 μ m; S(1), λ_{rest} = 2.1218 μ m; S(2)), λ_{rest} = 335 2.0338 μ m. These continuum and continuum-336 subtracted H_2 1-0 S(1) maps are shown in the 337 middle and right panels of Figure 1 respec-338 tively. The continuum map was made using the 339 Cube Analysis and Rendering Tool for Astron-340 omy (CARTA, Comrie et al. 2021) and the con-341 tinuum subtracted H_2 1-0 S(1) map was made using QFitsView (Ott 2012). Both images show 342 using QFitsView (Ott 2012). Both images show 343 peaks of emission on or near the position of the 344 central engine, and NGC 1068's circumnuclear 345 disk (CND) ring can be seen in the H_2 map.

2.2. ALMA Band 6 Long-baseline Interferometry

We chose the highest resolution CO J = (2-348 1) (hereafter CO(2-1)) available on the ALMA 350 archive that shows strong emission (PI García-Burillo, Project code 2016.1.00232.S; see also García-Burillo et al. 2019). We retrieved the 353 CO(2-1) spectral cube product from the ALMA archive, which has a rms of 0.25 mJy over 20 355 km s⁻¹, and was imaged using a Briggs (Briggs 356 1995) robust value of 0, resulting in a beam $_{357}$ size of 41×30 mas. We then used this spec-358 tral cube with the image cube analysis tools in 359 CARTA (Comrie et al. 2021) to create a moment $_{360}$ 0 (flux) map of the CO(2-1) emission. Figure 1 (left) shows this CO(2-1) moment 0 map which $_{362}$ is masked below $3\times \mathrm{rms}$ and is used for our anal-363 ysis in Section 3. Like in the warm H₂ observa-364 tions, both the AGN and CND ring are bright 365 sources in CO(2-1).

2.3. Nuclear structure of NGC 1068

NGC 1068 is one of the most-studied prototypical Seyfert galaxies, and as such a wealth of information has already been published about troits nuclear structure. The studies described here are not an exhaustive list, but are included to provide context relevant to our analysis.

Under our 2.2 pc resolution, NGC 1068 hosts water maser that is thought to originate from

the accretion disk on much smaller (<0.1 pc) scales. Greenhill et al. (1996) observed the maser with very long baseline interferometry to the VLBI) using both the Very Long Baseline Armay and Very Large Array to achieve 0.65 pc resolution. They used the velocity gradient of the maser emission to infer a rotational velocity of the gas, and in turn constrain $M_{\rm BH}$. Kumar (1999) modeled the 0.65-1.1 pc disk from which maser emission is thought to be ejected from. The clumps in their disk model interact with each other, leading to eventual accretion onto the SMBH.

On slightly larger scales with near and mid infrared interferometry, multiple authors were able to resolve a two-component dusty torus (Jaffe et al. 2004; Raban et al. 2009). One component is smaller and more elongated (1.35 × 0.45 pc) in size than the other (3 × 4 pc). In the nucleus of Circinus, another Seyfert 2 AGN, Tristram et al. (2014) also found a two-component dusty torus. Images like these that showed structure inconsistent with the prior, observationally-defined, Type 2 classification of these galaxies (unless foreground extinction was applied) fundamentally challenged the AGN unification model (Antonucci 1993).

Gámez Rosas et al. (2022) used sub-pc resolu-403 tion observations of NGC 1068 taken with the 404 MATISSE/ESO/VLTI interferometer between 405 3 and 13 μ m to map the dust temperature dis-406 tribution of the dust observed in the previously 407 mentioned studies. They confirm an optically 408 thick pc scale dusty structure and a second, less 409 optically thick disk that extends to at least 10 410 pc. García-Burillo et al. (2019) (who in part 411 use the same ALMA data as we describe in Sec-412 tion 2.2) find a 14 pc CO(2-1) nuclear disk with ₄₁₃ a PA (\sim 110-140 deg) aligned with the water 414 maser disk PA (140 deg). Also in García-Burillo 415 et al. (2019), they observe the CND, which as 416 can be seen in Figure 1, has a gas deficit inside 417 the outer ring in its central ~ 130 pc region.

To resolve the kinematics of the 10 pc in-419 ner disk (often referred to as the torus) and 420 outer ring, Imanishi et al. (2020) observe both of 421 these scales using the bright (relative to CO(2- $_{422}$ 1)) HCN J=(3-2) and HCO+ J = (3-2) tran-423 sitions with ALMA at 1.4 pc resolution. They 424 find that the torus as observed with these dense 425 gas tracers rotates in the opposite direction with 426 respect to the outer ring. This is particularly 427 surprising because the water maser emission is 428 rotating in the same direction as the outer ring 429 rather than the torus it is physically closer to 430 (see Figure 1 of Imanishi et al. 2020). In the 431 work of García-Burillo et al. (2019), the authors 432 find that a "significant part" of the observed 433 counter-rotation in CO(2-1) can be attributed 434 to a northern AGN-driven wind. To make 435 a more robust determination though, García-436 Burillo et al. (2019) say that higher resolution 437 data is required so that the outflowing compo-438 nent can be better disentangled from the rotat-439 ing component.

Outflows originating from the AGN can serve 441 to regulate black hole accretion, and NGC 1068 442 hosts a complex outflow in the NE direction, 443 perpendicular to the nuclear disk. The largest 444 outflow component is seen as the radio jet (e.g. 445 in Gallimore et al. 1996). Mutie et al. (2024) 446 present higher resolution (~ 4 pc) e-MERLIN 447 5 GHz data along with archival VLA 10 GHz, 448 and VLA 21 GHz images of the jet. 449 images together show not only the central jet 450 emission, but also detail in the larger scale bow 451 shock, >200 pc from the SMBH in the same 452 NE direction, which exhibits direct evidence of 453 the AGN's impact on the ISM. The impact 454 of the jet on the ISM is studied in part in 455 both Hviding et al. (2023) and Holden & Tad-456 hunter (2023), who both show evidence for gas 457 ionization consistent with shock ionization or 458 radiation-bounded AGN-photoionization along 459 the outflow's path on 160 pc to kpc scale. 460 García-Burillo et al. (2014) show that the CO

kinematics on distances 50 to 400 pc are spa-462 tially correlated with the radio jet, evidence 463 that the AGN is influencing even the cold ISM. 464 ALMA CO(6-5) observations from Gallimore 465 et al. (2016) show that this molecular outflow 466 originates within 2 pc from the SMBH, and has 467 velocities relative to systemic of about 400 km 468 s⁻¹. This outflow may have an impact on our 469 measurements of molecular gas mass, but that 470 impact is expected to be small as there is not 471 much CO(2-1) emission between the AGN and 472 CND ring, and the CND ring itself does not ap-473 pear very disturbed along the path of the out-474 flow.

3. PRESCRIPTION PARAMETERS

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In this pilot study, we examine the performance of the most commonly used accretion prescription for black hole growth in NGC 1068. The Bondi accretion formalism with a relative velocity of zero (also known as Bondi-Hoyle, or Bondi-Hoyle-Lyttleton e.g. Hoyle & Lyttleton Bondi 1939; Bondi & Hoyle 1944; Bondi 1952) follows the form:

$$\dot{M}_{Bondi} = 4\pi G^2 M_{BH}^2 \rho c_s^{-3} \tag{2}$$

where G is the gravitational constant, M_{BH} is the mass of the black hole, ρ is the gas density and c_s is the sound speed.

Bondi accretion is predicated on a spherically symmetric, non-self-gravitating gas distribution in which the gas inside the Bondi radius has no angular momentum. While this kind of environment may not be most appropriate for describing all galaxy nuclei (see Section 5 for additional information), Bondi accretion is a simple analytical prescription that can be applied inside a sphere of any radius, which makes it convenient as a sub-grid prescription.

In this subsection, we outline the methods for measuring each free parameter in the Bondi prescription using the available high resolution that a from Section 2. 502

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Greenhill et al. (1996) imaged NGC 1068's wa-503 ter maser emission at a 0.65 pc scale using very 505 long baseline interferometry. From the rotation 506 curve of the water maser emission, they found 507 the enclosed mass within that radius to be $\sim 1 \times$ 508 $10^7 \,\mathrm{M_{\odot}}$ (with uncertainty on order unity). An-509 other study by Lodato & Bertin (2003) derive ₅₁₀ a smaller black hole mass of $\sim 8 \pm 0.3 \times 10^6$ 511 in a self-gravitating accretion disk model that 512 matches the Greenhill et al. (1996) and Green-513 hill & Gwinn (1997) observations well. 514 Lodato & Bertin (2003) model corrects for non-515 Keplerian motion in the velocity profile of the 516 water maser emission, but this could be an over-517 correction. In fact, other studies have found 518 that the disk rotation may still be dominated 519 by the black hole (Imanishi et al. 2018). Al-520 beit with a worse fit to the velocities from the 521 maser emission, Lodato & Bertin (2003) also fit 522 a Keplerian rotation model, which has a best fit ₅₂₃ black hole mass of $\sim 1.5 \pm 0.02 \times 10^7 \,\mathrm{M}_{\odot}$. In the 524 absence of clear evidence in favor of one of the 525 newer modeling schemes, we adopt the Green-₅₂₆ hill et al. (1996) value of $M_{\rm BH} = \sim 1 \times 10^7 \ {\rm M}_{\odot}$ 527 as an intermediate M_{BH} measurement.

3.2. Parameter 2: gas density 3.2.1. Choice of volume element

To measure the gas density, we first must de-531 fine our volume element. In cosmological sim-532 ulations, typically, a fixed number gas particles 533 exist inside a spherical region with radius r cen-534 tered on the location of the SMBH. This vol-535 ume makes up the black hole kernel, in which 536 the accretion physics are prescribed. Although 537 studies like the ones discussed in Section 2.3 and 538 Vollmer et al. (2022) have shown that \sim 10 pc 539 cold gas distribution is more disk-like, we opt to 540 use a sphere of volume $V = \frac{4}{3}\pi r^3$ centered on the 541 AGN for which we vary the radius with the goal 542 of mimicking the accretion resolution elements 543 found in simulations that use Bondi accretion.

To measure the molecular gas (H₂ and He) mass inside the sphere, we use the CO(2-1) data 547 described in Section 2.2. To obtain a molecular 548 gas mass, we utilize the conversion factor $\alpha_{\rm CO}$. The exact value of $\alpha_{\rm CO}$ depends on several fac-550 tors including the size scale and environment 551 over which the CO flux is measured. The pic-552 ture is further complicated by the distinction between $\alpha_{\text{CO}(1-0)}$ and $\alpha_{\text{CO}(2-1)}$, where the dif-554 ference is dictated by the ratio between the line $_{555}$ luminosity of the two rotational transitions: r_{21} $_{\text{556}}~(r_{21}=L'_{\mathrm{CO}(2-1)}/L'_{\mathrm{CO}(1-0)}),$ which depends on the 557 temperature of the gas. In this work, we follow 558 the same $\alpha_{\rm CO}$ methodology as in García-Burillo 559 et al. (2019) who use the Milky Way $\alpha_{\rm CO(1-0)} =$ $_{560} 4.3 \pm 1.29 \text{ M}_{\odot} (\text{K km s}^{-1} \text{pc}^2)^{-1} \text{ recommended}$ ₅₆₁ by Bolatto et al. (2013). We use $\alpha_{\text{CO}(1-0)}$ in 562 conjunction with the averaged line intensity 563 ratios for NGC 1068's northern and southern 564 CND regions (because the CND ring contains the majority of the nuclear gas mass): $r_{21} = 2.2$ $_{566} \pm 0.4$, from Viti et al. (2014) to calculate a final

$$\alpha_{\text{CO(2-1)}} = \frac{\alpha_{\text{CO(1-0)}}}{r_{21}} = \frac{4.3 \pm 1.29}{2.2 \pm 0.4}$$

$$= 1.95 \pm 0.73 \ M_{\odot} (\text{K km s}^{-1} \text{ pc}^2)^{-1}. \quad (3)$$

569 The outflowing components of NGC 1068 may 570 have a lower $\alpha_{\text{CO}(1-0)}$, but we expect the Milky 571 Way value to be closer to the average for 572 the purpose of measuring integrated enclosed masses, especially at larger r. $\alpha_{\rm CO(2-1)}$ is then 574 multiplied by the sum of the flux density in-575 side a circular aperture of radius r, to match 576 our spherical geometry. The enclosed mass pro-577 file is shown alongside a snapshot of the aper-578 ture geometry in Figure 2. García-Burillo et al. $_{579}$ (2019), who center their r = 200 pc aperture 580 measurement on the center of the CND ring, find a molecular (H₂ + helium) gas mass of ≈ 1.4 $_{582} \times 10^8 \mathrm{~M}_{\odot}$. We measure molecular gas mass 583 within the same aperture (using CARTA to mea-₅₈₄ sure flux) and find $1.3 \pm 0.5 \times 10^8 \ \mathrm{M}_{\odot}$ (1.4

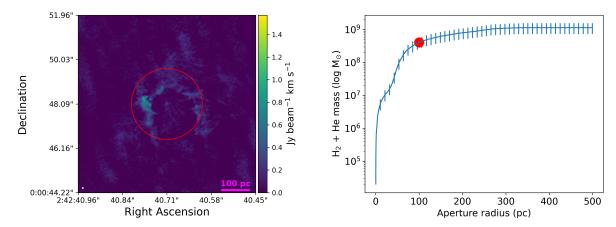


Figure 2. Left: Moment 0 map of CO(2-1) in NGC 1068, with flux density values masked below $3\times rms$. The red circle indicates the location and size of the 100 pc aperture (centered on the AGN) corresponding to the red dot in the right panel, which has $M_{enc,H_2+He} = 4.09 \pm 1.49 \times 10^8 M_{\odot}$. The small, white ellipse in the bottom left represents the beam size of the ALMA data (41×30 mas). Right: Integrated mass profile inside the radial aperture. Details on the conversion to molecular gas mass can be found in Section 3.2.

 $_{585}$ ± 0.5 × 10 8 M $_{\odot}$ if centered on the AGN), both $_{586}$ of which are consistent with the García-Burillo $_{587}$ et al. (2019) measurement. For comparison to $_{588}$ another nearby Seyfert 2, in the nuclear region $_{589}$ of Circinus, using the warm H₂ gas tracer H2 $_{590}$ 1-0 S(1), Müller Sánchez et al. (2006) find the $_{591}$ total molecular gas mass to be 1.7×10^{7} M $_{\odot}$ within 0.8" (52pc). Integrated inside the same $_{592}$ within 0.8" (52pc). Integrated inside the same $_{593}$ physical distance from the SMBH in NGC 1068, $_{594}$ we find a molecular gas mass of $_{8.8}$ ± $_{3.2}$ × $_{107}$ $_{595}$ M $_{\odot}$, higher by almost 1 dex.

To convert enclosed mass to density we divide by the volume element for a sphere (see Section 3.2.1) with r defined by our circular aperture size used for measuring mass. In this sphere with $r=100~\rm pc$ centered on the AGN as shown in Figure 2 (left), we find a molecular gas mass density of $93.3~\pm~71.1~\rm M_{\odot}pc^{-3}$.

3.2.3. Warm H_2 gas mass

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We also calculate an enclosed mass using the warm H_2 gas measured from the NIR data, following Equation 6 of Storchi-Bergmann et al. (2009), which uses the line flux of the H_2 1-0 so S(1) rovibrational transition at $\lambda_{\rm rest}=2.1218$ measured. In NGC 1068, Martins et al. (2010) used the NASA 3-m Infrared Telescope Facil-

 $_{611}$ ity (IRTF) and found a nuclear (slit 1"x 2") $_{612}$ extinction E(B-V) of 1.13 (from their Table $_{613}$ 4). Assuming the standard extinction law of $_{614}$ Cardelli et al. (1989) with $R_v = 3.1$, the extinc- $_{615}$ tion A_v ($A_v = R_v \times E(B-V)$) is ~ 3.5 . Based $_{616}$ on $A_k \sim A_v/10$ (Howarth 1983), the extinction- $_{617}$ corrected H_2 gas mass inside r < 1.7" (111 pc) $_{618}$ is $\sim 68 M_{\odot}$, which is about 1.38 times the observed value. The warm H_2 mass is inconsequential compared to the CO-derived value of $_{621}$ 4.08 \pm 1.49×10 8 M_{\odot} in the same region.

One reason that the warm gas measurement in this subsection may be so small is due to the radiative environment in NGC 1068's nucleus. Under local thermal equilibrium (LTE, where the energy distribution can be described by a single number locally) conditions, the H_2 emission can be excited by the equilibrium value for temperatures $T \approx 1000$ K (Davies et al. 2005). To reach such high excitation temperatures in NGC 1068, H_2 emission lines can be excited through several mechanisms, as described besize low:

 634 (1) *UV fluorescence*: This excitation mech- 635 anism dominates in photodissociation regions 636 (PDRs). Far-ultraviolet (FUV, $\lambda > 912$ Å) radi- 637 ation pumps the molecule into electronically ex-

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638 cited states, leading to subsequent cascades that
639 emit fluorescent emission (Wakelam et al. 2017).
640 This mechanism is dominant in Seyfert 1 galax641 ies (Davies et al. 2005). Although NGC 1068 is
642 classified as a Seyfert 2 galaxy and is expected
643 to have less FUV radiation, the HST/FOC UV
644 image shows a bright nucleus with polarization
645 (Barnouin et al. 2023) within our OSIRIS field
646 of view (FOV).

(2) Shocks and outflows: Veilleux et al. (1997) suggest that shocks associated with nuclear outflows are a likely heating source for H₂ in many Seyfert 2 galaxies. May & Steiner (2017) and alyzed VLT/SINFONI and Gemini/NIFS data with a larger FOV covering the entire CND and proposed that the CND could be an expanding bubble.

(3) X-ray heating from the AGN: X-ray emis-656 sion can penetrate deeply into regions that are 657 opaque to UV photons and influence H₂ excita-658 tion (Matt et al. 1997). All of these mechanisms 659 can contribute to H₂ emission.

We measure the H_2 1-0 S(1) extinction-661 corrected intrinsic flux ($F_{\rm intrinsic} = F_{\rm observed} \times$ 662 $10^{(0.4A_k)}$) and directly convert it to the warm 663 H_2 gas mass. Due to the rectangular FOV, only 664 an aperture radius of <0.3" is fully contained 665 within the OSIRIS FOV, suggesting that H_2 666 emission at radii >0.3" is incomplete.

3.3. Parameter 3: sound speed of the gas

The final parameter required in the Bondi accretion formalism is the sound speed of the gas.
The sound speed for an ideal gas is:

$$c_s = \sqrt{\frac{\gamma R T_K}{M}} \tag{4}$$

where γ is the adiabatic index (1, as the gas is assumed to be isothermal in each sub-region), R is the gas constant 8.3144598 J mol⁻¹ K⁻¹, T_K is the temperature of the gas (K), and M is the molar mass (kg) of the gas, for which we assume solar metallicity. All but the temperature in this case are constants.

For the temperature of the molecular gas, we $_{680}$ use two methods: one using CO rotation dia- $_{681}$ grams (cold gas), and another using an excita- $_{682}$ tion diagram for the molecular $_{2}$ (warm gas) $_{683}$ from our Keck/OSIRIS+AO NIR data.

3.3.1. CO-derived $c_{\rm s}$

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For a temperature from CO transitions we re-686 fer to the work of Viti et al. (2014) who infer the 687 temperature of the gas in the CND of NGC 1068 688 by using CO rotation diagrams. This method 689 assumes that the gas is in LTE, and that the 690 observations are mostly in the Rayleigh-Jeans 691 regime where the intensity of the radiation is 692 proportional to the temperature. This temper-693 ature is also known as the 'rotational temper-694 ature' and is equal to the kinetic temperature 695 if all CO levels are thermalized (Goldsmith & 696 Langer 1999). Because of these assumptions, 697 this temperature should be considered a lower 698 limit, which translates to an upper limit on our final accretion rate because $\dot{\rm M}_{\rm Bondi} \propto c_{\rm s}^{-3}$. 700 For the central region of NGC 1068, Viti et al. $_{701}$ (2014) find a temperature of 50 \pm 5-7 K via the 702 CO rotation diagram method (see Section 3.1.1. 703 of their work for more details). Plugging that 704 and the other constants into Equation 4, we find 705 that the speed of sound in the cold molecular 706 gas phase is $409.2 \pm 141.7 \text{ km s}^{-1}$.

3.3.2. H_2 -derived c_s

As shown in Section 3.2.3, warm H_2 is also present in NGC 1068's nuclear regions, so we also consider the sound speed for this component of the ISM. To measure the temperature which we then use in the c_s calculation, we use the H_2 1-0 S(0), S(1), and S(2) rovibrational line fluxes in the Keck/OSIRIS NIR data described in Section 2.1. Assuming the H_2 gas is in LTE, the H_2 excitation temperature is equal to the kinetic temperature. Figure 3(a) shows the H_2 excitation diagram, which is the column density in the upper level of each transition normalized by its statistical weight (N_u/g_u) as a function of

721 energy of the level as a temperature (E_u) . The 722 best-fit slope of this relationship is related to 723 T_K as $\frac{N_u}{g_u} \propto e^{(-\frac{h\nu}{kT_K})}$ in the LTE description of 724 energy level populations (see pages 322, 327 of 725 Wilson et al. 2013). Solving for T_K then yields 726 $-\frac{1}{T_K} \propto \frac{\ln \frac{N_u}{g_u}}{\frac{E_u}{k}}$.

Because we have spatially resolved data for $_{128}$ these H_2 lines, we can derive kinetic temper-729 atures from 12-111 pc and apply them at the 730 matched distances in the accretion rate predic-731 tion. While the Keck/OSIRIS+AO data has a $_{732}$ higher resolution than 6 pc, the H_2 1-0 S(1)733 and S(2) lines are not detected in a r \leq 6 pc $_{734}$ (0.1") aperture. Fluxes of the lines are mea-735 sured using the line fitting tool in QFitsView 736 (Ott 2012), which we use to fit the continuum 737 and one Gaussian component to the integrated 738 (within a region circular region with radius r) 739 spectrum. Figure 3(b) shows the range of ex-740 citation temperatures as a function of radius. $T_{\rm K}$ ranges from 678-2261 K, and peaks at r \leq 85 742 pc where $T_{\rm K} = 2261 \, ^{+3683}_{-1631} \, {\rm K}.$ High temperatures may be caused by the influence of the PDR (Sec-744 tion 3.2.2 describes observations of this for NGC 745 1068), which is found to increase the H_2 1-0 S(1)746 emission by up to 70% in the some luminous in-747 frared galaxies (Davies et al. 2000; Davies et al. 748 2003). Using Equation 4 (with a molar mass of 749 H₂) results in H₂ sound speeds between 1013- $_{750}$ 1850 km s⁻¹, peaking at r = 85 pc.

RESULTS: M _{Bondi}VS. M _{X-RAY} Calculating M _{Bondi}

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Now that we have calculated each paramer54 ter for the Bondi accretion prescription in Secr55 tion 3, we are ready to estimate a Bondi accrer56 tion rate. Because our parameters are spatially r57 resolved, we calculate accretion rate as a funcr58 tion of simulated resolution:

$$\dot{M}_{Bondi}(r) = 4\pi G^2 M_{BH}^2 \rho (\leq r) c_s (\leq r)^{-3}.$$
 (5)

760 Figure 4 shows the Bondi accretion rate for the 761 cold derived case as a function of radius, the

means of which range between about 10^2 and 10^{-3} ${\rm M}_{\odot}$ yr⁻¹. As the enclosed mass found in 764 Section 3.2 for the warm ${\rm H}_2$ gas component in 765 r< 170 pc is small (68 ${\rm M}_{\odot}$), and the temperature 766 gradient is high (678-2261 K, see Section 3.3.2) 767 relative to the values found for the cold CO 768 gas component, the resulting Bondi accretion 769 rates are much smaller (between about 10^{-10} 770 and 10^{-7} ${\rm M}_{\odot}$ yr⁻¹) for the warm gas. These re-771 sults suggest that the cold gas is the dominant 772 carrier of mass accretion on r< 170 pc scales. 773 Table 1 shows a range of precise values for both 774 the cold and hot Bondi accretion rates.

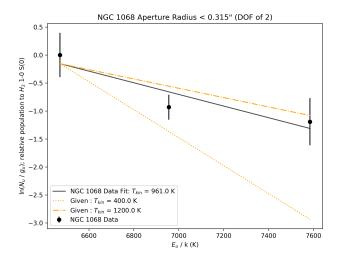
4.2. Calculating X-ray accretion rates

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To understand how well the Bondi accretion rate, formalism compares to the real accretion rate, we compare it to the X-ray derived accretion rate. To calculate an accretion rate from X-ray measurements, we use *Swift/BAT* data from the BAT AGN Spectroscopic Survey (BASS, Ricci et al. 2017). They present intrinsic luminosities in the 14-195 keV band, which we use alongside the bolometric correction, Equation 17 in Gupta et al. (2024):

$$\log(\kappa_{14-195}) = (0.13 \pm 0.04) \times \log(\lambda_{\rm Edd}) + (1.04 \pm 0.05) \quad (6)$$

to calculate bolometric luminosity. Because Ricci et al. (2017) measure a neutral column density of $\log N_{\rm H} = 25.0~{\rm cm^{-2}}$ in NGC 1068 and the X-ray continuum might not be well estimated when the emission is dominated by reprocessed radiation in environments like this, we conservatively estimate uncertainty on the input intrinsic 14-195 keV luminosity to be \pm 0.4 dex. We then use that bolometric luminosity in the equation from Netzer & Trakhten-top 100 mostly in the equation from Netzer & Trakhten-top 100 mostly in the equation conversion efficiency unitless mass-to-radiation conversion efficiency that depends on the spin of the black hole. For stationary, retrograde disk, and maximally rotating SMBHs respectively, the values for η are



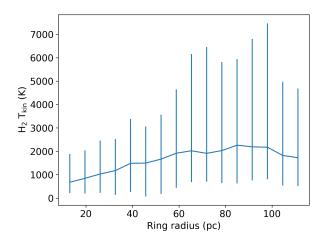


Figure 3. (Left:) Column density in the upper level of each H_2 1-0 S(0), S(1), and S(2) transition as a function of energy level of that transition as a temperature (K) inside a r=21 pc circular aperture centered on the AGN as shown in Figure 1. The best fit slope (using linear regression), as described in Section 3.3.2, is the temperature of the gas in that region if we assume LTE. (Right:) T_K estimated as in the excitation diagram on the left but instead inside circular apertures matching the methods of Section 3.2 from 0.2" to 1.7" in steps of 0.1". The mean of the derived temperatures is 1612^{+2840}_{-1216} K.

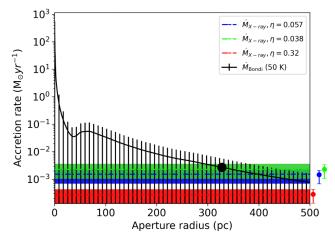


Figure 4. X-ray and (Cold-derived) Bondi accretion rates as a function of radius over which nuclear parameters are measured. Color bars and ranges displayed to the right denote uncertainties on each X-ray measurement. The Bondi prescription overestimates \dot{M}_{BH} by orders of magnitude for low aperture radii, but, above 327 pc (the black circle), the mean Bondi prescription value begins to agree and even dip below the mean minimum prediction from the X-ray by aperture size r=398 pc.

 $_{803}$ 0.057, 0.038, and 0.32 (Netzer & Trakhtenbrot $_{804}$ 2014). For NGC 1068, we find $\dot{M}_{\rm X-ray}$ values

sos equal to $1.51 \pm 0.81 \times 10^{-3} \ \rm{M_{\odot}yr^{-1}}$ (station-sos ary SMBH), $2.26 \pm 1.21 \times 10^{-3} \ \rm{M_{\odot}yr^{-1}}$ (retrosor grade accretion disk), and $2.69 \pm 1.43 \times 10^{-3}$ sos $\rm{M_{\odot}yr^{-1}}$ (maximally spinning SMBH). Figure 4 sos and shown in Table 1. $\rm{\dot{M}_{Bondi}}$ overestimates the accretion rate by several orders of magnitude at small distances from the SMBH where the gas density is high, but dips below the X-ray accresis tion rates at large distances, where density is side low.

Vollmer et al. (2022) used the IR-derived bolometric luminosity for the AGN in NGC 1068 from Vollmer et al. (2018) to calculate $\dot{\rm M}_{\rm BH}\sim$ L_{bol}/(0.1c²) \sim 0.05 M_{\odot}yr⁻¹. They calculate a mass accretion rate onto their modeled accretion disk for NGC 1068 to be 2 \times 10⁻³ M_{\odot}yr⁻¹ to in disk for NGC 1068 to be 2 \times 10⁻³ M_{\odot}yr⁻¹ kgl (η = 0.1), which is in agreement with our disk disk disk and the cold gas derived $\dot{\rm M}_{\rm Bondi}$ in aperture sizes of r \geq 363 pc.

5. DISCUSSION: RESULTS IN CONTEXT OF SIMULATIONS

To inform theorists on which accretion preszr scriptions in their simulations are best to use

Method				Accretion rate	$({\rm M}_{\odot}~{\rm yr}^{-1})$		
X-rays (ϵ = 0.57)				1.51 ± 0.81	$\times 10^{-3}$		
X-rays (ϵ = 0.38)				2.26 ± 1.21	$\times 10^{-3}$		
X-rays (ϵ = 0.32)				2.69 ± 1.43	$\times 10^{-3}$		
Bondi (<r)< td=""><td>5 pc</td><td>10 pc</td><td>25 pc</td><td>50 pc</td><td>100 pc</td><td>200 pc</td><td>500 pc</td></r)<>	5 pc	10 pc	25 pc	50 pc	100 pc	200 pc	500 pc
$(T_{Kin} = 50 \text{ K})$	$1.62 \pm$	$0.43~\pm$	$0.06~\pm$	$0.05~\pm$	$0.03~\pm$	$8.32~\pm$	$7.63~\pm$
	1.79	0.47	0.07	0.05	0.04	9.16×10^{-4}	8.41×10^{-4}
$(T_{Kin} = 678-2261 \text{ K})$	*	*	$8.16 {}^{+28.89}_{-21.6}$	$4.95 {}^{+15.87}_{-14.03}$	$5.04 {}^{+23.61}_{-11.20}$	*	*
			$\times 10^{-9}$	$\times 10^{-10}$	$\times 10^{-11}$		

Table 1. Accretion rate measurements and estimates for rates derived from X-ray luminosities and the pure Bondi accretion prescription inside various radii. In NGC 1068, where the cold gas phase makes up the bulk of the gas mass in the nucleus, the cold gas derived Bondi accretion estimate outpaces the X-ray derived accretion rates by between 2 and 4 orders of magnitude. *H₂ 1-0 S(1) and S(2) lines required to calculate temperature for the Bondi calculation are not detected in this aperture.

and when, we have designed our measurements 829 to fit in the practical context of those simu-830 lations. Large scale cosmological simulations 831 must use sub-grid physics for accretion because 832 of computing constraints. Some examples of hy-833 drodynamical galaxy evolution simulations that 834 use or have popular options to use a spheri-835 cally symmetric, Bondi or Bondi-like black hole 836 accretion formalisms are Illustris/IllustrisTNG (Genel et al. 2014; Vogelsberger et al. 2014; 838 Pillepich et al. 2018b), Magneticum Pathfinder (Hirschmann et al. 2014; Bocquet et al. 2016; 840 Dolag et al. 2016), MassiveBlack-II (Khandai 841 et al. 2015), *Eagle* (Schaye et al. 2015), *Horizon-*842 AGN (Dubois et al. 2016), Romulus (Tremmel 843 et al. 2017), and SIMBA (Davé et al. 2019b, 844 uses Bondi for hot gas only). The resolution of 845 the hydrodynamical gas cells in which these sub-846 grid physics are calculated ranges from to 10s of 847 pc to more typically kpc. Even in the highest 848 resolution zoom-in simulations, the spherical ra-849 dius in which particle calculations are made is approximately 10 pc (Wetzel et al. 2023).

Because we have spatially-resolved measurements, we are able to examine the performance bis of Bondi accretion at a range of spatial scales. For the Bondi accretion rate derived from warm sis gas we are limited by the field of view of OSIRIS $_{856}$ (0.56×2.24" with our observational setup), but $_{857}$ the ALMA data extends to over 500 pc away $_{858}$ from the SMBH.

Table 1 shows the Bondi accretion rates at radii between 5-500 pc as calculated in Secsit tion 4, and the X-ray accretion rates as calcusted in Section 4.2, which are all plotted together in Figure 4. At aperture radii $r \le 327$ pc, the parameterized Bondi accretion rate exceeds the X-ray derived accretion rate (by 2 or more dex in aperture sizes of $r \le 15$ pc and by 1 or more dex when $r \le 125$ pc).

This is, perhaps, not a surprising result. Past 869 studies have hinted towards Bondi accretion 870 overestimating the real accretion rate. Di Mat-871 teo et al. (2000) found that luminosities calcu-872 lated using estimated Bondi accretion rates for $_{873}$ six black holes with masses of 0.22-5.2 imes 10^9 $_{874}$ M_{\odot} determined in Magorrian et al. (1998) were 875 4-6 orders of magnitude higher than the real lu-876 minosities of the galaxy nuclei. Hopkins et al. 877 (2016) model SMBH accretion in a gas-rich nu-878 clear disk in a massive simulated galaxy with 0.1 879 pc resolution. In their study, applying a pure 880 Bondi accretion formalism resulted in an accre- $_{881}$ tion rate $\sim 10^8$ times higher than the luminosity-882 derived accretion rate native to their simulation. 883 Near the SMBH, pure Bondi accretion ignores 884 the possibility that gas particles may have angu-885 lar momentum. The gas in the simulation used 886 in Hopkins et al. (2016) is primarily cold and is 887 supported by angular momentum rather than 888 radiation pressure. Observations show that es-889 pecially in gas-rich galaxies that naturally host 890 molecular torii, the r<100 pc cold gas reservoir 891 is large, has significant angular momentum, and 892 is the primary candidate for black hole accretion sys fueling (Davies et al. 2004; Hicks et al. 2013; Medling et al. 2014; Lin et al. 2016; Gaspari 895 et al. 2015). Ignoring the angular momentum 896 of the cold gas is likely the primary cause of the 897 overestimate that Bondi accretion makes both 898 in Hopkins et al. (2016) the aperture sizes of 899 r \leq 327 pc in this work.

The performance of Bondi accretion between 200-500 pc is more realistic, and it even dips below the X-ray derived accretion rates for very large (r≥398) apertures. This is because, as is apparent in Figure 2, the cold gas has much lower average densities at large distances from the SMBH.

If NGC 1068 is typical, these results suggest 908 that the usage of pure Bondi accretion is likely 909 to struggle to accurately predict black hole ac-910 cretion rates. From our example, the accuracy 911 of Bondi predictions depends heavily on the size 912 of the black hole kernel used to calculate nu-913 clear conditions, overpredicting in the small ra-914 dius limit and underpredicting in the large ra-915 dius limit. Understanding the physical mecha-916 nisms that drive accretion on the sub-grid scales 917 in galactic nuclei can inform the future devel-918 opment of accretion prescriptions. The Bondi 919 prescription applies free-fall to particles inside 920 the Bondi radius, but our results suggest that 921 angular momentum plays an important role in 922 some nuclei.

6. CONCLUSIONS AND FUTURE EXPANSION OF THIS PROJECT

In this study we estimate a Bondi accretion rate as a function of radius for NGC 1068 using

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where the result to the direct accretion rate degrated from hard X-ray luminosity of the AGN. Compared to warm H₂ gas, CO gas is the dominant mass carrier close to the SMBH. Following ing this, the cold gas derived Bondi accretion that the the than 1 order of magnitude at aperture sizes r≤125 pc and up to 4 dex inside the smalligates apertures. In the case of warm gas Bondi accretion where the enclosed mass involved in the calculation is negligible, and in the cold gas case in aperture sizes of r≥327 pc, the Bondi accretion rate is instead lower than or equal to the X-ray accretion rates.

This paper is a pilot for a wider study of 943 AGN and accretion prescriptions. Direct probes 944 of sub-grid accretion prescriptions may, as our 945 sample expands, help identify which physical 946 processes dominate accretion on a variety of 947 spatial scales, and in turn provide recommenda-948 tions for appropriate sub-grid prescriptions to 949 describe them. The results in this work sup-950 port previous evidence that in high resolution 951 cosmological simulations, applying a Bondi ac-952 cretion prescription can lead to large overesti- $_{953}$ mates of $M_{\rm BH}$ and therefore large overestimates 954 of AGN feedback, which in turn impacts the 955 global galaxy evolutionary track. We note that 956 this is a test for a specific Seyfert 2 AGN. To 957 make more robust recommendations about the 958 application of the Bondi accretion prescription 959 for sub-grid accretion physics we must directly 960 test Bondi on more galaxies.

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¹⁰⁰⁴ Software: Astropy (Astropy Collaboration ¹⁰⁰⁵ et al. 2013, 2018, 2022), Matplotlib (Hunter ¹⁰⁰⁶ 2007), NumPy (Harris et al. 2020).

REFERENCES

1054

1055

1056

311, 507

Nature, 433, 604

1007 Anglés-Alcázar, D., Davé, R., Faucher-Giguère, C.-A., Özel, F., & Hopkins, P. F. 2017, 1008 MNRAS, 464, 2840 1009 1010 Antonucci, R. 1993, ARA&A, 31, 473 Astropy Collaboration et al. 2013, A&A, 558, A33 —. 2018, AJ, 156, 123 —. 2022, ApJ, 935, 167 1014 Barnouin, T., Marin, F., Lopez-Rodriguez, E., Huber, L., & Kishimoto, M. 2023, A&A, 678, A143 1016 1017 Barthelmy, S. D., et al. 2005, SSRv, 120, 143 1018 Behroozi, P. S., Wechsler, R. H., & Conroy, C. 2013, ApJ, 770, 57 1019 1020 Bocquet, S., Saro, A., Dolag, K., & Mohr, J. J. 2016, MNRAS, 456, 2361 1021 1022 Bolatto, A. D., Wolfire, M., & Leroy, A. K. 2013, ARA&A, 51, 207 1024 Bondi, H. 1952, MNRAS, 112, 195 1025 Bondi, H., & Hoyle, F. 1944, MNRAS, 104, 273 Booth, C. M., & Schaye, J. 2009, MNRAS, 398, 53 1027 Briggs, D. S. 1995, in American Astronomical

Society Meeting Abstracts, Vol. 187, American

1030 Burns, J. O., Feigelson, E. D., & Schreier, E. J.

1983, ApJ, 273, 128

Astronomical Society Meeting Abstracts, 112.02

1028

1029

1031

1032 Cardelli, J. A., Clayton, G. C., & Mathis, J. S. 1989, ApJ, 345, 245 Cielo, S., Bieri, R., Volonteri, M., Wagner, A. Y., 1034 & Dubois, Y. 2018, MNRAS, 477, 1336 1035 Comrie, A., et al. 2021, CARTA: The Cube Analysis and Rendering Tool for Astronomy 1037 Curtis, H. D. 1918, Publications of Lick Observatory, 13, 9 1039 1040 Davé, R., Anglés-Alcázar, D., Narayanan, D., Li, Q., Rafieferantsoa, M. H., & Appleby, S. 2019a, MNRAS, 486, 2827 -. 2019b, MNRAS, 486, 2827 1043 1044 Davies, R., Ward, M., & Sugai, H. 2000, ApJ, 535, 735 1045 Davies, R. I., Sternberg, A., Lehnert, M., & 1046 Tacconi-Garman, L. E. 2003, ApJ, 597, 907 1048 Davies, R. I., Sternberg, A., Lehnert, M. D., & Tacconi-Garman, L. E. 2005, ApJ, 633, 105 1049 Davies, R. I., Tacconi, L. J., & Genzel, R. 2004, 1050 ApJ, 613, 781 1051 1052 Di Matteo, T., Quataert, E., Allen, S. W., Narayan, R., & Fabian, A. C. 2000, MNRAS, 1053

Di Matteo, T., Springel, V., & Hernquist, L. 2005,

- 1057 Dolag, K., Komatsu, E., & Sunvaev, R. 2016,
- MNRAS, 463, 1797 1058
- 1059 Dubois, Y., Gavazzi, R., Peirani, S., & Silk, J.
- 2013a, MNRAS, 433, 3297 1060
- Dubois, Y., Peirani, S., Pichon, C., Devriendt, J., 1061
- Gavazzi, R., Welker, C., & Volonteri, M. 2016, 1062
- MNRAS, 463, 3948 1063
- 1064 Dubois, Y., Pichon, C., Devriendt, J., Silk, J.,
- Haehnelt, M., Kimm, T., & Slyz, A. 2013b, 1065
- MNRAS, 428, 2885 1066
- 1067 Fabian, A. C. 2012, ARA&A, 50, 455
- Ferrarese, L., & Merritt, D. 2000, ApJL, 539, L9
- Feruglio, C., Maiolino, R., Piconcelli, E., Menci, 1069
- N., Aussel, H., Lamastra, A., & Fiore, F. 2010, 1070
- A&A, 518, L155 1071
- 1072 Gallimore, J. F., Baum, S. A., O'Dea, C. P., &
- Pedlar, A. 1996, ApJ, 458, 136 1073
- Gallimore, J. F., & Impellizzeri, C. M. V. 2023. 1074
- ApJ, 951, 109 1075
- 1076 Gallimore, J. F., et al. 2016, ApJL, 829, L7
- Gámez Rosas, V., et al. 2022, Nature, 602, 403
- García-Burillo, S., et al. 2014, A&A, 567, A125
- —. 2019, A&A, 632, A61
- 1080 Gaspari, M., Brighenti, F., & Temi, P. 2015,
- A&A, 579, A62 1081
- Gebhardt, K., et al. 2000, ApJL, 539, L13 1082
- Gehrels, N., et al. 2004, ApJ, 611, 1005
- Genel, S., et al. 2014, MNRAS, 445, 175
- Goldsmith, P. F., & Langer, W. D. 1999, ApJ, 1085
- 1086
- Greenhill, L. J., & Gwinn, C. R. 1997, Ap&SS, 1087 248, 261
- 1088 1089 Greenhill, L. J., Gwinn, C. R., Antonucci, R., &
- Barvainis, R. 1996, ApJL, 472, L21 1090
- Gupta, K. K., et al. 2024, A&A, 691, A203 1091
- 1092 Hagiwara, Y., Baan, W. A., Imanishi, M., &
- Diamond, P. 2024, MNRAS, 528, 3668
- 1094 Harris, C. R., et al. 2020, Nature, 585, 357
- 1095 Hicks, E. K. S., Davies, R. I., Maciejewski, W.,
- Emsellem, E., Malkan, M. A., Dumas, G., 1096
- Müller-Sánchez, F., & Rivers, A. 2013, ApJ, 1097
- 768, 107 1098
- 1099 Hinshaw, G., et al. 2009, ApJS, 180, 225
- 1100 Hirschmann, M., Dolag, K., Saro, A., Bachmann,
- L., Borgani, S., & Burkert, A. 2014, MNRAS, 1101
- 442, 2304 1102
- 1103 Hobbs, A., Power, C., Nayakshin, S., & King,
- A. R. 2012, MNRAS, 421, 3443 1104
- 1105 Holden, L. R., & Tadhunter, C. N. 2023, MNRAS,
- 524, 886

- Hopkins, P. F., & Quataert, E. 2011, MNRAS,
- 415, 1027 1108
- 1109 Hopkins, P. F., Torrey, P., Faucher-Giguère,
- C.-A., Quataert, E., & Murray, N. 2016,
- MNRAS, 458, 816
- 1112 Howarth, I. D. 1983, MNRAS, 203, 301
- 1113 Hoyle, F., & Lyttleton, R. A. 1939, Proceedings of
- the Cambridge Philosophical Society, 35, 405
- 1115 Hunter, J. D. 2007, Computing in Science &
- Engineering, 9, 90 1116
- 1117 Hviding, R. E., Hickox, R. C., Väisänen, P.,
- Ramphul, R., & Hainline, K. N. 2023, AJ, 166, 1118
- 1119
- 1120 Imanishi, M., Nakanishi, K., Izumi, T., & Wada,
- K. 2018, ApJL, 853, L25
- 1122 Imanishi, M., et al. 2020, ApJ, 902, 99
- 1123 Jaffe, W., et al. 2004, Nature, 429, 47
- 1124 Khandai, N., Di Matteo, T., Croft, R., Wilkins,
- S., Feng, Y., Tucker, E., DeGraf, C., & Liu,
- M.-S. 2015, MNRAS, 450, 1349
- 1127 Kormendy, J., & Ho, L. C. 2013, ARA&A, 51, 511
- 1128 Krimm, H. A., et al. 2013, ApJS, 209, 14
- 1129 Kumar, P. 1999, ApJ, 519, 599
- Larkin, J., et al. 2006, in Society of Photo-Optical
- Instrumentation Engineers (SPIE) Conference
- Series, Vol. 6269, Ground-based and Airborne 1132
- Instrumentation for Astronomy, ed. I. S. 1133
- McLean & M. Iye, 62691A
- 1135 Lin, M.-Y., et al. 2016, MNRAS, 458, 1375
- 1136 Lockhart, K. E., et al. 2019, AJ, 157, 75
- 1137 Lodato, G., & Bertin, G. 2003, A&A, 398, 517
- 1138 Lyke, J., et al. 2017, OSIRIS Toolbox:
- OH-Suppressing InfraRed Imaging 1139
- Spectrograph pipeline, Astrophysics Source 1140
- Code Library, record ascl:1710.021
- 1142 Magorrian, J., et al. 1998, AJ, 115, 2285
- 1143 Markevitch, M. 1998, ApJ, 504, 27
- 1144 Martins, L. P., Rodríguez-Ardila, A., de Souza,
- R., & Gruenwald, R. 2010, MNRAS, 406, 2168
- 1146 Matt, G., et al. 1997, A&A, 325, L13
- 1147 May, D., & Steiner, J. E. 2017, MNRAS, 469, 994
- 1148 McConnell, N. J., & Ma, C.-P. 2013, ApJ, 764, 184
- 1149 Medling, A. M., et al. 2014, ApJ, 784, 70
- 1150 Meenakshi, M., et al. 2022, MNRAS, 516, 766
- ¹¹⁵¹ Morganti, R. 2017, Frontiers in Astronomy and
- Space Sciences, 4, 42
- 1153 Müller Sánchez, F., Davies, R. I., Eisenhauer, F.,
- Tacconi, L. J., Genzel, R., & Sternberg, A. 1154
- 2006, A&A, 454, 481 1155

- 1156 Müller-Sánchez, F., Prieto, M. A., Hicks, E. K. S.,
- Vives-Arias, H., Davies, R. I., Malkan, M.,
- ¹¹⁵⁸ Tacconi, L. J., & Genzel, R. 2011, ApJ, 739, 69
- Mushotzky, R. F. 1984, Physica Scripta Volume
 T, 7, 157
- 1161 Mutie, I. M., et al. 2024, MNRAS, 527, 11756
- 1162 Netzer, H., & Trakhtenbrot, B. 2014, MNRAS,
- 1163 438, 672
- 1164 Ott, T. 2012, QFitsView: FITS file viewer,
- 1165 Astrophysics Source Code Library, record
- ascl:1210.019
- 1167 Pillepich, A., et al. 2018a, MNRAS, 473, 4077
- ₁₁₆₈ 2018b, MNRAS, 473, 4077
- 1169 Raban, D., Jaffe, W., Röttgering, H.,
- 1170 Meisenheimer, K., & Tristram, K. R. W. 2009,
- 1171 MNRAS, 394, 1325
- 1172 Ricci, C., et al. 2017, ApJS, 233, 17
- 1173 Rosas-Guevara, Y. M., et al. 2015, MNRAS, 454,
- 1174 1038
- 1175 Saito, T., et al. 2022, ApJ, 935, 155
- 1176 Schaye, J., et al. 2015, MNRAS, 446, 521
- 1177 Springel, V., Di Matteo, T., & Hernquist, L. 2005,
- 1178 MNRAS, 361, 776
- 1179 Springel, V., & Hernquist, L. 2005, ApJL, 622, L9
- 1180 Storchi-Bergmann, T., McGregor, P. J., Riffel,
- 1181 R. A., Simões Lopes, R., Beck, T., & Dopita,
- 1182 M. 2009, MNRAS, 394, 1148
- 1183 Taylor, P., & Kobayashi, C. 2015, MNRAS, 448,
- 1184 1835
- 1185 Torrey, P., Vogelsberger, M., Genel, S., Sijacki,
- 1186 D., Springel, V., & Hernquist, L. 2014,
- 1187 MNRAS, 438, 1985
- 1188 Tremmel, M., Karcher, M., Governato, F.,
- Volonteri, M., Quinn, T. R., Pontzen, A.,
- Anderson, L., & Bellovary, J. 2017, MNRAS,
- 1191 470, 1121

- 1192 Tristram, K. R. W., Burtscher, L., Jaffe, W.,
- Meisenheimer, K., Hönig, S. F., Kishimoto, M.,
- Schartmann, M., & Weigelt, G. 2014, A&A,
- 1195 563, A82
- 1196 Valentini, M., et al. 2020, MNRAS, 491, 2779
- 1197 Veilleux, S., Goodrich, R. W., & Hill, G. J. 1997,
- 1198 ApJ, 477, 631
- 1199 Viti, S., et al. 2014, A&A, 570, A28
- 1200 Vogelsberger, M., Genel, S., Sijacki, D., Torrey,
- P., Springel, V., & Hernquist, L. 2013, MNRAS,
- 1202 436, 3031
- 1203 Vogelsberger, M., et al. 2014, MNRAS, 444, 1518
- 1204 Vollmer, B., Schartmann, M., Burtscher, L.,
- Marin, F., Hönig, S., Davies, R., & Goosmann,
- 1206 R. 2018, A&A, 615, A164
- 1207 Vollmer, B., et al. 2022, A&A, 665, A102
- 1208 Wada, K., Kudoh, Y., & Nagao, T. 2023,
- 1209 MNRAS, 526, 2717
- 1210 Wakelam, V., et al. 2017, Molecular Astrophysics,
- 1211 9, 1
- 1212 Weinberger, R., et al. 2017, MNRAS, 465, 3291
- 1213 Wetzel, A., et al. 2023, ApJS, 265, 44
- 1214 Williamson, D., Hönig, S., & Venanzi, M. 2020,
- 1215 ApJ, 897, 26
- 1216 Wilson, A. S., & Ulvestad, J. S. 1983, ApJ, 275, 8
- 1217 Wilson, T. L., Rohlfs, K., & Hüttemeister, S.
- 2013, Tools of Radio Astronomy
- 1219 Wright, E. L. 2006, PASP, 118, 1711