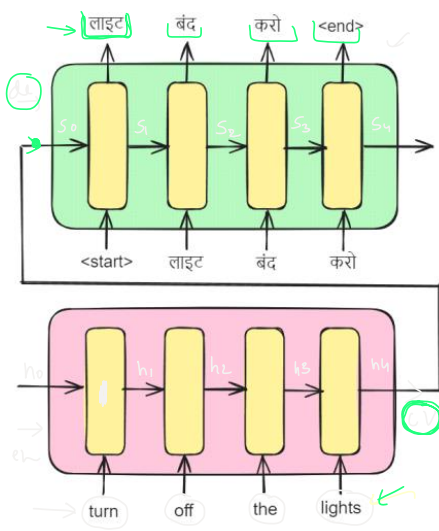


# Recap

16 January 2024 16:10



turn off the lights → एंड ऑन

[NMT]

encoder-decoder

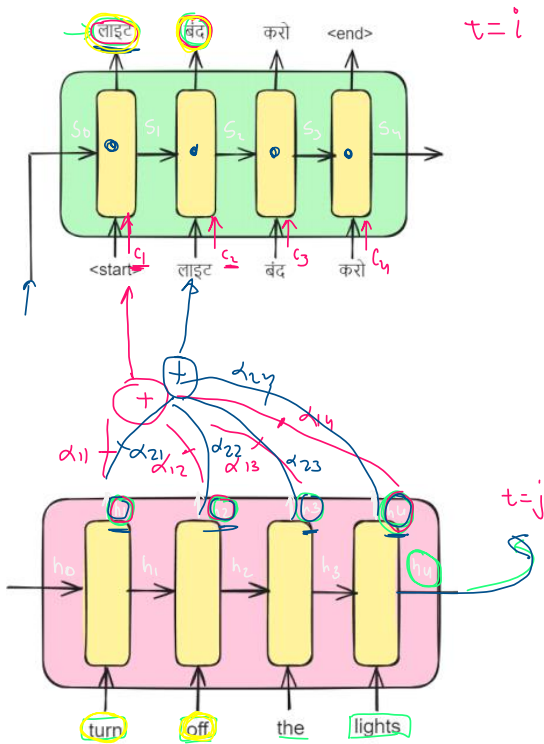
Hidden  
stacked lstm

sequence

translation

sentence > 30 words  
paragraph  
document

bottleneck → Attention mechanism



$t=i$

$C_1, C_2, C_3, C_4$

weighted sum

$$C_i = \sum_{j=1}^4 \alpha_{ij} h_j$$

$$4 \times 4 = 16$$

$\alpha \rightarrow$  alignment score

$$C_1 = \alpha_{11} h_1 + \alpha_{12} h_2 + \alpha_{13} h_3 + \alpha_{14} h_4$$

$$C_2 = \alpha_{21} h_1 + \alpha_{22} h_2 + \alpha_{23} h_3 + \alpha_{24} h_4$$

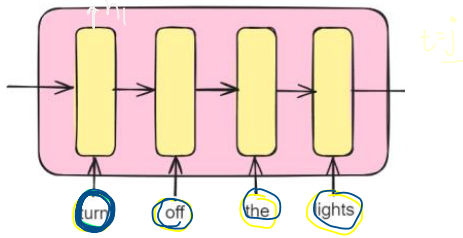
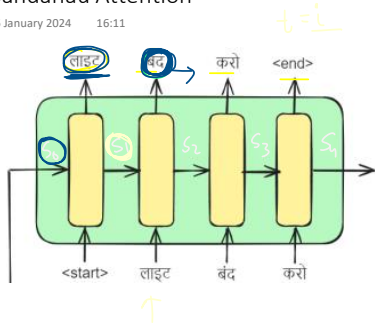
$\alpha \rightarrow$  find out

Bahdanau  
archite  
attention

Luong  
attention

# Bahdanau Attention

16 January 2024 16:11



alignment score

given

$$c_i = \sum \alpha_{ij} h_j$$

alignment

decode  
→ prev hidden state

$$\alpha_{11} \rightarrow \text{लाइट} \rightarrow \text{turn}$$

$$\alpha_{12} \rightarrow \text{बंद} \rightarrow \text{off}$$

$$\alpha_{11} = f(h_1, s_0)$$

$$\alpha_{21} = f(h_2, s_1)$$

$$\alpha_{ij} = f(h_j, s_{i-1})$$

approximate

main fund

the encoder hidden

deal prev hidden state

$$\text{FFN} \rightarrow \text{ANN} \rightarrow \text{UFA}$$

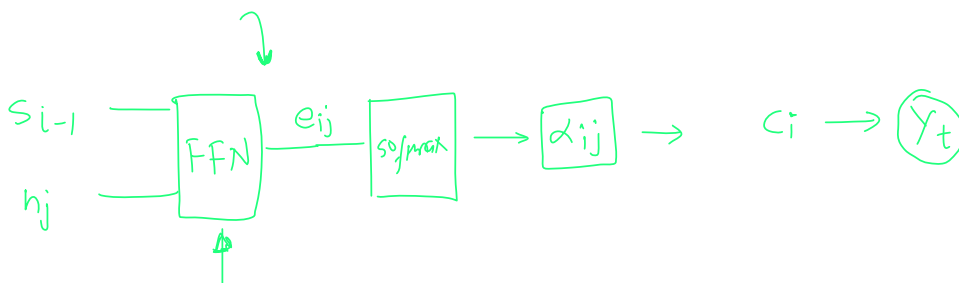
softmax

$e_{ij}$



$s_{i-1}$

$h_j$



$$s_0, y_{t-1}, c_i \rightarrow \text{dshn} \rightarrow y_t (\text{लाइट}) [s_1]$$

encoder hidden

$h_1, h_2, h_3, h_4$

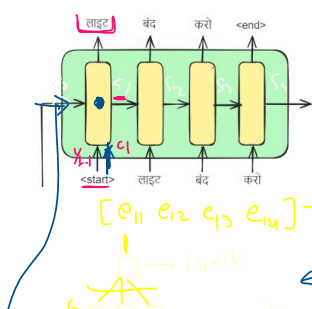
$(s_{i-1}) h_j$

$$s_0 = [e, f, g, h]$$

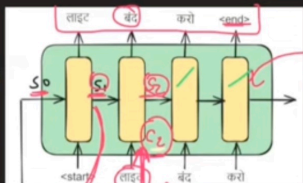
$$c_1 = \sum \alpha_{ij} h_j$$

$$[e_{11}, e_{12}, e_{13}, e_{14}] \rightarrow \text{softmax} \rightarrow [\alpha_{11}, \alpha_{12}, \alpha_{13}, \alpha_{14}]$$

$$c_1 = \frac{\alpha_{11} h_1}{\uparrow} + \frac{\alpha_{12} h_2}{\uparrow} + \frac{\alpha_{13} h_3}{\uparrow} + \frac{\alpha_{14} h_4}{\uparrow}$$



$i=2$  time label



$$c_2 = \alpha_{21} h_1 + \alpha_{22} h_2 + \alpha_{23} h_3 + \alpha_{24} h_4$$

$\alpha$

$s_{11}$	$s_{12}$	$s_{13}$	$s_{14}$	$h_{11}$	$h_{12}$	$h_{13}$	$h_{14}$
$s_{21}$	$s_{22}$	$s_{23}$	$s_{24}$	$h_{21}$	$h_{22}$	$h_{23}$	$h_{24}$
$s_{31}$	$s_{32}$	$s_{33}$	$s_{34}$	$h_{31}$	$h_{32}$	$h_{33}$	$h_{34}$
$s_{41}$	$s_{42}$	$s_{43}$	$s_{44}$	$h_{41}$	$h_{42}$	$h_{43}$	$h_{44}$

4x8

time distributed FNN

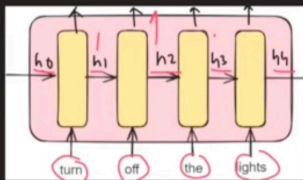
$$\begin{bmatrix} \alpha_{21} & \alpha_{22} & \alpha_{23} & \alpha_{24} \end{bmatrix} \begin{bmatrix} e_{21} & e_{22} & e_{23} & e_{24} \end{bmatrix}$$

$n \times 3$

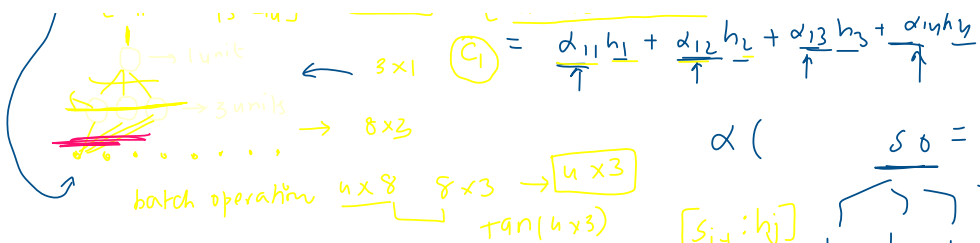
$$\begin{cases} c_{ij} = \sum \alpha_{ij} h_j \\ \alpha_{ij} = \frac{\exp(e_{ij})}{\sum_{k=1}^n \exp(e_{ik})} \end{cases}$$

$$e_{ij} = V \left[ \tanh(W[s_{i-1}:h_j] + b) \right]$$

alignment model

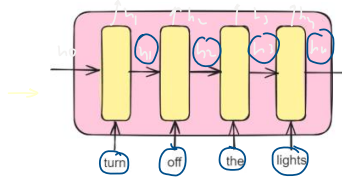


additive attention



$\alpha$  (  $s_0 = [e \ f \ g \ h]$  )

$[s_{i-1}:h_j]$   $\begin{matrix} \nearrow & \nearrow & \nearrow & \nearrow \\ h_1 & h_2 & h_3 & h_4 \end{matrix}$



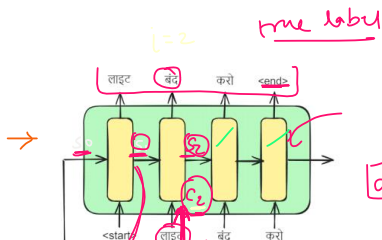
vectors  $h_0 = [a \ b \ c \ d]$

$(4 \times 3) (3 \times 1)$

$$\begin{bmatrix} e^{e^{11}} \\ e^{e^{11}} + e^{e^{12}} + e^{e^{13}} + e^{e^{14}} \end{bmatrix} (4 \times 1) \rightarrow 4 \text{ numbers}$$

4 rows / 8 cols

$s_{01}$	$s_{02}$	$s_{03}$	$s_{04}$	$h_{11}$	$h_{12}$	$h_{13}$	$h_{14}$
$s_{01}$	$s_{02}$	$s_{03}$	$s_{04}$	$h_{21}$	$h_{22}$	$h_{23}$	$h_{24}$
$s_{01}$	$s_{02}$	$s_{03}$	$s_{04}$	$h_{31}$	$h_{32}$	$h_{33}$	$h_{34}$
$s_{01}$	$s_{02}$	$s_{03}$	$s_{04}$	$h_{41}$	$h_{42}$	$h_{43}$	$h_{44}$

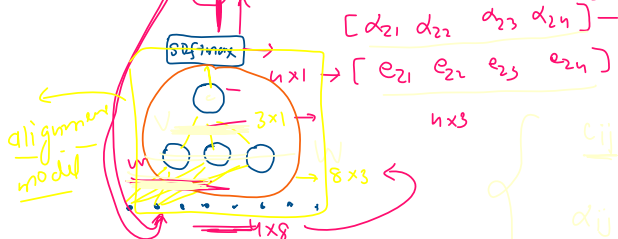


$C_2 = \alpha_{21} h_1 + \alpha_{22} h_2 + \alpha_{23} h_3 + \alpha_{24} h_4$

4x8

$s_{11}$	$s_{12}$	$s_{13}$	$s_{14}$	$h_{11}$	$h_{12}$	$h_{13}$	$h_{14}$
$s_{11}$	$s_{12}$	$s_{13}$	$s_{14}$	$h_{21}$	$h_{22}$	$h_{23}$	$h_{24}$
$s_{11}$	$s_{12}$	$s_{13}$	$s_{14}$	$h_{31}$	$h_{32}$	$h_{33}$	$h_{34}$
$s_{11}$	$s_{12}$	$s_{13}$	$s_{14}$	$h_{41}$	$h_{42}$	$h_{43}$	$h_{44}$

time distributed fnn



$[ \alpha_{21} \ \alpha_{22} \ \alpha_{23} \ \alpha_{24} ]$

$4 \times 3$

$[ e_{21} \ e_{22} \ e_{23} \ e_{24} ]$

$8 \times 3$

$1 \times 8$

additive attention

$e_{ij} = \sum_k \alpha_{ij} h_k$

$\alpha_{ij} = \frac{\exp(e_{ij})}{\sum_k \exp(e_{ik})}$

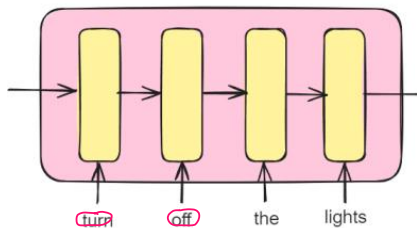
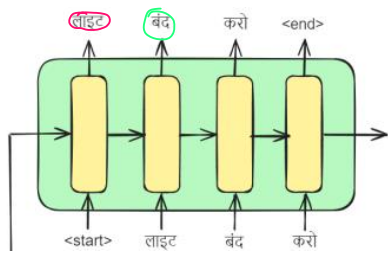
$e_{ij} = \frac{1}{\sqrt{d_k}} \tanh(w [s_{i-1}:h_j] + b)$

# Luong Attention

17 January 2024 00:09

Luong

parameters  $\rightarrow$  slow



$$c_i = \sum \alpha_{ij} h_j \rightarrow \text{FFN} \left\{ \left[ V + \tan(W[S_{i-1}:h_j] + b) \right] \right\}$$

$$\alpha_{ij} = f(S_{i-1}, h_j) \times$$

$$\alpha_{ij} = f(S_i, h_j) \rightarrow [S_i^T \cdot h_j] \rightarrow \text{dot product}$$

fast

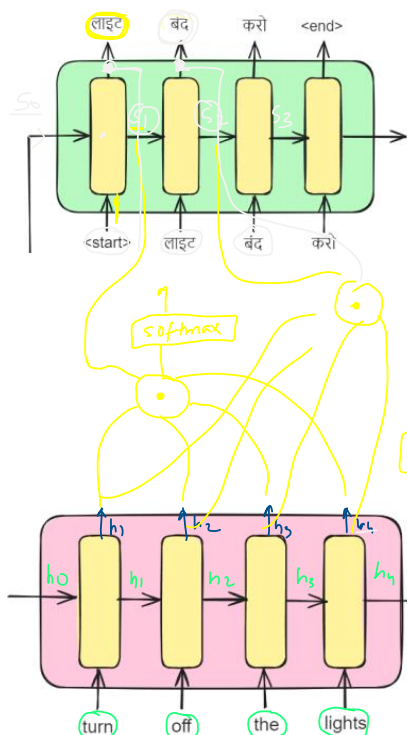
updated info  $\rightarrow$  current  $\oplus$  diff

$S_i = [a \ b \ c \ d]$

$h_j = [e \ f \ g \ h]$

$[a \ b \ c \ d] [e \ f \ g \ h]^T = [ae + bf + cg + dh]$

$\alpha_{ij} \leftarrow [e_{ij}] \leftarrow \text{softmax} \rightarrow \text{attention}$



output  $S_1: c_1 \rightarrow [S_1] \rightarrow \text{softmax}$

$S_2: c_2 \rightarrow \tilde{S}_2 \rightarrow \text{multiplicative after}$

$$[e_{21} \ e_{22} \ e_{23} \ e_{24}] \text{ softmax} \rightarrow \alpha_{21} \ \alpha_{22} \ \alpha_{23} \ \alpha_{24}$$

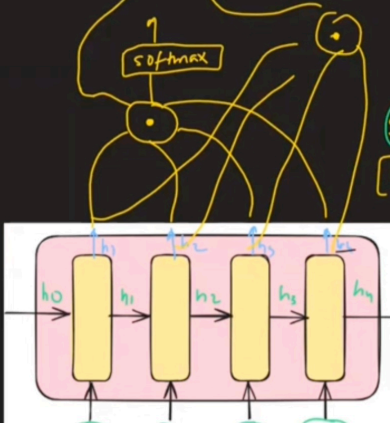
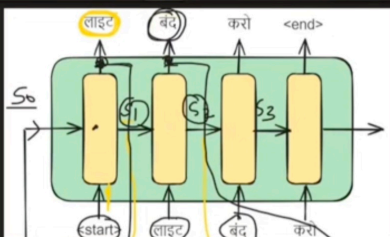
$$\sum \alpha_{ij} h_j \rightarrow c_2$$

$$\begin{bmatrix} S_1 h_1 & S_1 h_2 & S_1 h_3 & S_1 h_4 \\ e_{11} & e_{12} & e_{13} & e_{14} \end{bmatrix}$$

$$\alpha_{11} \ \alpha_{12} \ \alpha_{13} \ \alpha_{14} \rightarrow c_1$$

Here in Luong , we made two changes ,  
instead of providing context vector in input we are providing it in output , also it changes how alignment score is calculated now instead of neural network we are using dot product , also we are using current decoder hidden state and input to calculate (which is more dynamic)

Due to dot product involvement it is also called multiplicative attention.



output  
 $s_1: c_1 \rightarrow \tilde{s}_1 \rightarrow \text{softmax}$   $s_2: c_2 \rightarrow \tilde{s}_2 \rightarrow \text{multiplicative after}$

$[e_{21} \ e_{22} \ e_{23} \ e_{24}] \text{ softmax} \rightarrow \alpha_{21} \ \alpha_{22} \ \alpha_{23} \ \alpha_{24}$   
 $\rightarrow c_2$

$\sum \alpha_{ij} h_j$   
 $\begin{bmatrix} s_1 h_1 & s_1 h_2 & s_1 h_3 & s_1 h_4 \\ e_{11} & e_{12} & e_{13} & e_{14} \end{bmatrix}$   
 $\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$   
 $\alpha_{11} \quad \alpha_{12} \quad \alpha_{13} \quad \alpha_{14} \rightarrow c_1$