Assignment 1 - SOLUTION

Assignment 1 - Objectives:

- Conversion
- · Unsigned and signed arithmetic operations and overflow
- · C programming, endian and bit-level manipulation

Show your work (as illustrated in lectures).

If you write your answers by hand (as opposed to using a computer application to write them), when uploading your answer for each question, please, do not take photos (no .jpg) of your answers even if Crowdmark says so below! Scan them instead! Why? Because photos are often difficult to read. Scanning produces pdf documents of better quality, hence easier to read, hence easier to mark! :)

Marking scheme:

- · This assignment will be marked as follows:
 - Questions 1 and 2 will be marked for correctness.
 - The program for Question 3 will be tested for correctness, robustness and whether all the requirements are satisfied.
- The amount of marks for each question is indicated as part of the question.
- A solution will be posted on Monday after the due date.

Due: Friday January 20 at 23:59:59 on Crowdmark (for Q. 1, Q. 2 and Q. 3) and CourSys (for Q. 3)

Late assignments will receive a grade of 0, but they will be marked (if they are submitted before the solutions are posted on Monday) in order to provide feedback to the student.

Enjoy!

Q1 a.

Conversion

Convert each of the unsigned decimal values below into its corresponding binary value (w = 8), then convert the binary value into its corresponding hexadecimal value.

I. 157₁₀

II. 248₁₀

1.
$$157_{10}$$
 \rightarrow using division \Rightarrow using subtraction $157 \div 2 = 78 RI$ $78 = 39 RO$ $39 = 19 RI$ $13 - 8 (2^4) = 13$ $13 - 8 (2^4) = 15$ $19 = 9 RI$ $19 = 9 RI$ $19 = 10 RI$ $19 = 10 RI$ $10 = 10 R$

2486 = 111110002 = F816 (OXF8)

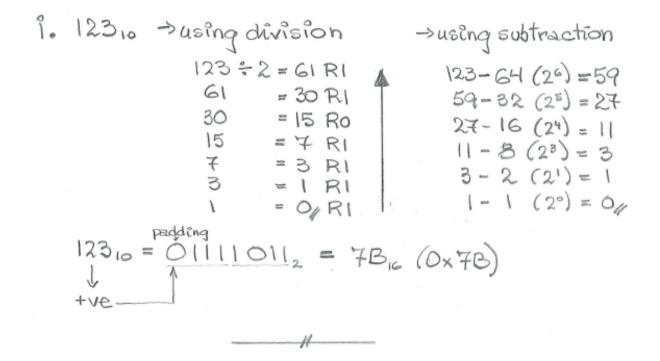
Q1 b. (2 points)

Conversion

Convert each of the signed decimal values below into its corresponding two's complement binary value (w = 8), then convert the binary value into its corresponding hexadecimal value.

I. 123₁₀

II. -74₁₀



91.
$$-74_{10} \rightarrow u2B (-74_{10} + 2^{w}) = u2B (-74_{10} + 256_{0})$$

$$= u2B (182_{10})$$

$$\Rightarrow 182 \div 2 = 91 R0$$

$$91 = 45 R1$$

$$45 = 22 R1$$

$$22 = 11 R0$$

$$11 = 5 R1$$

$$5 = 2 R1$$

$$2 = 1 R0$$

$$1 = 0, R1$$

$$= \frac{101101102}{2} = 86_{10}$$

$$\Rightarrow 182 \div 2 = 91 R0$$

$$1 = 90, R1$$

$$1 = 90, R1$$

$$1 = 101101102 = 101101012$$

$$\Rightarrow 1 - 74_{10} = 74_{10}$$

$$\Rightarrow 1 - 7$$

Q1 c. (2 points)

Conversion

Interpret each of the binary values below (w = 8) first as an unsigned decimal value, then as a signed decimal value (using the two's complement encoding scheme).

I. 11101001₂

II. 10010110₂

B2T (11101001₂)
$$\Rightarrow -1.2^{\frac{1}{4}} + 1.2^{6} + 1.2^{5} + 1.2^{3} + 1.2^{\circ}$$

$$= -128 + 64 + 32 + 8 + 1 = -23_{10}$$

$$\Rightarrow as an unsigned "decimal number"$$

$$B2U (111010012) $\Rightarrow 1.2^{\frac{7}{4}} + 1.2^{6} + 1.2^{5} + 1.2^{3} + 1.2^{\circ}$

$$= 128 + 64 + 32 + 8 + 1 = 233_{10}$$$$

10010110₂
$$\rightarrow$$
 as a signed "decimal number."

B2T (10010110₂) \Rightarrow -1.2⁷ + 1.2⁴ + 1.2² + 1.2¹ -

(can drop "1" \Rightarrow -2⁷ + 2⁴ + 2² + 2¹)

= -128 + 16 + 4 + 2 = -106₁₀,

 \Rightarrow as an unsigned "decimal number."

B2U (10010110₂) \Rightarrow 2⁷ + 2⁴ + 2² + 2¹

= 128 + 16 + 4 + 2 = 150₁₀

Q1 d. (2 points)

Conversion

Convert 247_{10} (unsigned value) into a signed value directly, without converting it first to its corresponding binary value (w = 8).

Answer:
$$U2T(247_{10}) = 247_{10} - 2^{W} = 247_{10} - 2^{8} = 247_{10} - 256 = -9_{10}$$

Q1 e. (2 points)

Conversion

Convert -112₁₀ (signed value) into an unsigned value directly, without converting it first to a binary number (w = 8).

Answer:
$$T2U(-112_{10}) = -112_{10} + 2^{W} = -112_{10} + 2^{8} = -112_{10} + 256 = 144_{10}$$

Q2 a. (3 points)

Unsigned and signed arithmetic operations and overflow

Convert each of the operands (unsigned decimal values), in I. and in II. below, into its corresponding binary value (w = 8), then perform both the decimal addition and the binary addition, indicating the **true sum** and the **actual sum** and whether these two sums are the same or not.

Unsigned addition:

$$1.74_{10} + 63_{10}$$

II.
$$123_{10} + 157_{10}$$

For the binary addition, clearly label all **carry in** bits (by using the label "carry in") and the **carry out** bit (by using the label "carry out").

Finally, indicate whether or not an **overflow** occurred. If an overflow occurred, explain how addition overflow can be detected when adding decimal operands in a C program where you do not have access to the carry out bit.

I.
$$74_{10} + 63_{10}$$

$$74_{10} \rightarrow using subtraction 63_{10}$$
 $74_{-64}(2^{6}) = 10$
 $10_{-8}(2^{3}) = 2$
 $2_{-2}(2^{1}) = 0$
 3_{10}
 3_{10}
 3_{10}

63.0
$$\Rightarrow$$
 using subtraction
63-32 (2⁵)=31
31-16 (2⁴)=15
15-8 (2³)=7
7-4 (2²)=3
3-2 (2¹)=1
1-1 (2⁰)=0

unsigned 137 to 4 true sum
$$\frac{663 \text{ to}}{63 \text{ to}}$$
 $\frac{63 \text{ to}}{137 \text{ to}}$ $\frac{63 \text{ to}}{100010012} = 137 \text{ to}$

Actual sum

"True sum" is what we obtain when we add two operands when we have infinite amount of space (paper) to record the sum.

"Actual sum" is what we obtain when we (the computer) add two operands when we (the computer memory) have finite amount of space to record the sum.

So, True sum = Actual sum -> no overflow occurred, i.e., the True sum has not overflowed the range of unsigned values that can be represented with 8 bits (w = 8) -> $[0..255_{10}]$

(extra) For unsigned addition, we can detect addition overflow when adding decimal operands in a C program, where we do not have access to the carry out bit, (in other words, whether the True sum overflows the range [0 .. 255₁₀] or not) by looking at whether or not the actual sum \geq one of the operand. Here, because $137_{10} \geq 74_{10}$ (or $137_{10} >= 63_{10}$), we know that the **True sum** does not overflow the range (no overflow occurred).

From Practice Problem 2.7 in our textbook:

```
/* Determine whether arguments can be added without
overflow. */
int uadd ok(unsigned x, unsigned y) {
 unsigned sum = x + y;
 return sum >= x; // or return sum >= y;
}
```

II. $123_{10} + 157_{10}$

12310
$$\Rightarrow$$
 using subtraction

123-64 (26) = 59

59-32 (25) = 27

27-16 (24) = 11

11-8 (23) = 3

3-2 (21) = 1

1-1 (20) = 0

: 12310 = OIIIIOII,

157,0
$$\Rightarrow$$
 using subtraction
157-128 (27) = 29
29-16 (24) = 13
13-8 (23) = 5
5-4 (22) = 1
1-1 (20) = 0,

So, True sum != Actual sum -> overflow occurred, i.e., the True sum has overflowed the range of unsigned values that can be represented with 8 bits (w = 8) -> [0..255₁₀]

For unsigned addition, we can **detect** addition overflow when adding decimal operands in a C program, where we do not have access to the carry out bit, (in other words, whether the **True sum** overflows the range $[0...255_{10}]$ or not) by looking at whether or not the actual sum >= one of the operand. Here, because it is not the case that 24_{10} >= 123_{10} (or it is not the case that 24_{10} >= 157_{10}), we know that the **True sum** has overflowed the range (overflow occurred).

From Practice Problem 2.7 in our textbook:

```
/* Determine whether arguments can be added without
overflow. */
int uadd_ok(unsigned x, unsigned y) {
  unsigned sum = x + y;
  return sum >= x; // or return sum >= y;
}
```

Q2 b. (6 points)

Unsigned and signed arithmetic operations and overflow

Convert each of the operands (signed decimal values), in I. to IV. below, into its corresponding **two's complement** binary value (w = 8), then perform both the decimal addition and the binary addition, indicating the **true sum** and the **actual sum** and whether these two sums are the same or not. Signed (two's complement) addition:

$$1.28_{10} + -74_{10}$$

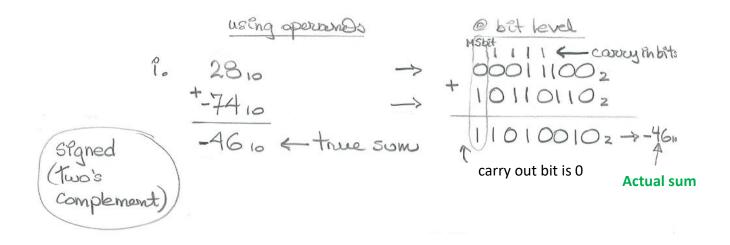
III.
$$74_{10} + 63_{10}$$

For the binary addition, clearly label all **carry in** bits (by using the label "carry in") and the **carry out** bit (by using the label "carry out").

Finally, indicate whether or not a **positive** or a **negative overflow** occurred. If an overflow occurred, explain how addition overflow can be detected when adding decimal operands in a C program where you do not have access to the carry out bit.

I. $28_{10} + -74_{10}$

$$28_{10} \rightarrow using subtraction -74_{10} \rightarrow see Question 1 b. ii.
 $28 - 16(24) = 12$
 $12 - 8(2^3) = 4$
 $4 - 4(2^2) = 0$$$



So, True sum = Actual sum -> no (positive/negative) overflow occurred, i.e., the True sum has not overflowed the range of signed values that can be represented with 8 bits $(w = 8) \rightarrow [-128_{10}...127_{10}].$

(extra) For signed (two's complement) addition, we can **detect** positive or negative addition overflow when adding decimal operands in a C program, where we do not have access to the carry out bit, (in other words, whether the **True sum** overflows the positive or negative range $[-128_{10}...127_{10}]$ or not) by looking at whether or not

 $x \ge 0 \& y \ge 0 \& actual sum < 0 -> if true, then positive overflow$

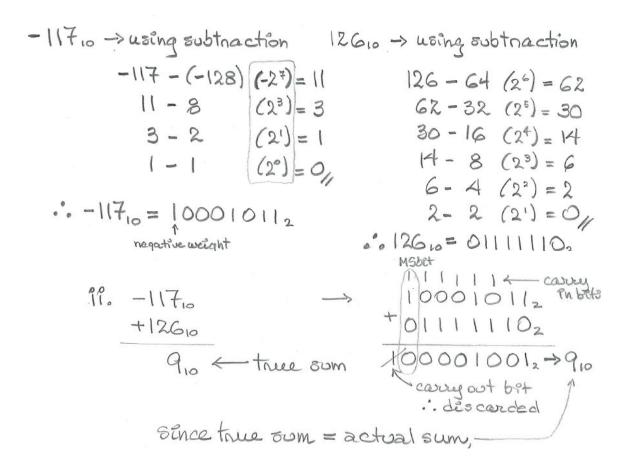
or

x < 0 && y < 0 && actual sum >= 0 -> if true, then negative overflow Here, because it is not the case (it is false) that

 $28_{10} >= 0 \&\& -74_{10} >= 0 \&\& -46_{10} < 0 -> true \&\& false \&\& true = false$

or

 $28_{10} < 0 \&\& -74_{10} < 0 \&\& -46_{10} >= 0$ -> false && true && false = false then we know that the **True sum** does not overflow the range (no overflow occurred).



So, True sum = Actual sum -> no (positive/negative) overflow occurred, i.e., the True sum has not overflowed the range of signed values that can be represented with 8 bits $(w = 8) -> [-128_{10}...127_{10}].$

(extra) For signed (two's complement) addition, we can **detect** positive or negative addition overflow when adding decimal operands in a C program, where we do not have access to the carry out bit, (in other words, whether the **True sum** overflows the positive or negative range [-128₁₀ .. 127₁₀] or not) by looking at whether or not

 $x \ge 0 \&\& y \ge 0 \&\&$ actual sum < 0 -> if true, then positive overflow

or

x < 0 && y < 0 && actual sum >= 0 -> if true, then negative overflow Here, because it is not the case (it is false) that

 $-117_{10} >= 0 \&\& 126_{10} >= 0 \&\& 9_{10} < 0 -> false \&\& true \&\& false = false$

or

 $-117_{10} < 0 \&\& 126_{10} < 0 \&\& 9_{10} >= 0 -> true \&\& false \&\& ture = false$ then we know that the **True sum** does not overflow the range (no overflow occurred).

III.
$$74_{10} + 63_{10}$$

For T2B(74₁₀) and T2B(63₁₀), see Question 2 a. i.

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Msbet

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 $+6$

Signed (two's complement)

True sum + actual sum

So, **True sum** != **Actual sum** -> **positive overflow occurred**, i.e., the **True sum** overflows the positive side of the range of signed values that can be represented by 8 bits (w = 8). Indeed, 137_{10} is beyond the positive side of the range [- 128_{10} .. 127_{10}].

For signed (two's complement) addition, we can **detect** positive or negative addition overflow when adding decimal operands in a C program, where we do not have access to the carry out bit, (in other words, whether the **True sum** overflows the positive or negative range $[-128_{10} ... 127_{10}]$ or not) by looking at whether or not

 $x \ge 0 \&\& y \ge 0 \&\& actual sum < 0 -> if true, then positive overflow$

O

x < 0 && y < 0 && actual sum >= 0 -> if true, then negative overflow Here, because it is the case (it is true) that

 $74_{10} >= 0 \&\& 63_{10} >= 0 \&\& -119_{10} < 0 -> true \&\& true &\& true = true$

then we know that a positive overflow occurred (the **True sum** does overflow the positive range).

= 119.6
$$\rightarrow$$
 using subtraction $-105_{10} \rightarrow$ using subtraction $-119 - (-128)(-27) = 9$ $-105 - (-128)(-27) = 23$ $9 - 8(27) = 1$ $23 - 16(27) = 7$ $7 - 4(27) = 3$ $3 - 2(27) = 1$ $1 - 1(2^{\circ}) = 0$ $3 - 2(27) = 1$ $1 - 1(2^{\circ}) = 0$ $3 - 2(27) = 1$ $1 - 1(2^{\circ}) = 0$ $0 - 10010111_2$

True sum + actual sum

So, True sum != Actual sum -> negative overflow occurred, i.e., the True sum overflows the negative side of the range of signed values that can be represented by 8 bits (w = 8). Indeed, -224₁₀ is beyond the negative side of the range [-128..127].

For signed (two's complement) addition, we can **detect** positive or negative addition overflow when adding decimal operands in a C program, where we do not have access to the carry out bit, (in other words, whether the **True sum** overflows the positive or negative range $[-128_{10}...127_{10}]$ or not) by looking at whether or not

 $x \ge 0 \&\& y \ge 0 \&\& actual sum < 0 -> if true, then positive overflow$

or

x < 0 && y < 0 && actual sum >= 0 -> if true, then negative overflow Here, because it is the case (it is true) that

```
-119_{10} < 0 \&\& -105_{10} < 0 \&\& 32_{10} >= 0 -> true \&\& true \&\& true = true
```

then we know that a negative overflow occurred (the **True sum** does overflow the negative range).

Q3 (13 points)

C Code, endian and bit-level manipulation

Download Assn1-files.zip from our course web site then extract and open Assn1_Q3.c, Assn1_main.c and makefile in a text editor. Read and understand their content.

Using the makefile, compile and execute the program.

Make sure you do all this on our **target machine**. Why? Because, when marking your assignment, the TA will be compiling and testing your code on the target machine. Hence, you want to make sure the code you submit does compile and execute as expected on the target machine.

Requirements:

- While answering this question, you must not change the prototype of the functions given. The reason is that these functions will be tested using a test driver built based on these function prototypes.
- Your code must be readable and easy to understand. Therefore:
 - o Comment your code and write your program such that its statements are well spaced.
 - · No goto statements, please!

a. [2 marks] Modify the printf statement of the show_bytes(...) function such that it first prints the memory address of each byte then the content of the byte itself on its own line. Here is an example:

0x7ffe5fb887cc 0x80

where 0x7ffe5fb887cc is the memory address of a byte which contains the value 0x80. Compile and test your program.

```
// Q3 a.
void show_bytes(byte_pointer start, size_t len) {
    size_t i;
    for (i = 0; i < len; i++)
        // printf(" %.2x", start[i]); // Original statement
        printf("%p 0x%.2x\n", &start[i], start[i]);
    printf("\n");
    return;
}</pre>
```

b. [2 marks] Looking at the output of this program, would you say that our target machine is a **little endian** or a **big endian** computer? Justify your answer by including some of the output of your program in your answer and pointing out the endianness.

Put your answer to this question in your Assn1_Q3.c file, just below the show_bytes(...) function and transform your answer into a comment such that your program still compiles.

```
/*03 b.
For number 12345 (0000 0000 0000 0000 0011 0000 0011 1001) I get:
      0x7ffe09e4097c 0x39
      0x7ffe09e4097d 0x30
      0x7ffe09e4097e 0x00
      0x7ffe09e4097f 0x00
where the least significant byte (LSB) is stored at memory
address 0x7ffe09e4097c and most significant byte (MSB) is stored
at memory address 0x7ffe09e4097f
since 0x7ffe09e4097c is a smaller memory address value than
0x7ffe09e4097f, this indicates that our target machine is a
little endian computer
For the negative number -12345 (1111 1111 1111 1111 1100 1111
1100 0111) I get:
      0x7ffd3e027fbc 0xc7
      0x7ffd3e027fbd 0xcf
      0x7ffd3e027fbe 0xff
      0x7ffd3e027fbf 0xff
Again little endian since the LSB is stored at 0x7ffd3e027fbc
and the MSB is stored at 0x7ffd3e027fbf.
*/
```

c. [2 marks] Modify the printf statement of the show_bytes_2(...) function such that, instead of using array notation to access each element of the array start, it uses pointer notation to access each of these elements. The output of your function should be the same as the function you modified in a. above, with each pair of values – memory address and memory content – printed on its own line:

```
0x7ffe5fb887cc 0x80
```

Bottom line: show_bytes(...) and show_bytes_2(...) should print the same thing given the same data. They just do it differently.

```
// Q3 c.
void show_bytes_2(byte_pointer start, size_t len) {
```

```
size t i;
  // WHY hx in 0x%.2hx"? Why not: 0x%.2x?
  for (i = 0; i < len; i++) {
      printf(" %p 0x%.2hx\n", start + i, *(start + i)); //
      // OR :for a more general version
      // printf("%p 0x%.2hx\n", (start + i * sizeof(*start)),
      //
                                       *(start + i * sizeof(*start)));
      // However, in the context of Q3 c. sizeof(*start) is
      // optional since start is a byte pointer.
      // Can you see why?
  printf("\n");
  return;
d. [4 marks] Write a function called show_bits( ... ). This function must have the following prototype:
                                void show_bits(int);
This function must print the bit pattern of the parameter of type int.
Compile and test your program.
Here are two test cases (data and expected results) to illustrate the behaviour of this function:
Test Case 1:
If the parameter (int) is 12345, then show_bits( ... ) prints:
                           00000000000000000011000000111001
Test Case 2:
If the parameter (int) is -12345, then show_bits( ... ) prints:
```

111111111111111111001111111000111

Check out Lab 2 for a possible solution!

e. [3 marks] Write a function called mask_LSbits(...). This function must have the following prototype:

```
int mask_LSbits( int n );
```

This function creates (returns) a mask with the **n** least significant bits set (to 1). For example, if **n** is 2, the function returns 3 (i.e., 0x000000003) and if **n** is 15, the function returns 32767 (i.e., 0x000007fff).

What happens when $\mathbf{n} >= \mathbf{w}$ or when $\mathbf{n} <= \mathbf{0}$?

When n >= w, your function must return a mask of all 1's.

When n <= 0, your function must return a mask of all 0's, i.e., 0.

Requirements (for e.):

- . When creating the mask, while implementing this function, you must not use
 - o division, modulus and/or multiplication,
 - o iterative statements (such as loops),
 - o call other function(s),
 - however, you can use sizeof(...).
- Exceptions:
 - You can call the function sizeof(...) as many times as you wish. If you call sizeof(...) (note that you
 do not have to), you can then use multiplication with it. For example: sizeof(...) * 8.
 - You can use conditional statements in your function only when you validate the parameter.

Testing: For part e., make sure you test your code with test cases that use valid and invalid test data.

Here is an example of a test case that uses valid test data: calling mask_LSbits(4)

Here is an example of a test case that uses **invalid test data**: calling mask_LSbits(0)

To test your program, make sure you add your test cases to the test provided test driver Assn1_main.c.

For this Question 3, you need to make two submissions:

- 1. Please, submit your Assn1_Q3.c on CourSys.
- 2. Please, scan your Assn1_Q3.c as a pdf document and upload it below.

```
//Q3 e.
```

```
int mask_LSbits(int shift_amount) {
    // Parameter validation:

    // if shift_amount <= 0, return 0 -> a mask of all 0s
    if( shift_amount <= 0 ) return 0;

    //if shift_amount >= 32 return -1 -> a mask of all 1s
    if( shift_amount >= 32) return -1;
```

```
// Way 1:
// "-1" is 32 1s
// shift these 1s to the left "shift_amount" times and
// then reverse (flip) the bits i.e 0 to 1 and 1 to 0
int new_value = ~(-1 << shift_amount);
return new_value;

// Way 2:
// "1" is 31 1s and 1 in LSbit position
// shift these bits to the left "shift_amount" times and
// then add "-1" (32 1s)
return (1 << shift_amount) - 1;</pre>
```