CHAPTER 4

Beyond Classical Search

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Search Algorithms So Far

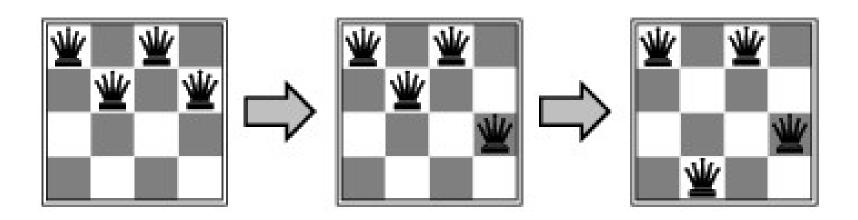
- Designed to explore search space systematically:
 - keep one or more paths in memory
 - record which have been explored and which have not
 - a path to goal represents the solution

Local Search Algorithms

- In many optimization problems, the path to the goal is irrelevant; the goal state itself is the solution
- State space = set of "complete" configurations
- Find configuration satisfying constraints, e.g., n-queens
- In such cases, we can use local search algorithms
- keep a single "current" state, try to improve it
 - use very little memory usually a constant amount
 - find reasonable solutions in large or infinite state spaces for which systematic solutions are unsuitable
 - useful for solving optimization problems, e.g. Darwinian evolution, no "goal test" or "path cost"

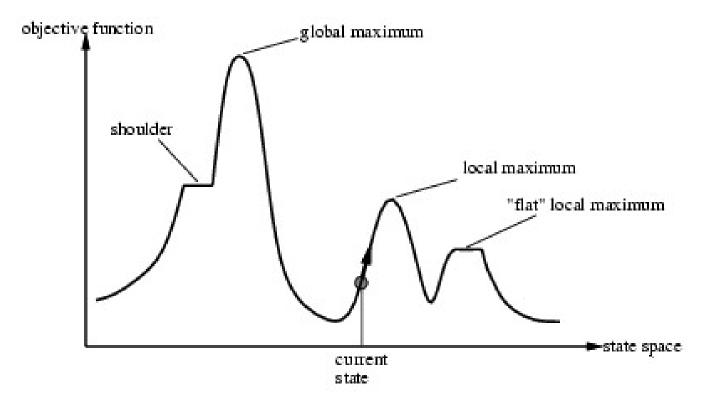
Example: n-Queen Problem

• Put n queens on an $n \times n$ board with no two queens on the same row, column, or diagonal

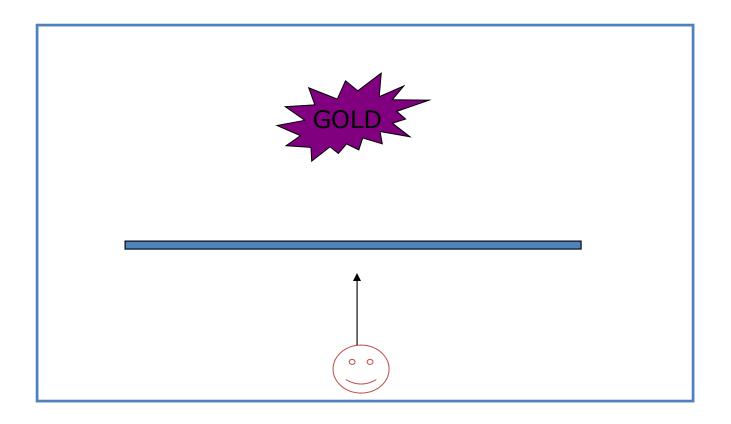


State Space Landscape

 Problem: depending on initial state, can get stuck in local maxima/minima

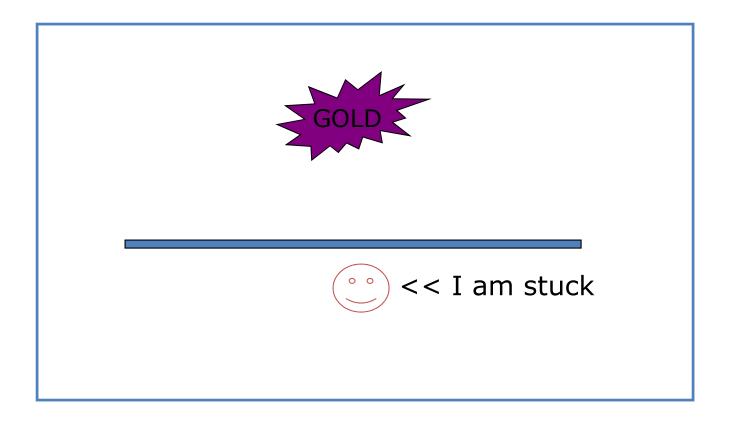


Example: Initial State



Assume the objective function measures the straight-line distance

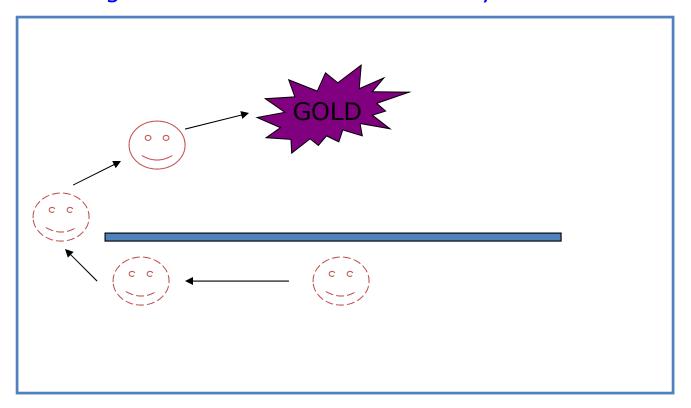
Example: Local Minima



Assume the objective function measures the straight-line distance

Example: A Plausible Solution

Making some "bad" choices is actually not that bad

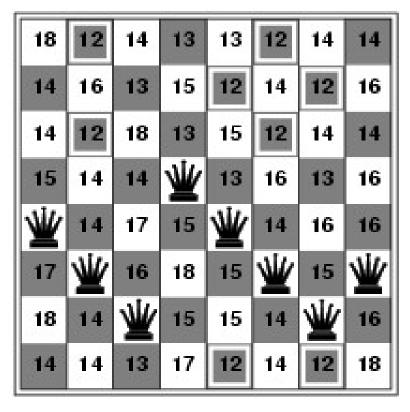


Assume the objective function measure the straight-line distance

Hill-Climbing Search

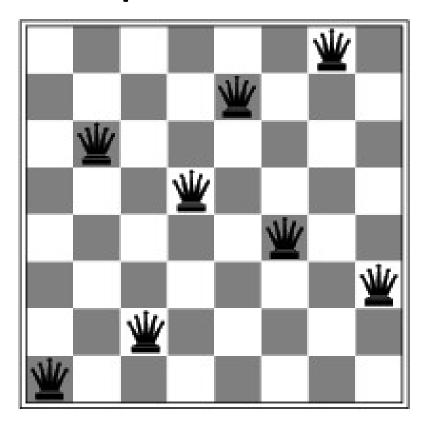
 "Like climbing Everest in thick fog with amnesia"

Example: 8-Queen



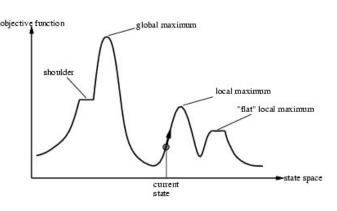
- h = number of pairs of queens that are attacking each other, either directly or indirectly
- h = 17 for the above state

Example: 8-Queen



• A local minimum with h = 1

More on Hill Clim



- Complete? Optimal?
- Hill climbing is sometimes called greedy local search
- Although greedy algorithms often perform well, hill climbing gets stuck when:
 - Local maxima/minima
 - Ridges
 - Plateau (shoulder or flat local maxima/minima)
- The steepest-ascent hill climbing solves only 14% of the randomlygenerated 8-queen problems with an avg. of 4 steps
- Allowing sideways move raises the success rate to 94% with an avg. of 21 steps, and 64 steps for each failure

Variants of Hill Climbing

- Stochastic hill climbing:
 - chooses at random from among uphill moves
 - converges more slowly, but finds better solutions in some landscapes
- First-choice hill climbing:
 - generate successors randomly until one is better than the current
 - good when a state has many successors
- Random-restart hill climbing:
 - conducts a series of hill climbing searches from randomly generated initial states, stops when a goal is found
 - It's complete with probability approaching 1

More on Random-Restart Hill Climbing

- Assume each hill climbing search has a probability p of success, then the expected number of restarts required is 1/p
- For 8-queen problem, p = 14%, so we need roughly 7 iterations to find a goal
- Expected # of steps = cost_to_success + (1-p)/p * cost_to_failure
- Random-restart hill climbing is very effective for n-queen problem
- 3 million queens can be solved < 1 min

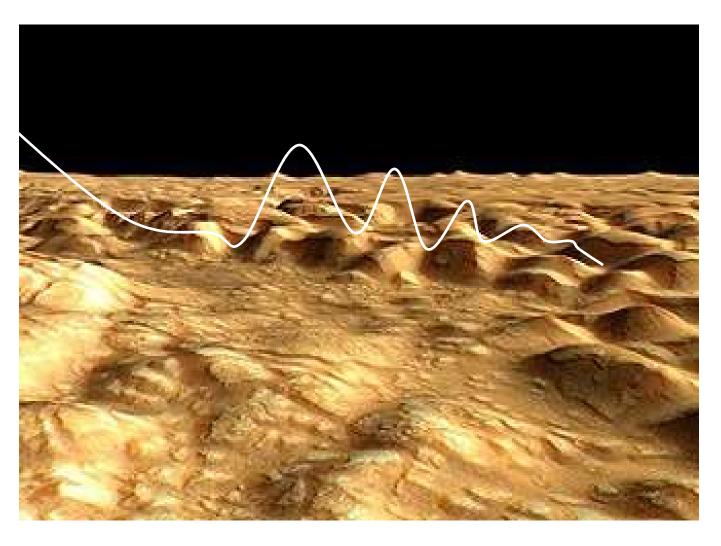
Some Thoughts

- NP-hard problems typically have an exponential number of local maxima/minima to get stuck on
- A hill climbing algorithm that never makes "downhill" (or "uphill") moves is guaranteed to be incomplete
- A purely random walk moving to a successor chosen uniformly at random – is complete, but extremely inefficient
- What should we do?
- Simulated annealing (P115)

What is Simulated Annealing?

 The process used to harden metals and glass by heating them to a high temperature and then gradually cooling them, thus allowing the material to reach a low-energy crystalline state

Ping-Pong Ball Example



Simulated Annealing

 Idea: escape local maxima by allowing some "bad" moves but gradually decrease their frequency

```
function Simulated-Annealing (problem, schedule) returns a solution state inputs: problem, a problem schedule, a mapping from time to "temperature" local variables: current, a node next, a node T, a "temperature" controlling prob. of downward steps  \begin{array}{c} current \leftarrow \text{Make-Node}(\text{Initial-State}[problem]) \\ \text{for } t \leftarrow 1 \text{ to} \infty \text{ do} \\ T \leftarrow schedule[t] \\ \text{if } T = 0 \text{ then return } current \\ next \leftarrow \text{a randomly selected successor of } current \\ \Delta E \leftarrow \text{Value}[next] - \text{Value}[current] \\ \text{if } \Delta E > 0 \text{ then } current \leftarrow next \\ \text{else } current \leftarrow next \text{ only with probability } e^{\Delta E/T} \\ \end{array}
```

Analysis of Simulated Annealing

- One can prove: If T decreases slowly enough, then simulated annealing search will find a global optimum with probability approaching 1
- Widely used in VLSI layout, airline scheduling, etc.
- An example: http://foghorn.cadlab.lafayette.edu/fp/fpIntro.html

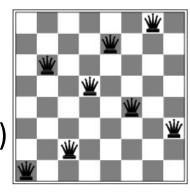
Local Beam Search

Idea:

- Keep track of k states rather than just one
- Start with k randomly generated states
- At each iteration, all the successors of all k states are generated
- If any one is a goal state, stop; else select the k best successors from the complete list and repeat
- Is it the same as running k random-restart searches?
- Useful information is passed among the k parallel search threads
- Stochastic beam search: similar to natural selection, offspring of a organism populate the next generation according to its fitness

Genetic Algorithms

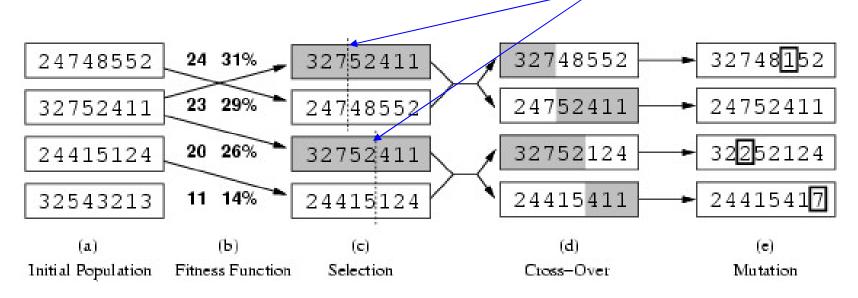
A successor state is generated by combining two parent states



- Start with k randomly generated states (population)
- A state is represented as a string over a finite alphabet 16257483 (often a string of 0s and 1s or digits)
- Evaluation function (fitness function). Higher values for better states
- Produce the next generation of states by selection, crossover, and mutation

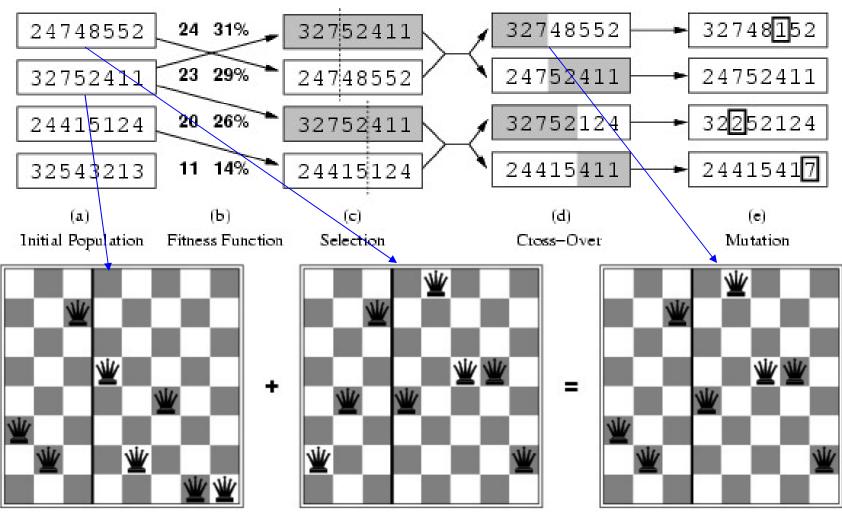
Genetic Algorithms

crossover point



- Fitness function: number of non-attacking pairs of queens (min = 0, max = $8 \times 7/2 = 28$)
- 24/(24+23+20+11) = 31%
- 23/(24+23+20+11) = 29% etc

Example: 8-Queen



CS 420: Artificial Intelligence

Example: TSA

 http://www.obitko.com/tutorials/geneticalgorithms/

More on Genetic Algorithms

- Genetic algorithms combine an uphill tendency with random exploration and exchange of information among parallel search threads
- Advantages come from "crossover", which raise the level of granularity

A Genetic Algorithm

```
function GENETIC-ALGORITHM(population, FITNESS-FN) returns an individual
  inputs: population, a set of individuals
           FITNESS-FN, a function that measures the fitness of an individual
  repeat
      new\_population \leftarrow empty set
      loop for i from 1 to SIZE(population) do
          x \leftarrow \text{RANDOM-SELECTION}(population, \text{FITNESS-FN})
          y \leftarrow \text{RANDOM-SELECTION}(population, FITNESS-FN)
          child \leftarrow REPRODUCE(x, y)
          if (small random probability) then child \leftarrow \text{MUTATE}(child)
          add child to new_population
      population \leftarrow new\_population
  until some individual is fit enough, or enough time has elapsed
  return the best individual in population, according to FITNESS-FN
function REPRODUCE(x, y) returns an individual
  inputs: x, y, parent individuals
  n \leftarrow \text{LENGTH}(x)
  c \leftarrow \text{random number from 1 to } n
```

return APPEND(SUBSTRING(x, 1, c), SUBSTRING(y, c + 1, n))

Exercise

- 4.11 Give the name of the algorithm that results from each of the following special cases:
 - Local beam search with k = 1
 - Local beam search with one initial state and no limit on the number of states retained
 - Simulated annealing with T = 0 at all times (and omitting the termination test)
 - Genetic algorithm with population size N = 1

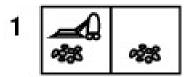
Searching With Partial Information

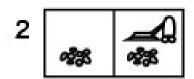
- We have covered: Deterministic, fully observable → single-state problem
 - agent knows exactly which state it will be in
 - solution is a sequence
- Deterministic, non-observable → multi-state problem
 - Also called sensorless problems (conformant problems)
 - agent may have no idea where it is
 - solution is a sequence
- Nondeterministic and/or partially observable → contingency problem
 - percepts provide new information about current state
 - often interleave search, execution
 - solution is a tree or policy
- Unknown state space → exploration problem ("online")
 - states and actions of the environment are unknown

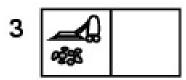
Example: Vacuum World

- Single-state, start in #5.Solution?
 - [Right, Suck]

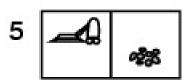
- Multi-state, start in #[1, 2, ..., 8]. Solution?
 - [Right, Suck, Left, Suck]



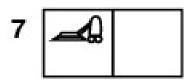




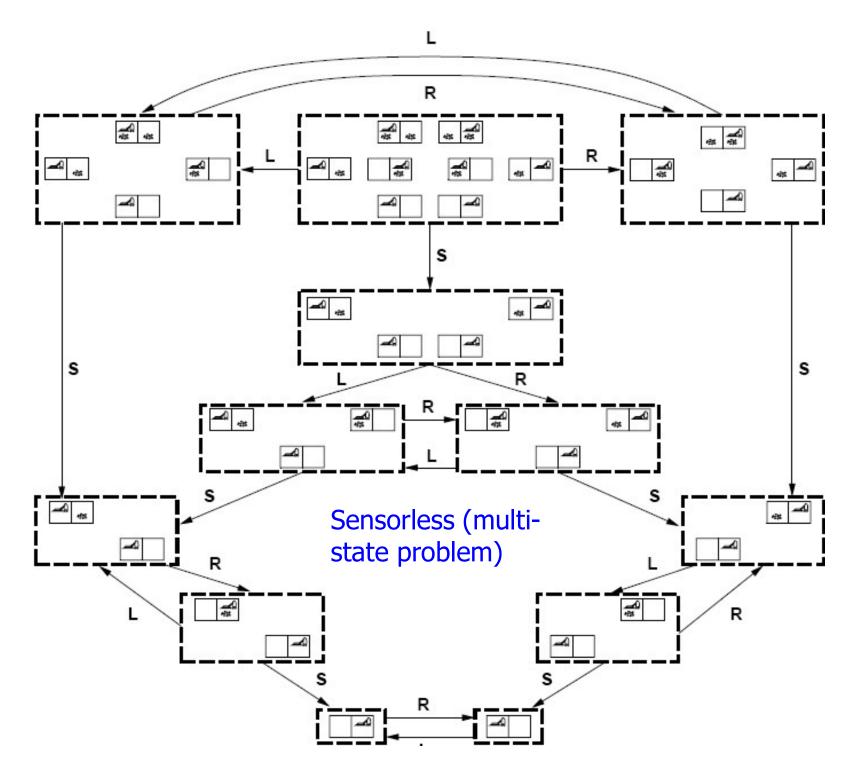








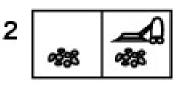


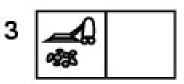


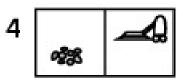
Contingency Problem

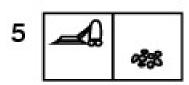
- Contingency, start in #5 & 7.
 - Nondeterministic: suck may dirty a clean carpet
 - local sensing: dirt, location only at current location
 - Solution?
 - Percept: [Left, Clean] → [Right, if dirty then Suck]



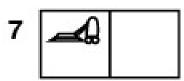














Exam 2

- Closed book and closed notes
- Coverage:
 - Informed Search
 - Local Search
- Format:
 - True/False
 - Short-Answer
 - Problem Solving

Informed Search

- Understand what is informed search
- Understand best-first, greedy, and A*
- Understand the optimality and completeness of each search
- Be able to draw search tree
- Understand the heuristic function in A*, under what condition will A* be optimal?
 - Admissible heuristic
 - Consistent heuristic

Local Search

- Hill climbing (HC)
 - Steepest HC, stochastic HC, 1st choice HC, random-restart HC
- HC with side-moves allowed
- Simulated annealing
- Local beam search
- Genetic algorithms
- Understand each search strategy
- Understand how to define the objective function for local search