

Multiclass SVC



$$f: \mathbb{R}^D \rightarrow \mathbb{R} \quad k \Rightarrow k\text{-classes}$$

$$W x_i + b = 0$$

$$W x_i + b = s$$

$$\begin{bmatrix} W_{11} & \dots & W_{1m} \\ \vdots & & \vdots \\ W_{k1} & \dots & W_{km} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_m \end{bmatrix} + \begin{bmatrix} b_1 \\ \vdots \\ b_m \end{bmatrix} = \begin{bmatrix} s_1 \\ s_2 \\ \vdots \\ s_k \end{bmatrix}$$

or

$s_1 \rightarrow \text{Car}$

$s_2 \rightarrow \text{horse}$

\vdots

$s_k \rightarrow k \text{ class}$

Scores for each class / Not necessary to add

$t_i \Delta$

Δ

$$S_j = f(X_j, w)_j$$

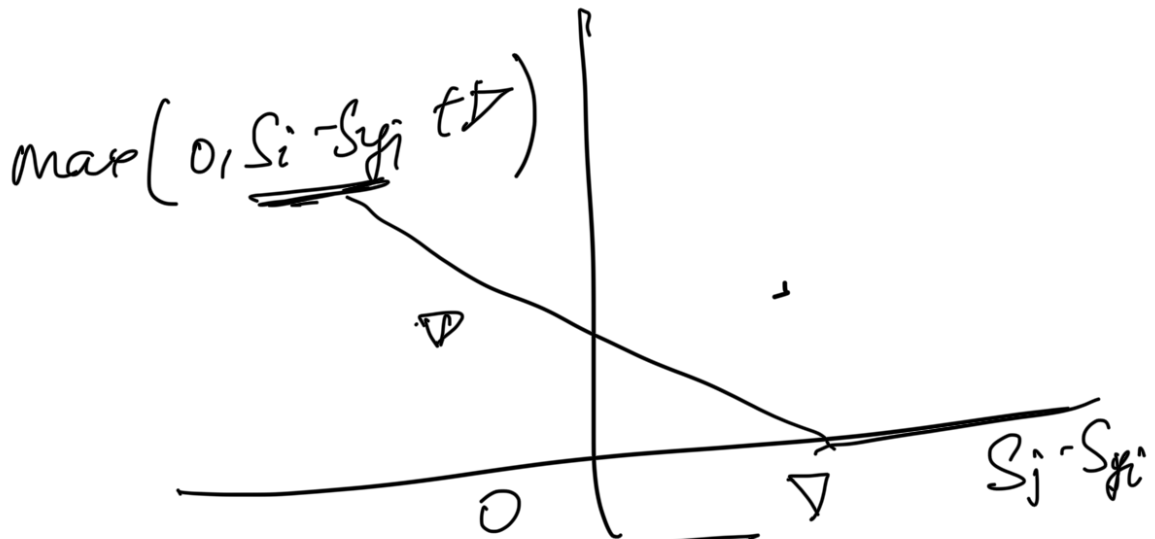
$$L_i = \sum_{j \neq y_i} \max(0, S_j - S_{y_i})$$

$D = 10$

$$S = [10, 20, 30, \dots, 20, 25]$$

$$S_{y_i} = 30 + 10$$

$$\max(0, 10 - 30) + \max(0, 20 - 30) + \dots$$



$$L = \max(0, 1 - y_i y_{pred})$$

Total Multi-class

$$L = \frac{1}{N} \sum_i \sum_{j \neq y_i} (\max(0, f(x_i, w) - \text{act}))$$

Total rows

$$L = \frac{1}{N} \sum_i L_i$$

$$+ \lambda \sum_k w_k^2$$

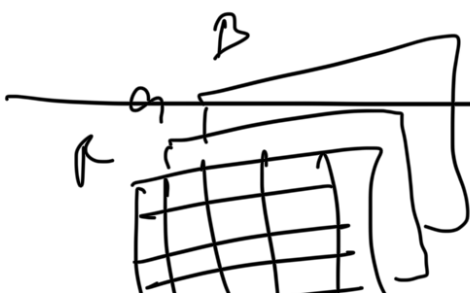
for 1 image \rightarrow 10 Scores \rightarrow

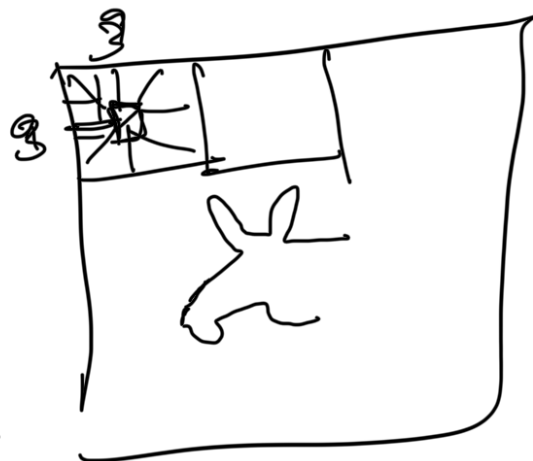
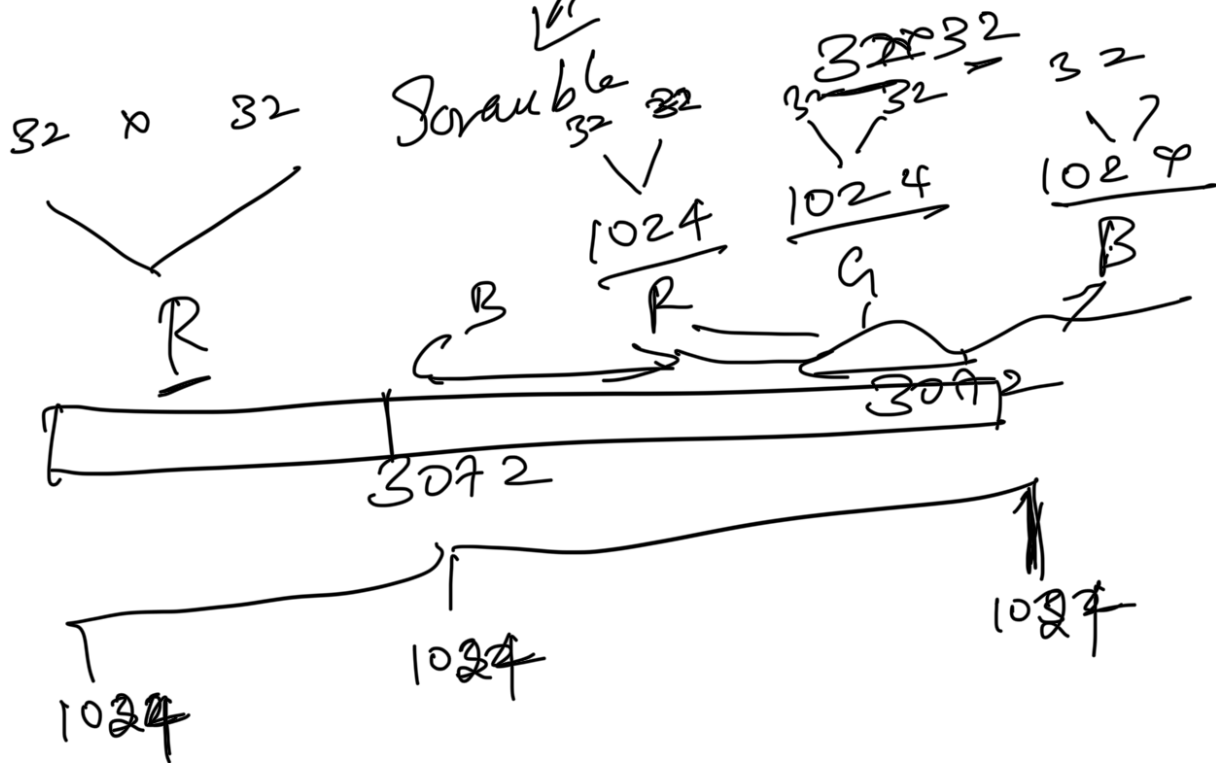
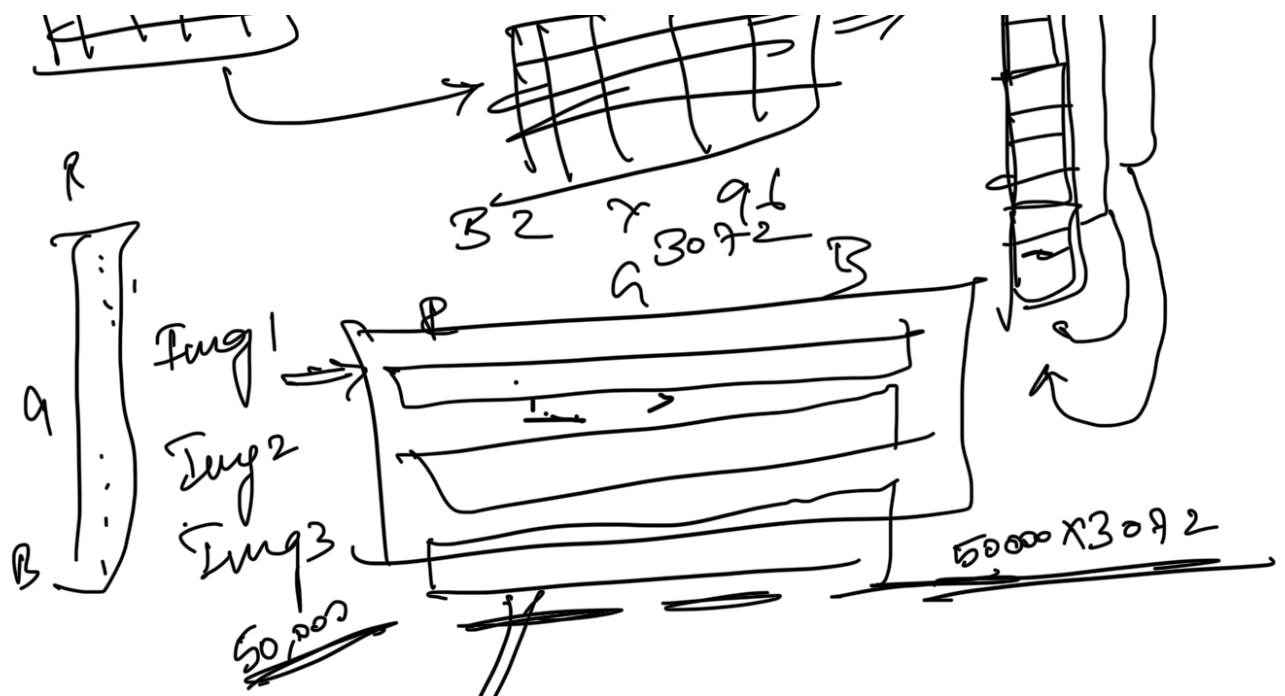
$$\text{Pred} \Rightarrow [0.002 \quad 0.008 \quad - \dots - \dots 0.01]$$

$$\text{Actual} \Rightarrow [0 \quad 0 \quad 0 \quad \dots 1 \quad 0 \quad 0]$$

one image 10-class

$$\begin{bmatrix} \max(O_1 \text{ pred-act}) & \dots & \max(O_1 \text{ pred-act}) \\ \vdots & \ddots & \vdots \\ \vdots & \ddots & \vdots \end{bmatrix}$$





1