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367 HW 4

① i) $E(x) = (0)(.54) + (1)(.16) + 2(.06) + 3(.04) + 4(.20) = \boxed{1.2}$

ii) $V(x) = (0)^2(.54) + (1)^2(.16) + 2^2(.06) + (3^2)(.04) + 4^2(.20)$
 $= 3.96$

$$V(x) = 3.96 - [E(x)]^2 = 3.96 - (1.2)^2$$
$$= \boxed{2.52}$$

② i) $E(x) = (1)(.05) + 2(.10) + (3)(.12) + (4)(.30) +$
 $5(.30) + 6(.11) + 7(.01) + 8(.01)$
 $= \boxed{4.12}$

ii) $V(x) = (1)^2(.05) + (2)^2(.10) + (3)^2(.12) + (4)^2(.30) +$
 $5^2(.30) + (6)^2(.11) + (7)^2(.01) + (8)^2(.01)$
 $= 18.92$

$$V(x) = 18.92 - [E(x)]^2 = 18.92 - (4.12)^2$$
$$= \boxed{1.94}$$

iii) $P(x \leq 5) = P(1) + P(2) + P(3) + P(4) + P(5)$
 $.05 + .10 + .12 + .30 + .30$
 $= \boxed{.87}$

iv) $P(x > 3) = P(4) + P(5) + P(6) + P(7) + P(8)$
 $.30 + .30 + .11 + .01 + .01 = \boxed{.73}$

③

$$\begin{aligned} \text{i) } E(X) &= (0)(.073) + (1)(.117) + (2)(.258) \\ &\quad + (3)(.322) + (4)(.230) \\ &= \boxed{2.519} \end{aligned}$$

$$\begin{aligned} \text{ii) } V(X) &= (0)^2(.073) + (1)^2(.117) + (2)^2(.258) \\ &\quad + (3)^2(.322) + (4)^2(.230) \\ &= 7.727 - [E(X)]^2 = 7.727 - (2.519)^2 \\ &= \boxed{1.38} \end{aligned}$$

④

$$\begin{aligned} \text{i) } E(4X_1 + \pi X_2 + eX_3 + 13) \\ = 4(4) + 5(\pi) + 7(e) + 13 = \boxed{63.74} \end{aligned}$$

$$\text{ii) } E(X_1 X_3 + X_2) = (4)(7) + 5 = \boxed{33}$$

$$\begin{aligned} \text{iii) } V(\sqrt{2} X_2 + 3\sqrt{X_3} + 17) \\ = (\sqrt{2})^2 \left(\frac{1}{2}\right) + (\sqrt{3})^2 (\sqrt{2}) + (0)^2 = \boxed{5.24} \end{aligned}$$

↑ becomes a constant