

Problem Name: Check whether a given number is even or odd DSA???

Step 01:

Approach: By Finding the Basic Remainder....?
Code and its time complexity.

Time Complexity:

- `input()` → Constant time, **O(1)**
- `int()` → Converting a string to an integer takes time **O(1)** (assuming reasonably small input).
- `num % 2` → Modulo operation is a basic arithmetic operation → **O(1)**
- `if...else + print()` → Both are constant-time operations → **O(1)**

Final Time Complexity:

✓ **O(1)** — constant time.

This means the program runs in the same amount of time regardless of the input size.

📦 **Space Complexity:**

Also **O(1)** — only one variable (`num`) is used.

Let me know if you'd like this explained in Bengali or need it for a larger set of numbers (like checking even/odd in a list).

✓ **Common Time Complexities:**

Complexity	Name	Example	Explanation
$O(1)$	Constant Time	Checking a single number <code>if num % 2 == 0</code>	The operation runs once no matter the input size.
$O(n)$	Linear Time	Checking all elements in a list	Time increases directly with the input size.

Complexity	Name	Example	Explanation
$O(n^2)$	Quadratic Time	Nested loops (a loop inside a loop)	If input doubles, time increases four times.
$O(\log n)$	Logarithmic Time	Binary search	Time increases slowly even if input size increases a lot.
$O(n \log n)$	Linearithmic Time	Merge Sort	Some efficient sorting algorithms run in this time complexity.

Step 02:

Approach: By Finding the Remainder....?

Logic Used:

Approach: By Finding the Remainder

- $n \% 2 \rightarrow$ This operation finds the remainder when n is divided by 2
- If the remainder is 0, then n is **even**
- If the remainder is 1, then n is **odd**

This method is **mathematically accurate** and **computationally efficient**.

Time Complexity Analysis:

Let's analyze each part of the code:

Line	Operation	Time Complexity	Reason
<code>input()</code>	Takes user input	$O(1)$	Constant time to read input
<code>int()</code>	Converts string to int	$O(1)$	Simple type conversion

Line	Operation	Time Complexity	Reason
<code>n % 2</code>	Modulo operation	$O(1)$	Basic arithmetic operation
<code>print()</code>	Displays result	$O(1)$	Constant time

✓ **Final Time Complexity:** $O(1)$

It runs in **constant time**, no matter what number you input.

📦 **Space Complexity:**

- Only one variable `n` is used → so space usage is constant.

✓ **Final Space Complexity:** $O(1)$

📌 **Summary:**

Metric	Value
Time Complexity	$O(1)$
Space Complexity	$O(1)$
Approach Used	By checking remainder using modulo <code>%</code>
Efficient?	✓ Yes, it's the most efficient method for this task

Step 03:

Approach: Using Bitwise AND Operator...?

Logic Behind Bitwise AND

- Binary of **even** numbers always ends with 0
Example: $4 \rightarrow 100$, $10 \rightarrow 1010$
- Binary of **odd** numbers always ends with 1
Example: $5 \rightarrow 101$, $11 \rightarrow 1011$

So, when you do $n \ \& \ 1$:

- For even: $n \ \& \ 1 \rightarrow 0$
- For odd: $n \ \& \ 1 \rightarrow 1$

✦ Example:

- $n = 6 \rightarrow$ binary: 110
 $6 \ \& \ 1 = 0 \rightarrow$ even
- $n = 7 \rightarrow$ binary: 111
 $7 \ \& \ 1 = 1 \rightarrow$ odd

Time Complexity Analysis:

Line	Operation	Time Complexity	Why?
<code>input()</code>	Take input from user	O(1)	One-time user input
<code>int()</code>	Convert input to integer	O(1)	Constant time conversion
<code>n & 1</code>	Bitwise AND operation	O(1)	Direct binary operation
<code>print()</code>	Output result	O(1)	Constant time printing

✓ Final Time Complexity: **O(1)** (Constant Time)

- The program's speed does **not** depend on the size of the number.
- Bitwise operations are extremely fast and always take constant time.

📦 Space Complexity:

- Only one variable n is used.

- So, **Space Complexity:** $O(1)$

Summary:

Metric	Value
Approach	Bitwise AND Operator
Time Complexity	$O(1)$
Space Complexity	$O(1)$
Efficient?	✓ Yes – Bitwise ops are very fast
Why it works	Because LSB (least significant bit) of odd = 1, even = 0

Step 04:

Approach: Using Bitwise Shift Operators

Logic Used: Using Bitwise Shift Operators

- $n \gg 1$: This shifts all bits of n **one place to the right** (i.e., divides the number by 2 and drops the remainder).
- $n \ll 1$: This shifts all bits **one place to the left** (i.e., multiplies the number by 2).

✓ Explanation with Example:

Let's say:

Check Number is Even or Odd using Bitwise Shift Operator

<u>Odd Number</u>			<u>Even Number</u>		
Number = 11	1 0 1 1		Number = 4	0 1 0 0	
Number >> 1	0 1 0 1	1 is popped out	Number >> 1	0 0 1 0	0 is popped out
Number << 1	1 0 1 0	0 is pushed in	Number << 1	0 1 0 0	0 is pushed in
Number = 9	1 0 0 1		Number = 14	1 1 1 0	
Number >> 1	0 1 0 0	1 is popped out	Number >> 1	0 1 1 1	0 is popped out
Number << 1	1 0 0 0	0 is pushed in	Number << 1	1 1 1 0	0 is pushed in
Initial number ≠ Final number			Initial number = Final number		
This bitwise operation ensures that only even numbers remain because shifting right (>>) removes the last bit (whether it's 0 or 1), and shifting left (<<) fills in a 0 by default.					

So the logic is:

- For **even** numbers: shifting right then left gives back the original number
- For **odd** numbers: you lose the 1-bit on the right, so the number changes

Time Complexity Analysis

Operation	Time Complexity	Why?
input()	$O(1)$	Constant-time user input
int()	$O(1)$	Simple type conversion
n >> 1 and << 1	$O(1)$	Bitwise shift = constant time
== comparison	$O(1)$	Just one comparison
print()	$O(1)$	Prints output once

✓ Final Time Complexity: $O(1)$

(Independent of input size)

Space Complexity

- You're only using one integer variable (n), and a few temporary values during the comparison.

✓ Space Complexity: $O(1)$ (Constant)

Summary Table:

Aspect	Details
Approach	Bitwise shift (right → left)
Time Complexity	$O(1)$
Space Complexity	$O(1)$
Efficiency	✓ Very fast – bitwise ops are CPU-level fast
Why It Works	Only even numbers retain value after $\gg 1$ then $\ll 1$

Bonus Tip:

Your function name has a small typo: `chack_odd_even`
Correct spelling: `check_odd_even`

```
python
CopyEdit
def check_odd_even(n):
    return n == (n >> 1) << 1
```