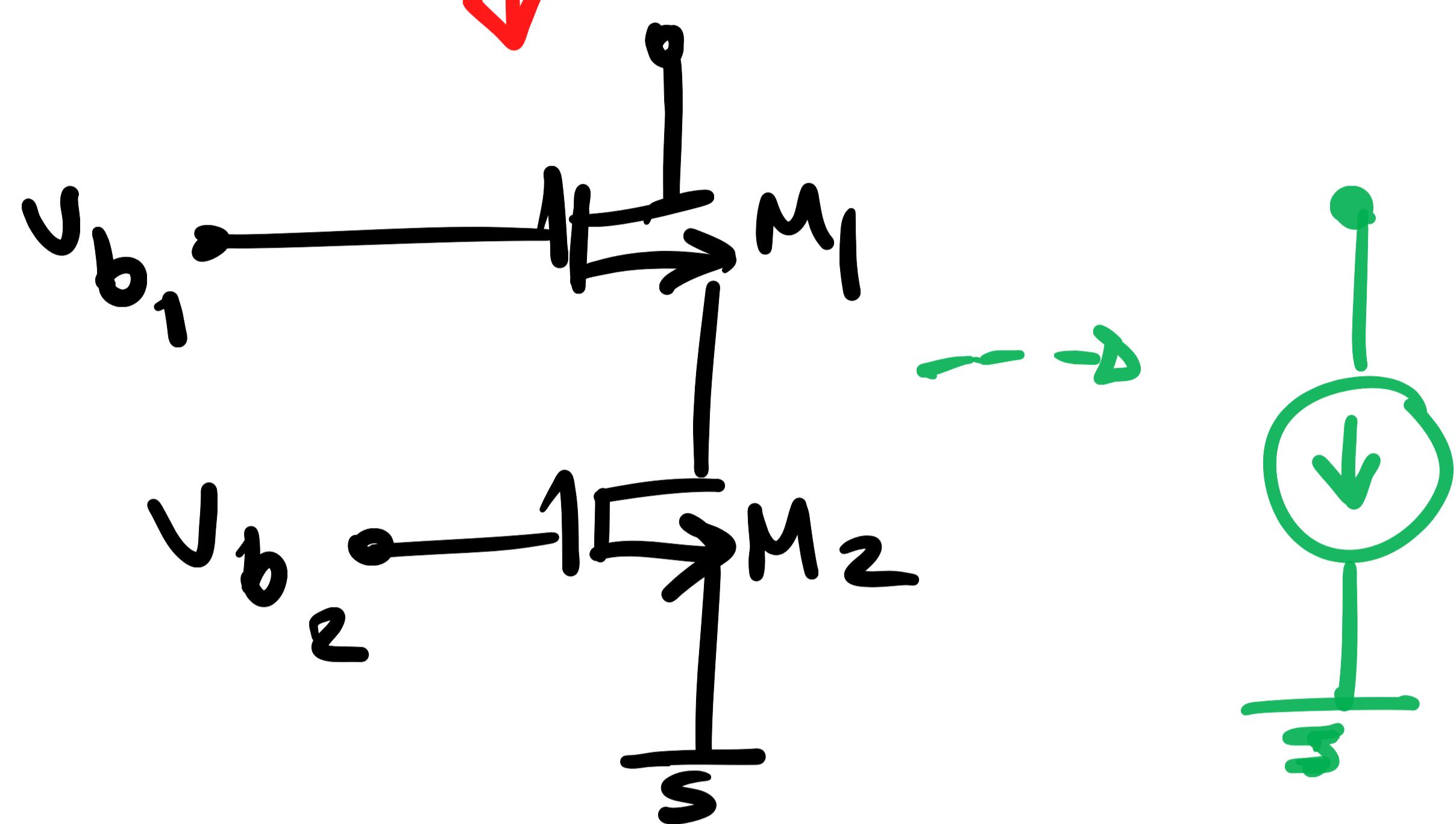


Ex: Design an NMOS cascode for an output impedance of $500\text{ k}\Omega$ and a current of 0.5 mA .

For simplicity assume M_1 and M_2 are identical and

$$\mu_n C_{ox} = 100 \mu\text{A}/\text{V}^2 \text{ and } \lambda = 0.1 \text{ V}^{-1}.$$

$$\text{R}_{\text{out}} = 500 \text{ k}\Omega$$



Since M_1 and M_2 are identical :-

$$r_{o1} = r_{o2}$$

$$r_{o1} = r_{o2} = \frac{1}{\lambda I_D}$$

$$r_{o1} = r_{o2} = \frac{1}{0.1 \cdot 0.5 \cdot 10^{-3}} = 20 \text{ k}\Omega$$

$$* I_D = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L} \right) V_{DS}^2 \rightarrow X$$

$$* R_{\text{out}} = g_{m1} \cdot r_{o1} \cdot r_{o2} = g_{m1} \cdot (r_{o1})^2$$

$$\Rightarrow g_{m1} = \frac{1}{800 \Omega} \Rightarrow \text{but } g_{m1} = \sqrt{2 \mu_n C_{ox} \left(\frac{W}{L} \right) I_D}$$

$$\Rightarrow \left(\frac{W}{L} \right)_1 = \frac{g_{m1}^2}{2 \mu_n C_{ox} I_D} = 15.6 = \left(\frac{W}{L} \right)_2$$

$$* V_{b2} \Rightarrow V_{GS2} \geq g_{m2} = \frac{2 I_D}{V_{DS}} \Rightarrow V_{DS} = \frac{2 I_D}{g_{m2}}$$

$$V_{DS} = 2 \cdot 0.5 \cdot 10^{-3} \cdot 800 = 800 \text{ mV}$$

assuming a $V_{TH} = 0.4V \Rightarrow$

$$V_{GS} = V_{OV} + V_{TH} = \boxed{1.2V}$$

$$\Rightarrow V_{D2} = \boxed{1.2V}$$

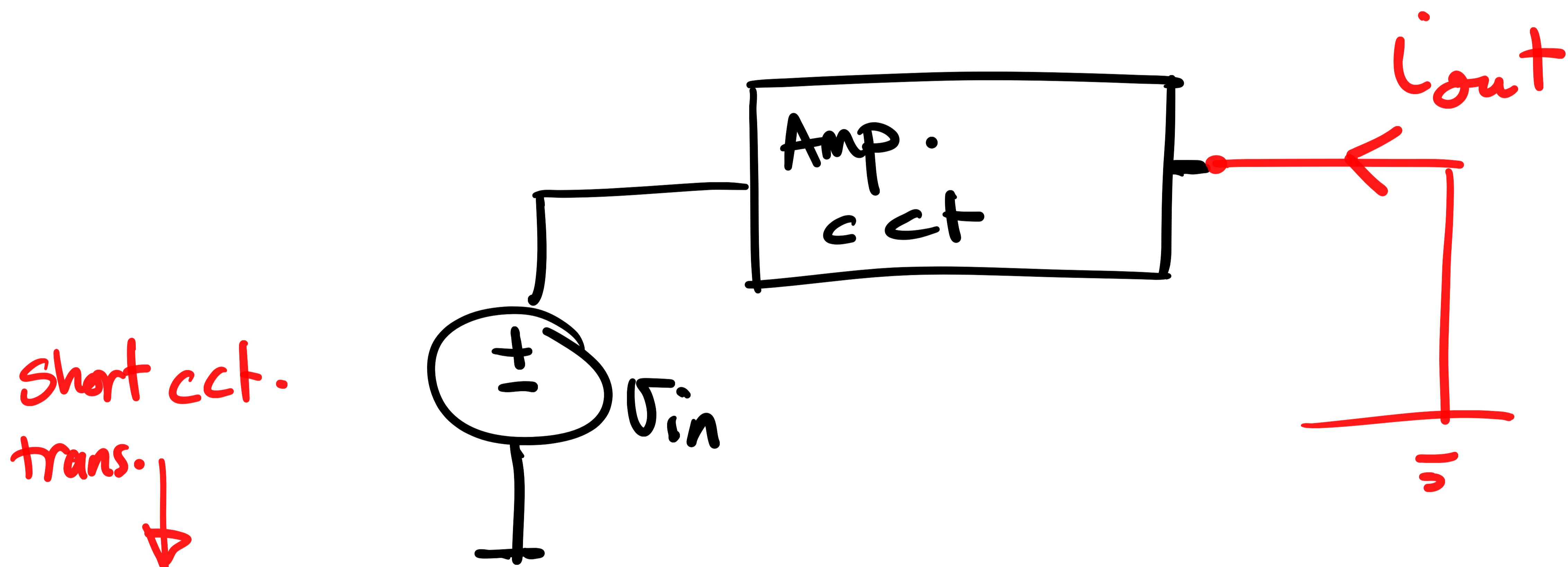


Cas Codes as Gain boosters :

Cascode amplifiers :-

To analyze A_V in cascode stage we can use the concept of **short cct. transconductance**

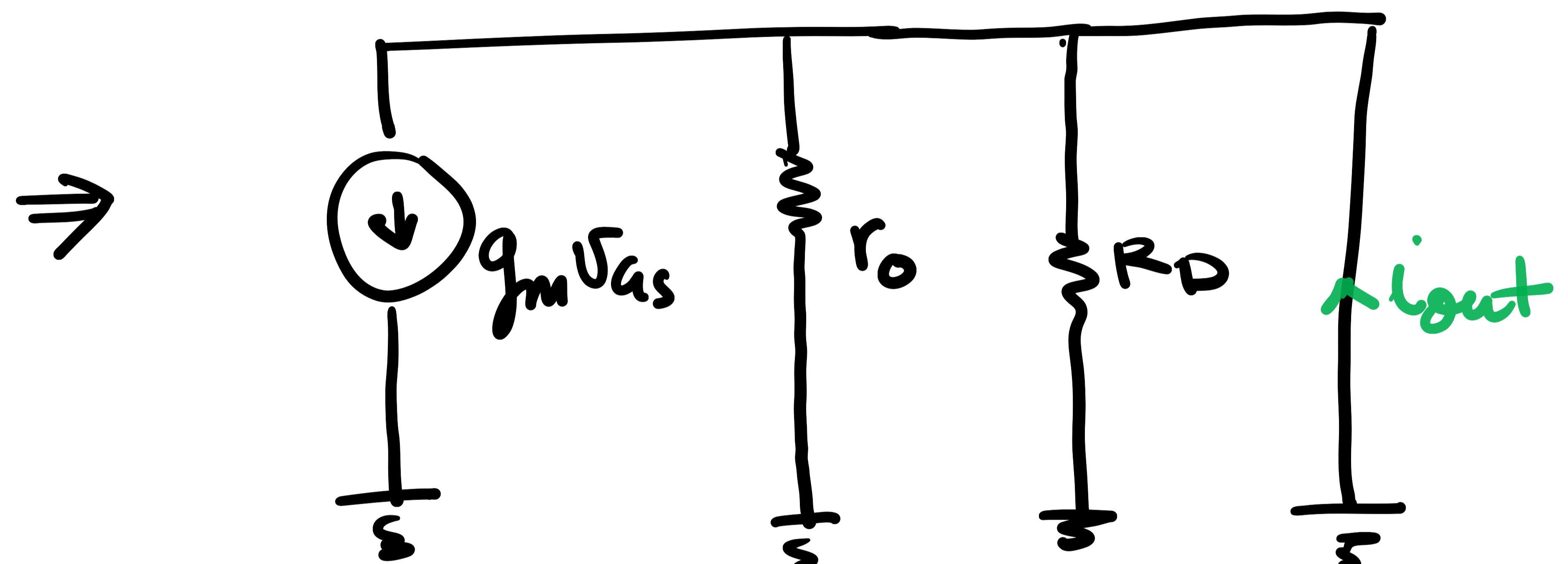
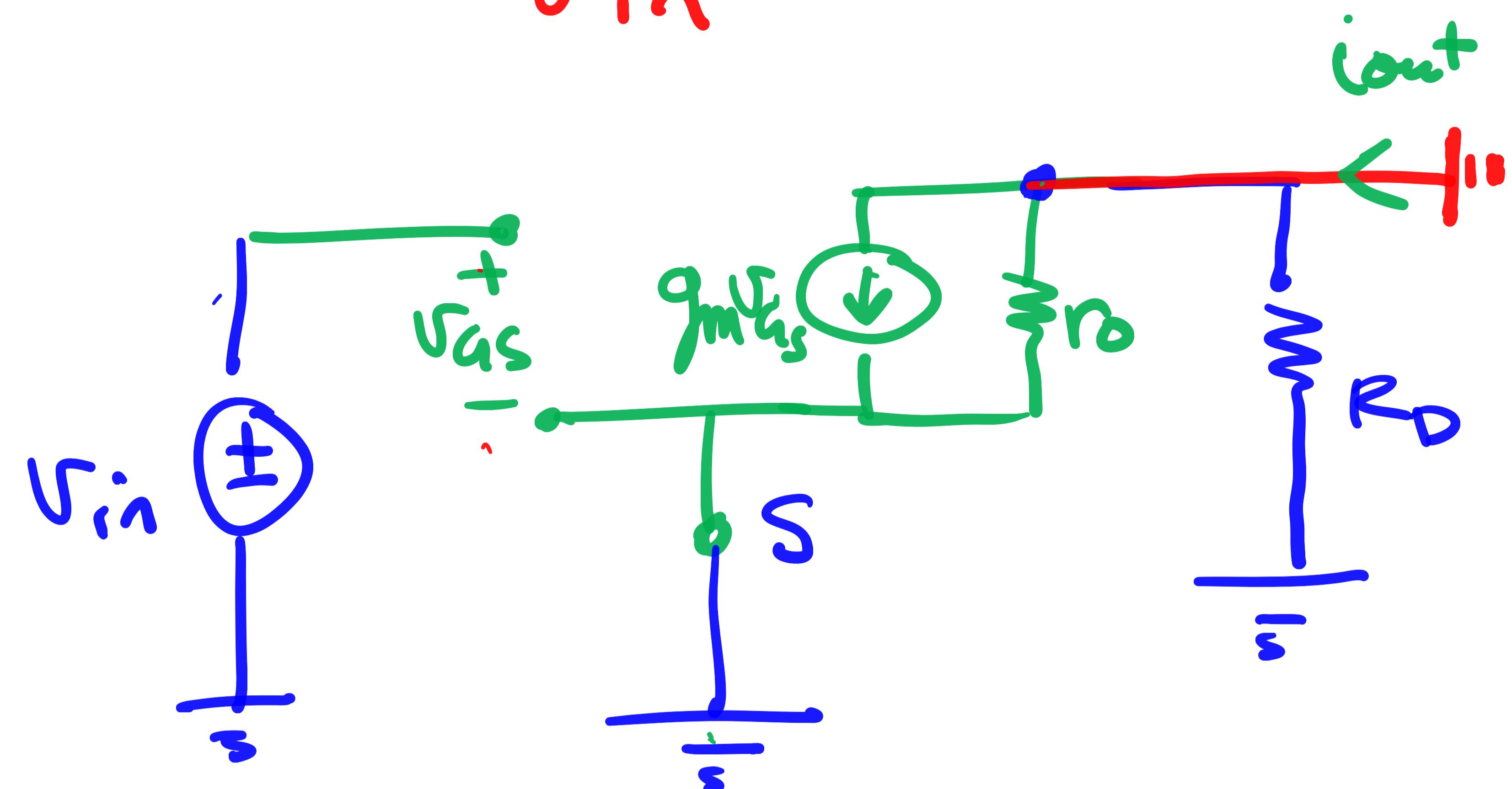
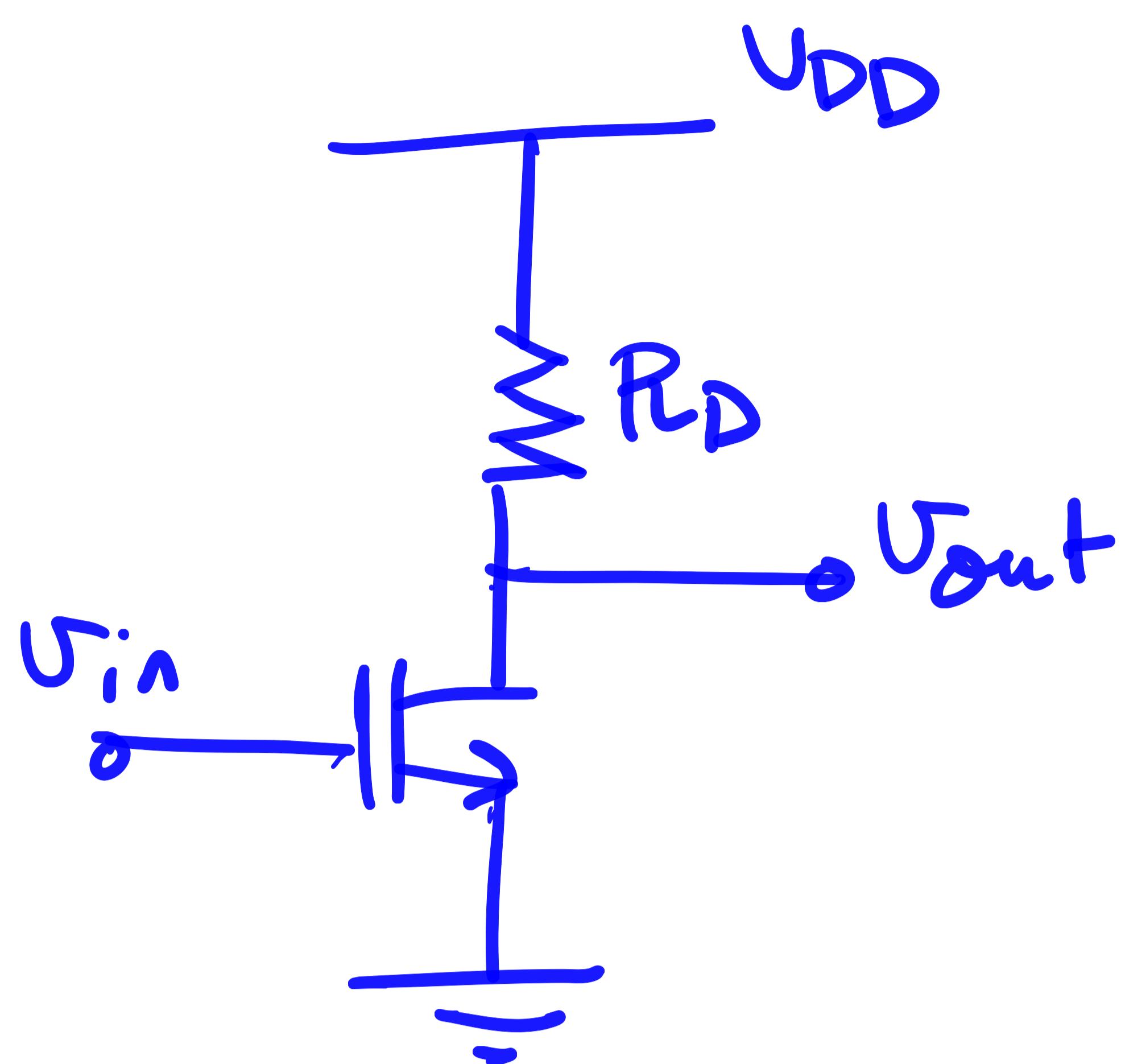
* Short cct. Transconductance technique:



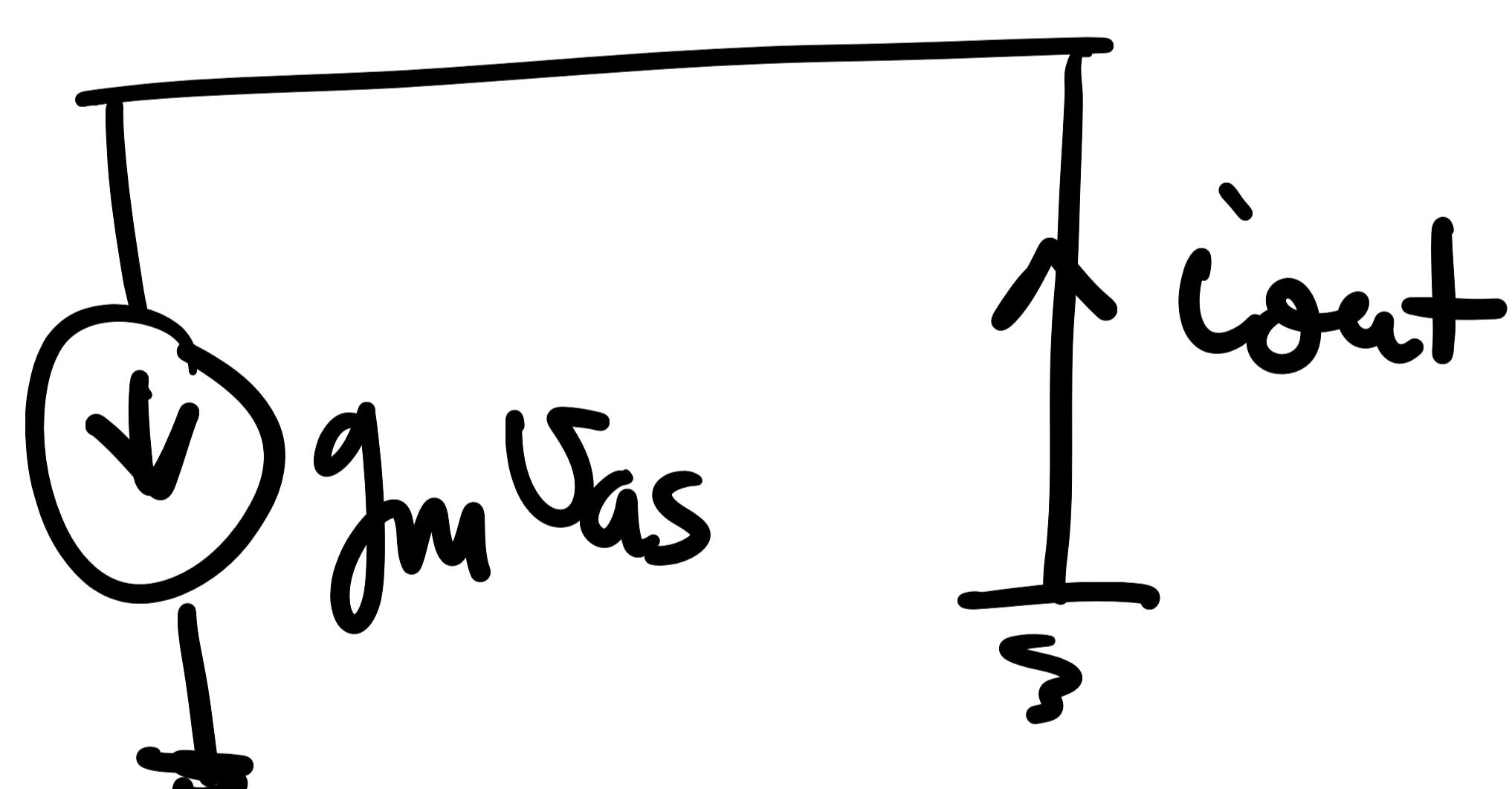
$$G_M = \frac{i_{out}}{V_{in}} \quad |_{V_{out}=0}$$

Ex: Calculate the short cct. transconductance for this CS stage?

$$G_m = \frac{i_{out}}{v_{in}}$$



⇒ due to the shorting of the output



$$i_{out} = g_m v_{AS}$$

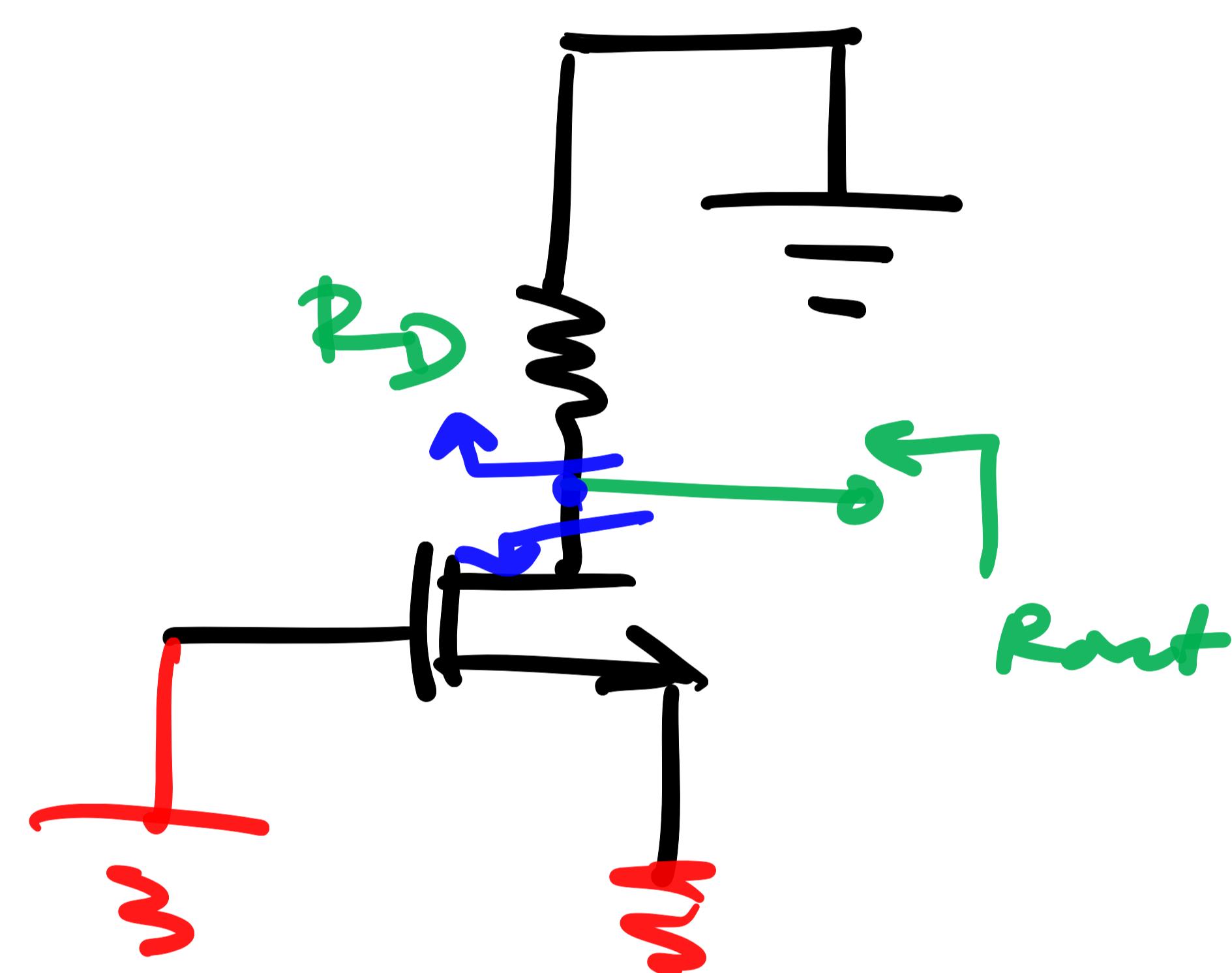
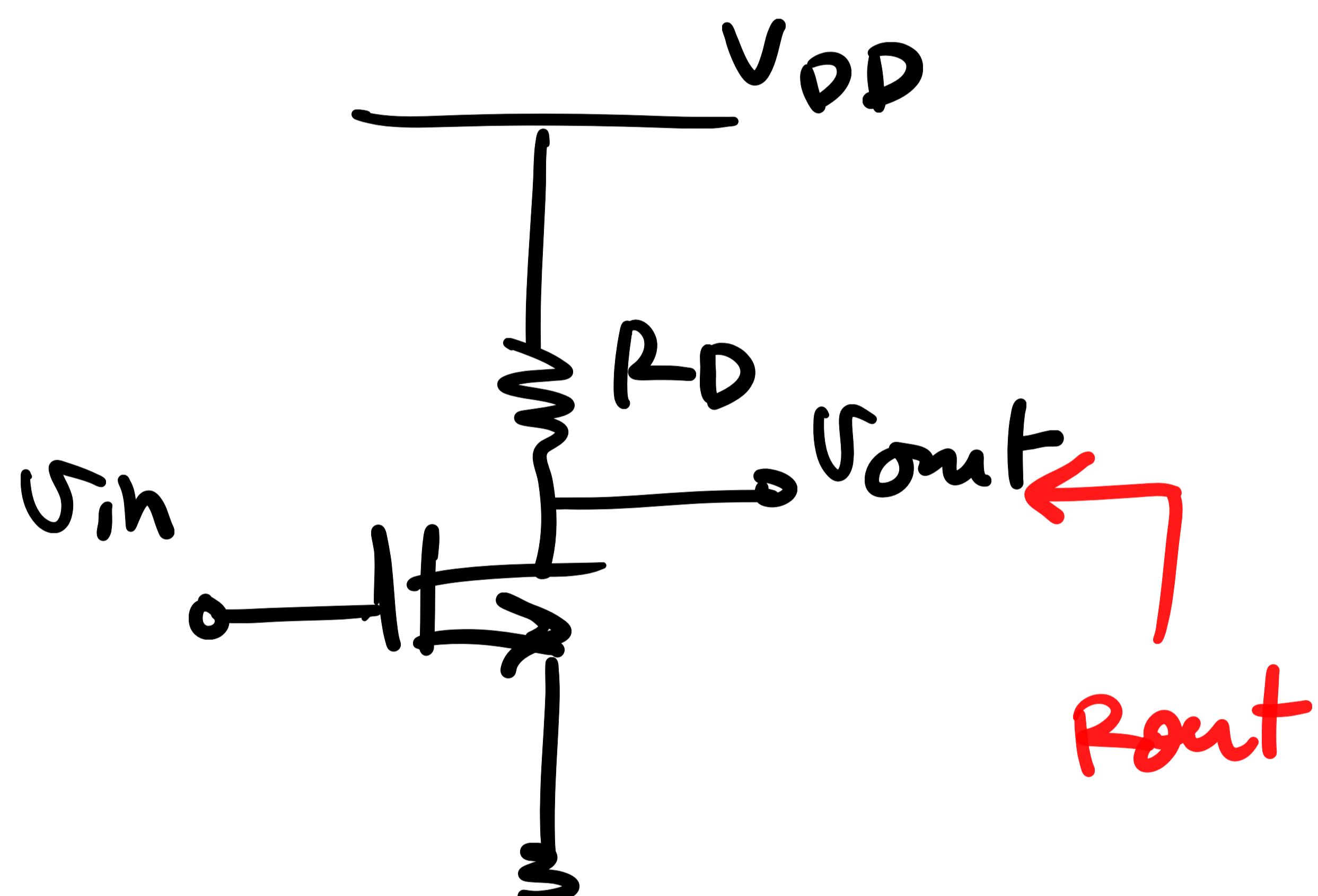
$$\Rightarrow V_{AS} = V_{in} \Rightarrow i_{out} = g_m \cdot V_{in}$$

$$\Rightarrow \frac{i_{out}}{V_{in}} = g_m = G_m$$

* The gain of any stage A_V can be defined as $A_V = - G_m \cdot R_{out}$

* Using the above conclusion show that the gain for the CS stage

$$A_V = G_m \cdot R_{out}$$

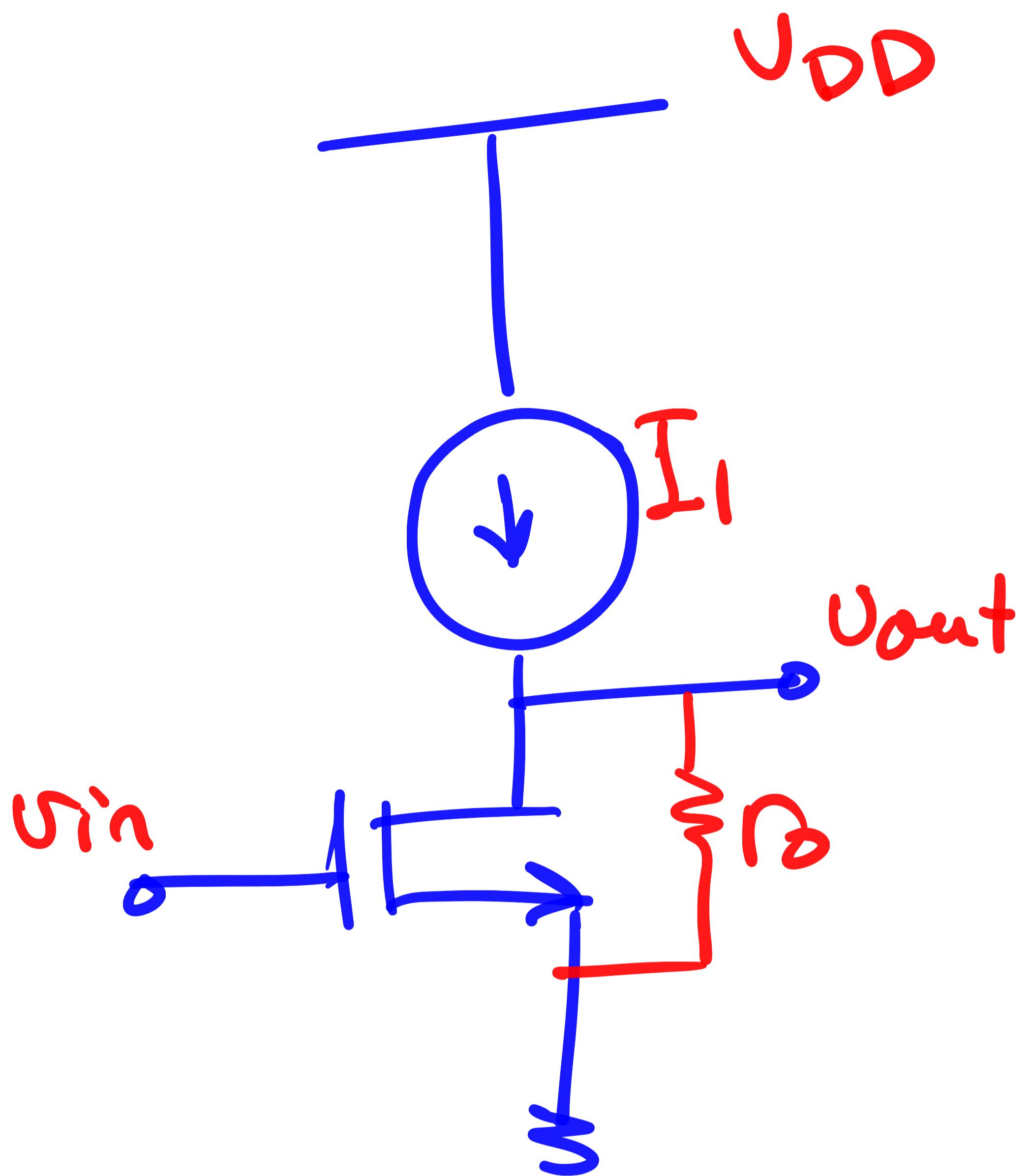


$$R_{out} = R_D \parallel r_o$$

$$A_V = - G_m \cdot R_{out}$$

$$= - g_m \cdot (R_D \parallel r_o)$$

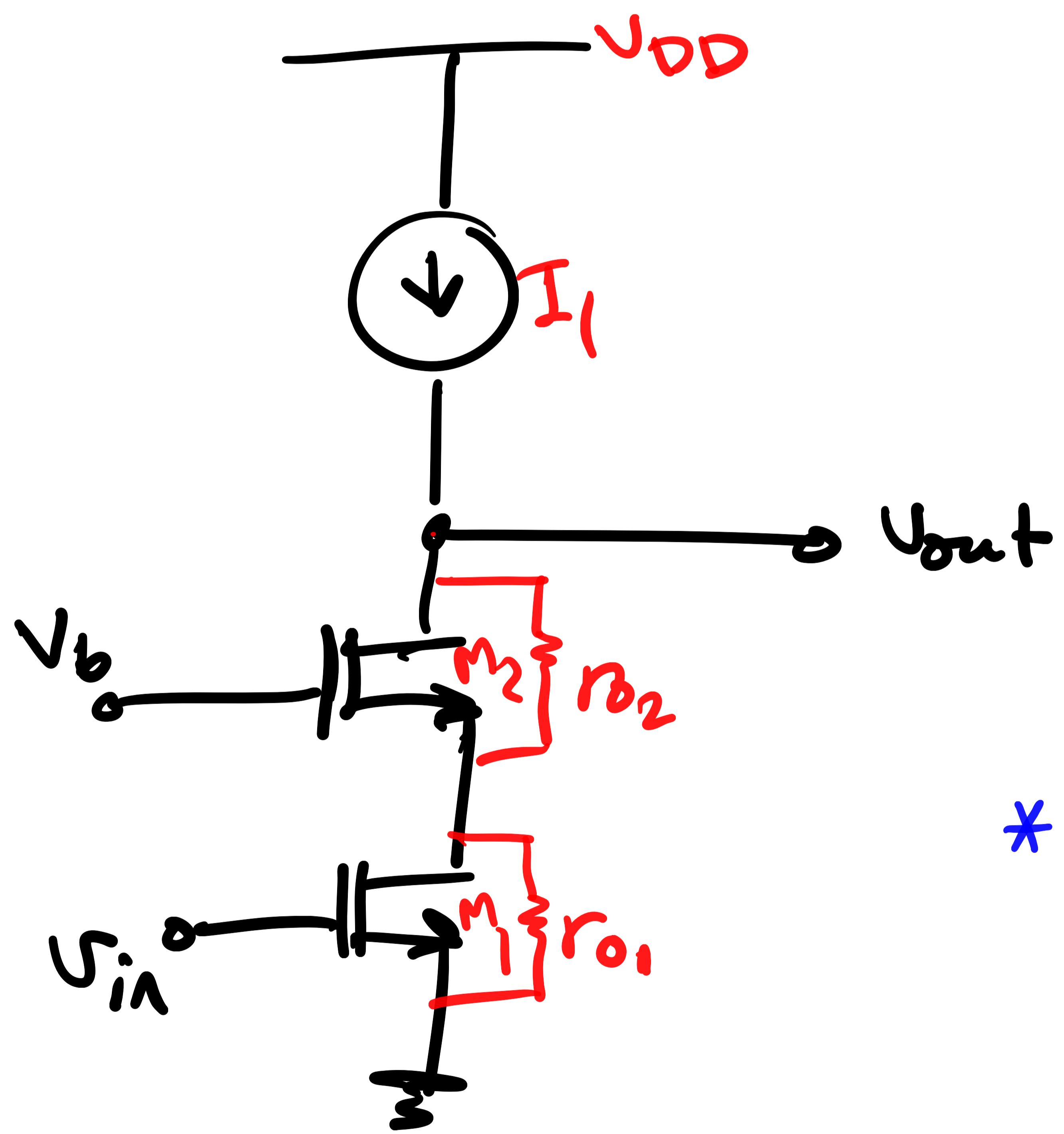
* CasCode Amplifiers :-



$$A_v = -g_m r_o$$

$A_v = -G_m \cdot R_{out}$

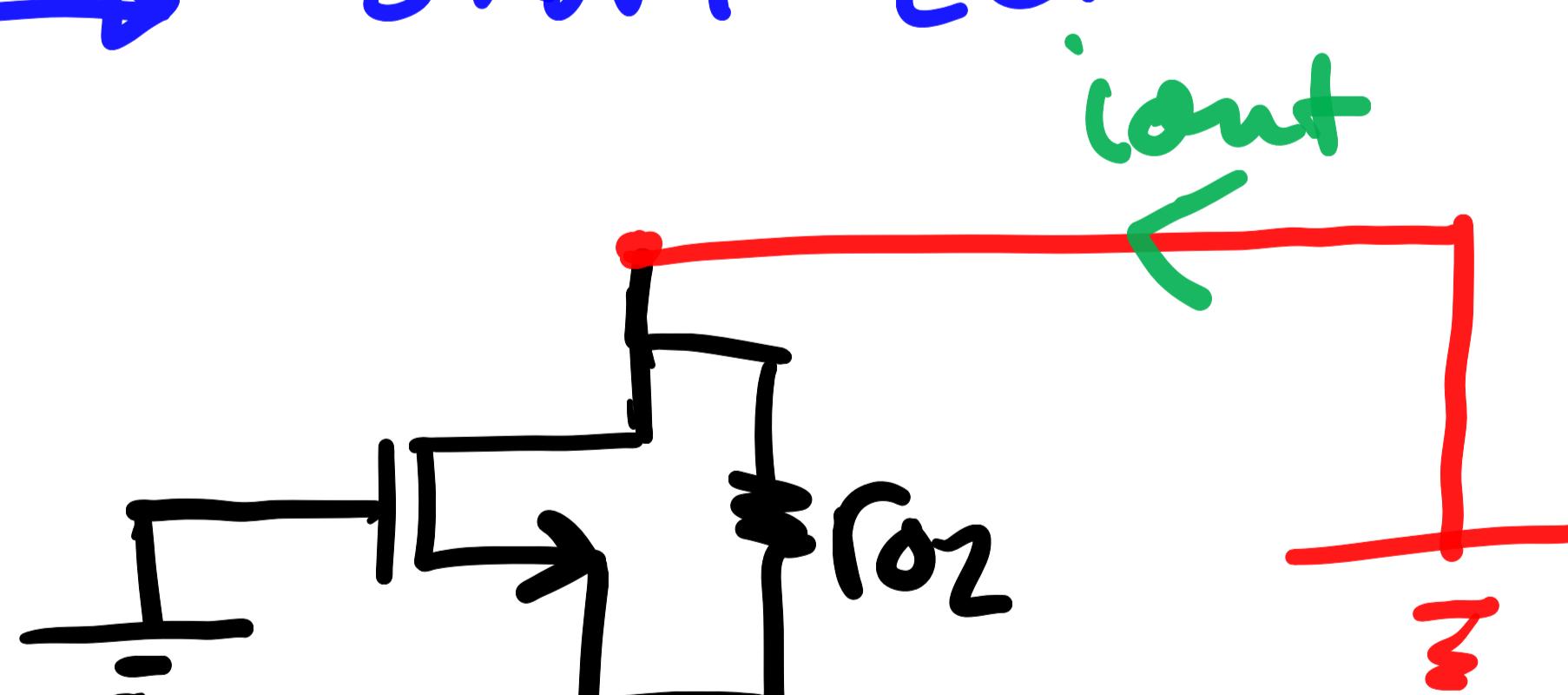
The gain can be increased as follows



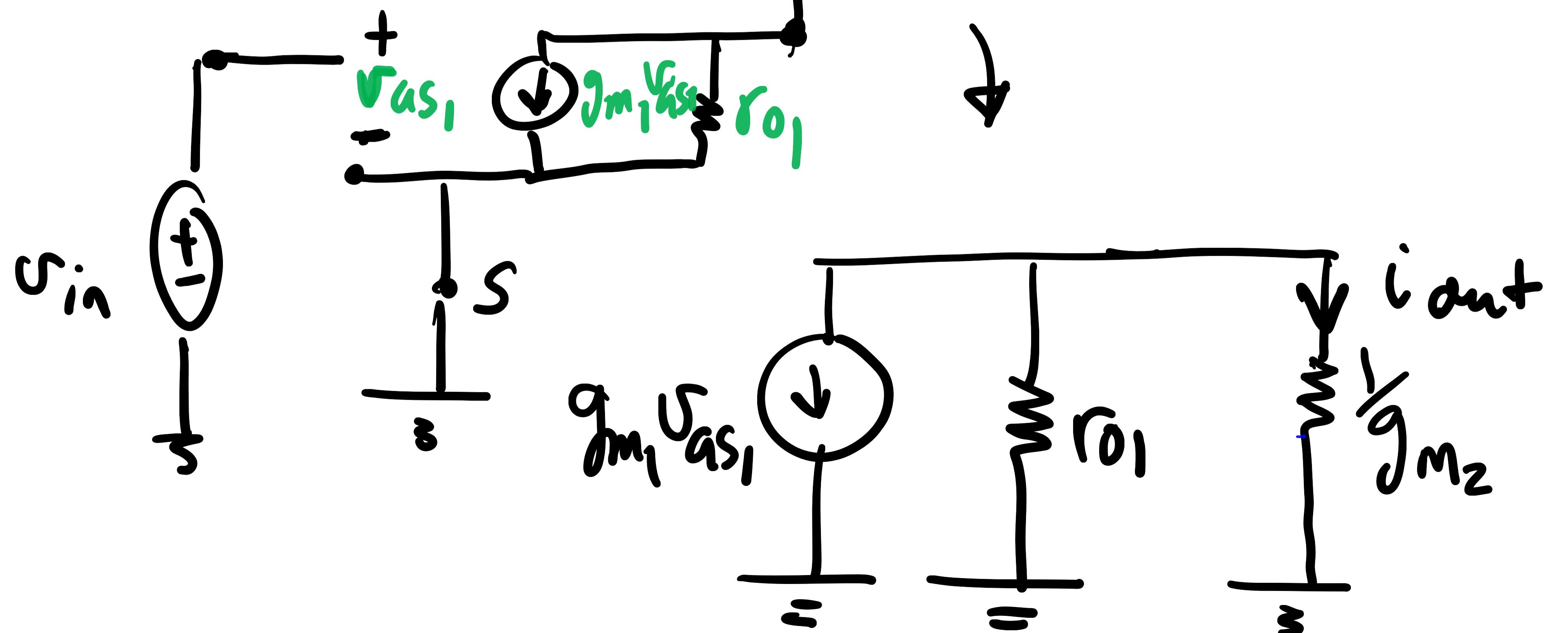
* Applying small signal analysis to find A_v :-

$$A_v = -G_m \cdot R_{out}$$

* $G_m \rightarrow$ short cct. trans.



$$G_m = \frac{i_{out}}{j_{in}}$$

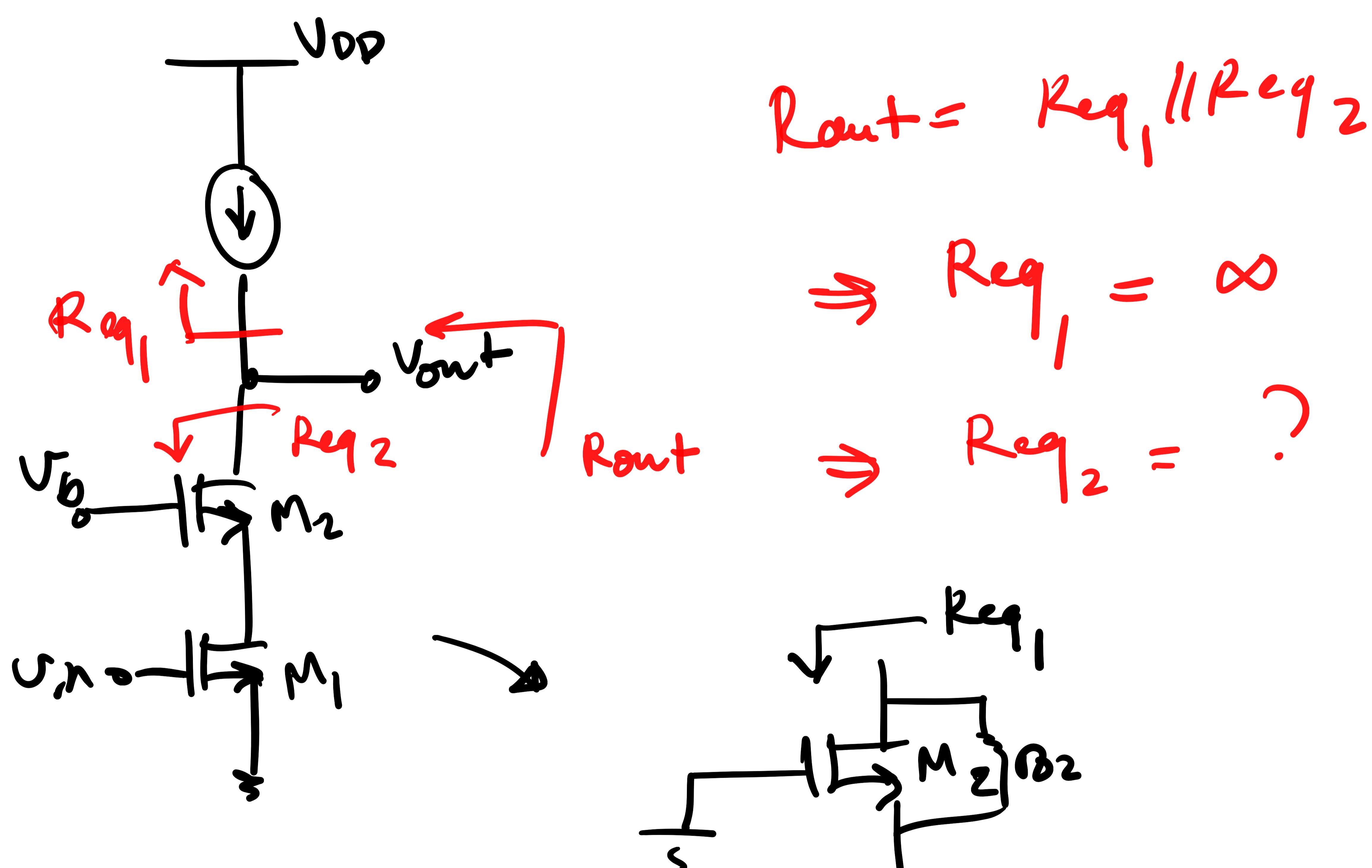


$$i_{out} = \frac{r_o}{r_o + \frac{1}{g_m}} \cdot g_m \cdot v_{as1} \Rightarrow v_{as1} = v_{in}$$

$$i_{out} = \frac{r_o}{r_o + \frac{1}{g_m}} \cdot g_m \cdot v_{in}$$

$$\Rightarrow \frac{i_{out}}{v_{in}} \approx g_m, r_o \gg \frac{1}{g_m}$$

$$G_m = g_m \Rightarrow R_{out} = ?$$



$$R_{eq2} = (1 + g_m r_o) \cdot r_o = r_o$$

$$R_{eq2} \approx g_m r_o = R_{out}$$

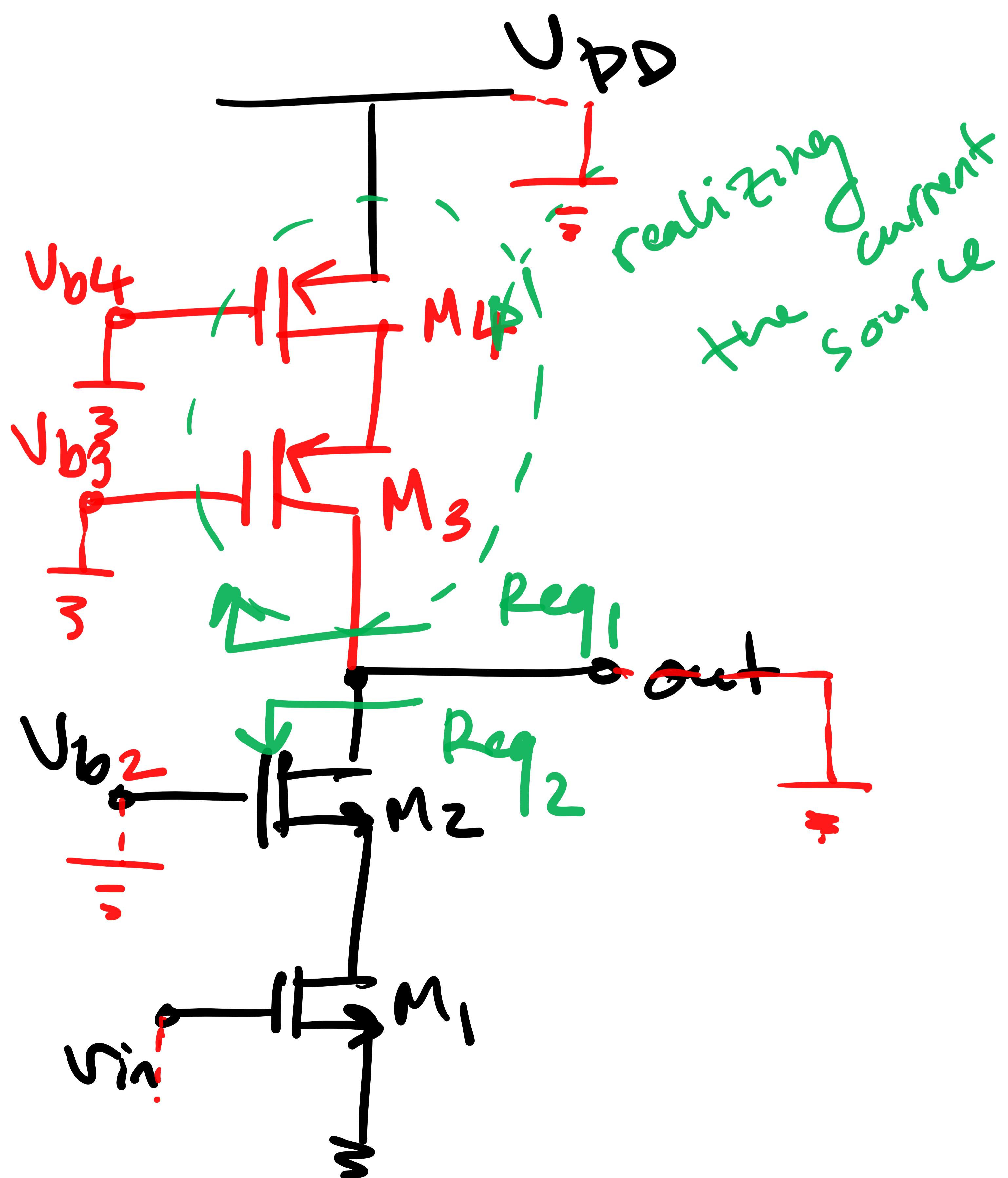
$$A_V \approx -g_{m_1} \cdot g_{m_2} r_o r_o$$

$$A_V \approx -g_{m_1} r_o \cdot g_{m_2} r_o$$

Note that with an ideal current source

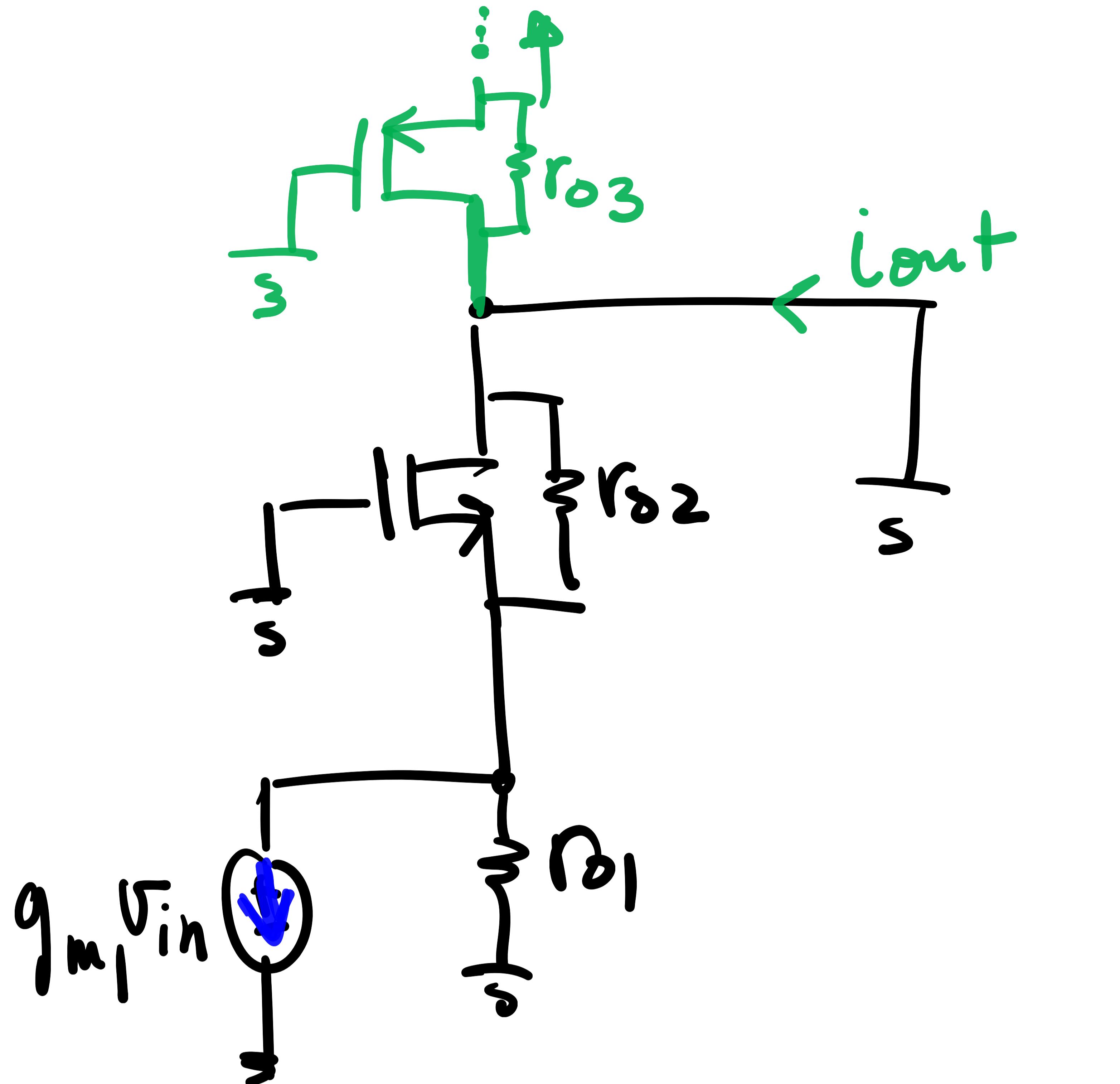
$$A_V = \text{Intrinsic gain 1} \times \text{Intrinsic Gain 2}$$

* When realizing the current source using MOS devices the gain will drop.



To analyze this stage we will repeat the above.

$$A_V = -G_m \cdot R_{out}$$



* Since V_{in} is the only ac small signal source the current i_{out} is not going to travel through M_3 and M_4 due to the short.

$$G_m = g_{m1}$$

$$R_{out} = R_{eq1} \parallel R_{eq2}$$

$$\Rightarrow R_{eq2} = g_{m2} r_{ds1} r_{ds2}, \quad R_{eq1} = g_{m3} r_{ds3} r_{ds4}$$

$$\Rightarrow A_{V \approx} = g_{m1} (g_{m2} r_{ds1} r_{ds2} \parallel g_{m3} r_{ds3} r_{ds4})$$

Ex: In the cct. above

$$(\omega/L)_{1,2} = 30, (\omega/L)_{3,4} = 40$$

$$I_{D1} = I_{D2} = I_{D3} = I_{D4} = 0.5 \text{ mA}$$

$$\mu_{n\text{ox}} = 100 \mu\text{A/V}^2, \mu_{p\text{ox}} = 50 \mu\text{A/V}^2$$

$$\lambda_n = 0.1 \text{ V}^{-1}, \lambda_p = 0.15 \text{ V}^{-1}$$

Find A_v ?

$$|A_v| = g_m_1 \left(g_{m_2} r_{02} r_0 \parallel g_{m_3} r_{03} r_{04} \right)$$

$$g_{m_1} = g_{m_2} = \sqrt{2\mu_{n\text{ox}} \left(\frac{\omega}{L}\right)_{1,2} \cdot I_D} = \frac{1}{577.52}$$

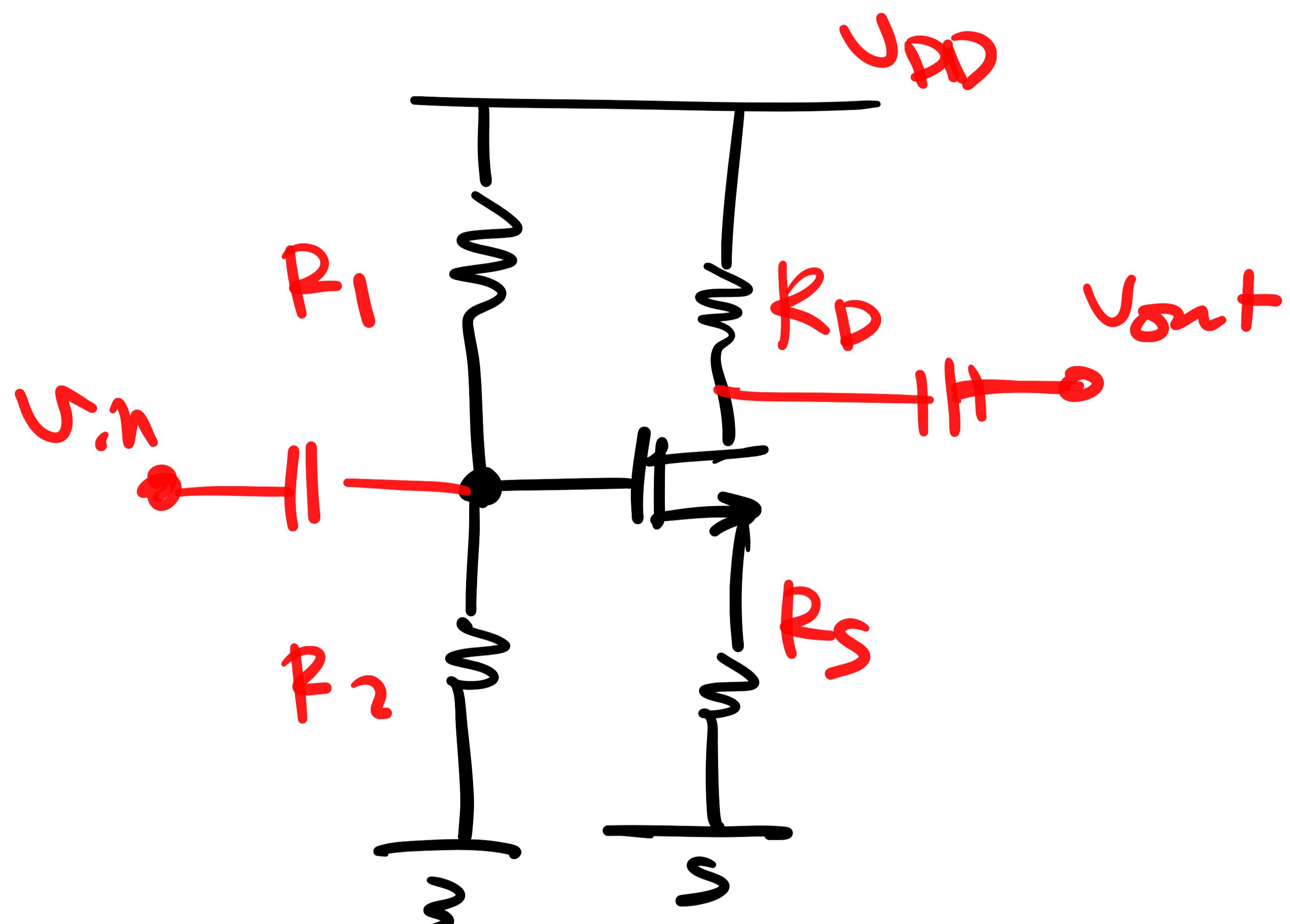
$$g_{m_3} = g_{m_4} = \sqrt{2\mu_{p\text{ox}} \left(\frac{\omega}{L}\right)_{3,4} \cdot I_D} = \frac{1}{707.52}$$

$$r_{01} = r_{02} = \frac{1}{\lambda_n I_D} = 20 \text{ k}\Omega$$

$$r_{03} = r_{04} = \frac{1}{\lambda_p I_D} = 13.3 \text{ k}\Omega$$

$$|A_V| = \boxed{318}$$

* Current Mirrors :-

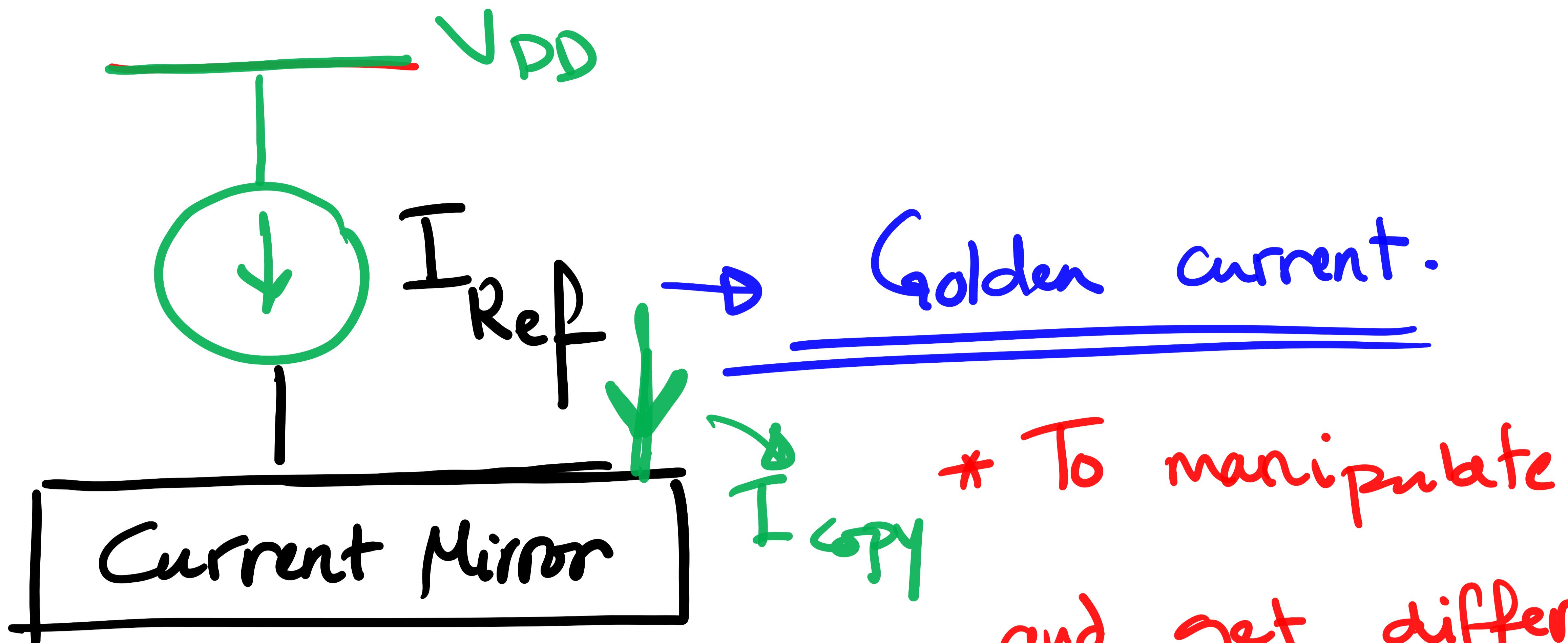


* when designing an amp.
we need to make sure
that I_D is in sat.
and is fixed regardless
of temperature changes
or V_{DD} drainage.

* temp. changes affect V_{TH}

* V_{DD} drainage affects biasing.

* The solution for this problem is to
use a current_source for biasing that
does not get affected by temp. or V_{DD}
changes. This current source is called
"Band-gap-reference-cct"

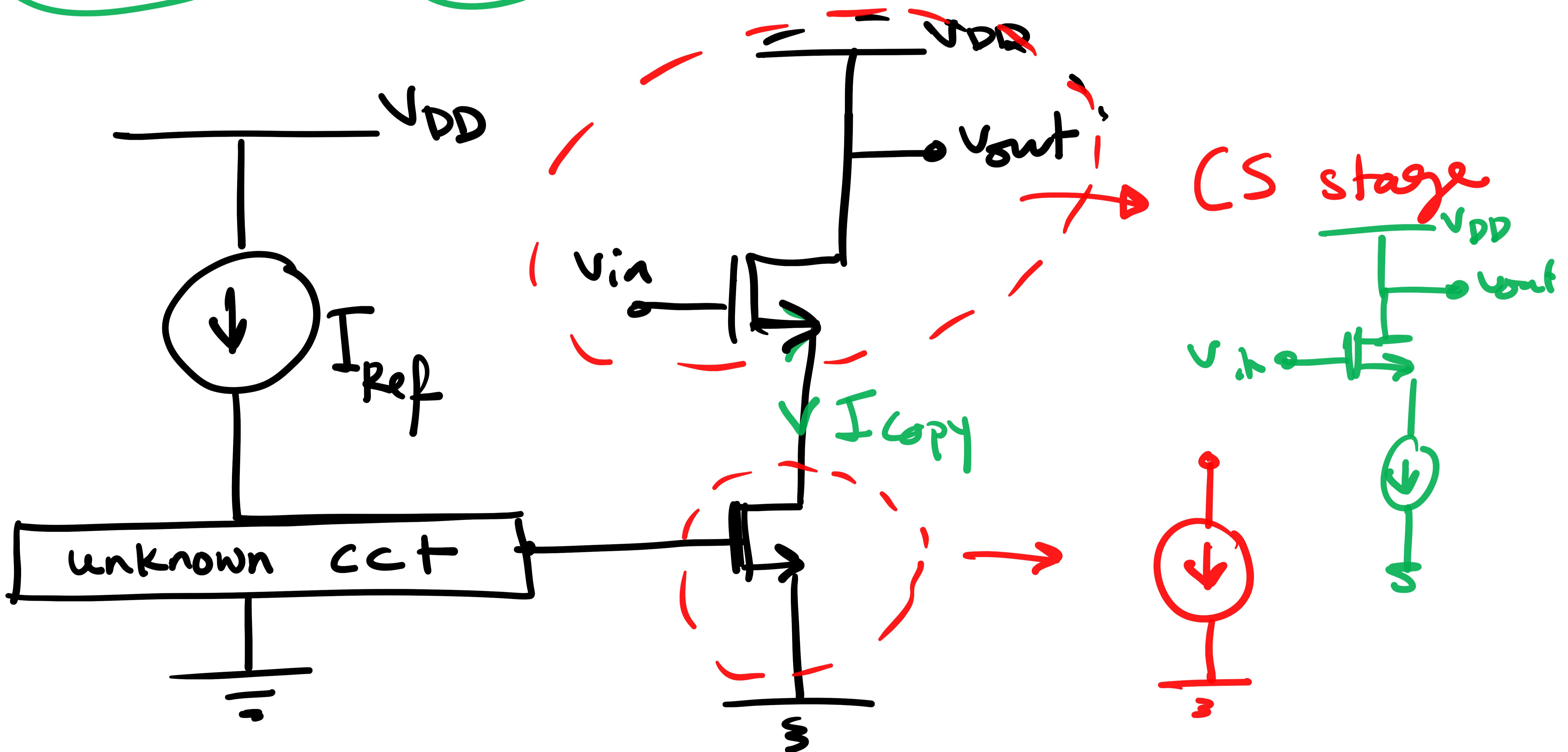


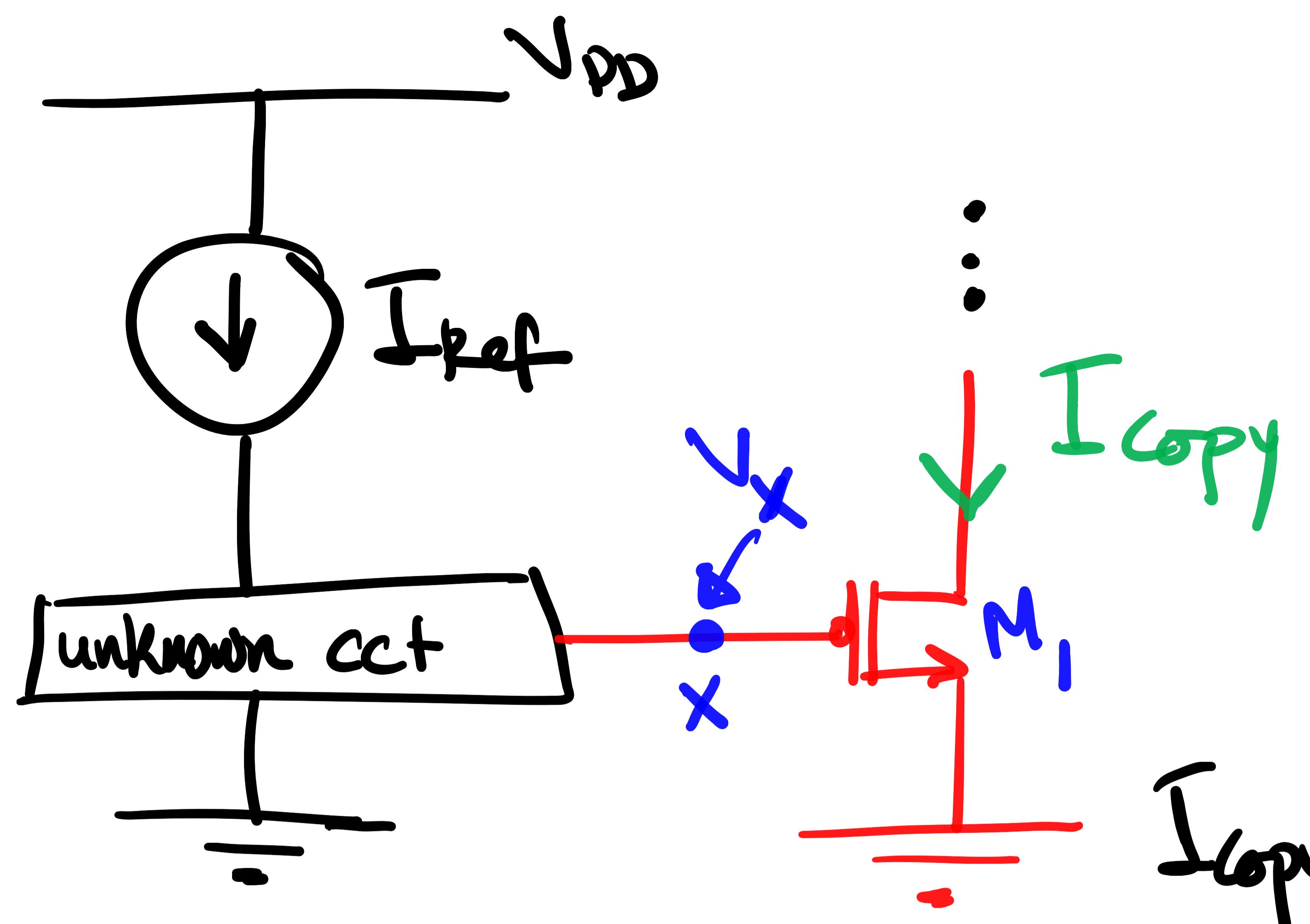
$$I_{Copy} = \alpha \cdot I_{Ref}$$

$0 < \alpha < 1$ either
 $\alpha \geq 1$

* To manipulate I_{Ref}
 and get different
 I_D values out of it
 we use current mirrors.

* The Design of current mirrors:





* V_x is V_{GS1}

$$I_{copy} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L} \right) \cdot (V_{GS} - V_{TH})^2$$

$$I_{copy} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L} \right) \cdot (V_x - V_{TH})^2$$

$$I_{copy} = I_{ref}$$

This unknown cct is responsible for

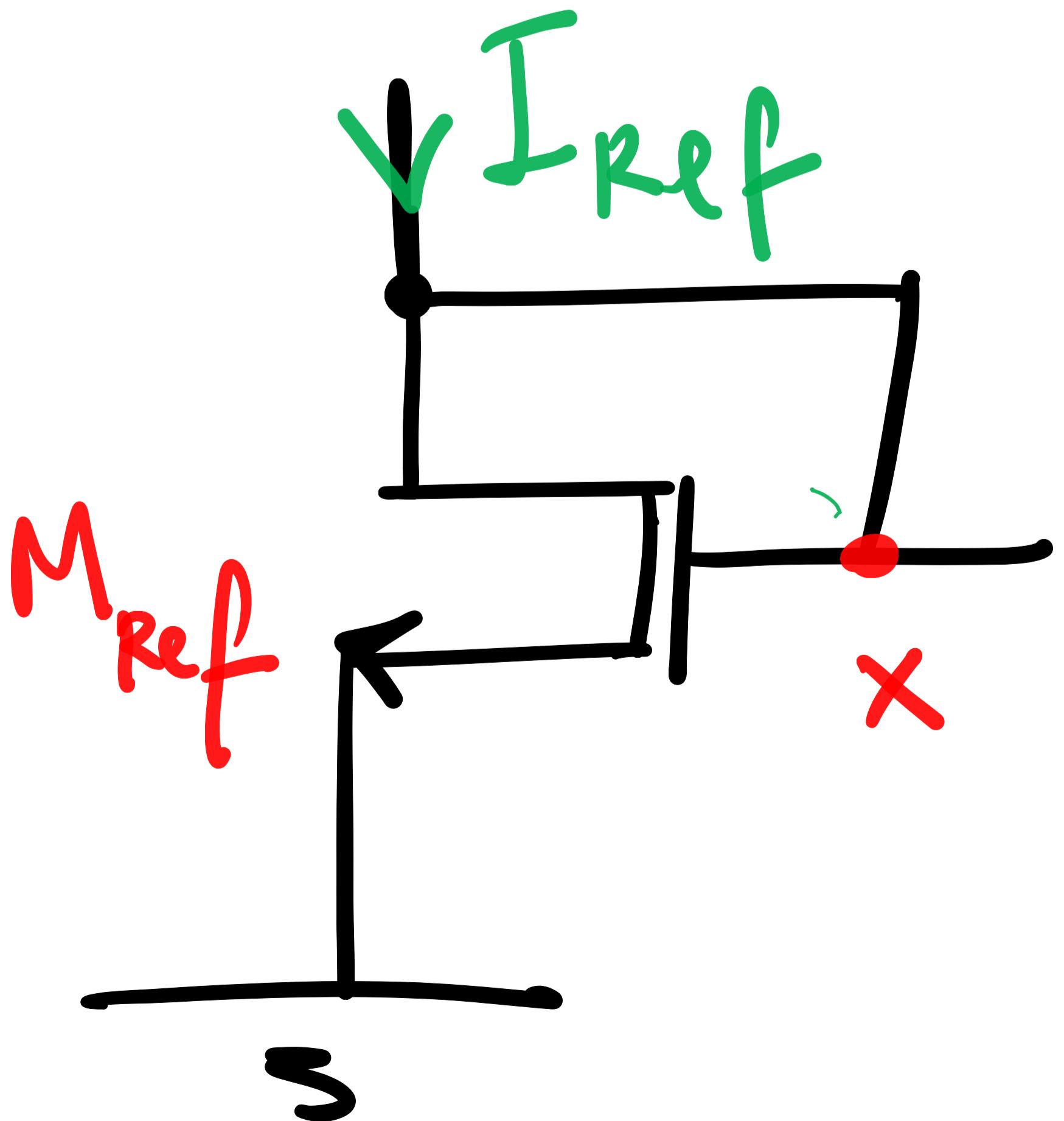
generating V_x that eventually controls

I_{copy} .

$$V_x = \sqrt{\frac{2 I_{ref}}{\mu_n C_{ox} \left(\frac{W}{L} \right)_1}} + V_{TH}$$

* we want a cct. that take $\sqrt{}$ of I_{ref} .

$\sqrt{I_{ref}}$



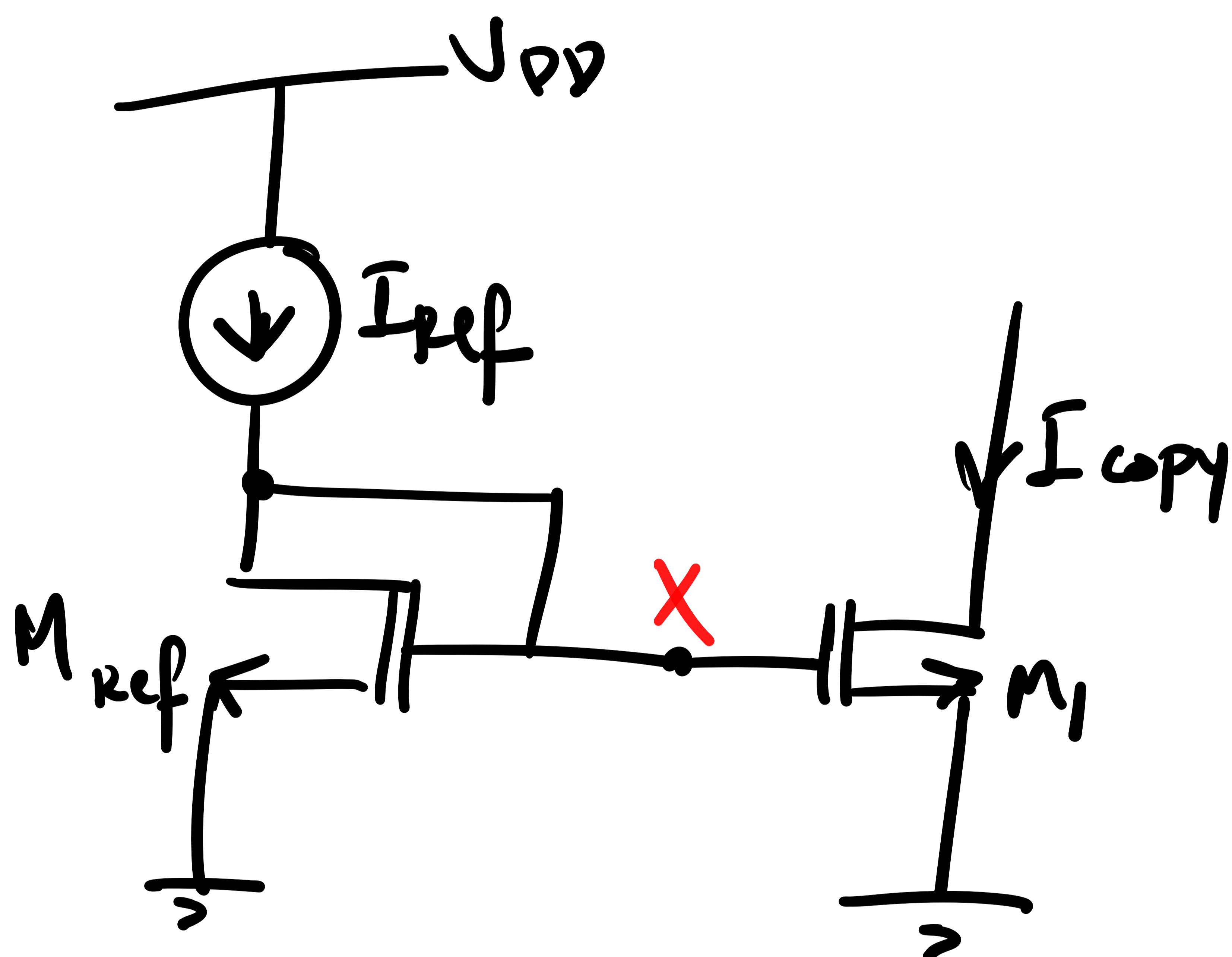
$$I_{ref} =$$

$$\frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L} \right)_{ref} \cdot (V_x - V_{TH})^2$$

$$V_X = \sqrt{\frac{2 I_{\text{ref}}}{\mu_n \text{Lox} \left(\frac{W}{L}\right)_{\text{ref}}}} + V_{TH}$$

$$* I_{\text{copy}} = \frac{1}{2} \mu_n \text{Lox} \left(\frac{W}{L}\right)_I (V_X - V_{TH})^2$$

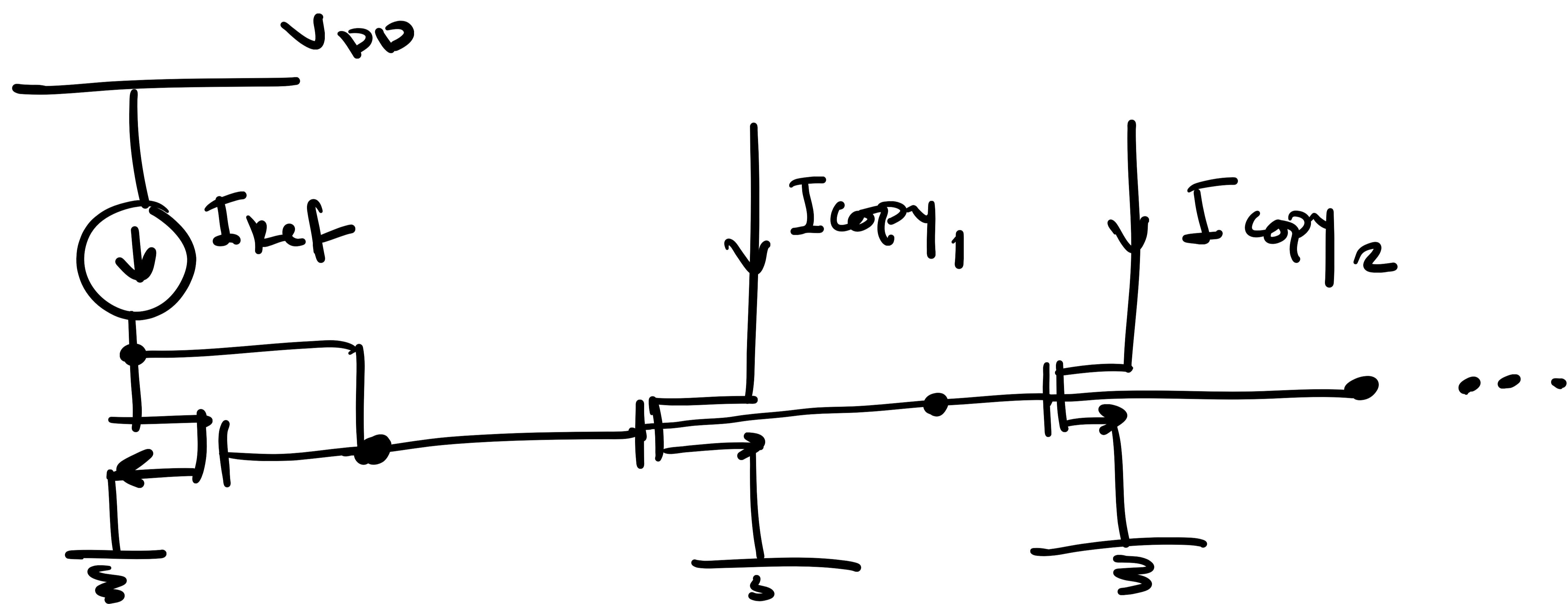
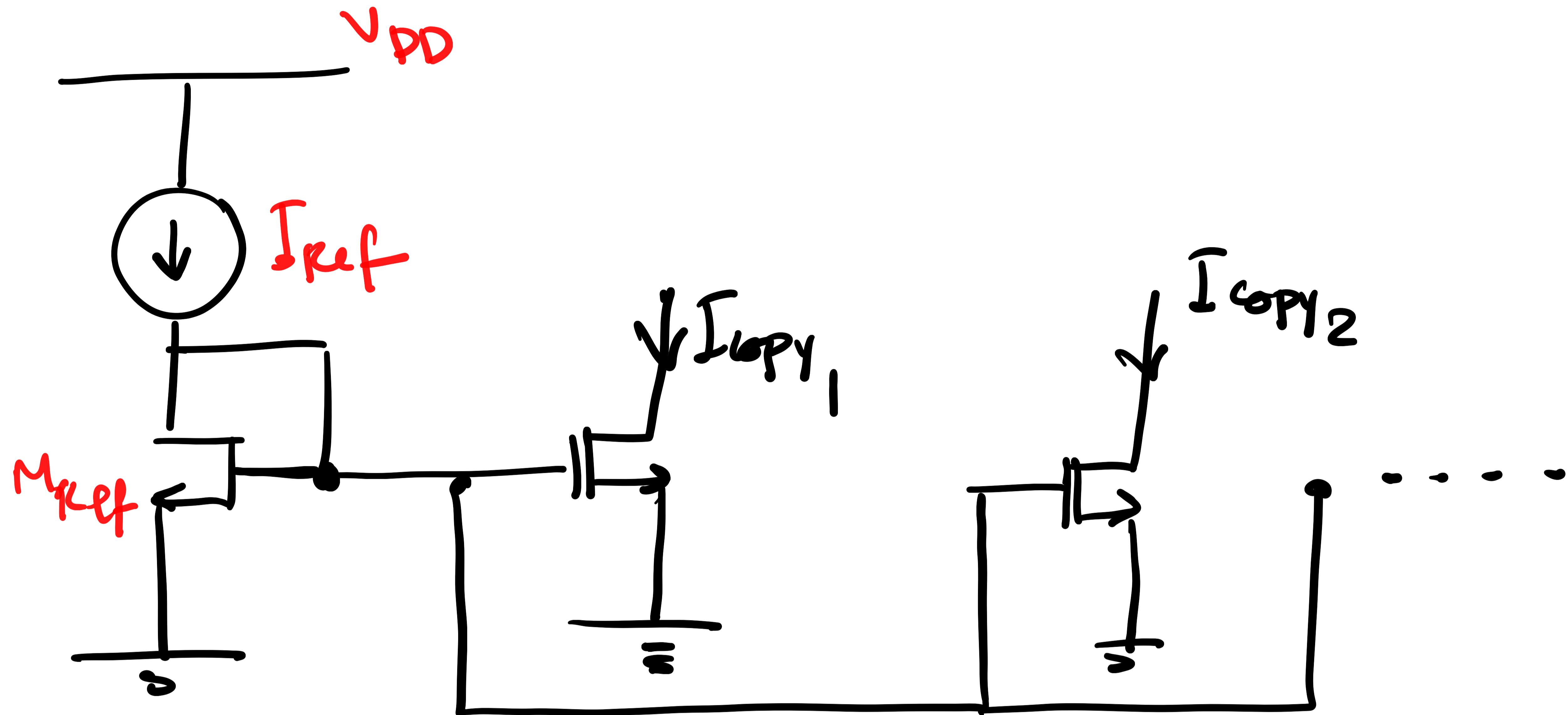
$$* I_{\text{ref}} = \frac{1}{2} \mu_n \text{Lox} \left(\frac{W}{L}\right)_{\text{ref}} (V_X - V_{TH})^2$$



$$\frac{I_{\text{copy}}}{I_{\text{ref}}} = \frac{(W/L)_I}{(W/L)_{\text{ref}}}$$

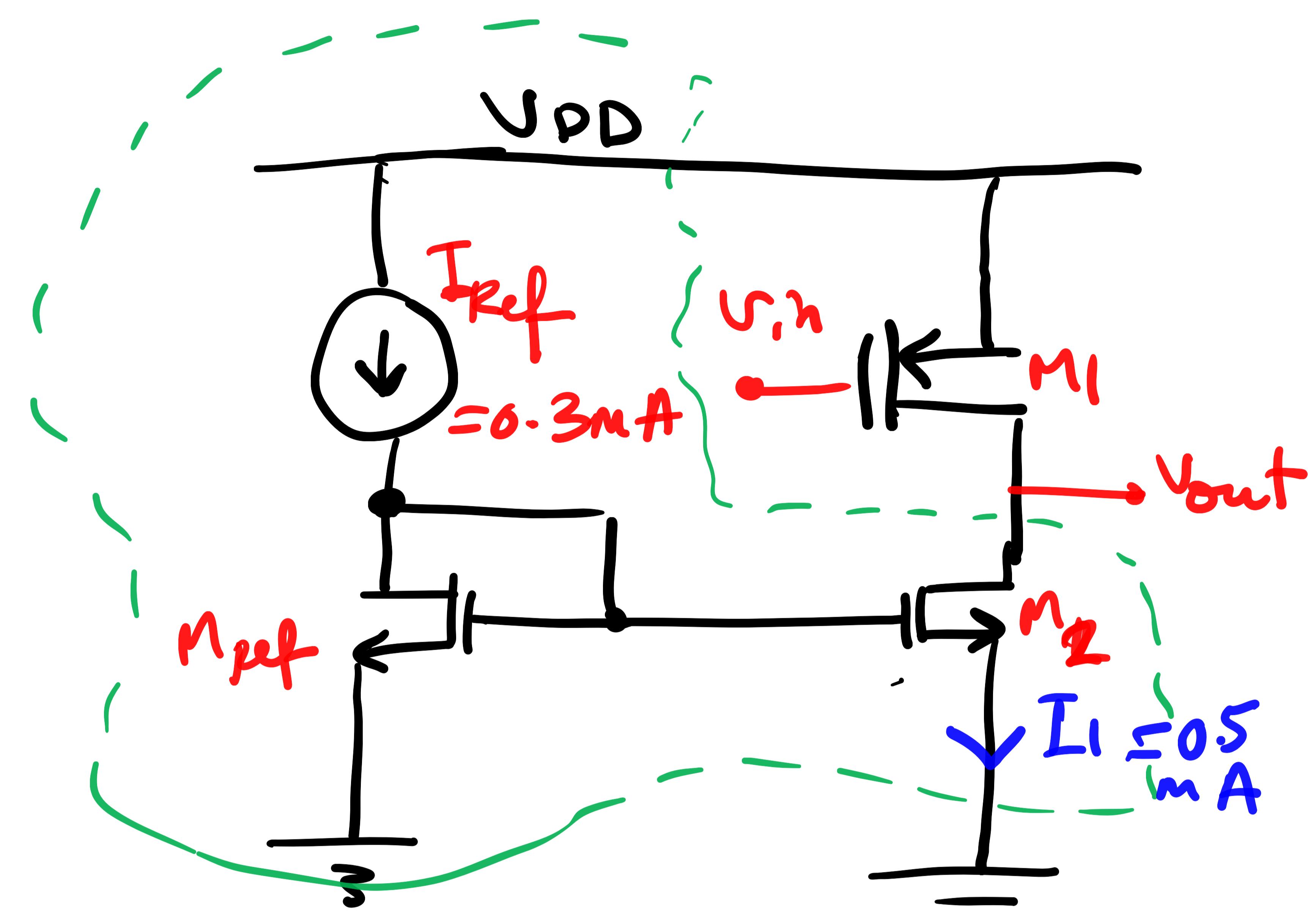
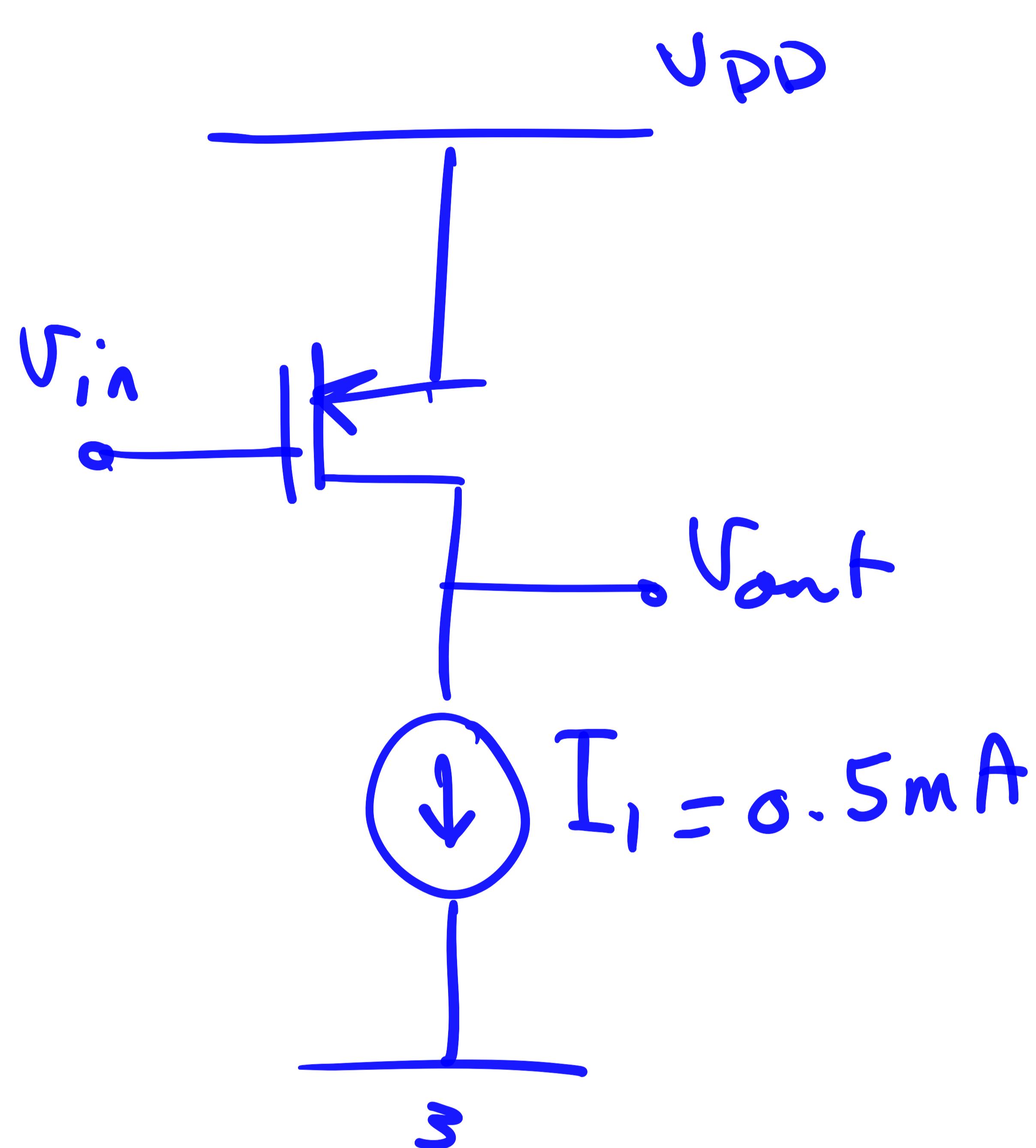
$$I_{\text{copy}} = \frac{(W/L)_I}{(W/L)_{\text{ref}}} \cdot I_{\text{ref}}$$

* Generating multiple currents in a cct. using I_{ref} :-



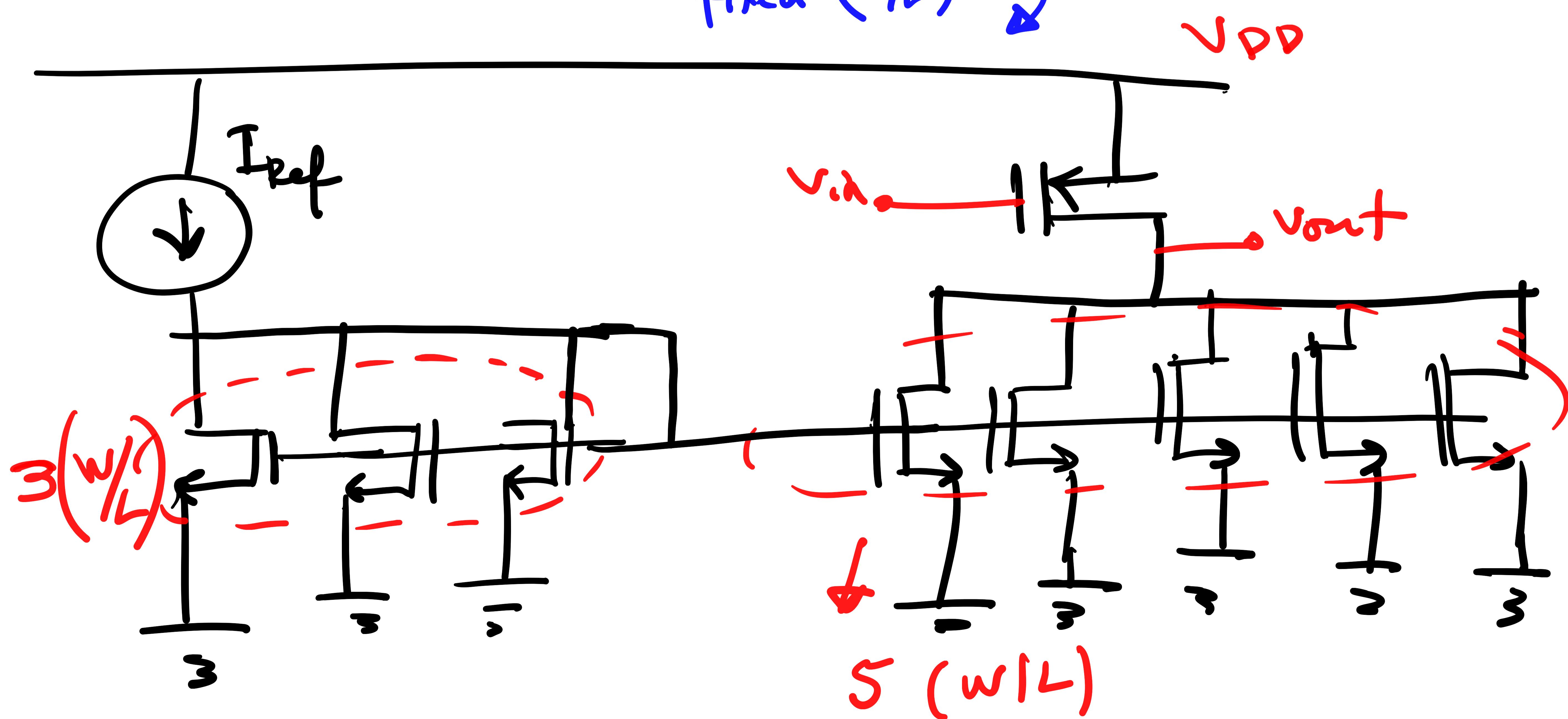
$$I_{copy_j} = \frac{(W/L)_j}{(W/L)_{REF}}$$

Ex: An Integrated cct. employs a CS stage, design a current mirror that produces $I_1 = 0.5 \text{ mA}$ from a $I_{\text{ref}} = 0.3 \text{ mA}$

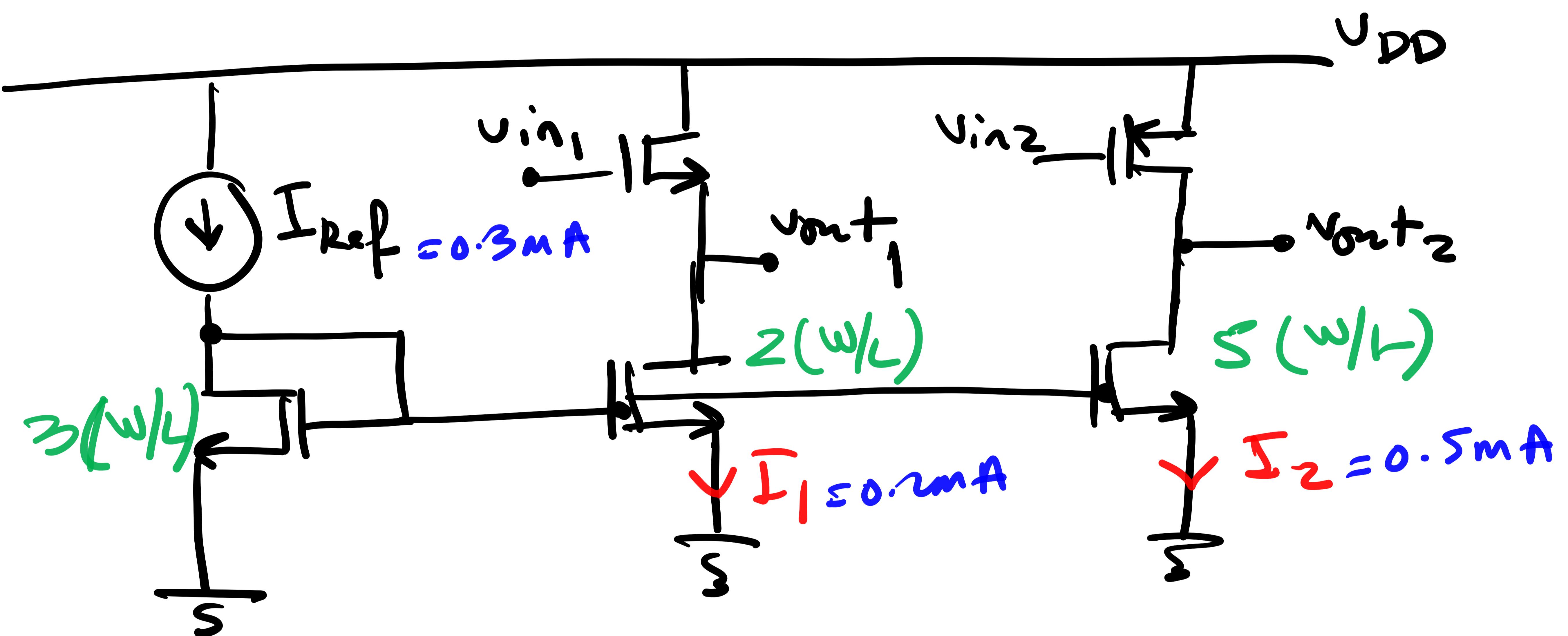
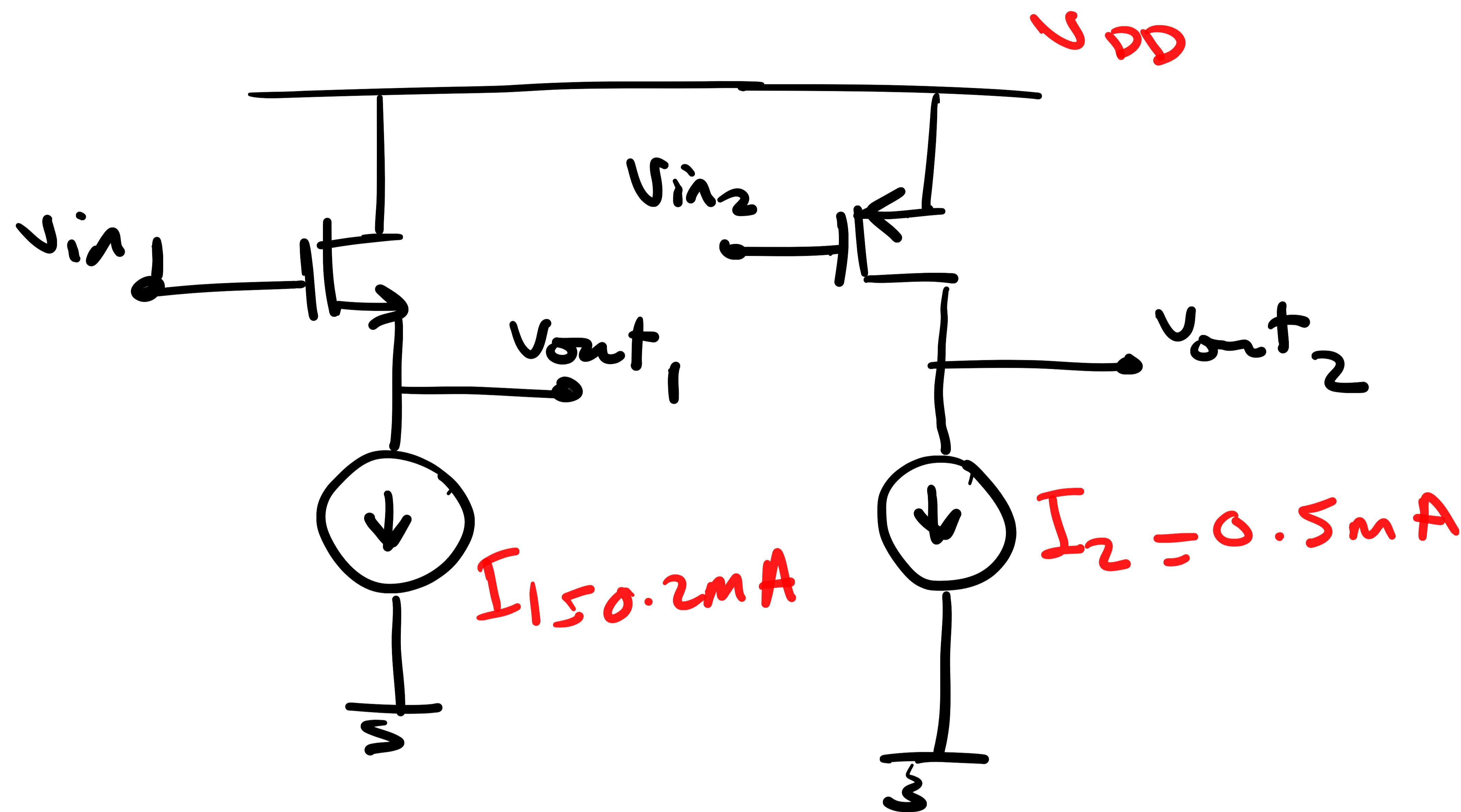


$$\frac{I_1}{I_{\text{ref}}} = \frac{(w/L)_2}{(w/L)_{\text{ref}}} = \frac{0.5 \text{ mA}}{0.3 \text{ mA}} = \frac{5}{3}$$

using unit transistor at
fixed (w/L)



Ex : Design this cct. using an $I_{ref} = 0.3 \text{ mA}$?



$$\frac{I_1}{I_{ref}} = \frac{0.2}{0.3} = \frac{2}{3}, \quad \frac{I_2}{I_{ref}} = \frac{0.5}{0.3} = \frac{5}{3}$$

* PMOS current Mirrors :-

