

CS-584 ASSIGNMENT 2

GENERATIVE LEARNING

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Q: 5) Naive Baye Binomial Feature

a) log likely hood function

$$l(\theta) = \left[\sum_{i=1}^m \sum_{j=1}^n \log \left(\frac{p^{(i)}}{x^{(i)}} \right) x_{j/y=y^{(i)}}^{(i)} \right. \\ \left. (p^{(i)} - x_{j/y=y^{(i)}}^{(i)})^{p^{(i)} - x^{(i)}} \right]$$

derivative respect to $x_{j/y=y^{(i)}}^{(i)}$ &
equate to zero : $\frac{\partial l(\theta)}{\partial x_{j/y=y^{(i)}}^{(i)}} = 0$

$$\frac{\partial}{\partial x_{j/y=y^{(i)}}^{(i)}} \left[\sum_{i=1}^m \sum_{j=1}^n \log \left(\frac{p^{(i)}}{x^{(i)}} \right) \right. \\ \left. + x_{j/y=y^{(i)}}^{(i)} \log x_{j/y=y^{(i)}}^{(i)} \right. \\ \left. + (p^{(i)} - x^{(i)}) \log (1 - x_{j/y=y^{(i)}}^{(i)}) \right] = 0$$

$$\therefore \sum_{i=1}^m \frac{x_p^{(i)}}{x_{j/y=j}} = \sum_{i=1}^m \frac{(p^{(i)} - x_{j/y=j}^{(i)})}{(1 - x_{j/y=j})} \log \frac{x_{j/y=j}^{(i)}}{p^{(i)} - x_{j/y=j}^{(i)}}$$

$$\therefore \frac{1}{x_{j/y=j}} \sum_{i=1}^m x_p^{(i)} = \frac{1}{1 - x_{j/y=j}} \left[\sum_{i=1}^m p^{(i)} - x_p^{(i)} \right]$$

$$\therefore \hat{\alpha}_j | y=j = \frac{\sum_{i=1}^m (y_{ij}) x_i}{\sum_{i=1}^m 1(y_{ij}) p^{(i)}}$$

$$\therefore \frac{\partial l(\theta)}{\partial \alpha_k} = \frac{\partial}{\partial \alpha_k} \sum_{i=1}^m \log(p^{(i)}(y_{ik}))$$

$$0 = \frac{\sum_{i=1}^m 1(y_{ik}) \alpha_k}{\sum_{i=1}^m p^{(i)}(y_{ik})}$$

$$\therefore p^{(i)}(y_{ik}) = \frac{\sum_{i=1}^m 1(y_{ik})}{m}$$