



✓ **Congratulations! You passed!**  
TO PASS 60% or higher

Keep Learning

Retake the assignment in 7h 58m

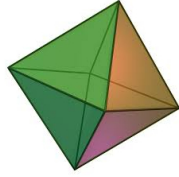
GRADE  
80%

## Linear Programming Quiz

LATEST SUBMISSION GRADE  
80%

1. What is the minimum number of linear inequalities needed to define the figure pictured below?

1 / 1 point



8

✓ **Correct**

The figure is cut out by 8 flat surfaces. Thus 8 equations are needed.

2. Given a solution to a linear program, one could try to show that it is optimal by finding a matching solution to the dual program. Which of the following theorems will make it easier to do so?

1 / 1 point

- ☐ Separation of convex sets from outside points by hyperplanes.
- ☒ Complementary slackness.
- ☐ Polytopes achieve optimum values at vertices.

✓ **Correct**

Correct! Complementary slackness tells you that your dual solution only uses equations that are tight in solutions to the primal.

3. Which of the following statements are true?

1 / 1 point

- ☒ A system of linear equations has always 0, 1, or infinitely many solutions.

✓ **Correct**

This statement is true. Unless there are no solutions, the solution set has some number of free variables. If there are no free variables, there is a unique solution. If there is at least one free variable, there are infinitely many solutions.

- ☒ A system of linear equations has a solution unless they can be combined in some combination to give the equation  $0=1$ .

✓ **Correct**

This statement is true. There is a solution unless the corresponding row reduced matrix has a row corresponding to this equation, this will happen only if  $0=1$  can be obtained by combining the original equations.

- ☐ A system of  $n$  linear equations in  $n$  variables always has a unique solution.

4. Suppose that you are trying to solve the optimization problem:

0 / 1 point

Maximize  $v \cdot x$  subject to  $Ax \geq b$  for some  $A \in \mathbb{R}^{m \times n}$  (i.e. trying to solve an optimization problem in  $n$  variables with  $m$  linear inequality constraints).

This problem can be reduced to running a solution finding algorithm on a different system of linear equations in  $k$  variables. What is the smallest value of  $k$  for which this can be done?

Preview

$x$

$x$

! **Incorrect**

5. What is the largest possible value of  $x+y$  achievable by pairs  $x,y$  of real numbers satisfying the constraints:

1 / 1 point

- $x \leq 7$
- $y \leq 10$
- $2x+y \leq 21$
- $-x + 2y \leq 12$
- $5x-y \leq 30$

✓ **Correct**

Correct. The optimum is at  $x=6$ ,  $y=9$  as shown below.

