

Homework 3

Problem 1. (30 points) Estimate the space usage of the Reuters dictionary with blocks of size $k = 8$ and $k = 16$ in blocked dictionary storage.

Solution:

As $K=8$, We will have: $(8 - 1) * 3 = 21$ bytes for term pointer.

We need additional $K=8$ for term length so space reduced by 13 bytes per 8 term block.

Total Space reduced = $4\,000\,000 * \frac{13}{8} = 0.65$ MB

Total Space is: $7.6 - 0.65 = 6.95$ MB

As $K=16$ then,

We will have : $(16 - 1) * 3 = 45$ bytes for term pointer.

Need additional $K=16$ for term length so space reduced by 29 bytes per 16 term block.

Problem 2. (35 points) For $n = 15$ splits, $r = 10$ segments, and $j = 3$ term partitions, how long would distributed index creation take for Reuters-RCV1 in a MapReduce architecture? Base your assumptions about cluster machines on Table below.

Symbol	Statistic	Value
s	average seek time	$5ms = 5 \times 10^{-3}s$
b	transfer time per byte	$0.02\mu s = 2 \times 10^{-8}s$
	processor?? clock rate	$10^9 s^{-1}$
p	lowlevel operation(e.g., compare & swap a word)	$0.01\mu s = 10^{-8}s$
	size of main memory	several GB
	size of disk space	1TB or more

Solution:

For Map-Reduce distributed index creation, Number of splits = 15

Number of machines = 10

Number of partitions = 3

Size of a split Reuters RCV1 to be parsed = $\frac{800}{15}$ MB

MAP Phase: 10 machines process simultaneously

Time spent by a machine = $\frac{800}{15} * 10^6$ bytes * $(10^{-7}(\text{reading}) + 10^{-7}(\text{comparison op.})) \frac{s}{\text{byte}} \approx 10s$

Time to parse entire data = $10 * 2$ (2 stages of MAP phase are required) = 20 s

REDUCE Phase:

For Reuters-RCV1, Number of postings per inverter = $\frac{100}{3}$ million
 For an inverter, Time spent in reading = $\frac{800}{3} * 10^6 \text{ bytes} * 10^{-7} s/bytes \approx 26s$
 Time spent in sorting = $(\frac{100}{3} * 10^6) * \log(\frac{100}{3} * 10^6) * 10^{-7} = 83s$
 Size of the index to be written = $(\frac{4*10^5}{3} * 4) + (\frac{100*10^6}{3} * 4) = \frac{4}{3} * 10^8$
 Time spent in Writing = $\frac{4}{3} * 10^8 \text{ bytes} * 10^{-7} s/bytes = 13s$
 Total Time in Distributed Index Creation = $20+26+83+13 = 162s \approx 3 \text{ min}$

Problem 3. (35 points) Assume that machines in MapReduce have 100 GB of disk space each. Assume further that the postings list of the term the has a size of 200 GB. Then the MapReduce algorithm as described cannot be run to construct the index. How would you modify MapReduce so that it can handle this case?

Solution:

We can partition it by DOC_ID as well as term for very frequent terms