Direct Tests of Black Hole Accretion Rate Prescriptions: I. Bondi Accretion at Different Scales

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ABSTRACT

We present spatially resolved parsec-scale measurements of nuclear conditions (gas density and kinetic temperature) relevant for black hole accretion rate predictions in the Seyfert 2 galaxy, NGC 1068. We inject these parameters into the prescription for a Bondi-like accretion model, then compare the resulting accretion rate prediction to the empirical accretion rate derived from hard X-ray observations. Cosmological simulations have spatial resolution ranging between, from ~ 10 pc to on order kpc, and so for reasonable comparison we test these accretion rate predictions in pixel-sized radial steps out to 500 pc. Compared to warm H₂ gas, CO gas is the dominant mass carrier close to the SMBH. We find that the Bondi accretion rate (M_{Bondi}) of cold molecular gas alone (measured using CO) overestimates the true accretion rate by up to 4 dex in a small aperture ($r \lesssim 6$ pc) around the black hole, but that it performs much better on large ($r \ge 300$ pc) scales. These results are the first in a series of direct tests of accretion rate prescriptions, and they suggest that using a Bondi accretion formalism to model supermassive black hole accretion in Seyfert 2 galaxies may lead to overestimated accretion rates depending on the resolution of the simulation.

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⁴¹ of influence (1~100 pc), are thought to be a
⁴² key piece of the connection between pc and
⁴³ kpc scales of galaxy evolution. Observations of
⁴⁴ galaxies with active galactic nuclei (AGN) have
⁴⁵ shown both directly and indirectly that AGN
⁴⁶ can inject energy into their surrounding envi⁴⁷ ronments, which can ultimately quench or in
⁴⁸ some cases trigger star formation (see Fabian
⁴⁹ 2012 for a review).

Active galactic nuclei do not only interact 51 with the central part of galaxies, they may 52 also significantly impact several global prop-53 erties of galaxies and their surrounding inter-54 galactic media, allowing us to indirectly infer 55 their influence on those observables. Relation-56 ships between black hole mass and global galaxy 57 properties, like the velocity dispersion of stars 58 in the galactic bulge, have been well-calibrated 59 and show tight correlations (see Kormendy & 60 Ho 2013; McConnell & Ma 2013 for reviews). 61 These correlations suggest that AGN radiative 62 feedback, which in part depends on black hole 63 mass, may leave an imprint on bulge stellar ve-64 locity dispersion (see Ferrarese & Merritt 2000; 65 Gebhardt et al. 2000 for seminal studies). Star 66 formation in massive halos is suppressed (e.g. in 67 Behroozi et al. 2013; Torrey et al. 2014), which 68 could be caused by heating of the interstellar 69 medium (ISM) from AGN feedback. In the high 70 energy regime, a discrepancy is found between 71 the observed and expected correlations between 72 X-ray luminosities and temperatures of gas in 73 the intra-cluster medium (called the L_X -T re-74 lation, see Mushotzky 1984; Markevitch 1998). 75 This discrepancy suggests that gas in the intra-76 cluster medium evolves differently from dark 77 matter; energetics input by host AGN could be 78 a factor as to why.

Indirect cases of the impact of AGN feedback on galaxy formation histories are only made more intriguing by direct evidence of AGN feedback. Since more than 100 years ago (M87; Curstis 1918) radio jets powered by a central SMBH

have been seen to extend up to ~0.9 Mpc outside from their host galaxies (e.g. Centaurus A; Burns et al. 1983). Outflows driven by these SMBHs have been observed in the process of depleting the ISM at outflow rates of 700 M_☉ yr⁻¹ (e.g. in Mrk 231; Feruglio et al. 2010). Our pilot galaxy for this study, NGC 1068, has a complex and well studied AGN-driven outflow that also impacts the ISM on sub-kpc scales (e.g. Wilson & Ulvestad 1983; Müller-Sánchez et al. 2011; García-Burillo et al. 2014; Saito et al. 2022; Hviding et al. 2023; Holden & Tadhunter 2023; Gallimore & Impellizzeri 2023; Mutie et al. 2024; Hagiwara et al. 2024).

The energy output of an AGN is driven by 99 mass accretion onto its accretion disk, fueled 100 by inflows in the nuclei of galaxies. This gas then accelerates to speeds of up to > 0.1c in 102 the accretion disk, and that disk can power ra-103 diative outflows. The direct observational feed-104 back can be classified as two mechanisms: radia-105 tive (quasar mode) or kinematic (radio mode) 106 (Fabian 2012). In the quasar mode, occurring when the black hole accretes mass quickly, photons from the accretion disk couple to the ISM, 109 transferring momentum in a powerful jet. In ra-110 dio mode, accretion onto the disk is slower, and 111 the primary feedback mechanism is in the form 112 of collimated radio jets that typically appear 113 narrower than quasar-mode jets (see Cielo et al. 114 2018 for a simulated comparison between the 115 feedback of the two modes). Both modes can 116 drive outflows, but the guasar-mode is thought 117 to start the quenching process (the spatial ex-118 tent of which grows over time) and then the 119 radio-mode maintains that quenched state (see 120 Fabian 2012 and Morganti 2017 for reviews).

As simulations of galaxy evolution have been informed by increasingly detailed observations, theorists have begun to study the physical mechanisms that drive AGN feedback and how that feedback impacts the simulated host galaxies. Dubois et al. (2013a) (see also Dubois et al.

127 2013b; Taylor & Kobayashi 2015) examined how 128 AGN jets impact cold gas and transform blue, 129 disky galaxies into red ellipticals. Building on 130 these studies, Rosas-Guevara et al. (2015), who 131 simulated accretion in galaxies of varied halo 132 mass, find that in galaxies with $M_{\rm Halo}$ above 133 $10^{11.5}~{\rm M}_{\odot}$, as was observed in Behroozi et al. 134 (2013), star formation is suppressed by AGN 135 feedback. Valentini et al. (2020) perform a suite 136 of cosmological simulations in which they couple 137 AGN feedback to different phases of the ISM. 138 They find, in part, that energy output from the 139 AGN as feedback must couple with both the 140 cold and hot phases in order to avoid excessive 141 SMBH growth.

As is seen in both observations and simula-143 tions, global galaxy properties can be affected 144 by accretion-dependent feedback. Theorists 145 have attempted to model the physical processes 146 causing those properties to change. Williamson 147 et al. (2020) perform radiation hydrodynamics 148 modeling of the 1-100 pc scales in a nuclear re-149 gion of a simulated AGN host. They demon-150 strate that increasingly polar winds are pro-151 duced when anisotropic radiation from the AGN 152 shifts the mass distribution of the outflow orig-153 inating from the AGN. Meenakshi et al. (2022) 154 simulated the direct interaction between AGN 155 jet-induced outflows on 2 kpc scale and the ISM 156 and found shocked emission fronts in the ISM 157 that could be responsible for stunting star formation. On r < 1 pc scale, Wada et al. (2023) 159 were able to induce radiation-driven dusty out-160 flows which impact the ISM as they continue on 161 their outward paths. Tying the small and large 162 scales together has been an ongoing challenge. Due to computational constraints, large-scale 164 cosmological simulations that can model hun-165 dreds of Mpc³ at a time are not able to directly 166 resolve the physical processes that drive gas ac-167 cretion at <<1 pc scales where accretion takes 168 place, and so sub-grid prescriptions for black 169 hole accretion and its subsequent feedback must be adopted. The 'sub-grid' is defined as the reimplication below the gridded resolution of the simuimplication. Unfortunately, there is no unified model implication these sub-grid physics, and different studimplication prescriptions. The implication most commonly applied prescription is the one implication (Bondi 1952), often referred to as implication. The equation follows the form:

$$\dot{M}_{Bondi} = \frac{4\pi G^2 M_{BH}^2 \rho}{\left(c_s^2 + v_{rel}^2\right)^{3/2}}$$
(1)

where G is the gravitational constant, M_{BH} is 180 the mass of the black hole, ρ is the gas density, 181 c_s is the sound speed, and v_{rel}^2 is the relative 182 velocity of the gas. In the pure Bondi case, the 183 gas is assumed to be stationary relative to the 184 galactic potential, so v_{rel}^2 is zero. This model is 185 theoretically predicated on gas free-falling onto 186 the SMBH once it reaches the Bondi radius, $_{187}$ R_{Bondi} = 2GM_{BH} $/c_s^2$. The Bondi radius is where 188 the escape velocity of the SMBH (based on its 189 mass) equals the sound speed of the gas in the 190 nuclear region. The physical scale of the Bondi 191 radius is typically on order 0.1-300 pc if we as- $_{\rm 192}$ sume $\rm c_{s}$ of 400 km $\rm s^{-1}$ and SMBH mass range 193 of $10^6 \sim 10^9 \ {\rm M}_{\odot}$. Some large scale cosmo-194 logical simulation suites use a pure Bondi pre-195 scription to account for SMBH accretion, like 196 MassiveBlack-II (Khandai et al. 2015), EAGLE 197 (Schaye et al. 2015), and IllustrisTNG (Weinberger et al. 2017; Pillepich et al. 2018a). Physically, the issue with the Bondi accre-200 tion formalism is that it ignores both the angu-201 lar momentum of the gas and interactions due

Although there is also much variation in AGN feedback prescriptions, this program will focus on discussing the accretion rate prescriptions, on which all feedback depends.

202 to self-gravity between gas particles, which is

²⁰³ only appropriate in the case of hot, virialized ²⁰⁴ gas (Hobbs et al. 2012). Recent studies have

205 shown that gas and other accreting material still

206 has angular momentum inside what may be the 207 Bondi radius, particularly in gas-rich mergers or 208 galaxies with Seyfert AGN (e.g. in Davies et al. 209 2004; Hicks et al. 2013; Medling et al. 2014; Lin 210 et al. 2016), and so Bondi accretion timescales 211 may be much shorter than in reality where an-212 gular momentum delays accretion.

To account for this problem, some large-214 scale cosmological simulation suites apply ac-215 cretion physics by using modified versions of 216 Bondi accretion. The prescription in the *Il*-217 lustris (the predecessor to IllustrisTNG; Vo-218 gelsberger et al. 2013; Genel et al. 2014) and 219 Magneticum Pathfinder hydrodynamical simu-220 lation suites (Hirschmann et al. 2014; Bocquet 221 et al. 2016; Dolag et al. 2016) modify Bondi 222 by multiplying Equation 1 by a constant (unit- $_{223}$ less) 'boost' factor α (following the prescription of Springel et al. 2005; Di Matteo et al. 2005; 225 Springel & Hernquist 2005). The boost factor 226 is used to account for the volume average of the 227 Bondi-rates for both the cold and hot phases 228 in the simulations and typically has a value = 229 100. Another large-scale cosmological model, ₂₃₀ Horizon-AGN (Dubois et al. 2016), uses an α 231 similar to *Illustris* and *Magneticum*, but instead 232 of a constant value, their boost factor (following 233 the prescription from Booth & Schaye 2009) de-234 pends on density of the gas. Another approach, 235 used by the large-scale *Romulus* suite (Tremmel 236 et al. 2017) is to adjust the Bondi accretion rate 237 depending on the motion of the simulated gas 238 particles. In Romulus, if the smallest relative 239 velocity (which they equate to v_{bulk}, the bulk 240 motion of the gas) of the gas particle closest to 241 the SMBH is faster than the rotational veloc-242 ity of the gas, they replace the relative velocity $_{243}$ of the SMBH with $v_{\rm bulk}$ and multiply the Bondi ²⁴⁴ rate by a boost factor dependent on gas density. Bondi or Bondi-like accretion prescriptions 246 are the most commonly used, but theorists have 247 also designed accretion prescriptions with very 248 different underlying physics. One large-scale

simulation ([100 h^{-1} Mpc]³ volume) suite that 250 in part uses one of these prescriptions is SIMBA 251 (Davé et al. 2019a). In SIMBA, pure Bondi 252 accretion is still applied for hot gas accretion 253 where, as we mentioned, it is most appropri-254 ate. But, they then apply a torque-limited ac-255 cretion formalism for the cold gas where insta-256 bilities in the disk drive mass inflow (Hopkins 257 & Quataert 2011; Anglés-Alcázar et al. 2017). 258 Understanding if and in which cases different 259 sub-grid prescriptions are accurately estimating 260 accretion rates onto the black holes of galaxies 261 is critically important to cosmological simula-262 tions. Without an accurate prescription for ac-263 cretion over time, simulations cannot accurately 264 implement the impact of AGN feedback, and as 265 such may have incorrect outcomes with regards 266 to galaxy formation and evolution.

Observationally testing how black hole accre-268 tion rate prescriptions perform has only be-269 come possible in recent times. In this study, 270 we directly measure the parameters that go into 271 Bondi accretion, $\rho_{\rm gas}$ and c_s , on physical scales 272 ranging from 2-170 pc. We then plug these mea-273 sured parameters into the pure Bondi accretion 274 prescription as a function of radius to mimic 275 what a simulation at that resolution would es-276 timate for the black hole accretion rate. Fi-277 nally we test these predicted Bondi accretion 278 rates against empirically derived accretion rates 279 using hard (14-195 keV) X-ray data from the 280 The Burst Alert Telescope (BAT) AGN Spec-281 troscopic Survey (BASS) survey (Ricci et al. 282 2017). The BAT instrument (Barthelmy et al. 283 2005; Krimm et al. 2013) on Swift (Gehrels et al. 284 2004) is a hard X-ray detector that surveys the 285 entire sky, reporting X-ray sources to within 1-4 286 arcmin accuracy.

In this work, we use cosmological parameters of $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.28$, and $\Omega_{\Lambda} = 0.72$ (Hinshaw et al. 2009). To calculate spatial scales and luminosity distance to NGC

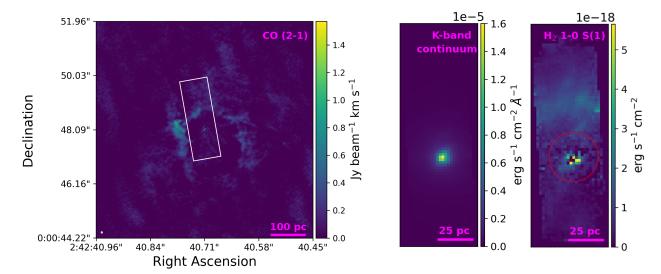


Figure 1. Nuclear region of NGC 1068 in the CO(2-1) flux (left, from ALMA), 2.2 μ m continuum (middle), and the continuum subtracted rovibrational H₂ 1-0 S(1) transition (right), described in Section 2. The CO(2-1) moment 0 map is masked below 3×rms and the white box in the CO(2-1) moment map represents the field of view of the NIR data. The very small, white ellipse in the bottom left represents the beam size of the ALMA data (41×30 mas). All three images show flux peaks at the AGN's location and both the CO and H₂ maps have enhanced emission in the CND ring. The red circle in the H₂ 1-0 S(1) moment map represents the aperture in which T_{Kin} is calculated in Figure 3.

²⁹¹ 1068 we use Ned Wright's Cosmology Calcula-²⁹² tor (Wright 2006).

2. NGC 1068 OBSERVATIONS

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For NGC 1068, we made use of <3 pc scale resolution both in the near infrared (NIR) with Keck/OSIRIS+AO (adaptive optics; PI Medling), and in the sub-mm with ALMA archival data (PI García-Burillo).

2.1. Keck/OSIRIS K-band Integral Field Spectroscopy

The first of two sets of data we are using in this project is a set of high resolution integral gral field unit (IFU) Keck/OSIRIS+AO (OH-304 Suppressing InfraRed Imaging Spectrograph, Larkin et al. 2006) integrations, for which we mosaic all frames into a single data cube. These observations were taken with the Kbb filter observations were taken with the Kbb filter (broad-band K between 1.965 - 2.381 μ m) with the 35 mas pixel⁻¹ plate scale on 2018 December 28th, 2019 January 22nd, and 2019 October 7th for a total exposure time of 6120 seconds

312 (51 frames, 120 seconds each). Weather impacted observations on 2019 October 7th, dur-314 ing which the laser guiding system was also not 315 working. We used the galaxy nucleus as the 316 natural guide star in NGS mode, and as the 317 tip/tilt star in LGS mode. AO corrections in 318 those frames without the laser produced larger 319 point spread functions with full-width at half-320 maximum (FWHM) values between 3 and 5 $_{321}$ pixels compared to ~ 2 with the laser on other 322 nights. We reduced the Keck/OSIRIS+AO ob-323 servations using the OSIRIS Data Reduction ³²⁴ Pipeline (OSIRISDRP, Lyke et al. 2017; Lockhart et al. 2019) version 4.2.0, which we use to 326 extract a spectrum for each spatial pixel, assem-327 ble the spectra into a cube, and mosaic the 51 328 total frames together to form the final image, 329 which has a 0.17" point spread function (PSF) 330 FWHM. Flux calibration was applied for each 331 night before final mosaicking.

The resulting mosaic reveals a strong K-Band continuum (particularly near the AGN) and

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 334 H₂ 1-0 rovibrational emission (S(0), $\lambda_{\rm rest} = ^{335}$ 2.2235 μ m; S(1), $\lambda_{\rm rest} = ^{2.1218}\mu$ m; S(2)), $\lambda_{\rm rest} = ^{336}$ 2.0338 μ m. These continuum and continuum- 337 subtracted H₂ 1-0 S(1) maps are shown in the 338 middle and right panels of Figure 1 respec- 339 tively. The continuum map was made using the 340 Cube Analysis and Rendering Tool for Astron- 341 omy (CARTA, Comrie et al. 2021) and the con- 342 tinuum subtracted H₂ 1-0 S(1) map was made 343 using QFitsView (Ott 2012). Both images show 344 peaks of emission on or near the position of the 345 central engine, and NGC 1068's circumnuclear 346 disk (CND) ring can be seen in the H₂ map.

2.2. ALMA Band 6 Long-baseline Interferometry

We chose the highest resolution CO J = (2-349 1) (hereafter CO(2-1)) available on the ALMA 351 archive that shows strong emission (PI García-352 Burillo, Project code 2016.1.00232.S; see also García-Burillo et al. 2019). We retrieved the 354 CO(2-1) spectral cube product from the ALMA archive, which has a rms of 0.25 mJy over 20 356 km s⁻¹, and was imaged using a Briggs (Briggs 357 1995) robust value of 0, resulting in a beam $_{358}$ size of 41×30 mas. We then used this spec-359 tral cube with the image cube analysis tools in 360 CARTA (Comrie et al. 2021) to create a moment $_{361}$ 0 (flux) map of the CO(2-1) emission. Figure 1 362 (left) shows this CO(2-1) moment 0 map which $_{363}$ is masked below $3\times \mathrm{rms}$ and is used for our anal-364 ysis in Section 3. Like in the warm H₂ observa-365 tions, both the AGN and CND ring are bright 366 sources in CO(2-1).

2.3. Nuclear structure of NGC 1068

NGC 1068 is one of the most-studied prototypical Seyfert galaxies, and as such a wealth of information has already been published about trickly are not an exhaustive list, but are included to provide context relevant to our analysis.

Under our 2.2 pc resolution, NGC 1068 hosts a water maser that is thought to originate from

376 the accretion disk on much smaller (<0.1 pc) 377 scales. Greenhill et al. (1996) observed the 378 maser with very long baseline interferometry 379 (VLBI) using both the Very Long Baseline Ar-380 ray and Very Large Array to achieve 0.65 pc 381 resolution. They used the velocity gradient of 382 the maser emission to infer a rotational velocity 383 of the gas, and in turn constrain $M_{\rm BH}$. Kumar 384 (1999) modeled the 0.65-1.1 pc disk from which 385 the maser emission is thought to be ejected 386 from. The clumps in their disk model interact 387 with each other, leading to eventual accretion 388 onto the SMBH.

On slightly larger scales with near and mid infrared interferometry, multiple authors were able to resolve a two-component dusty torus (Jaffe et al. 2004; Raban et al. 2009). One component is smaller and more elongated (1.35 source) in size than the other (3 × 4 pc). In the nucleus of Circinus, another Seyfert 2 source AGN, Tristram et al. (2014) also found a two-component dusty torus. Images like these that source showed structure inconsistent with the prior, source observationally-defined, Type 2 classification of these galaxies (unless foreground extinction was unification model (Antonucci 1993).

Gámez Rosas et al. (2022) used sub-pc resolu-404 tion observations of NGC 1068 taken with the 405 MATISSE/ESO/VLTI interferometer between 406 3 and 13 μ m to map the dust temperature dis-407 tribution of the dust observed in the previously 408 mentioned studies. They confirm an optically 409 thick pc scale dusty structure and a second, less 410 optically thick disk that extends to at least 10 411 pc. García-Burillo et al. (2019) (who in part 412 use the same ALMA data as we describe in Sec-413 tion 2.2) find a 14 pc CO(2-1) nuclear disk with ₄₁₄ a PA (\sim 110-140 deg) aligned with the water 415 maser disk PA (140 deg). Also in García-Burillo 416 et al. (2019), they observe the CND, which as 417 can be seen in Figure 1, has a gas deficit inside 418 the outer ring in its central ~ 130 pc region.

To resolve the kinematics of the 10 pc in-420 ner disk (often referred to as the torus) and 421 outer ring, Imanishi et al. (2020) observe both of 422 these scales using the bright (relative to CO(2- $_{423}$ 1)) HCN J=(3-2) and HCO+ J = (3-2) tran-424 sitions with ALMA at 1.4 pc resolution. They 425 find that the torus as observed with these dense 426 gas tracers rotates in the opposite direction with 427 respect to the outer ring. This is particularly 428 surprising because the water maser emission is 429 rotating in the same direction as the outer ring 430 rather than the torus it is physically closer to 431 (see Figure 1 of Imanishi et al. 2020). In the 432 work of García-Burillo et al. (2019), the authors 433 find that a "significant part" of the observed 434 counter-rotation in CO(2-1) can be attributed 435 to a northern AGN-driven wind. To make 436 a more robust determination though, García-Burillo et al. (2019) say that higher resolution 438 data is required so that the outflowing compo-439 nent can be better disentangled from the rotat-440 ing component.

Outflows originating from the AGN can serve 442 to regulate black hole accretion, and NGC 1068 443 hosts a complex outflow in the NE direction, 444 perpendicular to the nuclear disk. The largest 445 outflow component is seen as the radio jet (e.g. 446 in Gallimore et al. 1996). Mutie et al. (2024) 447 present higher resolution (~ 4 pc) e-MERLIN 448 5 GHz data along with archival VLA 10 GHz, and VLA 21 GHz images of the jet. 450 images together show not only the central jet 451 emission, but also detail in the larger scale bow 452 shock, >200 pc from the SMBH in the same 453 NE direction, which exhibits direct evidence of 454 the AGN's impact on the ISM. The impact 455 of the jet on the ISM is studied in part in 456 both Hviding et al. (2023) and Holden & Tad-457 hunter (2023), who both show evidence for gas 458 ionization consistent with shock ionization or 459 radiation-bounded AGN-photoionization along 460 the outflow's path on 160 pc to kpc scale. 461 García-Burillo et al. (2014) show that the CO

kinematics on distances 50 to 400 pc are spa-463 tially correlated with the radio jet, evidence 464 that the AGN is influencing even the cold ISM. 465 ALMA CO(6-5) observations from Gallimore 466 et al. (2016) show that this molecular outflow 467 originates within 2 pc from the SMBH, and has 468 velocities relative to systemic of about 400 km 469 s⁻¹. This outflow may have an impact on our 470 measurements of molecular gas mass, but that 471 impact is expected to be small as there is not 472 much CO(2-1) emission between the AGN and 473 CND ring, and the CND ring itself does not ap-474 pear very disturbed along the path of the out-475 flow.

3. PRESCRIPTION PARAMETERS

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In this pilot study, we examine the performance of the most commonly used accretion prescription for black hole growth in NGC 1068. The Bondi accretion formalism with a relative velocity of zero (also known as Bondi-Hoyle, or Bondi-Hoyle-Lyttleton e.g. Hoyle & Lyttleton Bondi 1939; Bondi & Hoyle 1944; Bondi 1952) follows the form:

$$\dot{M}_{Bondi} = 4\pi G^2 M_{BH}^2 \rho c_s^{-3} \tag{2}$$

 $_{486}$ where G is the gravitational constant, $\rm M_{BH}$ is $_{487}$ the mass of the black hole, ρ is the gas density $_{488}$ and $\rm c_s$ is the sound speed.

Bondi accretion is predicated on a spherically symmetric, non-self-gravitating gas distribution in which the gas inside the Bondi radius has no angular momentum. While this kind of environment may not be most appropriate for describing all galaxy nuclei (see Section 5 for additional information), Bondi accretion is a simple analytical prescription that can be applied inside a sphere of any radius, which makes it convenient as a sub-grid prescription.

In this subsection, we outline the methods for measuring each free parameter in the Bondi prescription using the available high resolution data from Section 2.

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Greenhill et al. (1996) imaged NGC 1068's wa-504 ter maser emission at a 0.65 pc scale using very 506 long baseline interferometry. From the rotation 507 curve of the water maser emission, they found 508 the enclosed mass within that radius to be $\sim 1 \times$ $_{509}$ 10⁷ M_{\odot} (with uncertainty on order unity). An-510 other study by Lodato & Bertin (2003) derive ₅₁₁ a smaller black hole mass of $\sim 8 \pm 0.3 \times 10^6$ 512 in a self-gravitating accretion disk model that matches the Greenhill et al. (1996) and Green-514 hill & Gwinn (1997) observations well. 515 Lodato & Bertin (2003) model corrects for non-516 Keplerian motion in the velocity profile of the 517 water maser emission, but this could be an over-518 correction. In fact, other studies have found 519 that the disk rotation may still be dominated 520 by the black hole (Imanishi et al. 2018). Al-521 beit with a worse fit to the velocities from the 522 maser emission, Lodato & Bertin (2003) also fit 523 a Keplerian rotation model, which has a best fit ₅₂₄ black hole mass of $\sim 1.5 \pm 0.02 \times 10^7 \,\mathrm{M}_{\odot}$. In the 525 absence of clear evidence in favor of one of the 526 newer modeling schemes, we adopt the Green-₅₂₇ hill et al. (1996) value of $M_{\rm BH} = \sim 1 \times 10^7 \ {\rm M}_{\odot}$ $_{528}$ as an intermediate M_{BH} measurement.

3.2. Parameter 2: gas density 3.2.1. Choice of volume element

To measure the gas density, we first must define our volume element. In cosmological simfine our volume element. In cosmological simfine curve typically, a fixed number gas particles fine exist inside a spherical region with radius r cenfine tered on the location of the SMBH. This volfine makes up the black hole kernel, in which fine the accretion physics are prescribed. Although fine studies like the ones discussed in Section 2.3 and fine volumer et al. (2022) have shown that \sim 10 pc fine cold gas distribution is more disk-like, we opt to fine a sphere of volume $V = \frac{4}{3}\pi r^3$ centered on the fine accretion resolution elements found in simulations that use Bondi accretion.

To measure the molecular gas (H₂ and He) mass inside the sphere, we use the CO(2-1) data 548 described in Section 2.2. To obtain a molecular gas mass, we utilize the conversion factor $\alpha_{\rm CO}$. 550 The exact value of $\alpha_{\rm CO}$ depends on several fac-551 tors including the size scale and environment 552 over which the CO flux is measured. The pic-553 ture is further complicated by the distinction between $\alpha_{\text{CO}(1-0)}$ and $\alpha_{\text{CO}(2-1)}$, where the dif-555 ference is dictated by the ratio between the line $_{556}$ luminosity of the two rotational transitions: r_{21} $_{\text{557}}~(r_{21}=L'_{\mathrm{CO}(2-1)}/L'_{\mathrm{CO}(1-0)}),$ which depends on the 558 temperature of the gas. In this work, we follow the same $\alpha_{\rm CO}$ methodology as in García-Burillo 560 et al. (2019) who use the Milky Way $\alpha_{\rm CO(1-0)} =$ $_{561} 4.3 \pm 1.29 \text{ M}_{\odot} (\text{K km s}^{-1} \text{pc}^2)^{-1} \text{ recommended}$ ₅₆₂ by Bolatto et al. (2013). We use $\alpha_{\text{CO}(1-0)}$ in 563 conjunction with the averaged line intensity 564 ratios for NGC 1068's northern and southern 565 CND regions (because the CND ring contains 566 the majority of the nuclear gas mass): $r_{21} = 2.2$ $_{567} \pm 0.4$, from Viti et al. (2014) to calculate a final

$$\alpha_{\text{CO(2-1)}} = \frac{\alpha_{\text{CO(1-0)}}}{r_{21}} = \frac{4.3 \pm 1.29}{2.2 \pm 0.4}$$

$$= 1.95 \pm 0.73 \ M_{\odot} (\text{K km s}^{-1} \text{ pc}^2)^{-1}. \quad (3)$$

570 The outflowing components of NGC 1068 may 571 have a lower $\alpha_{\text{CO}(1-0)}$, but we expect the Milky 572 Way value to be closer to the average for 573 the purpose of measuring integrated enclosed masses, especially at larger r. $\alpha_{\rm CO(2-1)}$ is then 575 multiplied by the sum of the flux density in-576 side a circular aperture of radius r, to match 577 our spherical geometry. The enclosed mass pro-578 file is shown alongside a snapshot of the aper-579 ture geometry in Figure 2. García-Burillo et al. $_{580}$ (2019), who center their r = 200 pc aperture 581 measurement on the center of the CND ring, find a molecular (H₂ + helium) gas mass of \approx 1.4 $_{583} \times 10^8 \mathrm{~M}_{\odot}$. We measure molecular gas mass 584 within the same aperture (using CARTA to measure flux) and find 1.3 \pm 0.5 \times 10⁸ M $_{\odot}$ (1.4

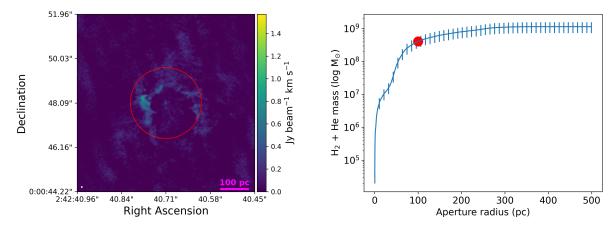


Figure 2. Left: Moment 0 map of CO(2-1) in NGC 1068, with flux density values masked below $3\times rms$. The red circle indicates the location and size of the 100 pc aperture (centered on the AGN) corresponding to the red dot in the right panel, which has $M_{enc,H_2+He} = 4.09 \pm 1.49 \times 10^8 M_{\odot}$. The small, white ellipse in the bottom left represents the beam size of the ALMA data (41×30 mas). Right: Integrated mass profile inside the radial aperture. Details on the conversion to molecular gas mass can be found in Section 3.2.

 $_{596}$ ± 0.5 × 10 8 M $_{\odot}$ if centered on the AGN), both $_{587}$ of which are consistent with the García-Burillo $_{588}$ et al. (2019) measurement. For comparison to $_{589}$ another nearby Seyfert 2, in the nuclear region $_{590}$ of Circinus, using the warm H₂ gas tracer H2 $_{591}$ 1-0 S(1), Müller Sánchez et al. (2006) find the $_{592}$ total molecular gas mass to be 1.7 × 10 7 M $_{\odot}$ within 0.8" (52pc). Integrated inside the same $_{594}$ physical distance from the SMBH in NGC 1068, $_{595}$ we find a molecular gas mass of 8.8 ± 3.2× 10 7 $_{596}$ M $_{\odot}$, higher by almost 1 dex.

To convert enclosed mass to density we divide by the volume element for a sphere (see Section 3.2.1) with r defined by our circular aperture size used for measuring mass. In this sphere with $r=100~\rm pc$ centered on the AGN as shown in Figure 2 (left), we find a molecular gas mass density of $93.3~\pm~71.1~\rm M_{\odot}pc^{-3}$.

3.2.3. Warm H_2 gas mass

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We also calculate an enclosed mass using the warm H_2 gas measured from the NIR data, following Equation 6 of Storchi-Bergmann et al. (2009), which uses the line flux of the H_2 1-0 S(1) rovibrational transition at $\lambda_{\rm rest}=2.1218$ In NGC 1068, Martins et al. (2010) used the NASA 3-m Infrared Telescope Facil-

 $_{612}$ ity (IRTF) and found a nuclear (slit 1"x 2") $_{613}$ extinction E(B-V) of 1.13 (from their Table $_{614}$ 4). Assuming the standard extinction law of $_{615}$ Cardelli et al. (1989) with $R_v = 3.1$, the extinc- $_{616}$ tion A_v ($A_v = R_v \times E(B-V)$) is ~ 3.5 . Based $_{617}$ on $A_k \sim A_v/10$ (Howarth 1983), the extinction- $_{618}$ corrected H_2 gas mass inside r < 1.7" (111 pc) $_{619}$ is $\sim 68 M_{\odot}$, which is about 1.38 times the observed value. The warm H_2 mass is inconsequential compared to the CO-derived value of $_{622}$ 4.08 \pm 1.49×10⁸ M_{\odot} in the same region.

One reason that the warm gas measurement in this subsection may be so small is due to the radiative environment in NGC 1068's nucleus. Under local thermal equilibrium (LTE, where the energy distribution can be described by a single number locally) conditions, the H_2 emission can be excited by the equilibrium value for temperatures $T \approx 1000$ K (Davies et al. 2005). To reach such high excitation temperatures in NGC 1068, H_2 emission lines can be excited through several mechanisms, as described be-

 635 (1) *UV fluorescence*: This excitation mech- 636 anism dominates in photodissociation regions 637 (PDRs). Far-ultraviolet (FUV, $\lambda > 912$ Å) radi- 638 ation pumps the molecule into electronically ex-

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639 cited states, leading to subsequent cascades that
640 emit fluorescent emission (Wakelam et al. 2017).
641 This mechanism is dominant in Seyfert 1 galax642 ies (Davies et al. 2005). Although NGC 1068 is
643 classified as a Seyfert 2 galaxy and is expected
644 to have less FUV radiation, the HST/FOC UV
645 image shows a bright nucleus with polarization
646 (Barnouin et al. 2023) within our OSIRIS field
647 of view (FOV).

(2) Shocks and outflows: Veilleux et al. (1997) suggest that shocks associated with nuclear outflows are a likely heating source for H₂ in many Seyfert 2 galaxies. May & Steiner (2017) and slyzed VLT/SINFONI and Gemini/NIFS data with a larger FOV covering the entire CND and proposed that the CND could be an expanding bubble.

(3) X-ray heating from the AGN: X-ray emis-557 sion can penetrate deeply into regions that are 558 opaque to UV photons and influence H₂ excita-559 tion (Matt et al. 1997). All of these mechanisms 560 can contribute to H₂ emission.

We measure the H_2 1-0 S(1) extinction-662 corrected intrinsic flux ($F_{\rm intrinsic} = F_{\rm observed} \times$ 663 $10^{(0.4A_k)}$) and directly convert it to the warm 664 H_2 gas mass. Due to the rectangular FOV, only 665 an aperture radius of <0.3" is fully contained 666 within the OSIRIS FOV, suggesting that H_2 667 emission at radii >0.3" is incomplete.

3.3. Parameter 3: sound speed of the gas

The final parameter required in the Bondi ac-670 cretion formalism is the sound speed of the gas. 671 The sound speed for an ideal gas is:

$$c_s = \sqrt{\frac{\gamma R T_K}{M}} \tag{4}$$

where γ is the adiabatic index (1, as the gas is assumed to be isothermal in each sub-region), R is the gas constant 8.3144598 J mol⁻¹ K⁻¹, T_K is the temperature of the gas (K), and M is the molar mass (kg) of the gas, for which we assume solar metallicity. All but the temperature in this case are constants.

For the temperature of the molecular gas, we $_{681}$ use two methods: one using CO rotation dia- $_{682}$ grams (cold gas), and another using an excitation diagram for the molecular $_{42}$ (warm gas) $_{684}$ from our Keck/OSIRIS+AO NIR data.

3.3.1. CO-derived $c_{\rm s}$

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For a temperature from CO transitions we re-687 fer to the work of Viti et al. (2014) who infer the 688 temperature of the gas in the CND of NGC 1068 689 by using CO rotation diagrams. This method 690 assumes that the gas is in LTE, and that the 691 observations are mostly in the Rayleigh-Jeans 692 regime where the intensity of the radiation is 693 proportional to the temperature. This temper-694 ature is also known as the 'rotational temper-695 ature' and is equal to the kinetic temperature 696 if all CO levels are thermalized (Goldsmith & 697 Langer 1999). Because of these assumptions, 698 this temperature should be considered a lower 699 limit, which translates to an upper limit on 700 our final accretion rate because $\dot{M}_{Bondi} \propto c_s^{-3}$. 701 For the central region of NGC 1068, Viti et al. $_{702}$ (2014) find a temperature of 50 ± 5 -7 K via the 703 CO rotation diagram method (see Section 3.1.1. 704 of their work for more details). Plugging that 705 and the other constants into Equation 4, we find 706 that the speed of sound in the cold molecular 707 gas phase is $409.2 \pm 141.7 \text{ km s}^{-1}$.

3.3.2. H_2 -derived c_s

As shown in Section 3.2.3, warm H_2 is also present in NGC 1068's nuclear regions, so we label{eq:10} also consider the sound speed for this component of the ISM. To measure the temperature which we then use in the c_s calculation, we use the H_2 1-0 S(0), S(1), and S(2) rovibrational line fluxes in the Keck/OSIRIS NIR data described in Section 2.1. Assuming the H_2 gas is in LTE, the H_2 excitation temperature is equal to the kinetic temperature. Figure 3(a) shows the H_2 excitation diagram, which is the column density in the upper level of each transition normalized by its statistical weight (N_u/g_u) as a function of

722 energy of the level as a temperature (E_u) . The 723 best-fit slope of this relationship is related to 724 T_K as $\frac{N_u}{g_u} \propto e^{(-\frac{h\nu}{kT_K})}$ in the LTE description of 725 energy level populations (see pages 322, 327 of 726 Wilson et al. 2013). Solving for T_K then yields 727 $-\frac{1}{T_K} \propto \frac{\ln \frac{N_u}{g_u}}{\frac{E_u}{k}}$.

Because we have spatially resolved data for $_{129}$ these H_2 lines, we can derive kinetic temper-730 atures from 12-111 pc and apply them at the matched distances in the accretion rate predic-732 tion. While the Keck/OSIRIS+AO data has a $_{733}$ higher resolution than 6 pc, the H_2 1-0 S(1) $_{734}$ and S(2) lines are not detected in a r ≤ 6 pc $_{735}$ (0.1") aperture. Fluxes of the lines are mea-736 sured using the line fitting tool in QFitsView 737 (Ott 2012), which we use to fit the continuum 738 and one Gaussian component to the integrated 739 (within a region circular region with radius r) 740 spectrum. Figure 3(b) shows the range of ex-741 citation temperatures as a function of radius. $_{742}$ T_K ranges from 678-2261 K, and peaks at r \leq 85 743 pc where $T_{\rm K} = 2261 \, ^{+3683}_{-1631} \, {\rm K}.$ High temperatures may be caused by the influence of the PDR (Sec-745 tion 3.2.2 describes observations of this for NGC 746 1068), which is found to increase the H_2 1-0 S(1)747 emission by up to 70% in the some luminous in-748 frared galaxies (Davies et al. 2000; Davies et al. 749 2003). Using Equation 4 (with a molar mass of 750 H₂) results in H₂ sound speeds between 1013- 1850 km s^{-1} , peaking at r = 85 pc.

RESULTS: M _{Bondi} VS. M _{X-RAY} Calculating M _{Bondi}

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Now that we have calculated each paramerss ter for the Bondi accretion prescription in Secrss tion 3, we are ready to estimate a Bondi accrers tion rate. Because our parameters are spatially rss resolved, we calculate accretion rate as a funcrs tion of simulated resolution:

$$\dot{M}_{Bondi}(r) = 4\pi G^2 M_{BH}^2 \rho (\leq r) c_s (\leq r)^{-3}.$$
 (5)

 $_{761}$ Figure 4 shows the Bondi accretion rate for the $_{762}$ cold derived case as a function of radius, the

means of which range between about 10^2 and $_{764}$ 10^{-3} ${\rm M}_{\odot}$ yr⁻¹. As the enclosed mass found in Section 3.2 for the warm ${\rm H}_2$ gas component in $_{766}$ r< 170 pc is small (68 ${\rm M}_{\odot}$), and the temperature gradient is high (678-2261 K, see Section 3.3.2) $_{768}$ relative to the values found for the cold CO $_{769}$ gas component, the resulting Bondi accretion $_{770}$ rates are much smaller (between about $_{771}$ and $_{771}$ and $_{771}$ $_{771}$ for the warm gas. These results suggest that the cold gas is the dominant $_{773}$ carrier of mass accretion on r< 170 pc scales. $_{774}$ Table 1 shows a range of precise values for both $_{775}$ the cold and hot Bondi accretion rates.

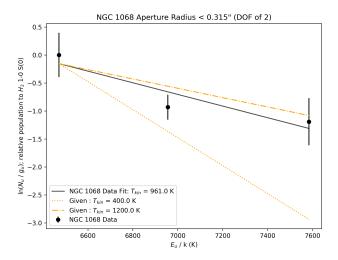
4.2. Calculating X-ray accretion rates

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To understand how well the Bondi accretion rate, formalism compares to the real accretion rate, we compare it to the X-ray derived accretion rate. To calculate an accretion rate from X-ray measurements, we use Swift/BAT data from the BAT AGN Spectroscopic Survey (BASS, Ricci et al. 2017). They present intrinsic luminosities the bolometric correction, Equation 17 in Gupta the bolometric correction, Equation 17 in Gupta et al. (2024):

$$\log(\kappa_{14-195}) = (0.13 \pm 0.04) \times \log(\lambda_{\rm Edd}) + (1.04 \pm 0.05)$$
 (6)

to calculate bolometric luminosity. Because Ricci et al. (2017) measure a neutral column lensity of $\log N_{\rm H} = 25.0~{\rm cm^{-2}}$ in NGC 1068 and lensity of logN_H = 25.0 cm⁻² in NGC 1068 and lensity of the X-ray continuum might not be well estimated when the emission is dominated by respectively processed radiation in environments like this, like this, we conservatively estimate uncertainty on the input intrinsic 14-195 keV luminosity to be \pm lensity in the equation from Netzer & Trakhtenson nosity in the equation from Netzer & Trakhtenson the spin of the black hole. For that depends on the spin of the black hole. For stationary, retrograde disk, and maximally rosum tating SMBHs respectively, the values for η are



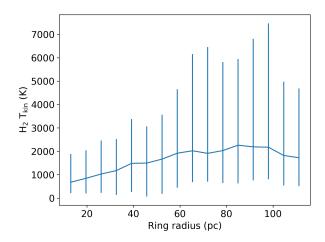


Figure 3. (Left:) Column density in the upper level of each H_2 1-0 S(0), S(1), and S(2) transition as a function of energy level of that transition as a temperature (K) inside a r=21 pc circular aperture centered on the AGN as shown in Figure 1. The best fit slope (using linear regression), as described in Section 3.3.2, is the temperature of the gas in that region if we assume LTE. (Right:) T_K estimated as in the excitation diagram on the left but instead inside circular apertures matching the methods of Section 3.2 from 0.2" to 1.7" in steps of 0.1". The mean of the derived temperatures is 1612^{+2840}_{-1216} K.

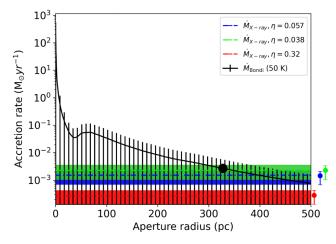


Figure 4. X-ray and (Cold-derived) Bondi accretion rates as a function of radius over which nuclear parameters are measured. Color bars and ranges displayed to the right denote uncertainties on each X-ray measurement. The Bondi prescription overestimates \dot{M}_{BH} by orders of magnitude for low aperture radii, but, above 327 pc (the black circle), the mean Bondi prescription value begins to agree and even dip below the mean minimum prediction from the X-ray by aperture size r=398 pc.

 $_{804}$ 0.057, 0.038, and 0.32 (Netzer & Trakhtenbrot $_{805}$ 2014). For NGC 1068, we find $\dot{M}_{\rm X-ray}$ values

806 equal to $1.51 \pm 0.81 \times 10^{-3} \ \rm{M_{\odot}yr^{-1}}$ (station-807 ary SMBH), $2.26 \pm 1.21 \times 10^{-3} \ \rm{M_{\odot}yr^{-1}}$ (retro-808 grade accretion disk), and $2.69 \pm 1.43 \times 10^{-3}$ 809 $\rm{M_{\odot}yr^{-1}}$ (maximally spinning SMBH). Figure 4 810 and shown in Table 1. $\rm{\dot{M}_{Bondi}}$ overestimates the 811 accretion rate by several orders of magnitude at 812 small distances from the SMBH where the gas 813 density is high, but dips below the X-ray accresitation rates at large distances, where density is 815 low.

Vollmer et al. (2022) used the IR-derived bolometric luminosity for the AGN in NGC 1068 from Vollmer et al. (2018) to calculate $\dot{\rm M}_{\rm BH}\sim$ $\rm L_{bol}/(0.1c^2)\sim0.05~M_{\odot}\rm yr^{-1}$. They calculate a coremass accretion rate onto their modeled accresion disk for NGC 1068 to be $\rm 2\times10^{-3}~M_{\odot}\rm yr^{-1}$ curve ($\rm \eta=0.1$), which is in agreement with our $\rm M_{\rm S23}~\dot{M}_{\rm X-ray}$ values and the cold gas derived $\rm \dot{M}_{\rm Bondi}$ in aperture sizes of r \geq 363 pc.

5. DISCUSSION: RESULTS IN CONTEXT OF SIMULATIONS

To inform theorists on which accretion preszs scriptions in their simulations are best to use

Method				Accretion rate	$({\rm M}_{\odot}~{\rm yr}^{-1})$		
X-rays (ϵ = 0.57)				1.51 ± 0.81	$\times 10^{-3}$		
X-rays (ϵ = 0.38)				2.26 ± 1.21	$\times 10^{-3}$		
X-rays (ϵ = 0.32)				2.69 ± 1.43	$\times 10^{-3}$		
Bondi (<r)< td=""><td>5 pc</td><td>10 pc</td><td>25 pc</td><td>50 pc</td><td>100 pc</td><td>200 pc</td><td>500 pc</td></r)<>	5 pc	10 pc	25 pc	50 pc	100 pc	200 pc	500 pc
$(T_{Kin} = 50 \text{ K})$	$1.62 \pm$	$0.43~\pm$	$0.06 \pm$	$0.05~\pm$	$0.03~\pm$	$8.32~\pm$	$7.63~\pm$
	1.79	0.47	0.07	0.05	0.04	9.16×10^{-4}	8.41×10^{-4}
$(T_{Kin} = 678-2261 \text{ K})$	*	*	$8.16 {}^{+28.89}_{-21.6}$	$4.95 {}^{+15.87}_{-14.03}$	$5.04 {}^{+23.61}_{-11.20}$	*	*
			$\times 10^{-9}$	$\times 10^{-10}$	$\times 10^{-11}$		

Table 1. Accretion rate measurements and estimates for rates derived from X-ray luminosities and the pure Bondi accretion prescription inside various radii. In NGC 1068, where the cold gas phase makes up the bulk of the gas mass in the nucleus, the cold gas derived Bondi accretion estimate outpaces the X-ray derived accretion rates by between 2 and 4 orders of magnitude. *H_2 1-0 S(1) and S(2) lines required to calculate temperature for the Bondi calculation are not detected in this aperture.

and when, we have designed our measurements 830 to fit in the practical context of those simu-831 lations. Large scale cosmological simulations 832 must use sub-grid physics for accretion because 833 of computing constraints. Some examples of hy-834 drodynamical galaxy evolution simulations that 835 use or have popular options to use a spheri-836 cally symmetric, Bondi or Bondi-like black hole 837 accretion formalisms are Illustris/IllustrisTNG (Genel et al. 2014; Vogelsberger et al. 2014; Pillepich et al. 2018b), Magneticum Pathfinder 840 (Hirschmann et al. 2014; Bocquet et al. 2016; 841 Dolag et al. 2016), MassiveBlack-II (Khandai 842 et al. 2015), Eagle (Schaye et al. 2015), Horizon-843 AGN (Dubois et al. 2016), Romulus (Tremmel 844 et al. 2017), and SIMBA (Davé et al. 2019b, 845 uses Bondi for hot gas only). The resolution of 846 the hydrodynamical gas cells in which these sub-847 grid physics are calculated ranges from to 10s of 848 pc to more typically kpc. Even in the highest 849 resolution zoom-in simulations, the spherical ra-850 dius in which particle calculations are made is approximately 10 pc (Wetzel et al. 2023).

Because we have spatially-resolved measurements, we are able to examine the performance for Bondi accretion at a range of spatial scales. For the Bondi accretion rate derived from warm gas we are limited by the field of view of OSIRIS $_{857}$ (0.56×2.24" with our observational setup), but $_{858}$ the ALMA data extends to over 500 pc away $_{859}$ from the SMBH.

Table 1 shows the Bondi accretion rates at radii between 5-500 pc as calculated in Secset tion 4, and the X-ray accretion rates as calcused lated in Section 4.2, which are all plotted together in Figure 4. At aperture radii $r \le 327$ pc, the parameterized Bondi accretion rate exceeds the X-ray derived accretion rate (by 2 or more dex in aperture sizes of $r \le 15$ pc and by 1 or more dex when $r \le 125$ pc).

This is, perhaps, not a surprising result. Past 870 studies have hinted towards Bondi accretion 871 overestimating the real accretion rate. Di Mat-872 teo et al. (2000) found that luminosities calcu-873 lated using estimated Bondi accretion rates for $_{874}$ six black holes with masses of 0.22-5.2 \times 10 9 875 M_{\odot} determined in Magorrian et al. (1998) were 876 4-6 orders of magnitude higher than the real lu-877 minosities of the galaxy nuclei. Hopkins et al. 878 (2016) model SMBH accretion in a gas-rich nu-879 clear disk in a massive simulated galaxy with 0.1 880 pc resolution. In their study, applying a pure 881 Bondi accretion formalism resulted in an accre- $_{882}$ tion rate $\sim 10^8$ times higher than the luminosity-883 derived accretion rate native to their simulation. 884 Near the SMBH, pure Bondi accretion ignores 885 the possibility that gas particles may have angu-886 lar momentum. The gas in the simulation used 887 in Hopkins et al. (2016) is primarily cold and is 888 supported by angular momentum rather than 889 radiation pressure. Observations show that es-890 pecially in gas-rich galaxies that naturally host molecular torii, the r<100 pc cold gas reservoir 892 is large, has significant angular momentum, and 893 is the primary candidate for black hole accretion 894 fueling (Davies et al. 2004; Hicks et al. 2013; 895 Medling et al. 2014; Lin et al. 2016; Gaspari 896 et al. 2015). Ignoring the angular momentum 897 of the cold gas is likely the primary cause of the 898 overestimate that Bondi accretion makes both 899 in Hopkins et al. (2016) the aperture sizes of 900 r \leq 327 pc in this work.

The performance of Bondi accretion between 200-500 pc is more realistic, and it even dips below the X-ray derived accretion rates for very large (r≥398) apertures. This is because, as is apparent in Figure 2, the cold gas has much lower average densities at large distances from the SMBH.

If NGC 1068 is typical, these results suggest 909 that the usage of pure Bondi accretion is likely 910 to struggle to accurately predict black hole ac-911 cretion rates. From our example, the accuracy 912 of Bondi predictions depends heavily on the size 913 of the black hole kernel used to calculate nu-914 clear conditions, overpredicting in the small ra-915 dius limit and underpredicting in the large ra-916 dius limit. Understanding the physical mecha-917 nisms that drive accretion on the sub-grid scales 918 in galactic nuclei can inform the future devel-919 opment of accretion prescriptions. The Bondi 920 prescription applies free-fall to particles inside 921 the Bondi radius, but our results suggest that 922 angular momentum plays an important role in 923 some nuclei.

6. CONCLUSIONS AND FUTURE EXPANSION OF THIS PROJECT

In this study we estimate a Bondi accretion rate as a function of radius for NGC 1068 using

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928 two different molecular gas tracers, and com929 pare the result to the direct accretion rate de930 rived from hard X-ray luminosity of the AGN.
931 Compared to warm H₂ gas, CO gas is the dom932 inant mass carrier close to the SMBH. Follow933 ing this, the cold gas derived Bondi accretion
934 rate estimate outpaces the X-ray derived value
935 by more than 1 order of magnitude at aperture
936 sizes r≤125 pc and up to 4 dex inside the small937 est apertures. In the case of warm gas Bondi
938 accretion where the enclosed mass involved in
939 the calculation is negligible, and in the cold gas
940 case in aperture sizes of r≥327 pc, the Bondi
941 accretion rate is instead lower than or equal to
942 the X-ray accretion rates.

This paper is a pilot for a wider study of 944 AGN and accretion prescriptions. Direct probes 945 of sub-grid accretion prescriptions may, as our 946 sample expands, help identify which physical 947 processes dominate accretion on a variety of 948 spatial scales, and in turn provide recommenda-949 tions for appropriate sub-grid prescriptions to 950 describe them. The results in this work sup-951 port previous evidence that in high resolution 952 cosmological simulations, applying a Bondi ac-953 cretion prescription can lead to large overesti-954 mates of M_{BH} and therefore large overestimates 955 of AGN feedback, which in turn impacts the 956 global galaxy evolutionary track. We note that 957 this is a test for a specific Seyfert 2 AGN. To 958 make more robust recommendations about the 959 application of the Bondi accretion prescription 960 for sub-grid accretion physics we must directly 961 test Bondi on more galaxies.

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962

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¹⁰⁰⁵ Software: Astropy (Astropy Collaboration ¹⁰⁰⁶ et al. 2013, 2018, 2022), Matplotlib (Hunter ¹⁰⁰⁷ 2007), NumPy (Harris et al. 2020).

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