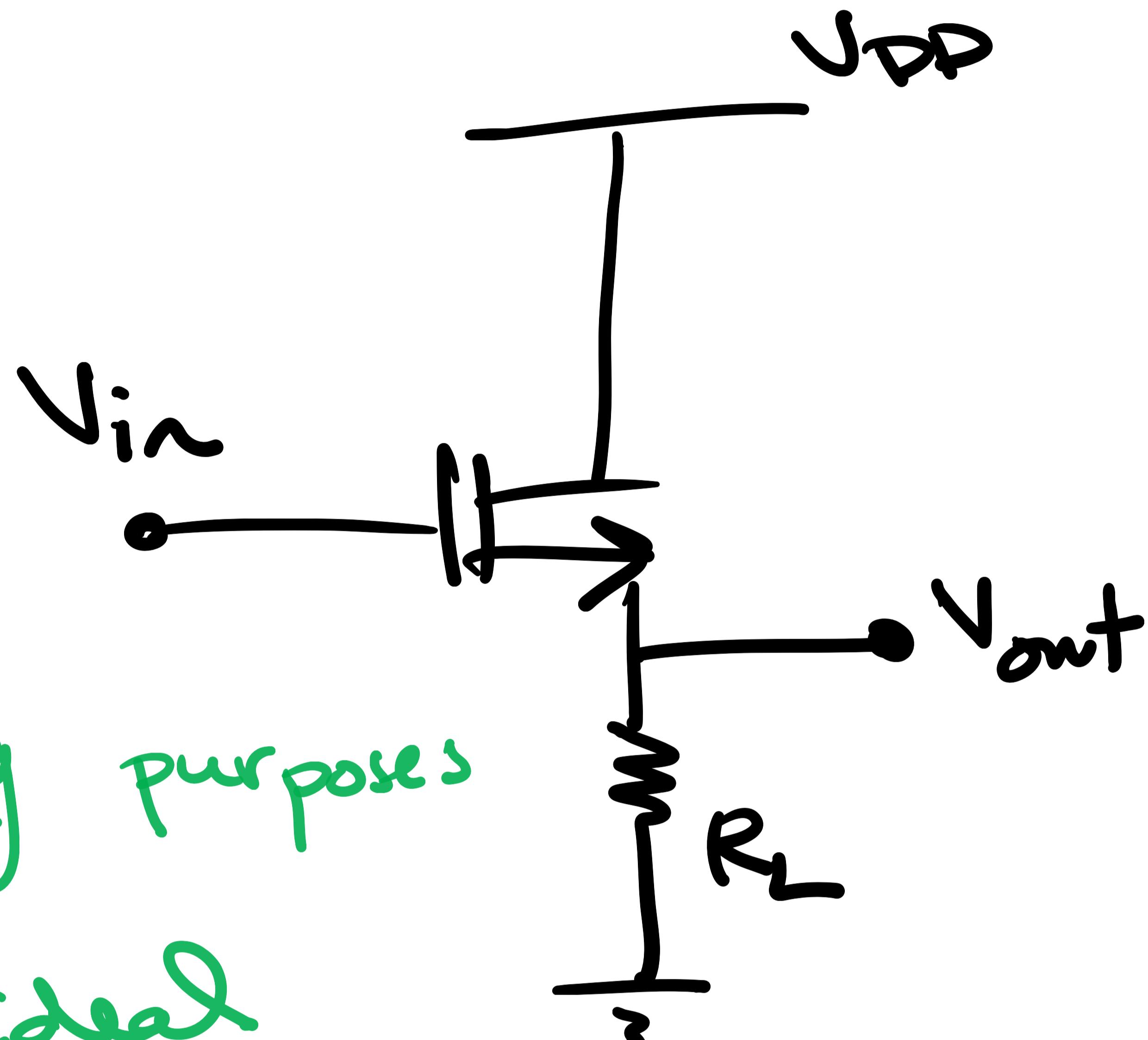


* Common Drain Stage (Source Follower):

more common -



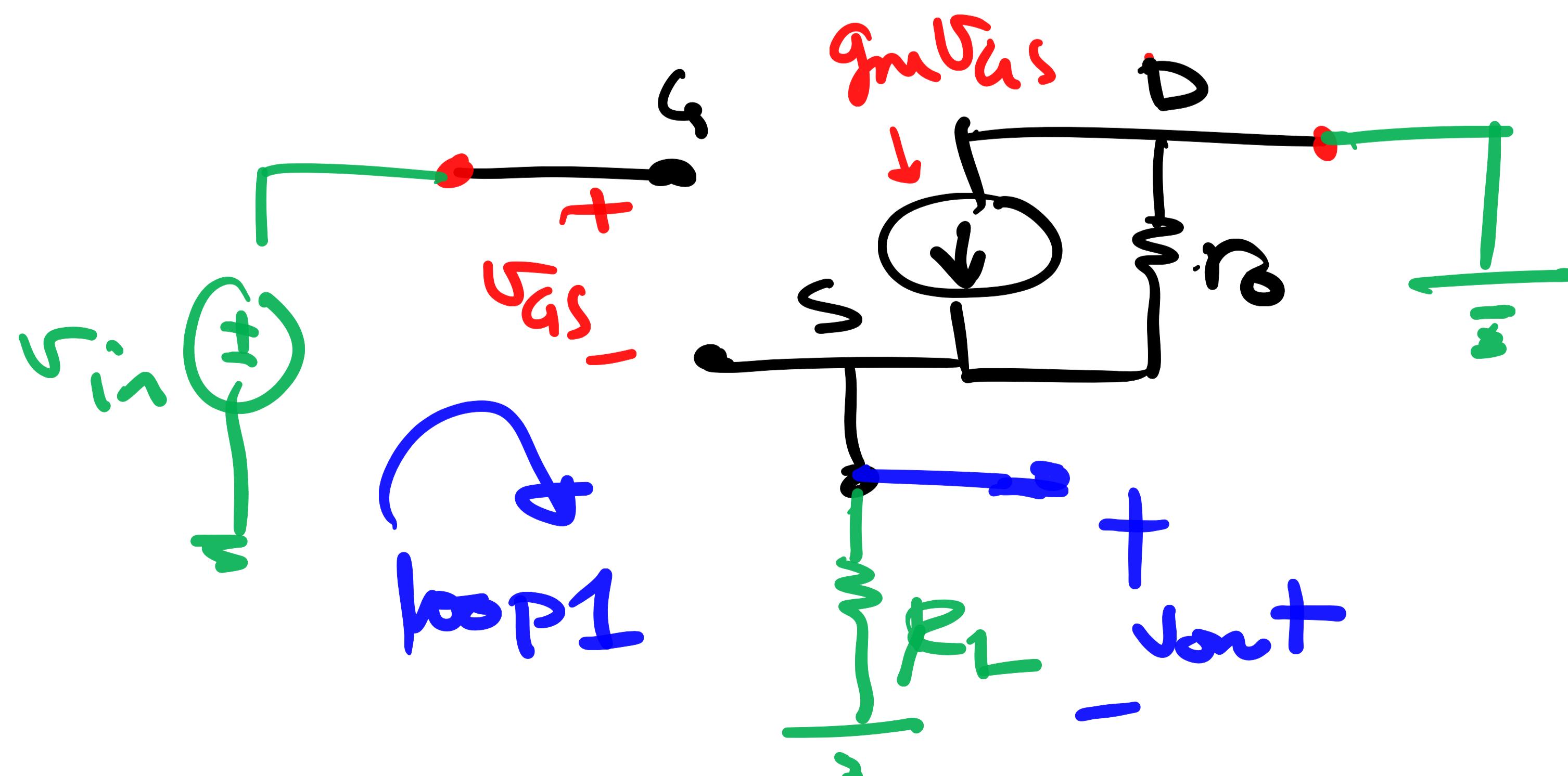
- * This stage is used for buffering purposes

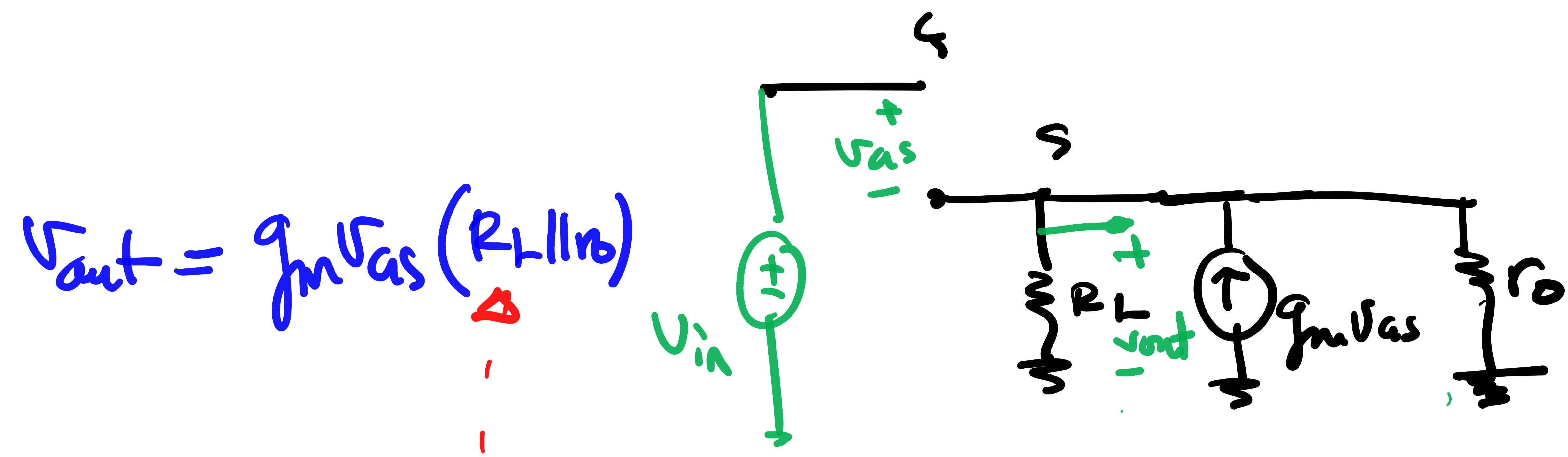
- * They have an ideal voltage gain of 1 ($A_V \approx 1$)

- * a high input impedance
- * a low output impedance

- * Gain Analysis $A_V = \cancel{1}$

$$A_V = \frac{V_{out}}{V_{in}}$$





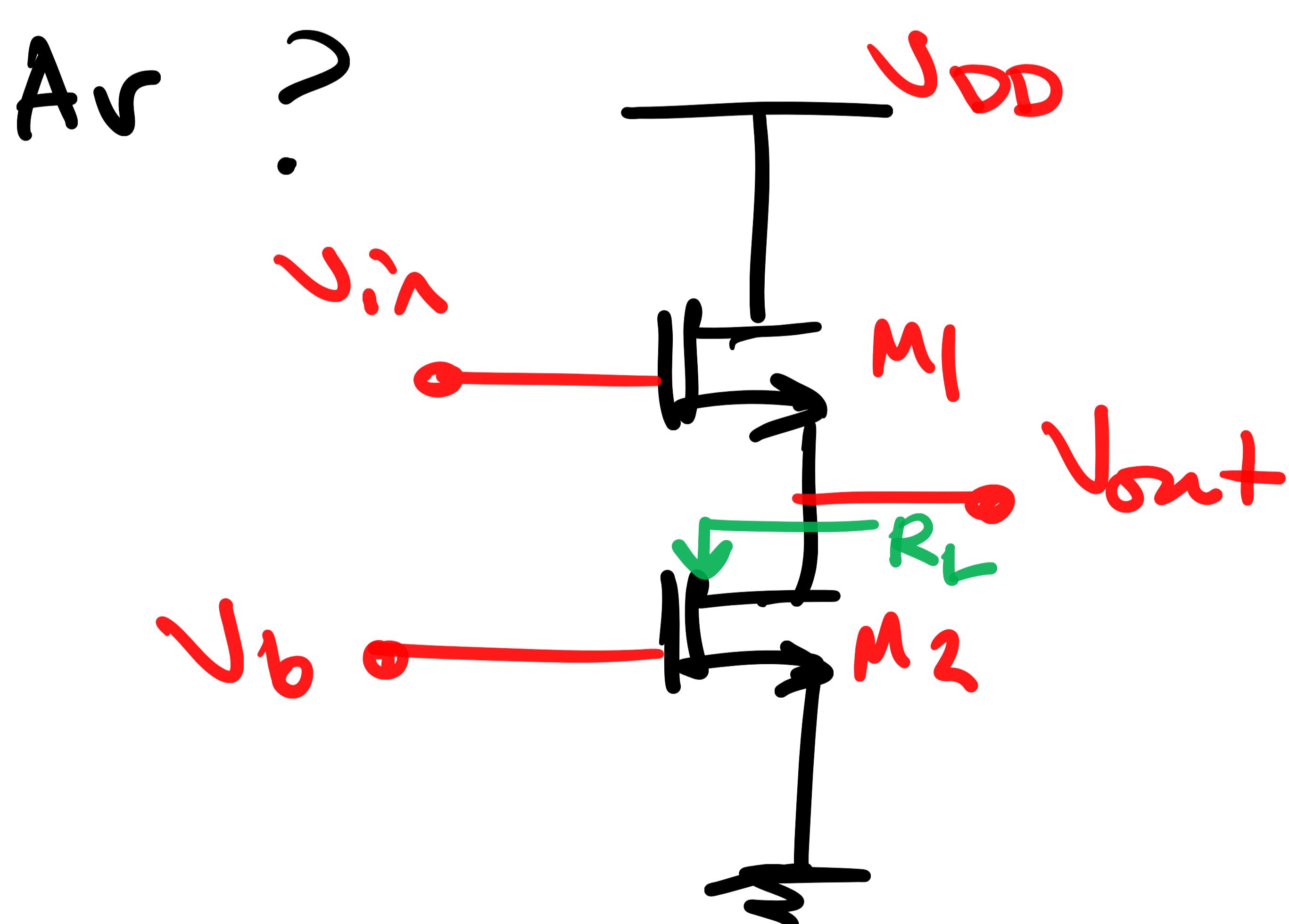
applying KVL @ loop 1 :-

$$V_{AS} = V_{in} - V_{out}$$

$$Av = \frac{V_{out}}{V_{in}} = \boxed{\frac{R_L/r_o}{R_L/r_o + g_m}}$$

if $R_L/r_o \gg g_m \Rightarrow Av \approx 1$

Ex: a S.F. is realized as follows, calculate A_v ?



\Rightarrow Standard def. for
a S.F. A_v

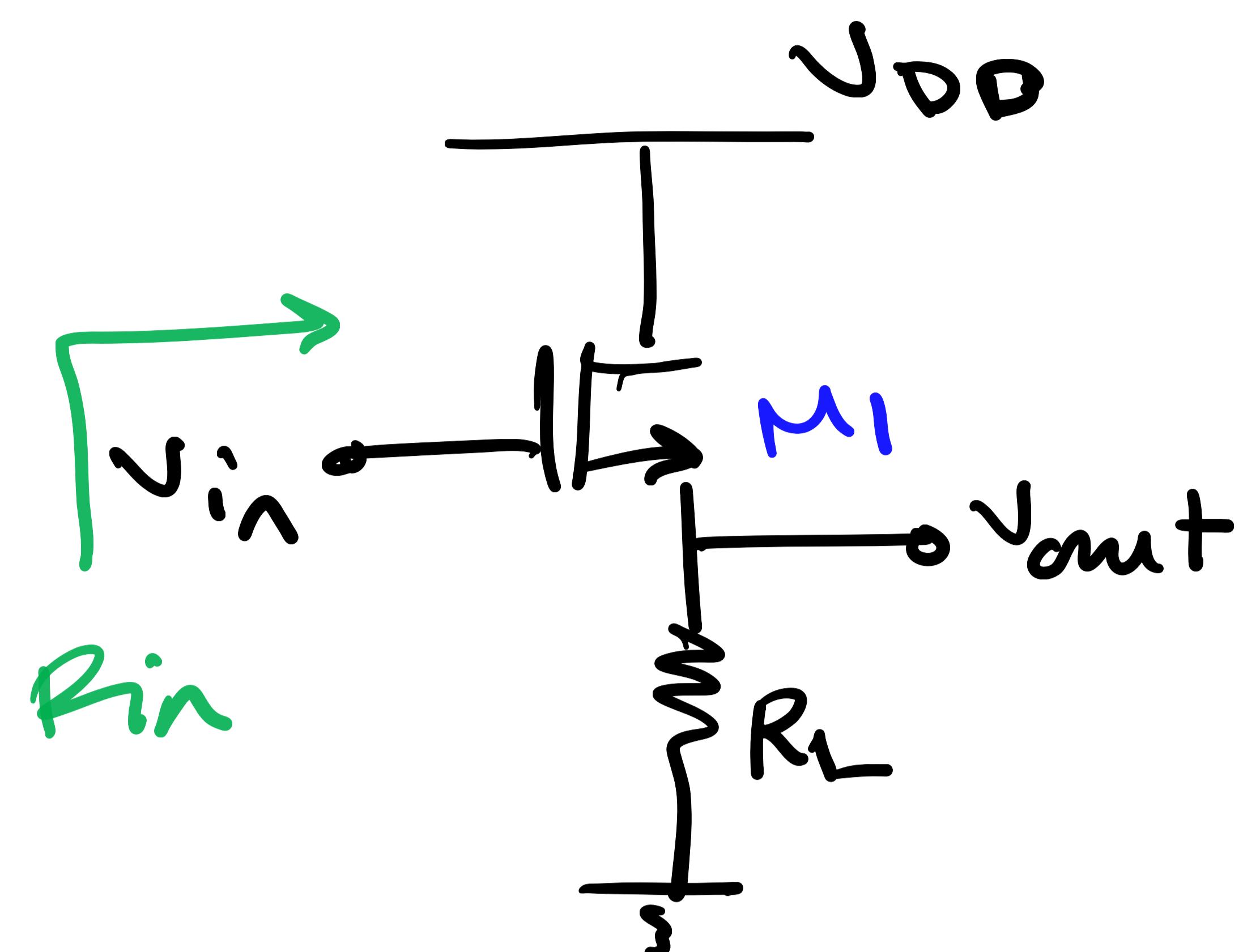
$$= \frac{R_L/r_o}{R_L/r_o + g_m}$$

if $\lambda \neq 0 \Rightarrow R_L = r_{o2}$

$$\Rightarrow A_v = \frac{r_{o2}/r_{o1}}{r_{o2}/r_{o1} + g_m}$$

* Input Impedance Analysis :-

$$R_{in} = \infty$$

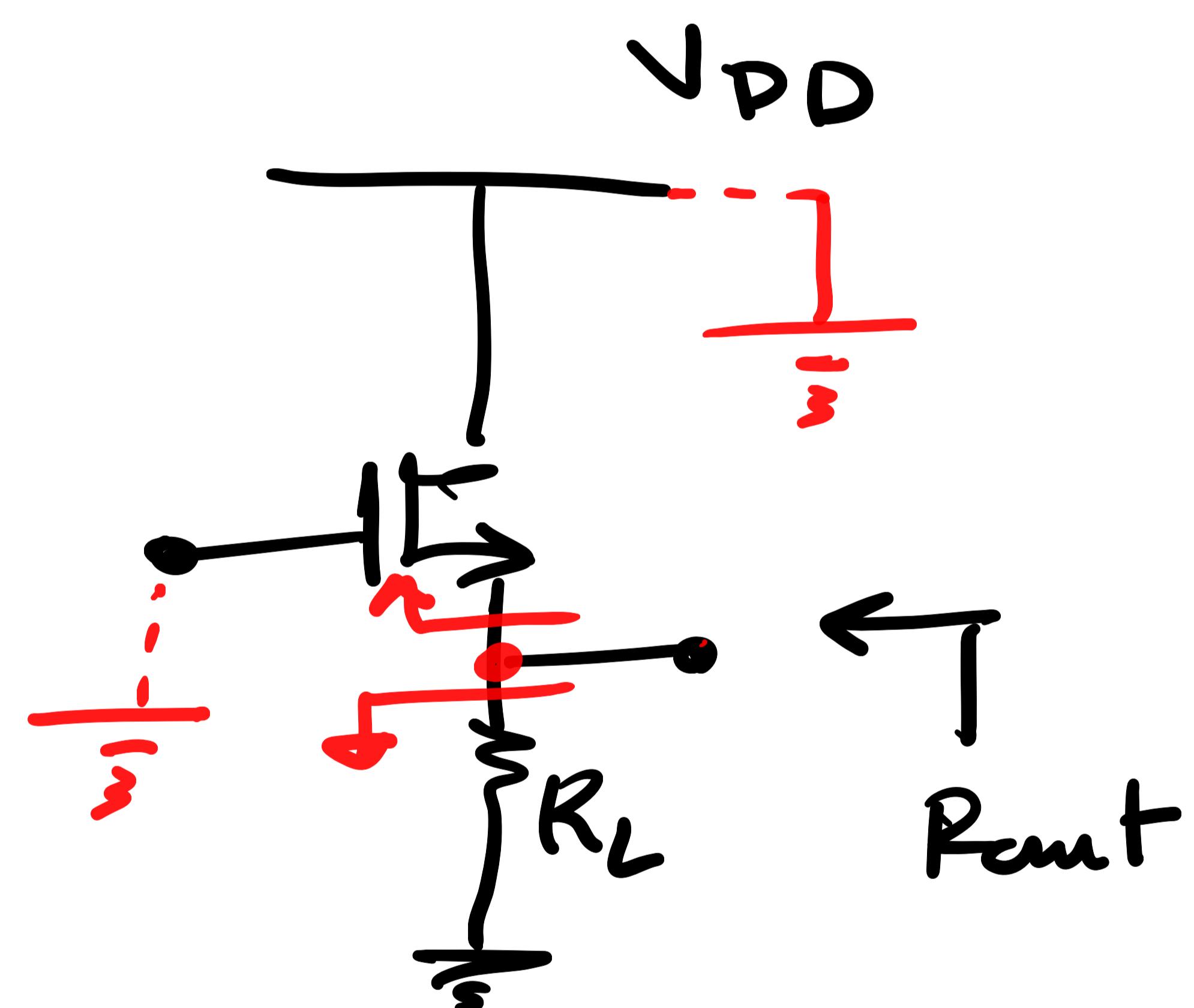


* Remember that

R_{in} will drop when we bias M_1 using resistors.

* Output Impedance Analysis :-

$$R_{out} = \boxed{\frac{1}{g_m} \| R_L}$$



Notice that R_{out} is low compared to CS and CG stages.

* Source Follower biasing :-

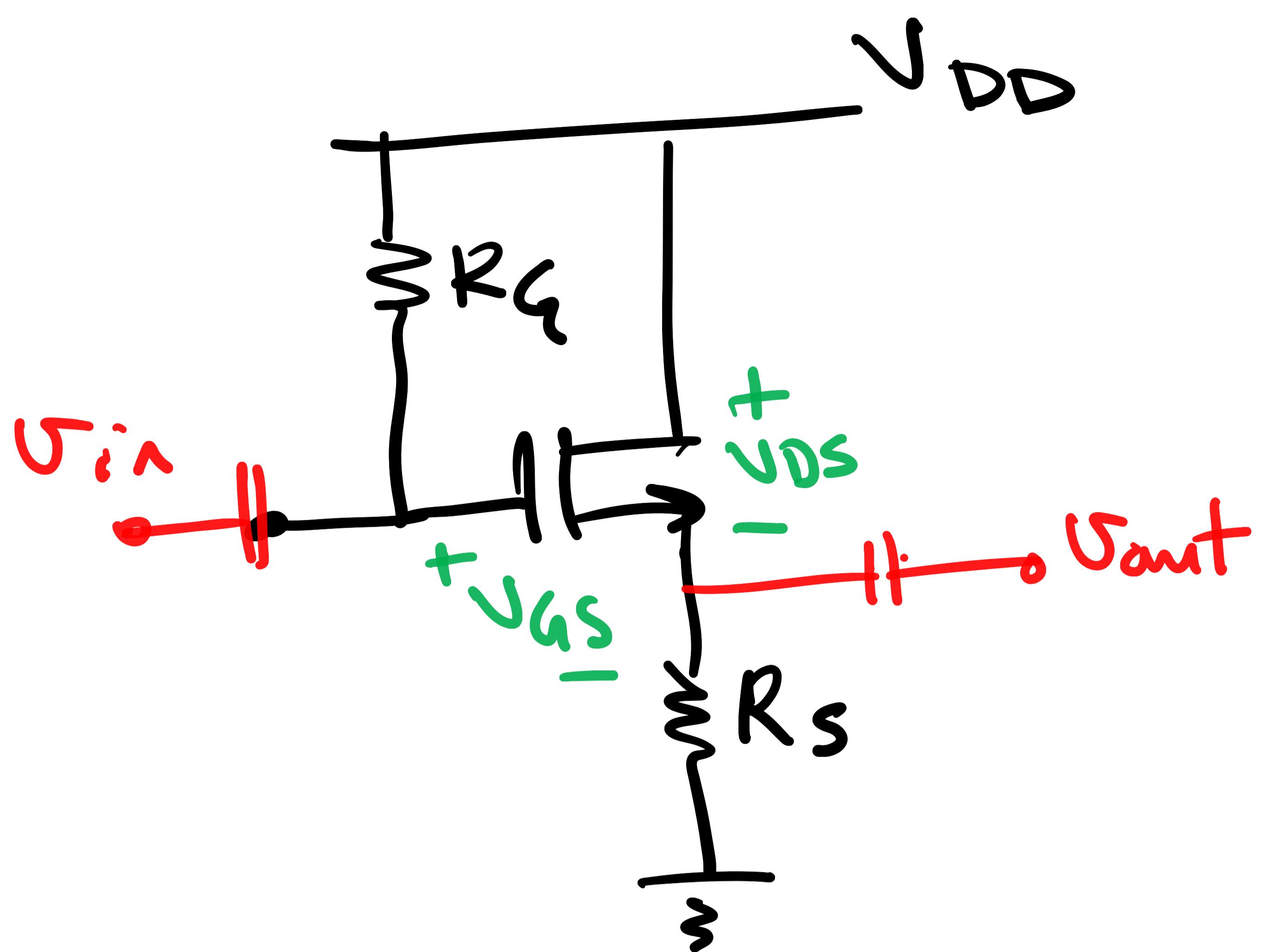
Since $\sum I_G = 0$

$$\Rightarrow V_G = V_D = V_{DD}$$

$$\Rightarrow V_{GS} = V_{DS}$$

$$\text{hence } V_{DS} > V_{GS} - V_{TH}$$

\rightarrow always in saturation.



$$I_D = \frac{1}{2} \mu_n C_o x \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$\Rightarrow V_{DS} = V_{DD} - I_D R_S \Rightarrow V_{GS} = V_{DD} - I_D R_S$$

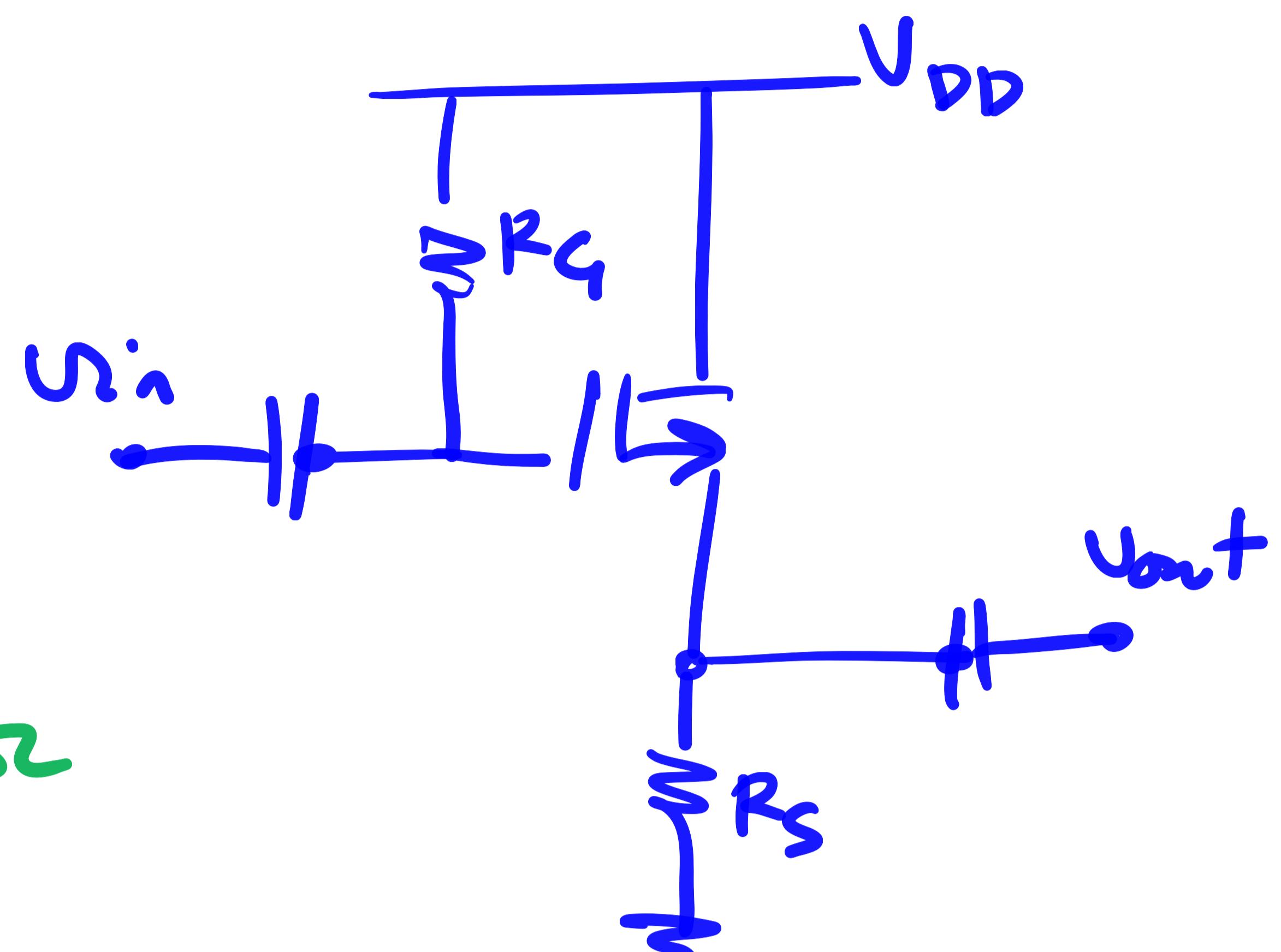
$$I_D = \frac{1}{2} \mu_n C_o x \frac{W}{L} (V_{DD} - I_D R_S - V_{TH})^2$$

Solve for I_D then define V_{GS}, V_{DS}

Ex: Design a S.F. for a Drain current of $I_{mA} = 1mA$ and an A_V of 0.8. Assume $\mu_nC_{ox} = 100 \mu A/V^2$, $V_{TH} = 500mV$, $\lambda = 0$, $V_{DD} = 1.8V$ and $R_G = 50k\Omega$.

Sol: $I_D = 1mA$

$A_V = 0.8, R_G = 50k\Omega$



$$A_V = \frac{R_S \| r_o}{R_S \| r_o + Y_{gm}} = \frac{R_S}{R_S + Y_{gm}} = 0.8$$

$$\Rightarrow \text{but } g_m = \frac{2I_D}{V_{GS} - V_{TH}} \Rightarrow V_{GS} = V_{DD} - I_D R_S$$

$$g_m = \frac{2I_D}{(V_{DD} - I_D R_S - V_{TH})}$$

$$\Rightarrow A_V = 0.8 = \frac{R_S}{R_S + \frac{(V_{DD} - I_D R_S - V_{TH})}{2I_D}}$$

$$\Rightarrow \text{Solving for } R_S \Rightarrow R_S = 867 \Omega$$

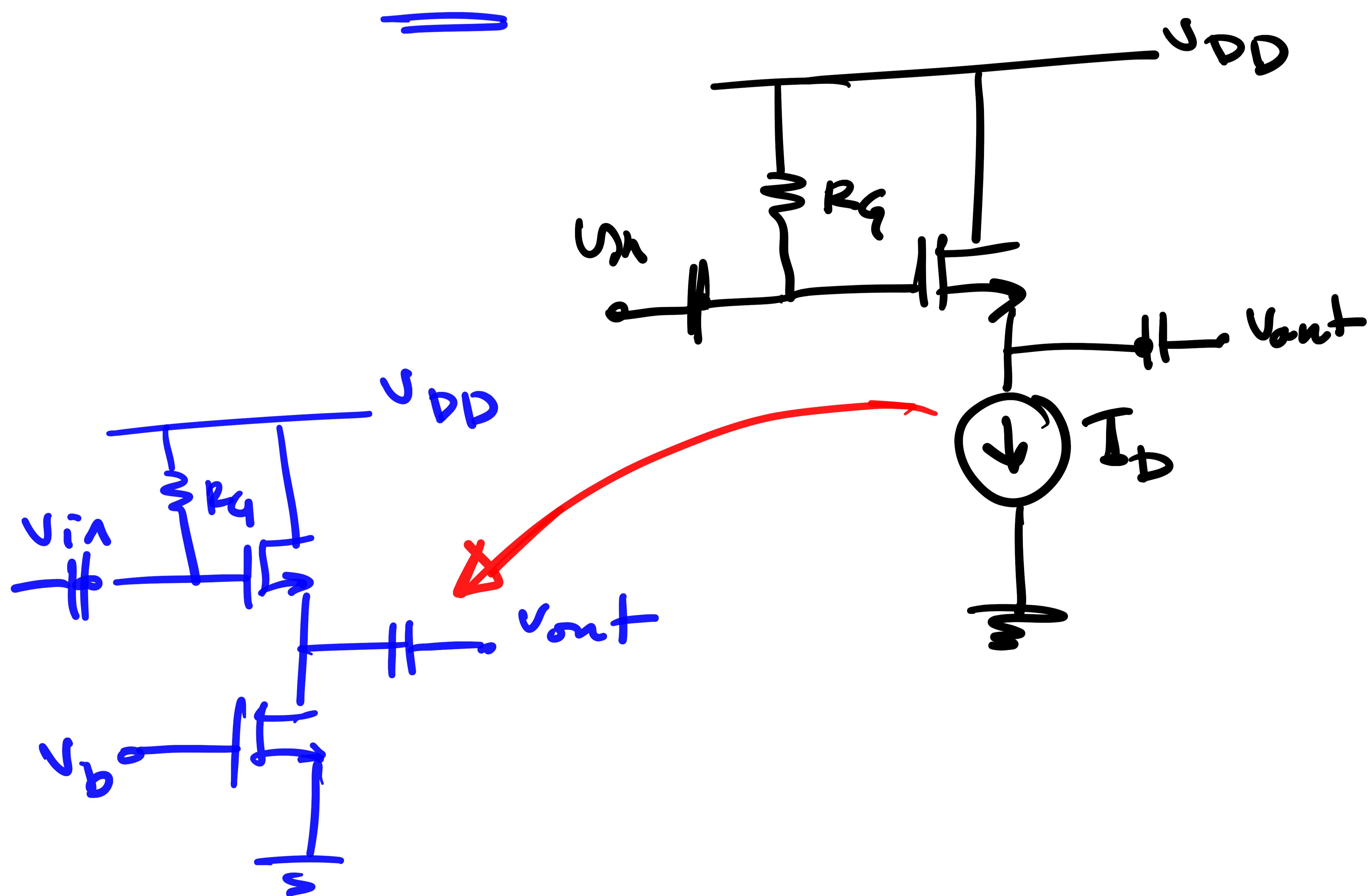
$$\Rightarrow \frac{W}{L} = \frac{2I_D}{\mu_n C_{ox} (V_{GS} - V_{TH})^2}, \text{ but } V_{GS} = V_{DD} - I_D R_S \\ = 0.933 \text{ V}$$

$$\Rightarrow \boxed{\frac{W}{L} = 207}.? 107$$

since V_{GS} depends on R_S and I_D

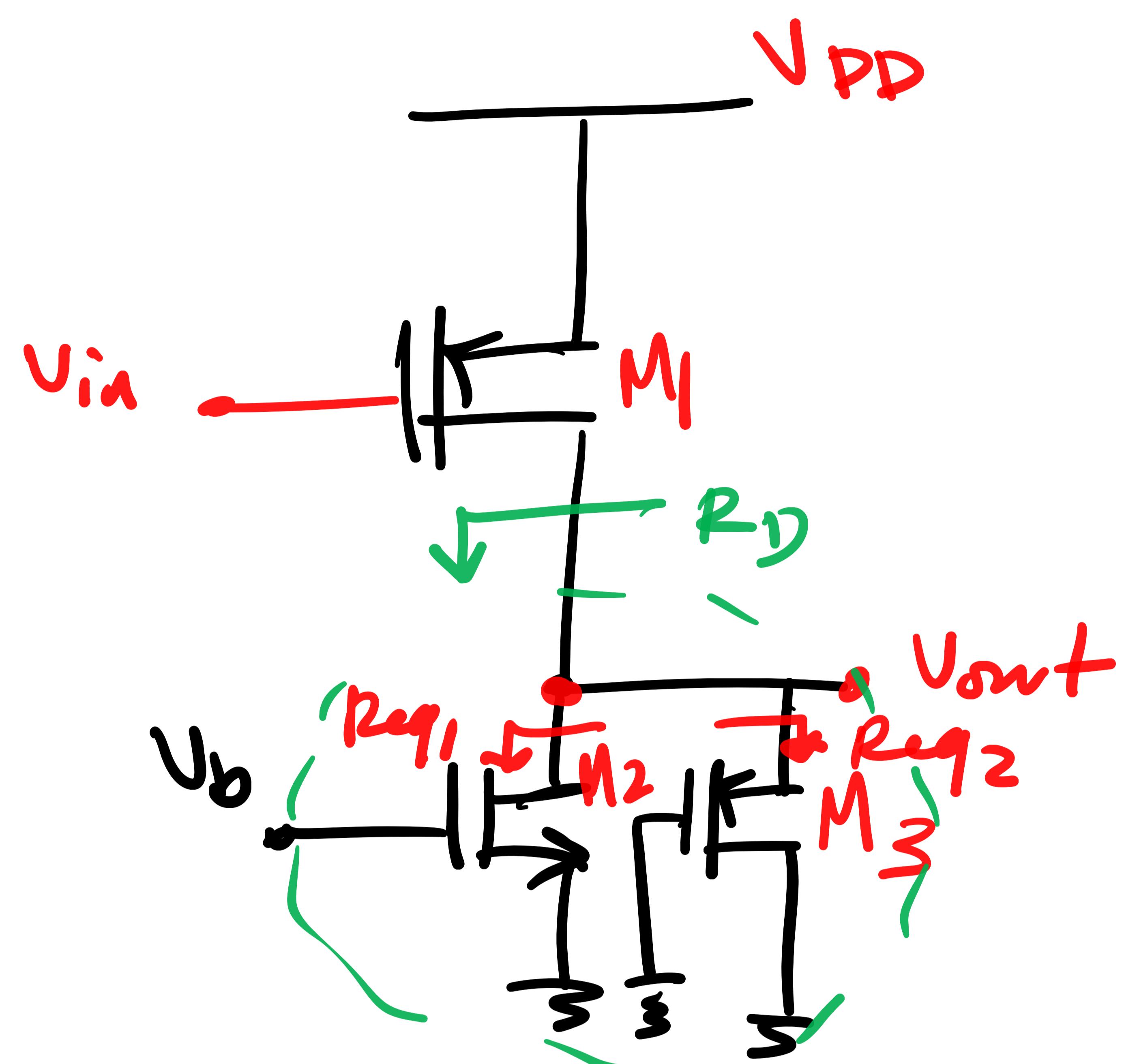
pay attention to the increase in either R_S or I_D as it may turn the transistor OFF.

* To solve the above issue we can bias the S.F. using a current source realized as a MOS.



* Examples on different MOS amp stages :-

Ex: Calculate A_v and R_{out} for this stage



$$A_v = -g_m R_D$$

$$R_D = R_{req_1} \parallel R_{req_2}$$

$$R_{req_1} = R_2$$

$$R_{req_2} = \frac{1}{g_m 3}$$

$$A_v = -g_m 1 \cdot R_2 \parallel \frac{1}{g_m 3} \approx \frac{-g_m 1}{g_m 3}$$

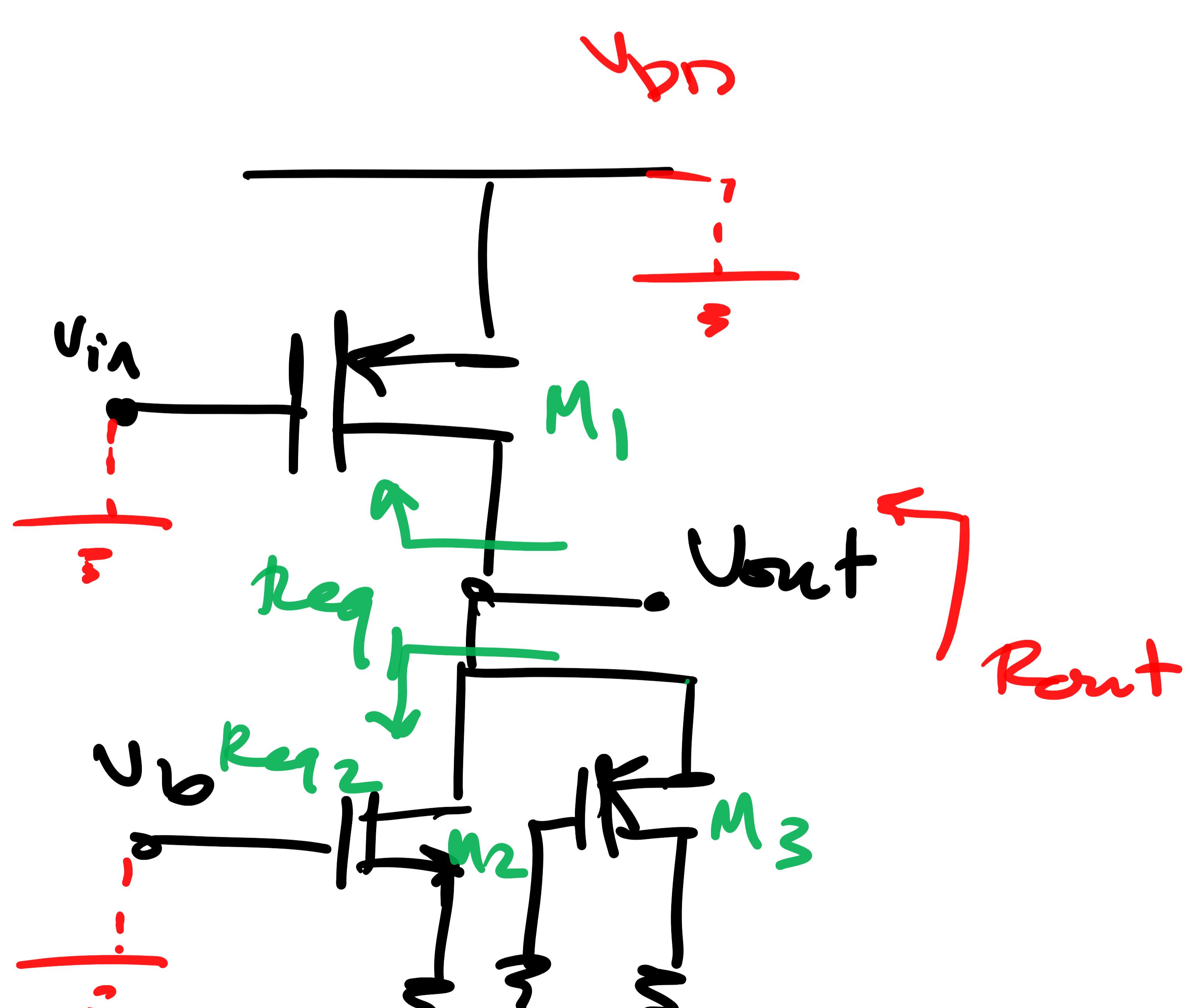
$$\Rightarrow R_{out} = ?$$

$$R_{out} = R_{req_1} \parallel R_{req_2}$$

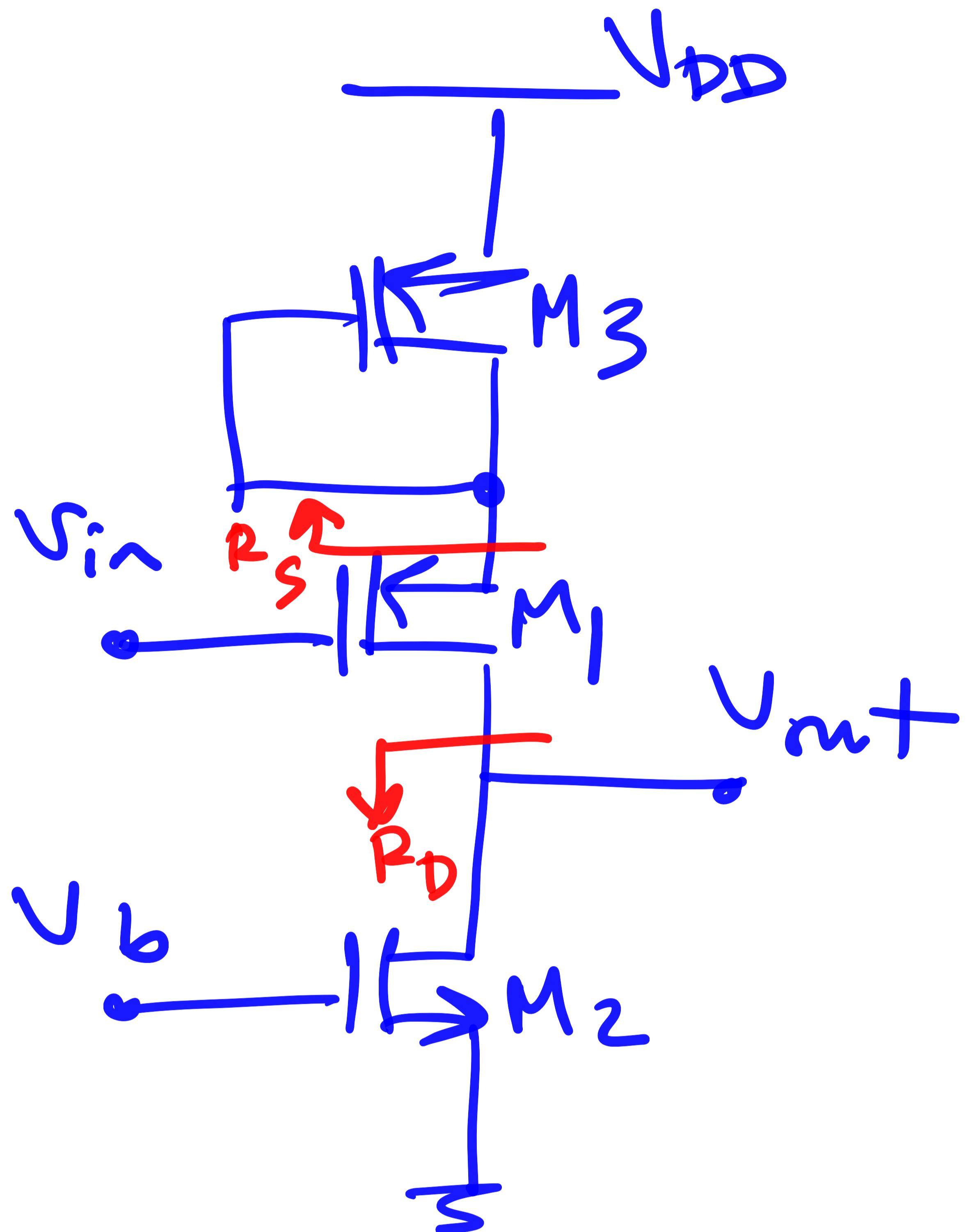
$$R_{req_1} = R_0 1$$

$$R_{req_2} = R_2 \parallel \frac{1}{g_m 3}$$

$$R_{out} = R_0 1 \parallel R_2 \parallel \frac{1}{g_m 3} \Rightarrow \approx \frac{1}{g_m 3}$$



Ex : Calculate A_v for this cct assuming $d \neq 0$.



→ This is a degenerate CS core

$$A_v = -\frac{R_D}{g_{m1} + R_S}$$

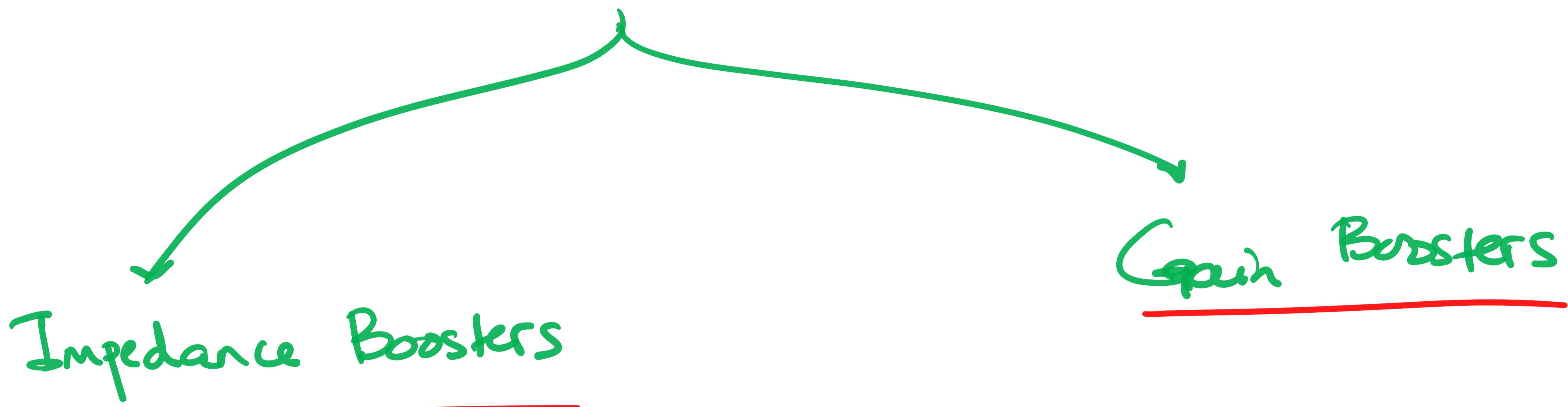
$$R_S = \frac{1}{g_{m3}}$$

$$R_D = r_o2$$

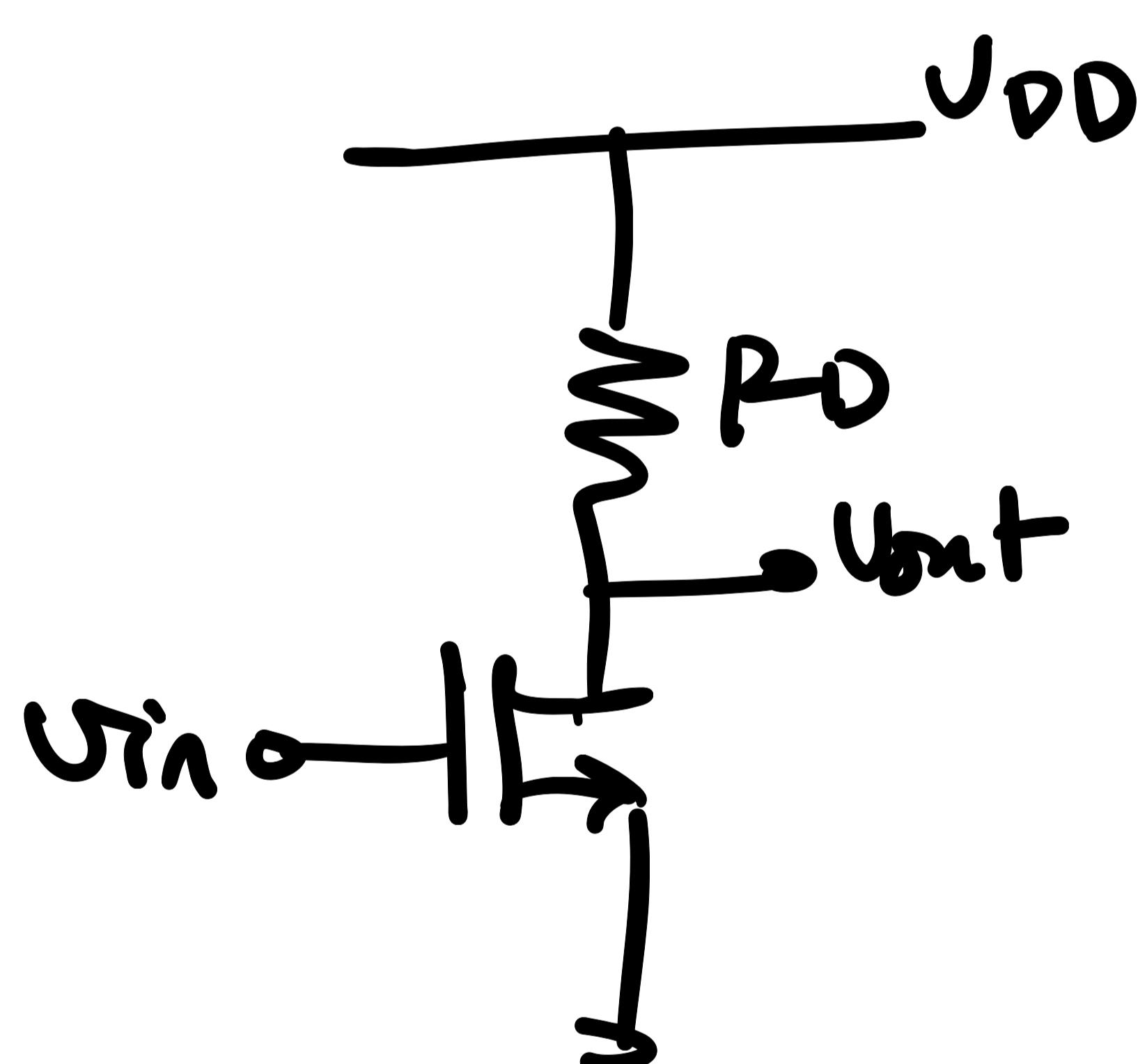
$$A_v = -\frac{r_{o2}}{\frac{1}{g_{m1}} + \frac{1}{g_{m3}}}$$

* Chapter 9 :- Cascode Stages and
Current Mirrors :-

* Cascode Amplifiers :-



* Impedance Boosters :-



$$\lambda = 0 \Rightarrow \text{The gain } |A_v| = +g_m R_D$$

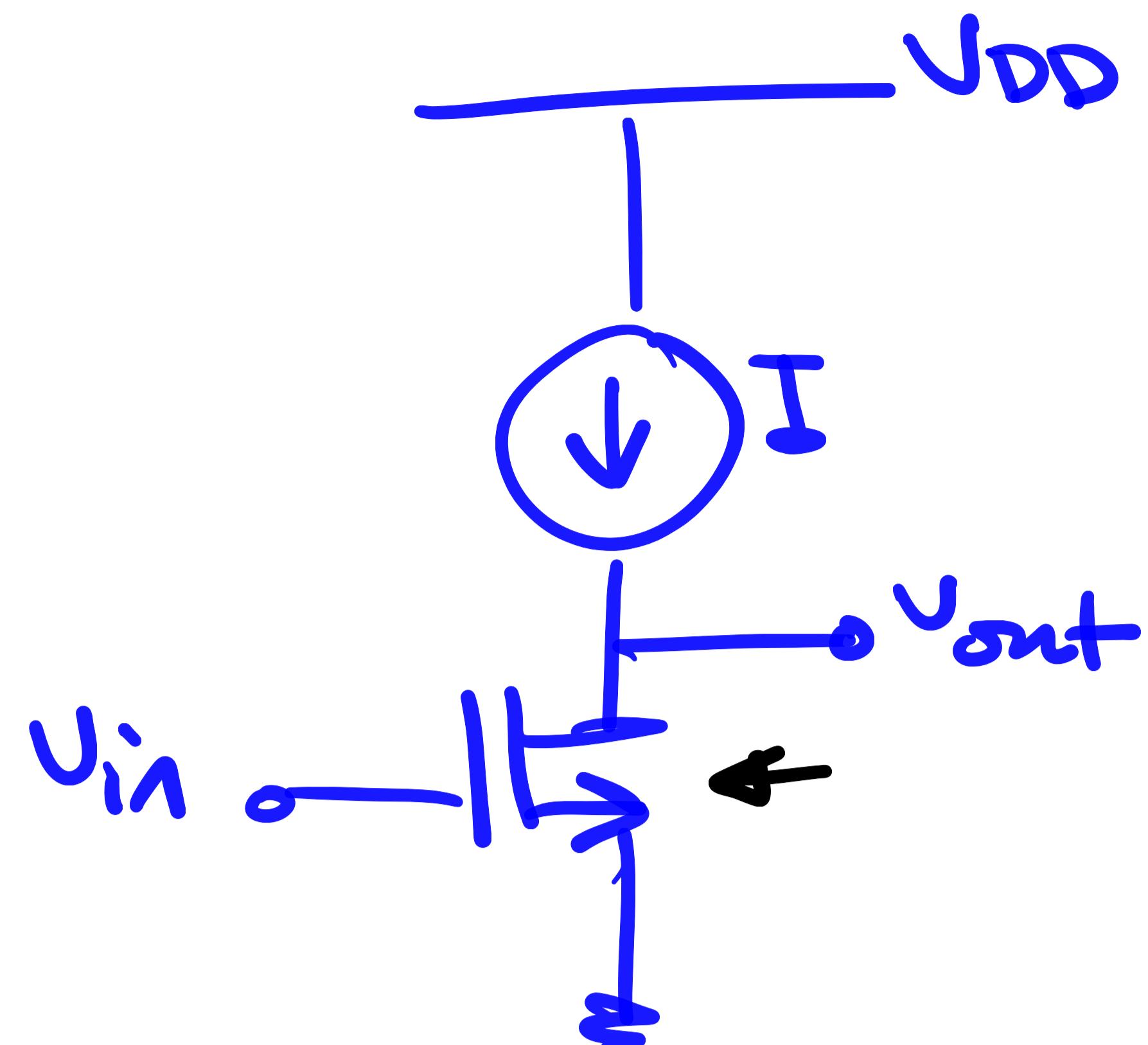
to increase $|A_v| \uparrow \rightarrow g_m \uparrow \text{ or } R_D \uparrow$

when $g_m \uparrow \rightarrow I_D \uparrow \rightarrow$ Consuming more power

$I_D \uparrow \rightarrow V_{DS} \downarrow \rightarrow$ placing the Q point closer
to the triode region.

$R_D \uparrow \rightarrow V_{DS} \downarrow \rightarrow$ same as above

* Cascodes solve the above problem as follows:



if the current source is ideal

assume $\lambda = 0$

$$|Av| = g_m \cdot \infty$$

current source
acts as an
open

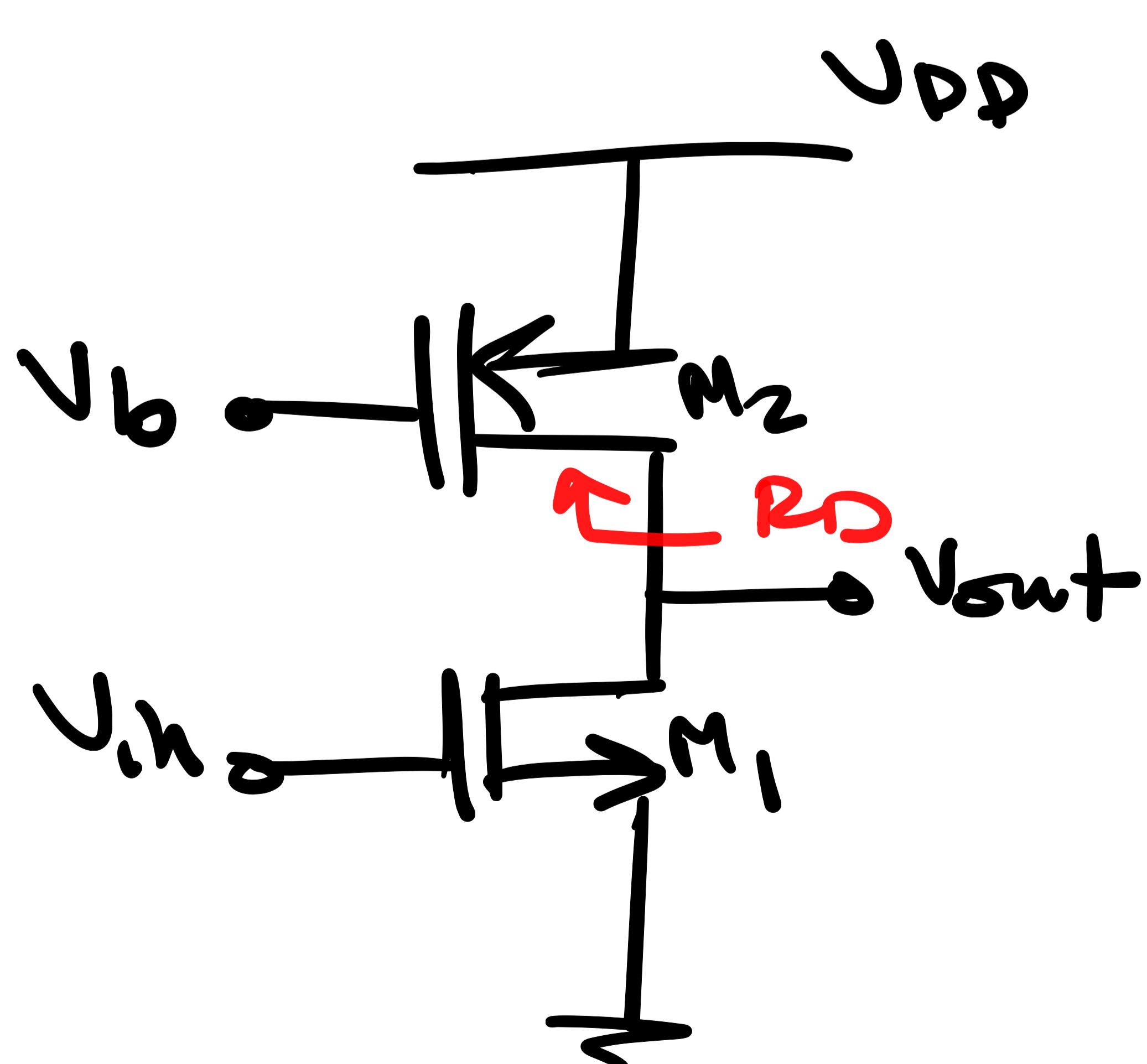
but if $\lambda \neq 0$

$$|Av| = g_m \cdot r_o$$

\Rightarrow The ideal current source is assumed to have an infinite small signal resistance allowing

$$|Av| = g_m \cdot (r_{o1}/\lambda) = (g_m r_o)$$

\Rightarrow Let us see what happens when the current source is realized using MOS devices?



assume $\lambda \neq 0$

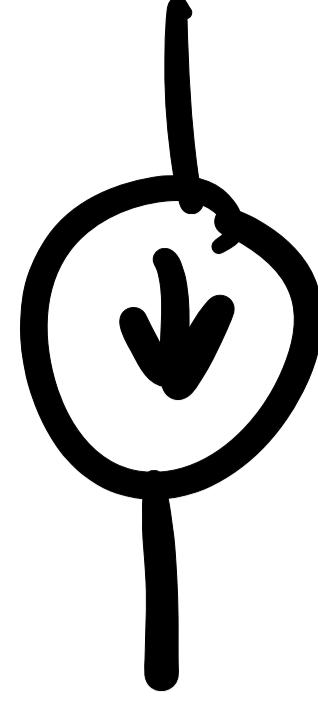
and M_1 and M_2 are identical

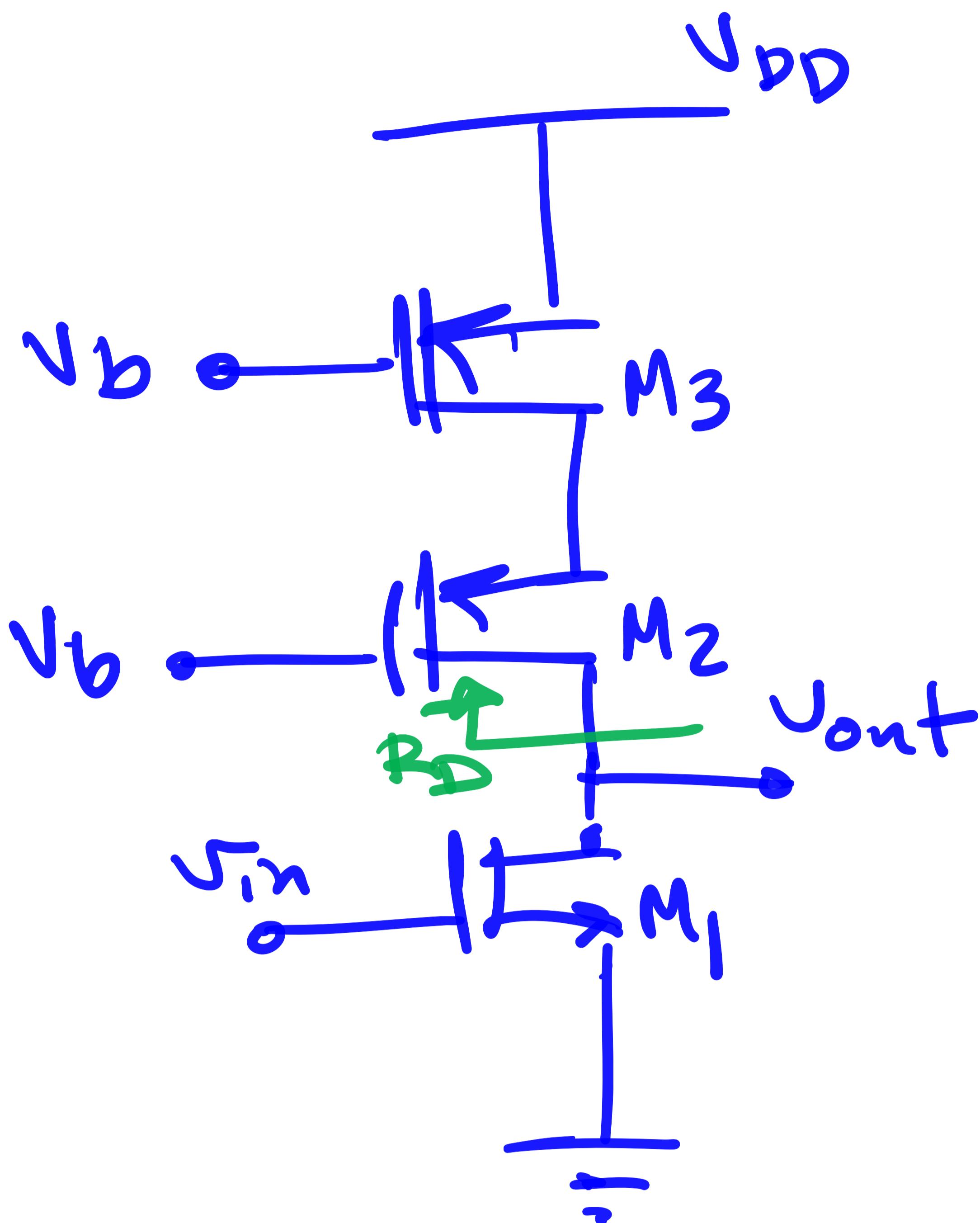
$$|Av| = g_{m1} (R_D \parallel r_{o1})$$

$$= g_{m1} (r_{o2} \parallel r_{o1})$$

$$\Rightarrow |Av| = g_{m1} r_{o2}/2 \quad [M_1 \text{ and } M_2 \text{ are identical}]$$

$r_{o1} = r_{o2}$

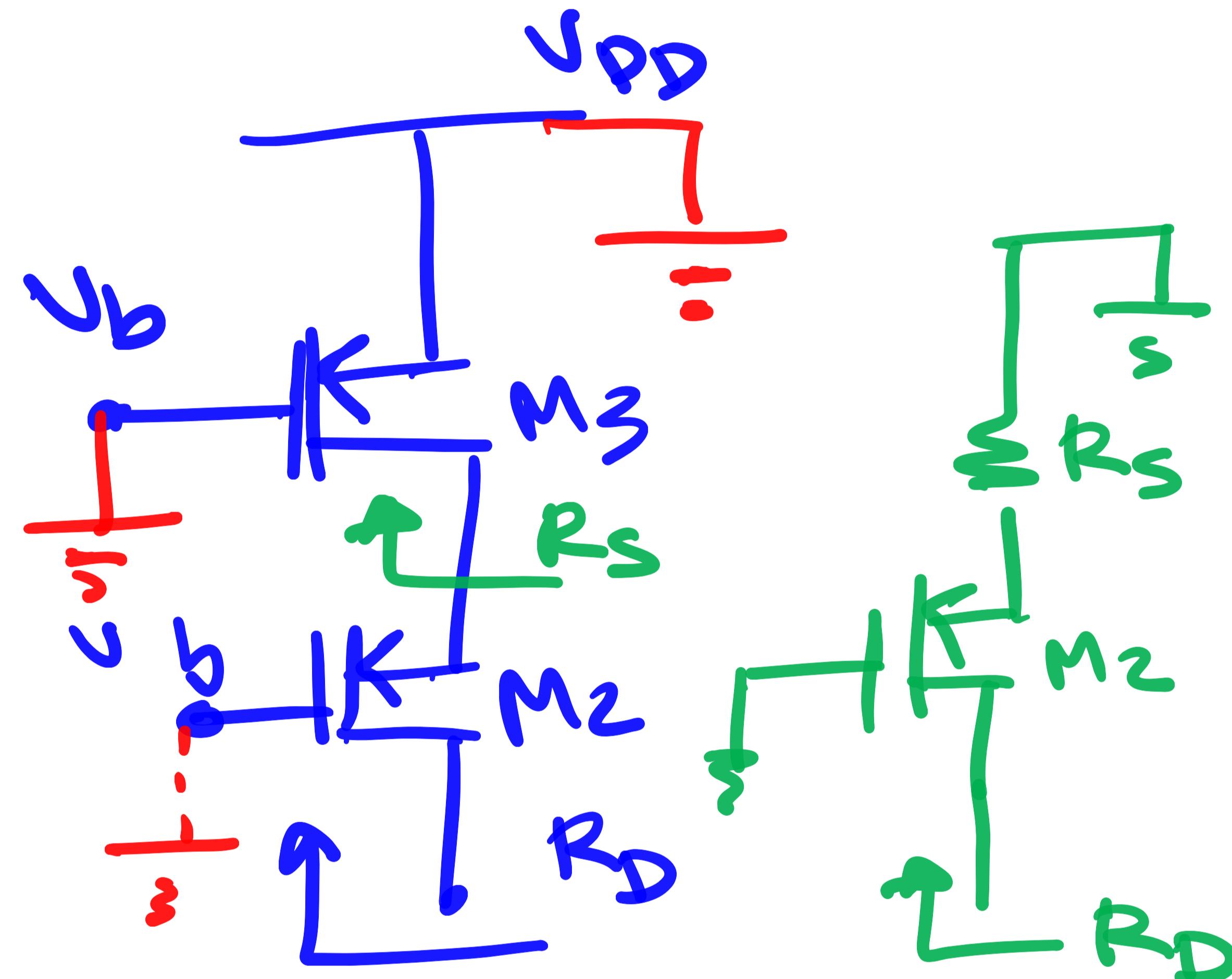
realizing  with one MOS will drop $|Av|$,
solution is use a cascode :



$$\lambda \neq 0$$

$$|Av| = g_{m_1} (R_D / (r_{o1}))$$

$$\Rightarrow R_D ?$$



$$R_D = (1 + g_{m_2} R_S) \cdot r_{o2}$$

$$R_D = (1 + \underbrace{g_{m_2} r_{o3}}_{\text{red}}) \cdot r_{o2} \quad \Rightarrow R_S = r_{o3}$$

$$R_D \approx g_{m_2} r_{o3} \cdot r_{o2}$$

$$\Rightarrow |Av| = g_{m_1} (r_{o1} / (g_{m_2} r_{o2} r_{o3}))$$