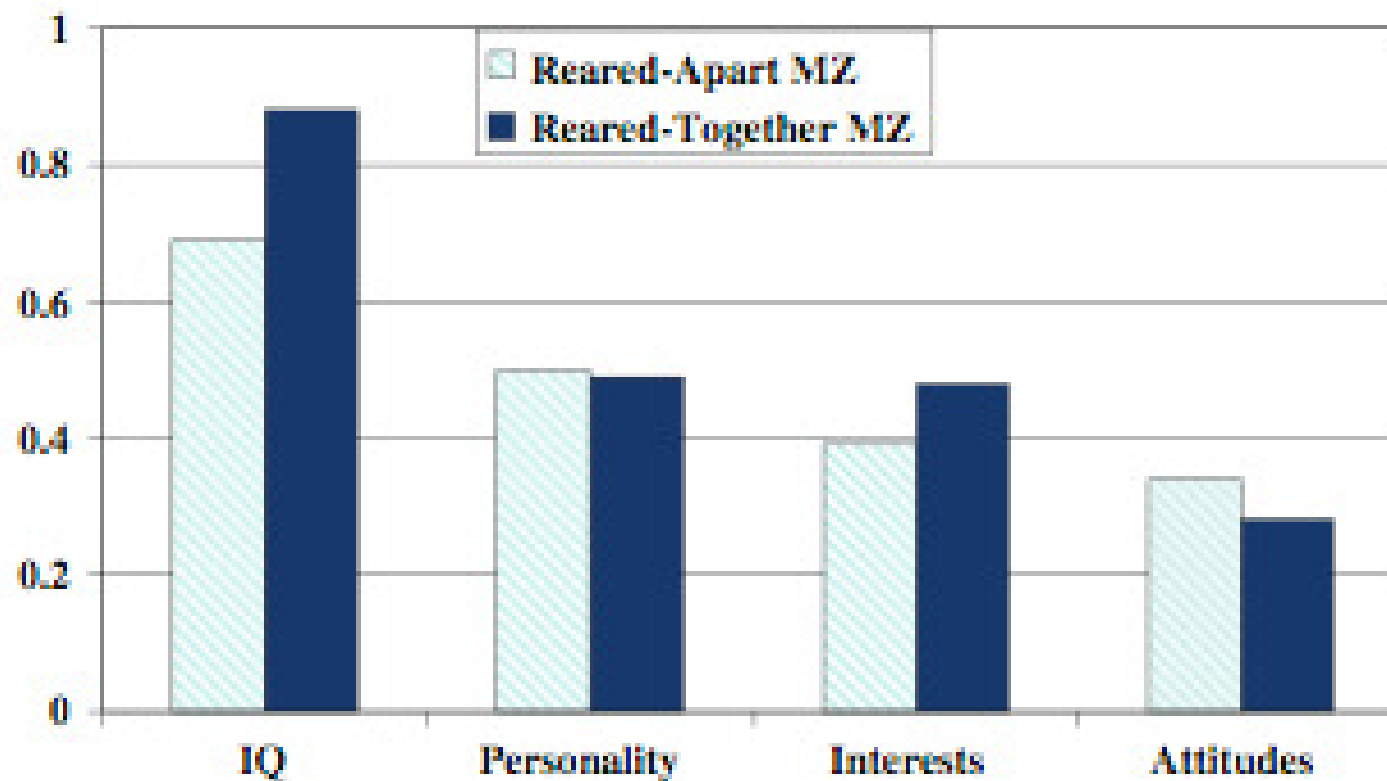


# Twins Studies

- Monozygotic (MZ; “identical”)
  - Fertilization of a single egg by a single sperm
  - Share 100% of their genetic material.
- Dizygotic (DZ, “fraternal” or “non-identical”)
  - Result from the independent fertilization of two eggs by two sperm
  - Share on average 50% of their genes (just like full siblings).

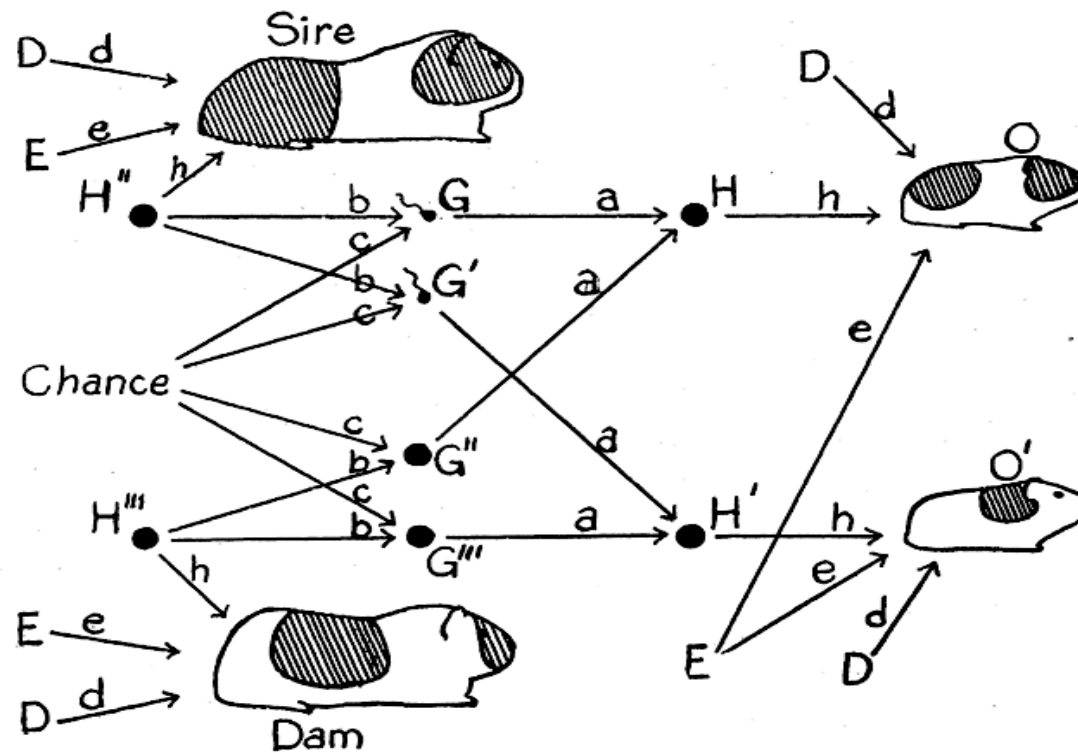
# A Natural Experiment

- Twins reared apart
  - They did not experience the same environment
  - Gives a much stronger test of genetic and non-shared environmental contributions
  - But separated MZs are rare



**Fig. 2** Average reared-apart and reared-together monozygotic (MZ) twin correlations in four domains of psychological functioning. Adapted from Bouchard et al. (1990)

# Path Diagram



# Path Analysis

- Derive predictions for the variances and covariances of the variables under the specified model
  - Present relationships between variables using **diagrams**
  - The relationships can also be represented as **structural equations** and **covariance matrices**
  - Structural equation modelling (SEM) represents a unified platform for path analytic and variance components models

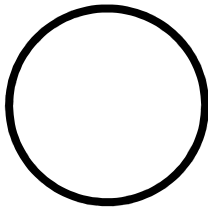
# Maximum Likelihood Estimation

- Likelihood: probability that an observation (data point) is predicted by specified model
- For MLE, determine most likely values of population parameter value (e.g,  $\mu$ ,  $\sigma$ ,  $\beta$ ) given observed sample value
  - define model
  - define probability of observing a given event conditional on a particular set of parameters
  - choose a set of parameters which are most likely to have produced observed results

# Path Diagram Conventions



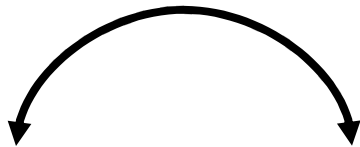
Observed Variable



Latent Variable

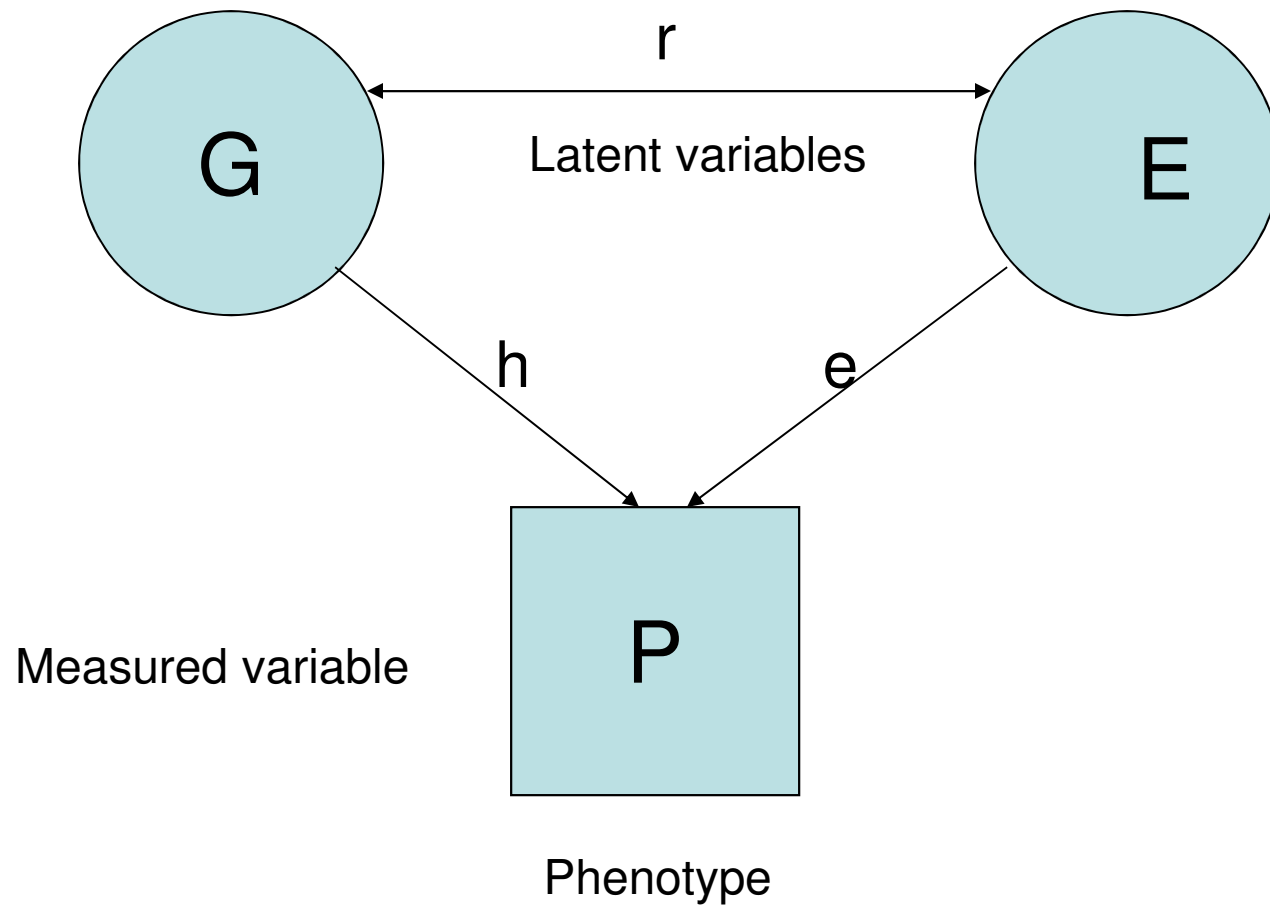


Causal Path



Covariance Path

Path diagram for the effects of genes and environment on phenotype





# Variance Components

- Heritability (narrow-sense,  $A$  or  $a^2$ ; broad-sense,  $H$  or  $h^2$ ): phenotypic variance in a sample that can be attributed to genotypic variance.
- Shared or common environment ( $C$  or  $c^2$ ): experiences that makes individuals more similar to one another, regardless of genetic similarity
- Non-shared or Unique environment and Error ( $E$  or  $e^2$ ): What is left over

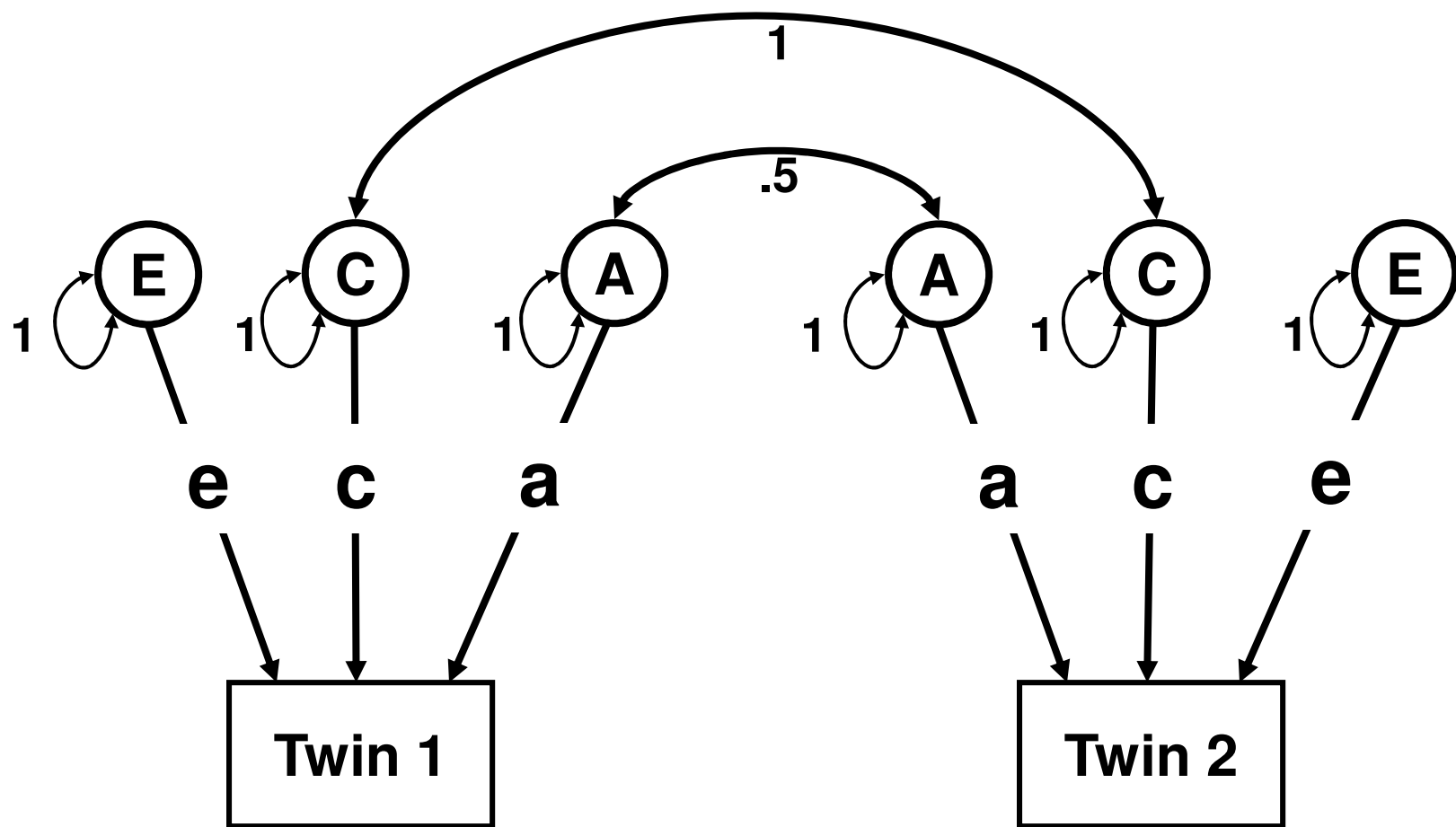
## **IDENTICAL TWINS**

- MONOZYGOTIC:
- Have IDENTICAL genes (A)
- Come from the same family (C)
- Have unique experiences during life (E)

## **FRATERNAL TWINS**

- DIZYGOTIC: Have DIFFERENT genes (A)
- Come from the same family (C)
- Have unique experiences during life (E)

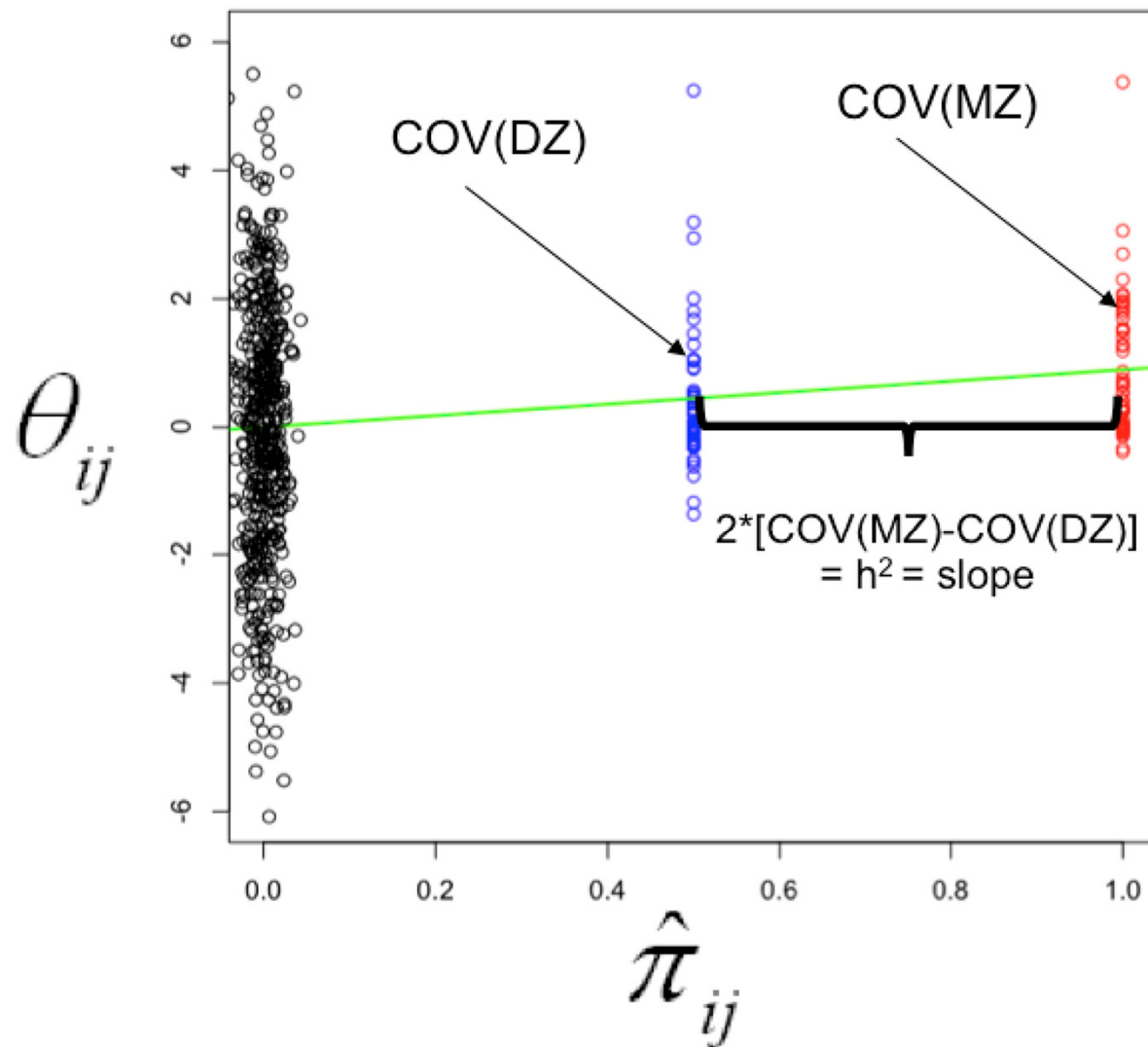
Note: a, c and e are the same cross twins



## Model for a DZ PAIR

Note: a, c and e are also the same cross groups

# Heritability among unrelateds



$$V_P = a^2 + c^2 + e^2$$

# Falconer's model

Assumes all genetic effects are additive ( $h^2 = a^2$ )

$$r_{MZ} = a^2 + c^2$$

$$r_{DZ} = 0.5a^2 + c^2$$

$$1.0 = a^2 + c^2 + e^2$$

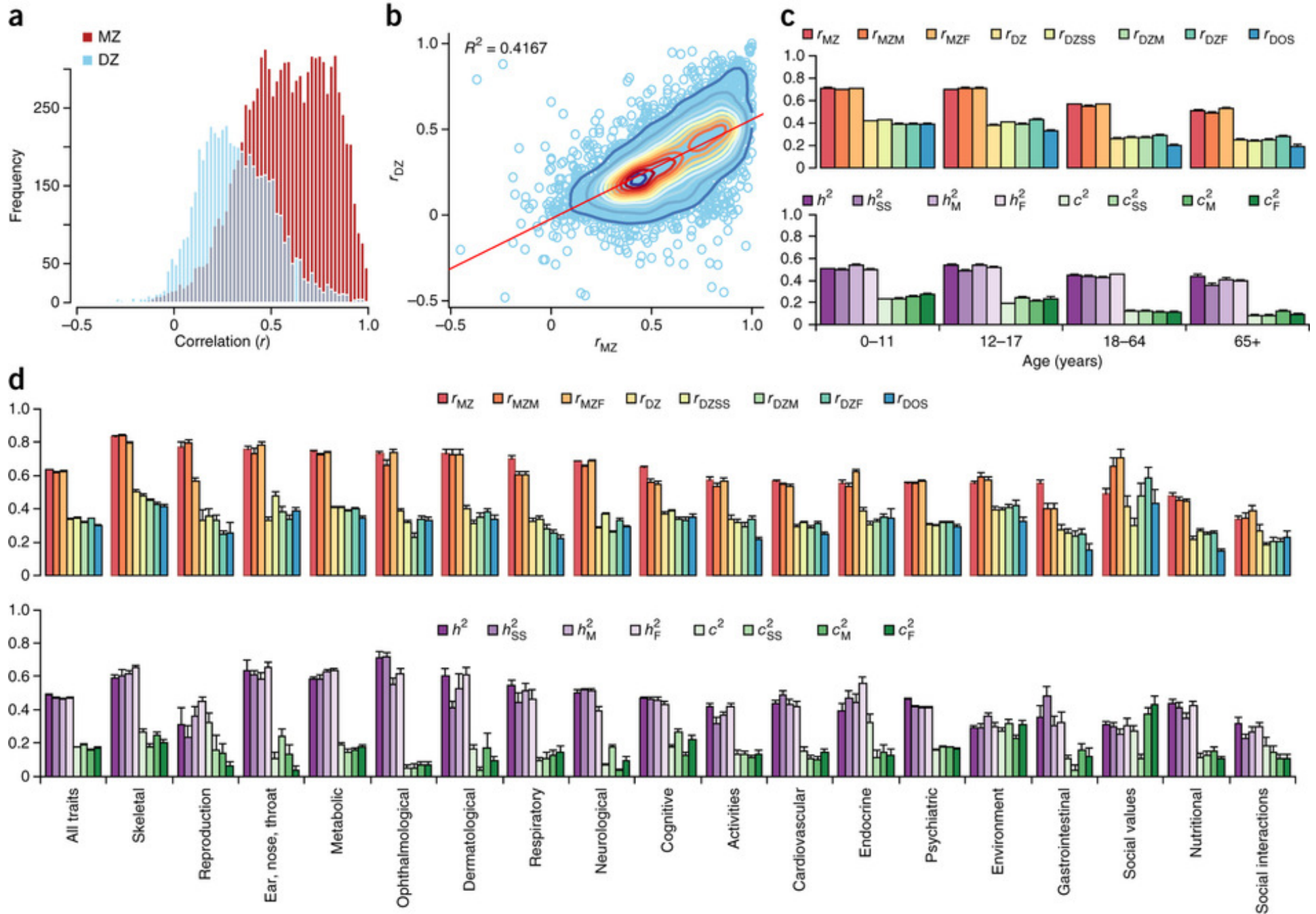
# Falconer estimates

$$a^2 = 2(r_{MZ} - r_{DZ})$$

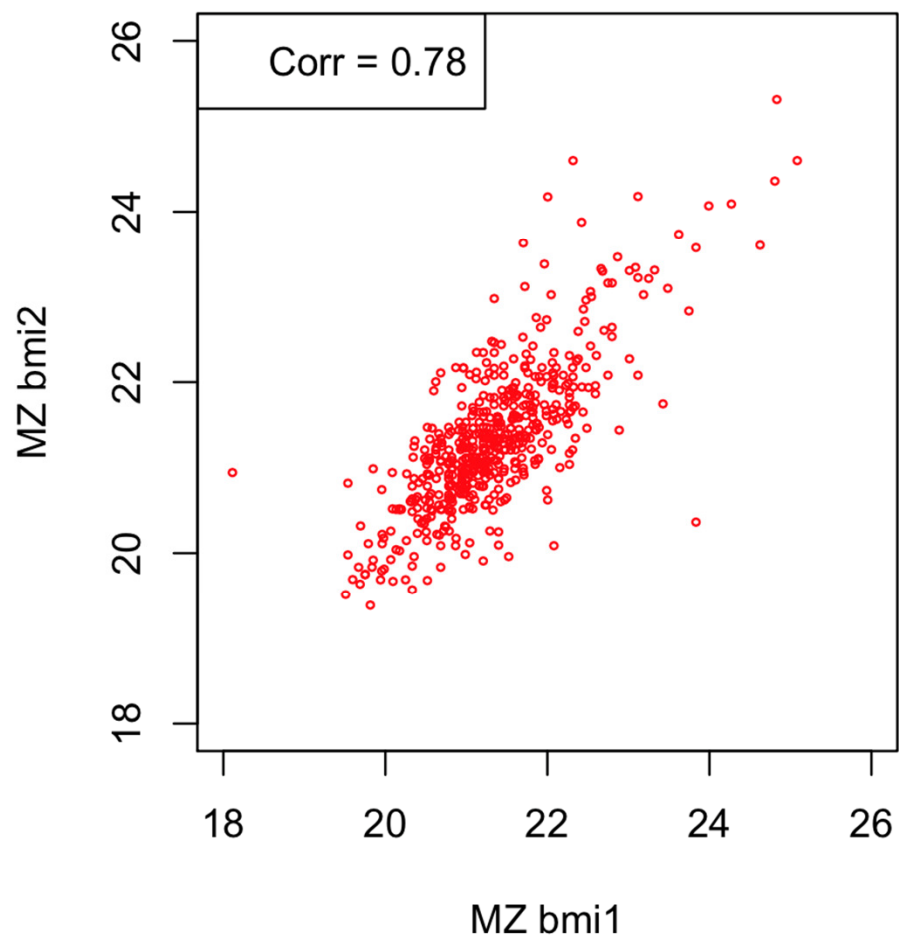
$$c^2 = 2r_{DZ} - r_{MZ}$$

$$e^2 = 1 - r_{MZ}$$

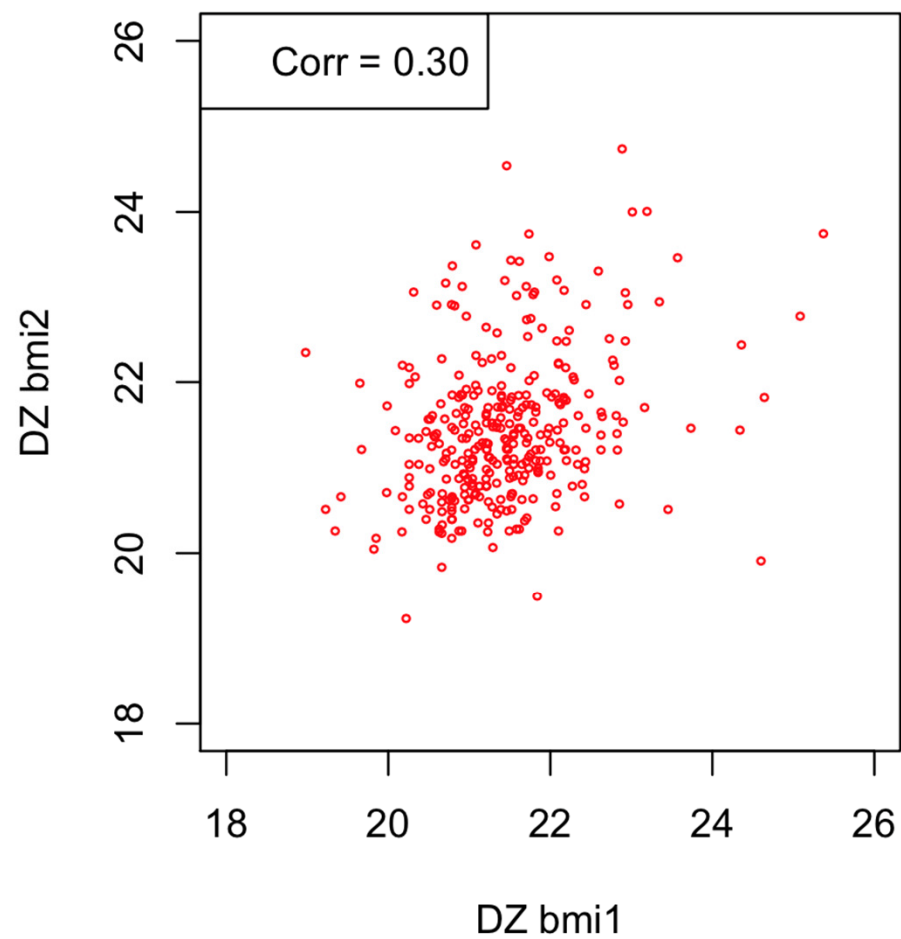




**MZ BMI**



**DZ BMI**



What about “dominance”<sup>\*</sup> effects?

$$V_P = a^2 + d^2 + c^2 + e^2$$

\* Dominance defined statistically as individuals being more similar on the basis of genetic overlap alone than would be predicted by a linear model – i.e., **any** non-linear genotype “dosage” effects

## ACE **or** ADE

$$\text{Cov(mz)} = a^2 + c^2 \quad \mathbf{or} \quad a^2 + d^2$$

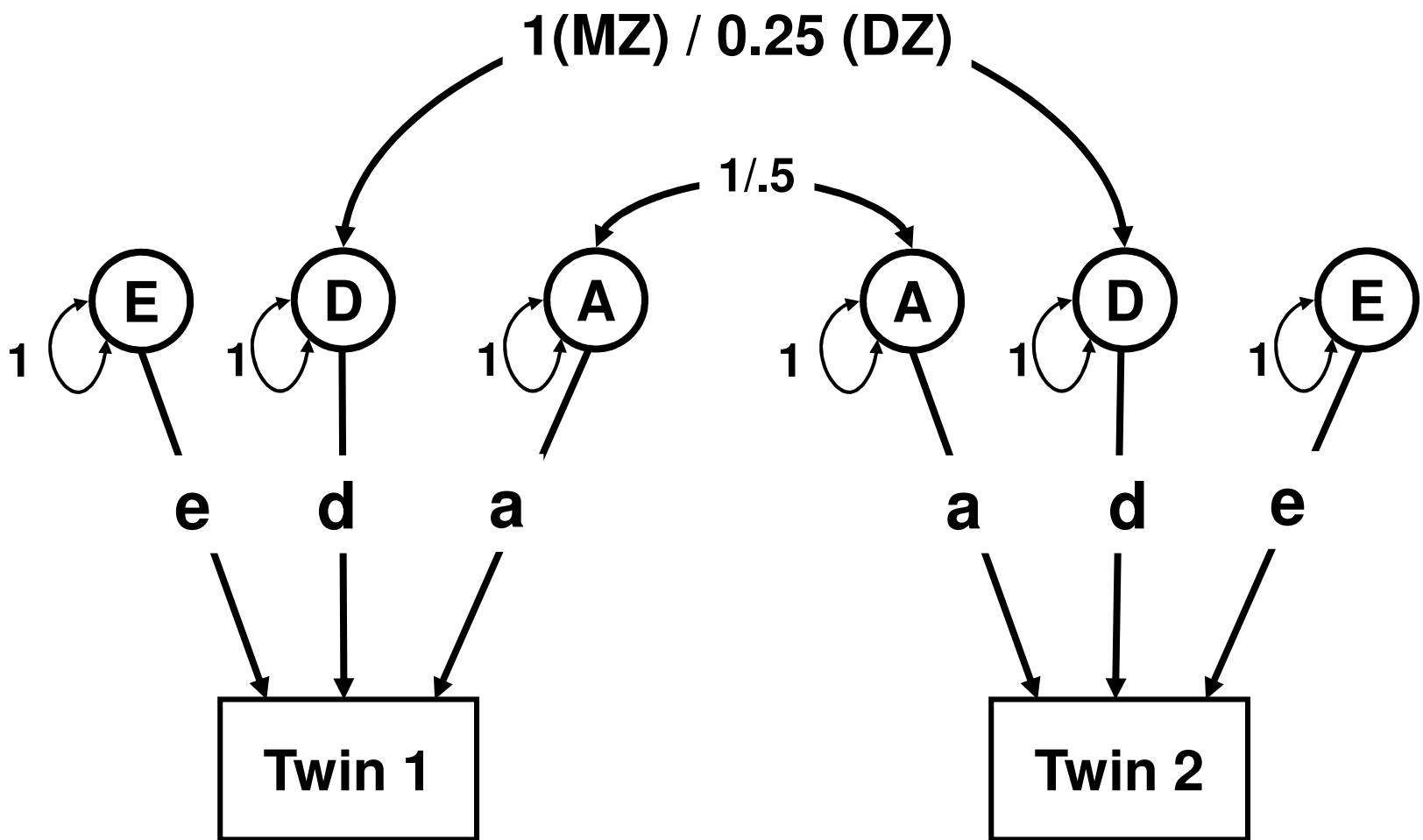
$$\text{Cov(dz)} = \frac{1}{2} a^2 + c^2 \quad \mathbf{or} \quad \frac{1}{2} a^2 + \frac{1}{4} d^2$$

$$V_p = a^2 + c^2 + e^2 \quad \mathbf{or} \quad a^2 + d^2 + e^2$$

**3** unknown parameters (a, c, e or a, d, e),  
and only **3** distinctive predicted statistics:

Cov MZ, Cov DZ,  $V_p$ )

this model is **just identified**



# Twin Correlations → Sources of Variance

$r_{MZ} > r_{DZ}$	A
$r_{MZ} = 2 r_{DZ}$	only A (no C,D)
$r_{MZ} = r_{DZ}$	only C (no A,D)
$r_{MZ} < 2 r_{DZ}$	A & C
$r_{MZ} > 2 r_{DZ}$	A & D

# Classical Twin Study Assumptions

- Equal means/variances in Twin 1 and Twin 2
- Equal means/variances in MZ and DZ twins
- Random Mating
- Equal Environments of MZ and DZ pairs
- No GE Correlation
- No G x E Interaction
- No Sex Limitation