

# Basic Principles of Wireless Networks (I)

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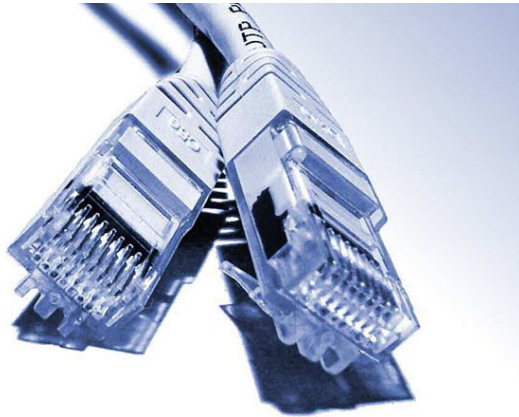
*Based on slides prepared by Nima Seifi at Chalmers, based on slides from P. Viswanath/Tse, A. Goldsmith, Shiv Kalyanaraman, Tae Hyun Kim, David Gesbert & textbooks by Tse/Viswanath, A. Goldsmith, J. Andrews et al.*

# Outline

- Wireless channel
- Physical layer
- Mitigating the wireless channel impairments
  - Equalization
  - Spread spectrum
  - Multicarrier modulation and OFDM
  - Antenna solutions
- Multi-antenna techniques

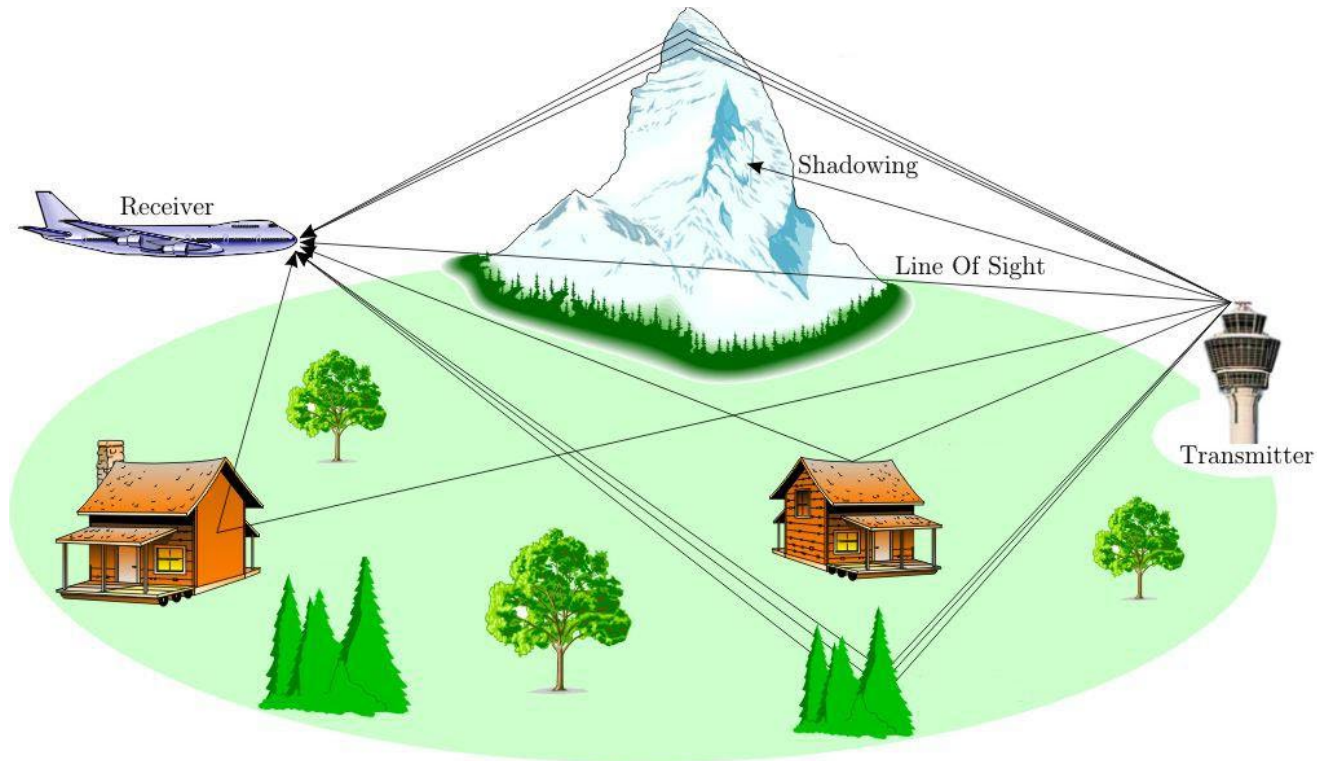
# Wireless Channel

# Wireless Channel is Very Different!



Wired	Wireless
Each cable is a different channel	One media (cable) shared by all
Signal attenuation is low	High signal attenuation
Small (no) interference	High interference noise; co-channel interference; adjacent channel interference

# Wireless Multipath Channel

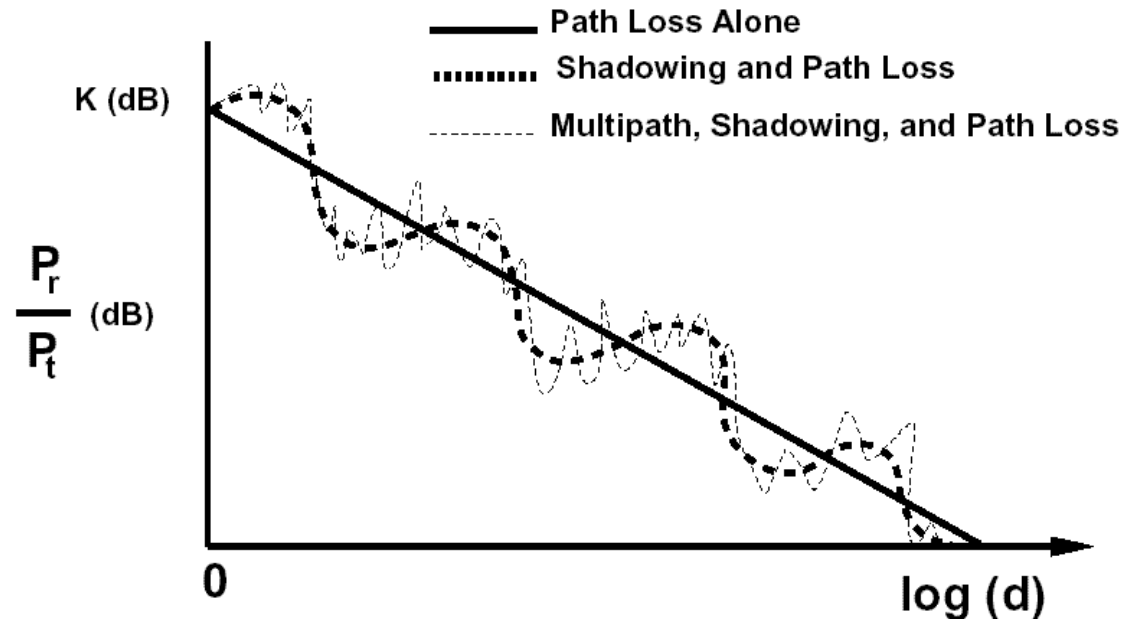


Channel varies at two spatial scales:

- Large scale fading: path loss, shadowing
- Small scale fading: Multi-path fading, Doppler

# Path Loss, Shadowing, Fading

- Variable decay of signal due to environment, multipaths, mobility



Source: A. Goldsmith book

# Path Loss Modeling

- Maxwell's equations
  - Complex and impractical
- Free space path loss model
  - Too simple
- Ray tracing models
  - Requires site-specific information
- Empirical Models
  - Don't always generalize to other environments
- Simplified power falloff models
  - Main characteristics: good for high-level analysis
  - A simple model for path loss,  $L$ , is

$$L = \frac{\bar{P}_r}{P_t} = K \left( \frac{d_0}{d} \right)^\gamma$$

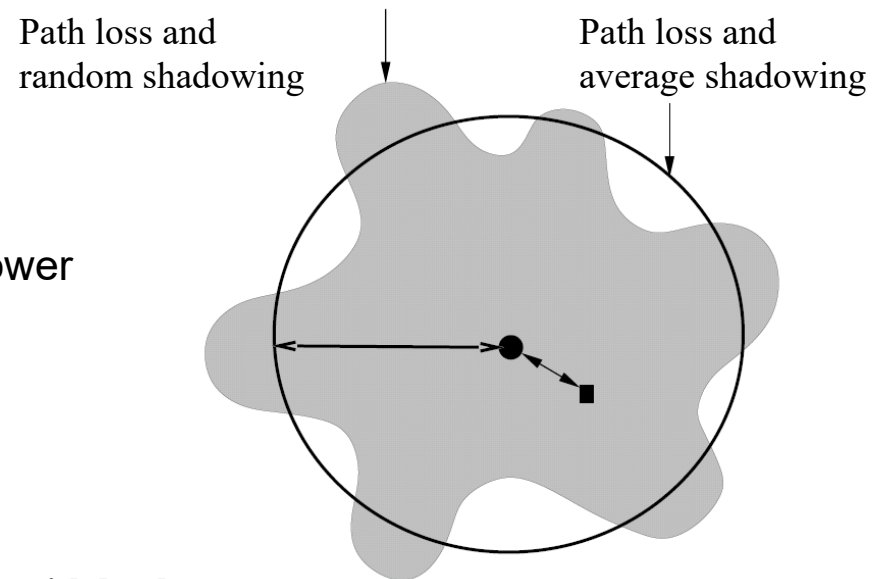
- $\gamma$  is the path loss exponent
- $P_t$  transmit power
- $\bar{P}_r$  local mean receive power
- $d_0$  reference distance
- $d$  transmit-receive distance
- $K$  transmission constant

# Shadowing

- The received signal is shadowed by obstructions such as hills and buildings.
- This results in variation in the local mean received signal power

$$P_r(dB) = \bar{P}_r(dB) + \chi \quad \text{where } \chi \sim \mathcal{N}(0, \sigma), 4 \leq \sigma \leq 10 \text{ dB}$$

- Implications:
  - nonuniform coverage
  - increases the required transmit power



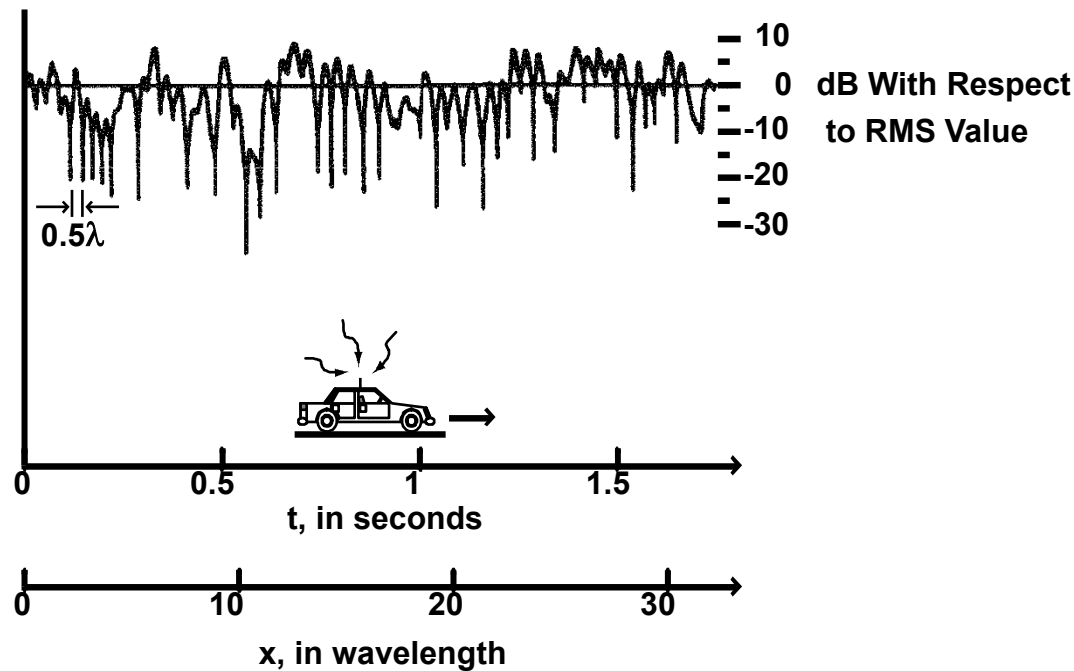
Source: A. Goldsmith book

Figure 2.10: Contours of Constant Received Power.



# Small-scale Multipath fading

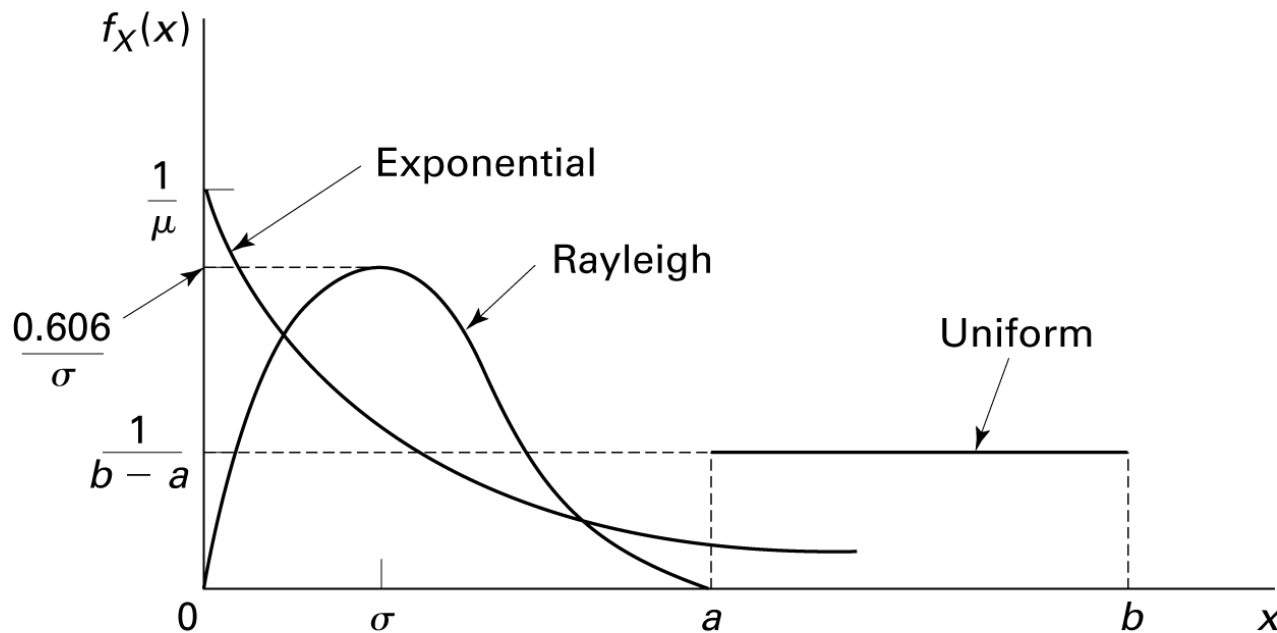
- Multipath fading due to **constructive** and **destructive** interference of the transmitted waves.



# Single-Tap Channel: Rayleigh Fading

- Path loss, shadowing => average signal power loss
  - Fading around this average.
  - Subtract out average => fading modeled as a zero-mean random process
- Narrowband Fading channel: Each symbol is long in time
- Fading w/ many scatterers: Central Limit Theorem
  - In-phase (cosine) and quadrature (sine) components of the snapshot  $r(0)$ , denoted as  $r_I(0)$  and  $r_Q(0)$  are independent Gaussian random variables.
  - Envelope Amplitude:  $|r| = \sqrt{r_I^2 + r_Q^2}$  is Rayleigh,
  - Received Power:  $|r|^2 = r_I^2 + r_Q^2$  is exponentially distributed.

# Normal Vector R.V, Rayleigh, Chi-Squared



The rayleigh, exponential, and uniform pdf 's.

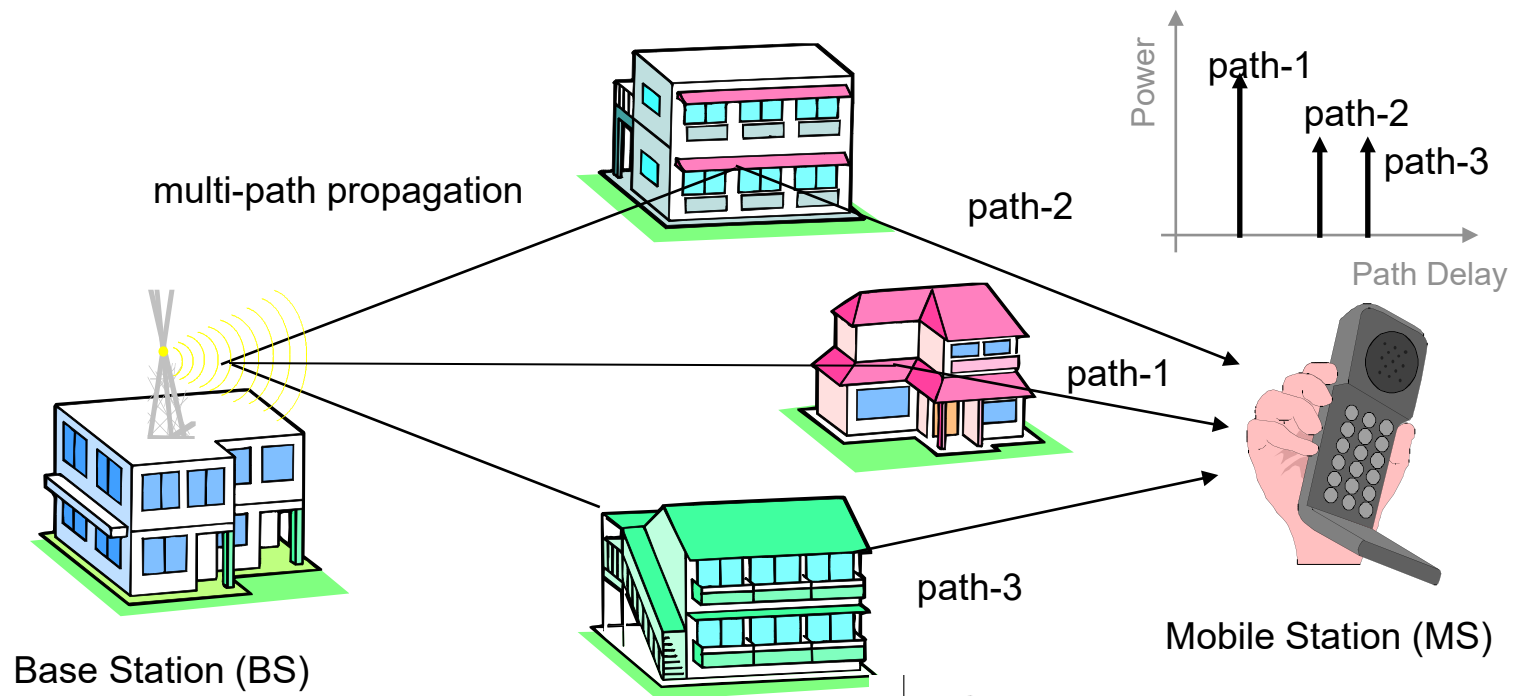
$X = [X_1, \dots, X_n]$  is **Normal random vector**

$\|X\|$  is **Rayleigh** { eg: magnitude of a complex gaussian channel  $X_1 + jX_2$  }

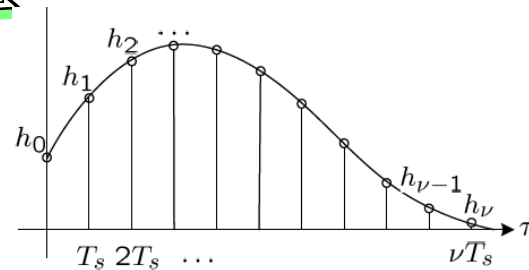
$\|X\|^2$  is **Chi-Squared w/  $n$ -degrees of freedom**

When  $n = 2$ , chi-squared becomes **exponential**. {eg: power in complex gaussian channel: sum of squares...}

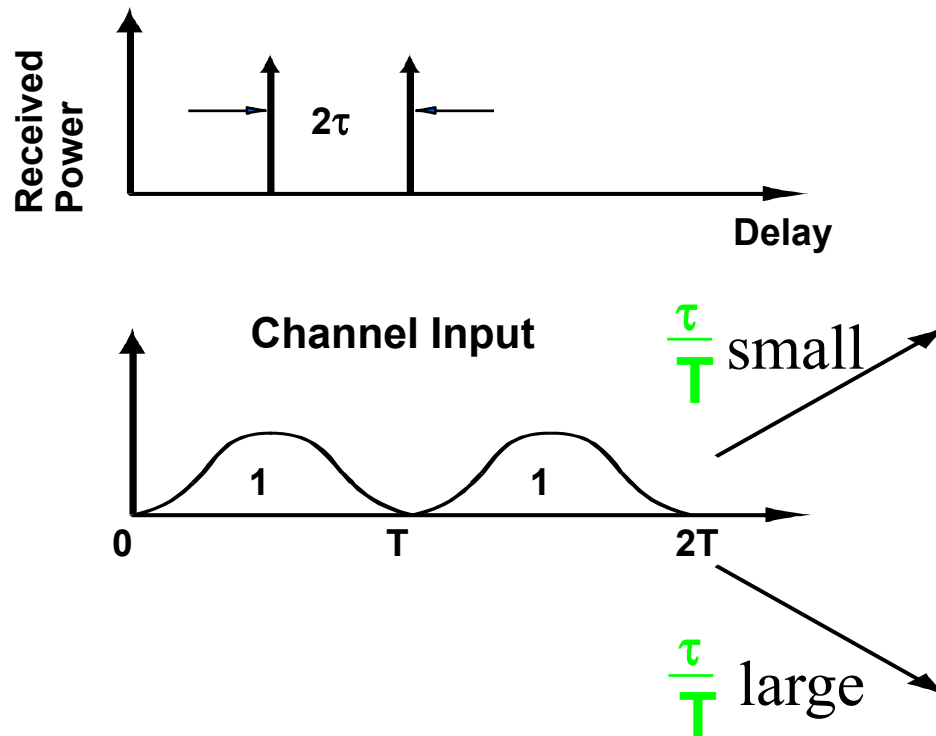
# Multipaths: Power-Delay Profile



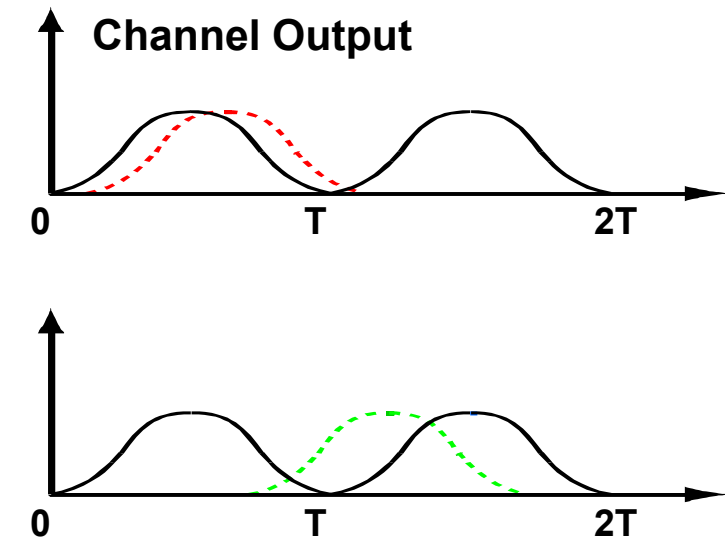
**Channel Impulse Response:**  
Channel amplitude  $|h|$  correlated at delays  $\tau$ .  
Each “tap” value @  $kT_s$  Rayleigh distributed  
(actually the sum of several sub-paths)



# Delay Spread: Time Domain Interpretation



Two-ray model  
 $\tau$  = rms delay spread



- $\frac{\tau}{T}$  small  $\Rightarrow$  negligible intersymbol interference
- $\frac{\tau}{T}$  large  $\Rightarrow$  significant intersymbol interference, which causes an irreducible error floor

# Dispersion-Selectivity Duality

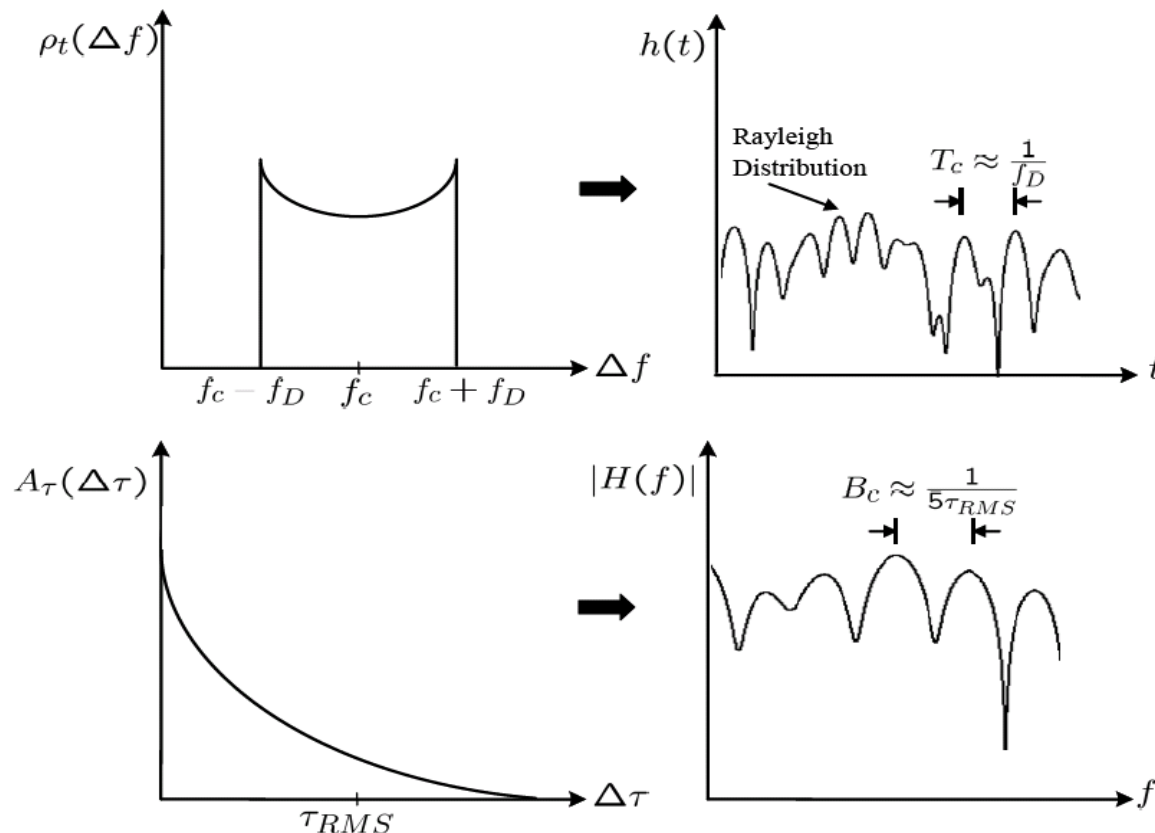


Figure 3.18: The shape of the Doppler power spectrum  $\rho_t(\Delta f)$  determines the correlation envelope of the channel in time (top). Similarly, the shape of the multipath intensity profile  $A_\tau(\Delta\tau)$  determines the correlation pattern of the channel frequency response (bottom)

# Fading: Jargon

- **Flat fading**: no multipath ISI effects.
  - Eg: narrowband, indoors
- **Frequency-selective fading**: multipath ISI effects.
  - Eg: broadband, outdoor.
- **Slow fading**: no Doppler effects.
  - Eg: indoor Wi-fi home networking
- **Fast Fading**: Doppler effects, time-selective channel
  - Eg: cellular, vehicular
  - Doppler: *not an LTI system*
- Broadband cellular + vehicular => Fast + frequency-selective

# Summary of Wireless Channel

- We have discussed the concepts of path loss, shadowing, fading (multipath, Doppler), and some of their design impacts.
- We have discussed how time and frequency selectivity of wireless channels depend on key physical parameters.



# Physical Layer

# Physical Layer Issue

- **Link Performance Measures**
- **Modulation Tradeoffs**
- **Flat Fading Countermeasures**
- **Delay Spread Countermeasures**

# Link Performance Measures

## PROBABILITY OF BIT/ BLOCK ERROR

- The bit error probability (BER),  $P_b$ , in a radio environment is a random variable.
  - Average  $P_b$ ,  $\overline{P_b}$
  - Outage  $P_b$ ,  $P_{out} = \Pr[P_b > P_{b,target}]$
- Similarly, the block error probability (BLER),  $P_{bl}$ , in a radio environment is a random variable.
  - Average  $P_{bl}$ ,  $\overline{P_{bl}}$
  - Outage  $P_{bl}$ ,  $P_{out} = \Pr[P_{bl} > P_{bl,target}]$

# Link Performance Measures

## EFFICIENCY

- Spectral Efficiency
  - A measure of data rate per unit bandwidth for a given bit error probability and transmitted power.
- Power Efficiency
  - A measure of required transmit power to achieve a given data rate for a given bit error probability and bandwidth.

# What is Modulation?

- Encoding information in a manner suitable for transmission.
  - Translate baseband source signal to bandpass signal
  - Bandpass signal: “modulated signal”
- How?
  - Vary amplitude, phase or frequency of a carrier
- Demodulation
  - Extract baseband message from carrier

# Digital Modulation

- Any modulated signal can be represented as

$$s(t) = A(t) \cos [\omega_c t + \phi(t)]$$

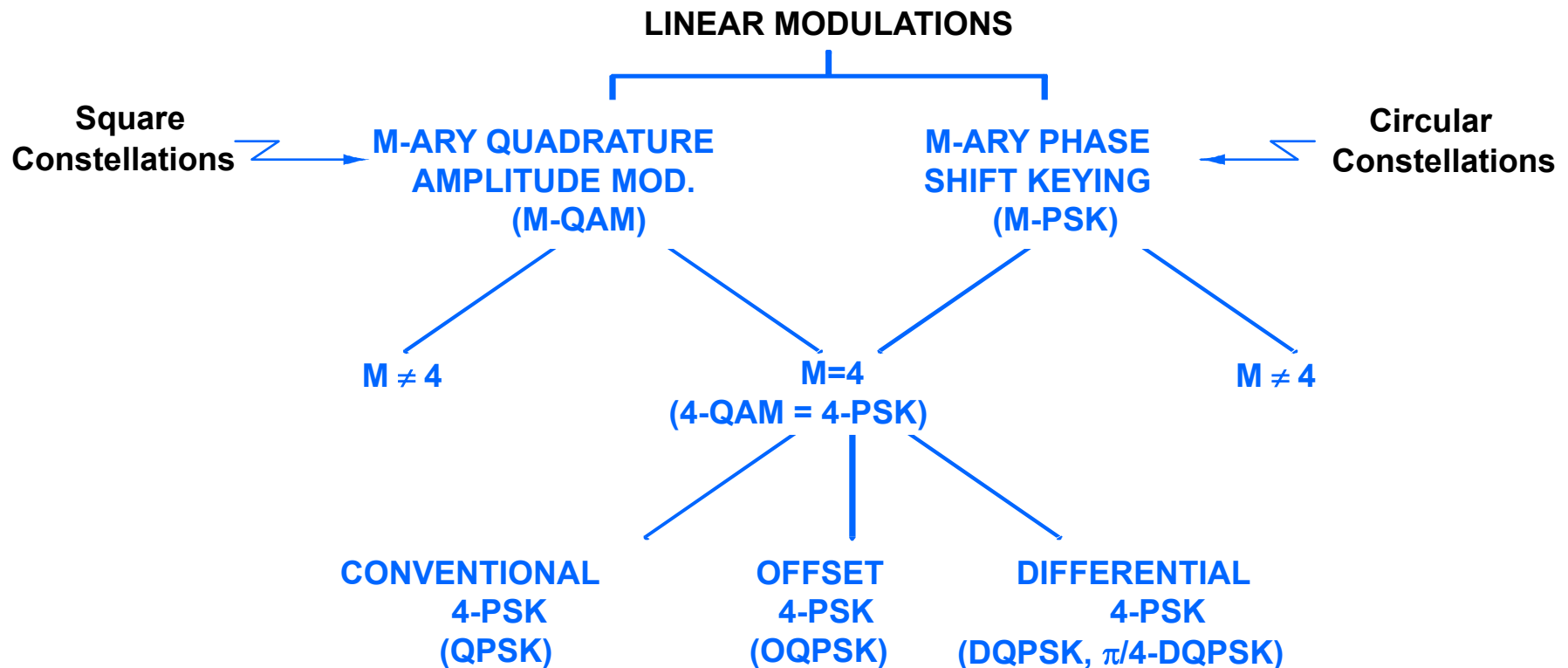
↑                      ↑  
amplitude   phase or frequency

$$= \underbrace{A(t) \cos \phi(t)}_{\text{in-phase}} \cos \omega_c t - \underbrace{A(t) \sin \phi(t)}_{\text{quadrature}} \sin \omega_c t$$

- Linear versus nonlinear modulation
- Constant envelope versus non-constant envelope

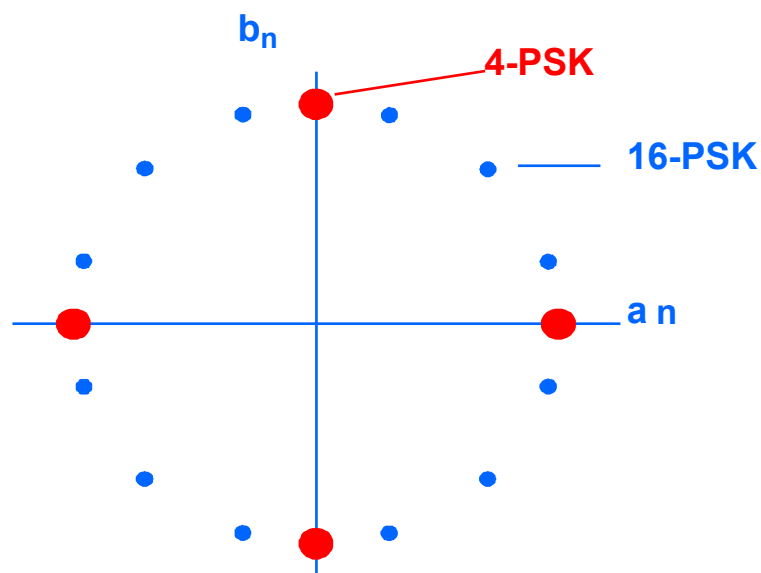
# Linear Modulation Techniques

$$s(t) = \underbrace{\left[ \sum a_n g(t-nT) \right]}_{I(t), \text{ in-phase}} \cos \omega_c t - \underbrace{\left[ \sum b_n g(t-nT) \right]}_{Q(t), \text{ quadrature}} \sin \omega_c t$$

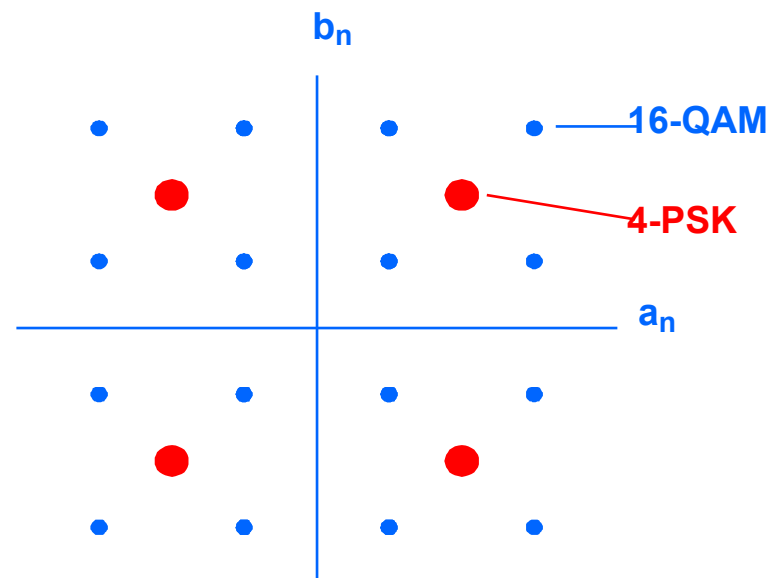


# Signal Constellation

## M-PSK (Circular Constellations)



## M-QAM (Square Constellations)

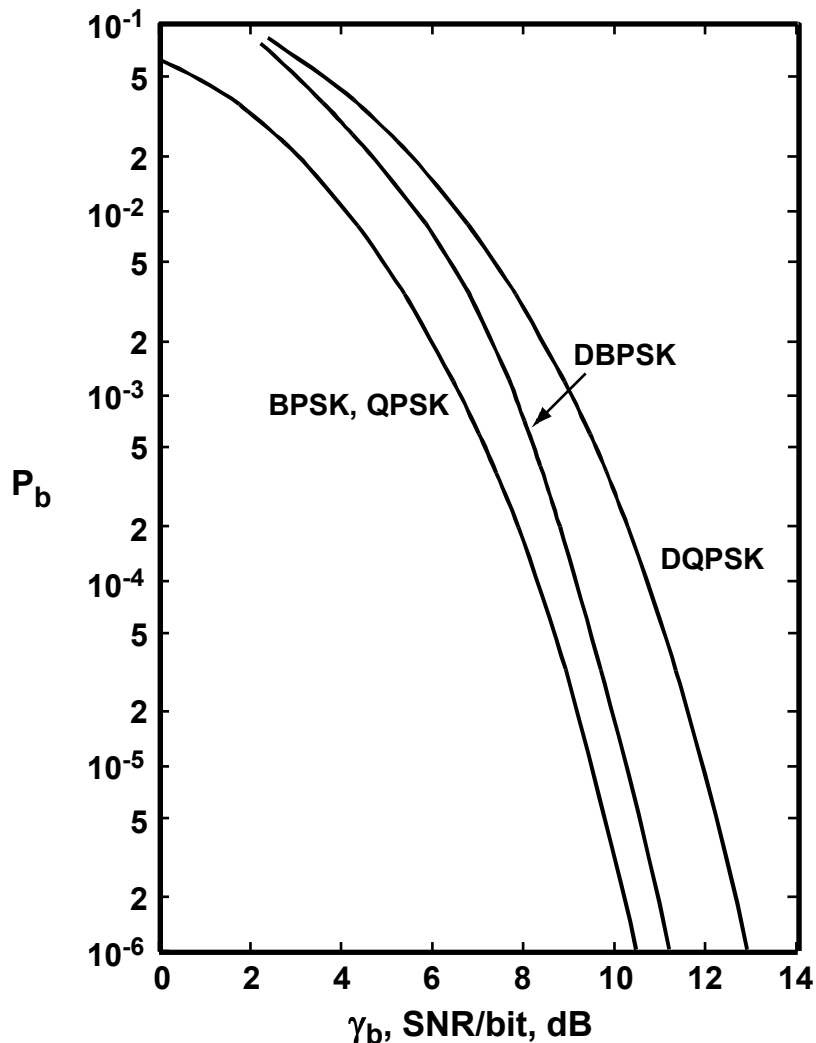




# Demodulation

- Coherent detection requires a coherent phase reference.
  - difficult to obtain in a rapidly fading environment
  - increases receiver complexity
- Differential detection uses the previous symbol for the reference signal.
  - eliminates need for coherent reference
  - Doppler causes irreducible error floor, typically small for high bit rates

# Bit Error Rate (BER): AWGN



For  $P_b = 10^{-3}$

BPSK 6.5 dB

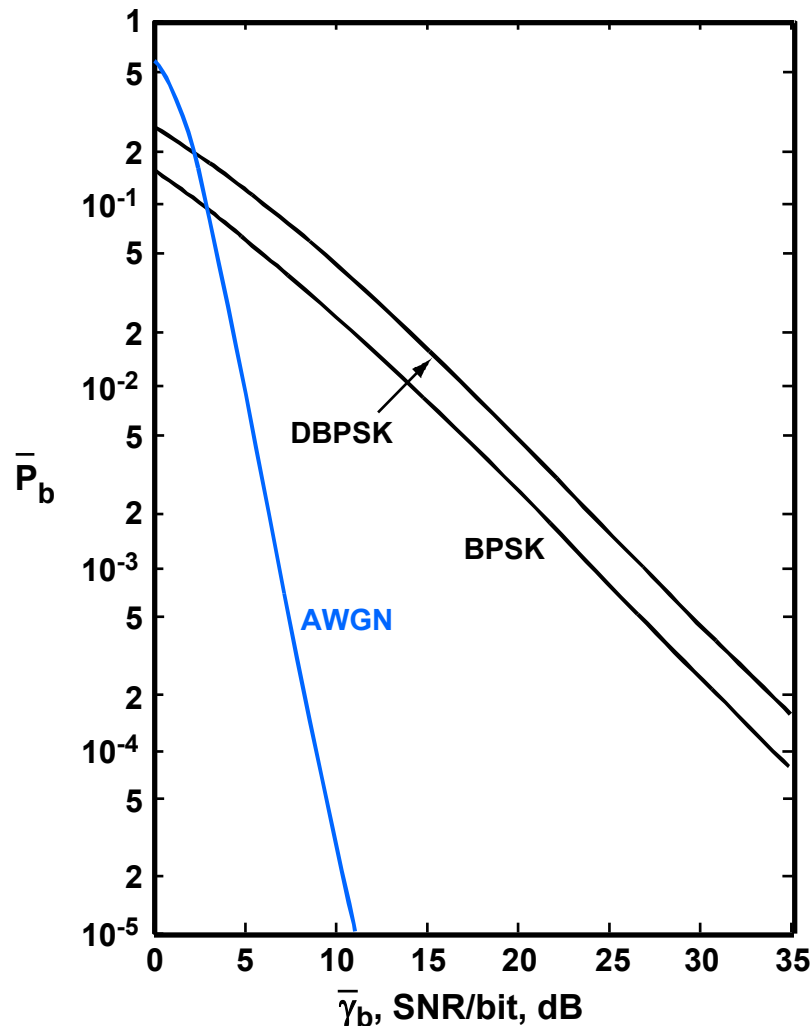
QPSK 6.5 dB

DBPSK ~8 dB

DQPSK ~9 dB

- QPSK is more spectrally efficient than BPSK with the same performance.
- There is a ~3 dB power penalty for differential detection.

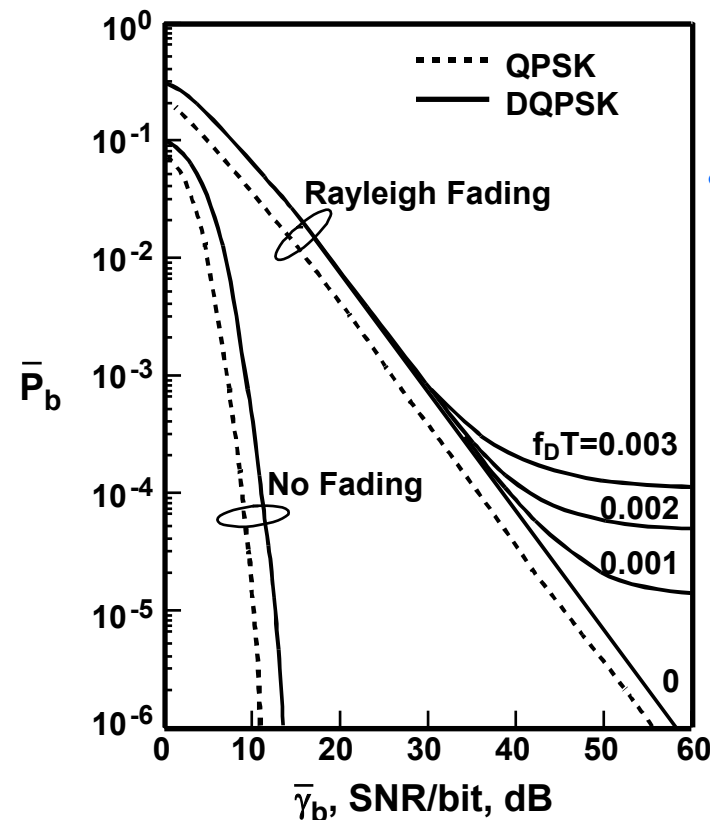
# Bit Error Rate (BER): Fading Channel



- $\bar{P}_b$  is inversely proportion to the average SNR per bit.
- Transmission in a fading environment requires about 18 dB more power for  $\bar{P}_b \approx 10^{-3}$ .

# Bit Error Probability (BER): Doppler Effects

- Doppler causes an irreducible error floor when differential detection is used  $\Rightarrow$  decorrelation of reference signal and distortion of signal shape.



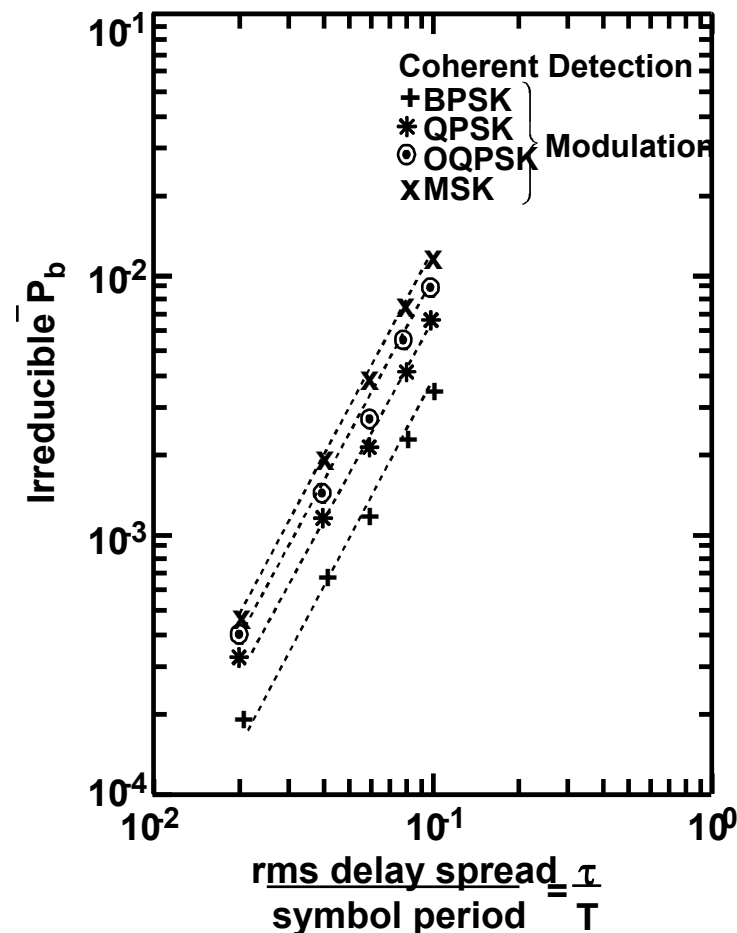
- The irreducible  $\bar{P}_b$  depends on the data rate and the Doppler. For  $f_D = 80$  Hz,

data rate	T	$\bar{P}_{b\text{floor}}$
10 kbps	$10^{-4}$ s	$3 \times 10^{-4}$
100 kbps	$10^{-5}$ s	$3 \times 10^{-6}$
1 Mbps	$10^{-6}$ s	$3 \times 10^{-8}$

The implication is that Doppler is not an issue for high-speed wireless data.

[M. D. Yacoub, *Foundations of Mobile Radio Engineering*, CRC Press, 1993]

# Bit Error Probability (BER): Delay Spread



- ISI causes an irreducible error floor.
- The rms delay spread imposes a limit on the maximum bit rate in a multipath environment.

For example, for QPSK,

	$\tau$	Maximum Bit Rate
Mobile (rural)	25 $\mu$ sec	8 kbps
Mobile (city)	2.5 $\mu$ sec	80 kbps
Microcells	500 nsec	400 kbps
Large Building	100 nsec	2 Mbps

[J. C.-I. Chuang, "The Effects of Time Delay Spread on Portable Radio Communications Channels with Digital Modulation," *IEEE JSAC*, June 1987]

# Summary of Modulation Issues

- Tradeoffs
  - linear versus nonlinear modulation
  - constant envelope versus non-constant envelope
  - coherent versus differential detection
  - power efficiency versus spectral efficiency
- Limitations
  - flat fading
  - Doppler
  - delay spread