

ELEC-2110

# Electric Circuit Analysis

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LAB SECTION: 002

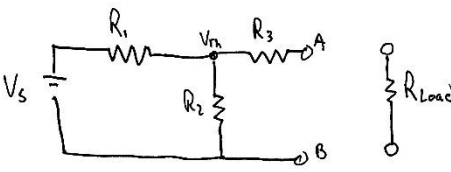
***Electrical Measurements:  
Thevenin Equivalent Circuits***

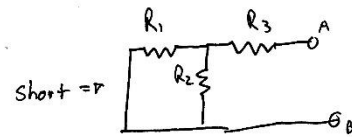
## Introduction

The Objective of this lab was to review and work with Thevenin's and Norton's theorems. We used black boxes with unknown circuits inside to test and confirm Thevenin's and Norton's theorems.

## Exercise 1

In exercise 1, we were asked to show the mathematical derivation for how we know the voltage at two nodes will be  $V_{OC}/2$  when a resistor,  $R_{load}$ , is connected to those nodes that is equal to  $R_{Th}$  [1]. Calculations shown in Calculations 1.



$$V_{Th} = \frac{V_s \times R_2}{R_1 + R_2}$$


$$R_{Th} = (R_1 \parallel R_2) + R_3$$

$$R_{Th} = \left( \frac{1}{R_1} + \frac{1}{R_2} \right)^{-1} + R_3$$

*Calculations 1*

## Exercise 2

In exercise 2, we were asked to measure and record the resistance between pin<sub>1</sub> - pin<sub>2</sub> and between pin<sub>2</sub> - pin<sub>3</sub> of your variable resistor [1]. The sum of both should be close to 10 kΩ. The data is shown in Table 1 below.

<b>Pin<sub>1</sub> &amp; Pin<sub>2</sub></b>	5.3345 k $\Omega$
<b>Pin<sub>2</sub> &amp; Pin<sub>3</sub></b>	4.7218 k $\Omega$
<b>Sum of Pins 1&amp;2 and Pins 2&amp;3</b>	10.0877 k $\Omega$

*Table 1*

### Exercise 3

In exercise 3, we were asked to experimentally determine the Thevenin equivalent circuit for the black box at terminals B1-B2. We were told to connect the 15V supply on the NI ELVIS Board to terminals A1-A2 as shown in the schematic in Figure. Turn on the component box and [1]

- Measure the voltage of the power supply on the NI ELIVIS Board
- Measure the voltage at terminals B1 - B2, which would be  $V_{oc}$ .
- Calculate  $V_{oc}/2$
- Measure the voltage drop across the variable resistor as you vary its resistance.
- Measure the variable resistor's resistance, which is  $R_{Th}$ .

Each of these steps will be repeated for each unknown circuit box, so they will be labeled accordingly below. The voltage from the Elvis board will be constant ( $V_s = 15.656V$ ).

<b><math>V_s</math></b>	15.629 V
<b><math>V_{oc}</math></b>	15.567 V
<b><math>V_{oc}/2</math></b>	7.7835 V
<b><math>R_{TH}</math></b>	2.0007 k $\Omega$

*Box 1 Measured Data*

<b><math>V_{oc}</math></b>	5.2065 V
<b><math>V_{oc}/2</math></b>	2.60325 V
<b><math>R_{Th}</math></b>	5.3168 k $\Omega$

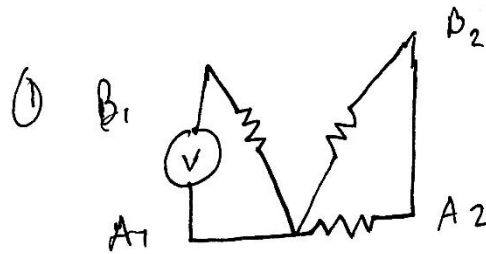
*Box 2 Measured Data*

<b><math>V_{oc}</math></b>	-3.1250
<b><math>V_{oc}/2</math></b>	-1.5625
<b><math>R_{Th}</math></b>	1.1974

*Box 3 Measured Data*

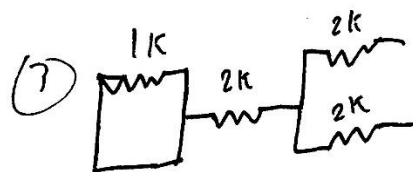
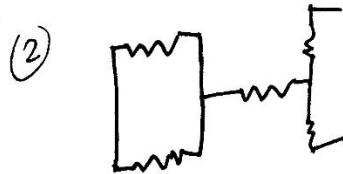
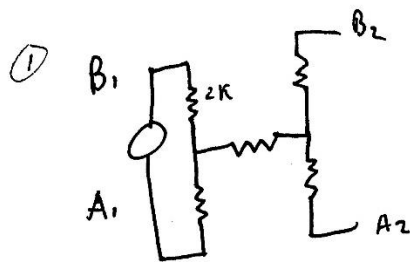
## Exercise 4

In exercise 4, we were asked to open the boxes of unknown circuits, draw the circuits with Thevenin and Norton equivalent. We then used the equivalent circuits to calculate [1]. Each circuit is labeled for the appropriate box. (*Note that each resistor is 2k $\Omega$  and  $V_s$  is 15.656 V*)



$$R_{Th} = 1k\Omega$$

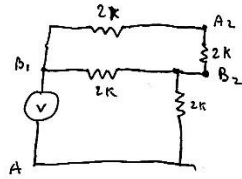
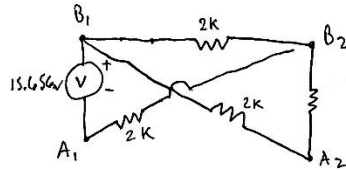
*Circuit and  $R_{Th}$  for Box 1*



$$R_{Th} = 5.32 \text{ k}\Omega$$

*Circuit and  $R_{th}$  for Box 2*

(Circuit 3)

Thevenin

$$V_{B_1 B_2} = 15.656 \frac{(4k \parallel 2k)}{2k + (4k \parallel 2k)}$$

$$= 15.6 \times \left( \frac{\frac{4}{3}k}{\frac{4}{3}k + 2k} \right) = 6.2468V$$

$$V_{A_2 B_2} = V_{B_1 B_2} \times \frac{2k}{2k + 2k} = 3.123V$$

$$V_{oc} = V_{B_2 A_2} = -V_{A_2 B_2} = -3.1234V$$

$$R_{Th} = 2k \parallel (2k + 2k \parallel 2k)$$

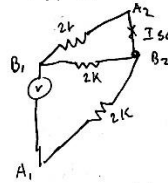
$$= 2k \parallel (2k + 1k)$$

$$= 2k \parallel 3k$$

$$R_{Th} = 1.2k$$

Norton

$$V_{B_1 A_1} \approx 15.6V$$



$$I_{sc} = \frac{-V_{B_1 B_2}}{2k}$$

$$V_{B_1 B_2} = 15.6 \cdot \frac{1k}{1k + 2k} = 5.20V$$

$$I_{sc} = \frac{-V_{B_1 B_2}}{2k} = \frac{-5.2056}{2k}$$

$$I_{sc} = -2.6028A$$

Circuit,  $I_{sc}$  and  $R_{th}$  for Box 3

## Exercise 5

In exercise 5, we were asked knowing what we do about this specific black box, is it possible to measure the Thevenin resistance at B1-B2 directly from the black box?

The answer is yes, we are able to measure  $R_{Th}$  directly when we short circuit terminals a1 and b1.

## Conclusion

This lab was used as an overview of Thevenin's and Norton's theorem. We were given circuits and asked to calculate various things using Thevenin equations and then verify it through Multisim. I did have some struggles with this lab. The TA helped explain some things before we started so the lab was clearer.



# Bibliography

[1] Nelms, R. Mark, and Elizabeth Devore. *Recitation & MultiSim: Thevenin's and Norton's Theorems*. 2016, p. 5, Accessed 12 Feb 2020.