

Given $f(x)$ value for $x \geq a$ $x \leq b$

are negative, $x \in [a, b]$

$$\int_a^b f(x) dx = \text{Area bounded by } f(x) \text{ and } x\text{-axis}$$

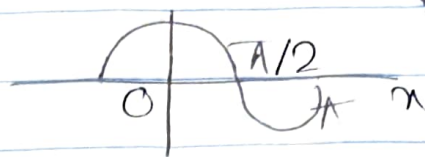
If the graph is (above x -axis - positive
(below x -axis - negative

As $f(x)$ below x -axis, Area is negative

for $x \in [a, b]$

$$\int_a^b f(x) dx \text{ is negative } < 0$$

$$18) \int_0^{\pi} \cos x \, dx$$



$(0 \rightarrow \pi/2) \rightarrow$ positive

$(\pi/2 \rightarrow \pi) \rightarrow$ negative

$$\therefore \text{Net signed area} = \int_0^{\pi} \cos x \, dx$$

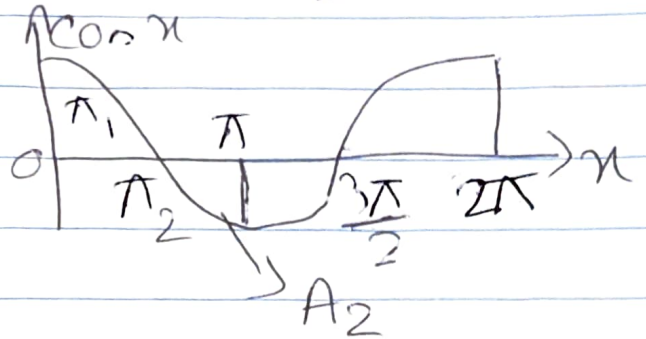
$$= [\sin x]_0^{\pi}$$

$$= \sin \pi - \sin 0$$

$$= 0$$

17) Given, $\int_0^{\pi/2} \cos x \, dx = I$ $\int_{\pi/2}^{\pi} \cos(x) \, dx$

We know,



$0 \leq x < \frac{\pi}{2} \Rightarrow \cos x > 0 \Rightarrow \text{Area I}$

$\frac{\pi}{2} \leq x < \pi \Rightarrow \cos x < 0 \Rightarrow \text{Area 2 } A_2$

We know, both areas are ~~not~~ equal

$\int_{\pi/2}^{\pi} \cos(x) \, dx = A_2 = -I$