

Probability Problems

1. Students A, B, C, ...

$$P(A \text{ answers } 1^{\text{st}} Q) = \frac{1}{15} \quad P(A \rightarrow 1^{\text{st}} Q, B \rightarrow 2^{\text{nd}} Q \dots) = \left(\frac{1}{15}\right)^8$$

Ways to choose 8 from 15 students (order matters) = $P(15, 8)$

$$\text{Ans} = \left(\frac{1}{15}\right)^8 P(15, 8) = .1012 = 10.12\%$$

2. even integers, 1st 2 digits=odd, all digits unique -----

$$(5)(4)(8)(7)(6) = \# \text{ of integers that satisfy criteria}$$

$$P(\text{integer meets criteria}) = \frac{5 \cdot 4 \cdot 8 \cdot 7 \cdot 6}{10^5} = .0672$$

$$P(\text{exactly 5 of 8 integers meet criteria}) = (.0672)^5 (1 - .0672)^3 = 1.112 \times 10^{-6} \rightarrow 1.112 \times 10^{-4} \%$$

$$3. P(A) = \binom{3}{2} \left(\frac{3}{6}\right)^2 + \binom{3}{3} \left(\frac{3}{6}\right)^3 = \frac{11}{21} = \frac{7}{8}$$

$$P(B) = \left(\frac{1}{6}\right)^3 \cdot 6 = \frac{1}{6^2} = \frac{1}{36}$$

$$\text{Check if } P(A) \cdot P(B) = P(A \cap B)$$

$$P(A) \cdot P(B) = \frac{1}{72}$$

$$P(A \cap B) = \left(\frac{1}{6}\right)^3 \cdot 3 = \frac{1}{72}$$

Since $P(A) \cdot P(B) = P(A \cap B)$, A & B are independent

$$4. \quad \left(\frac{13}{52}\right)\left(\frac{12}{51}\right)\left(\frac{11}{50}\right)\left(\frac{10}{49}\right)\left(\frac{9}{48}\right) \cdot 4 = P(4, 4) = .04754$$

\uparrow for 4 suits \uparrow order doesn't matter

$\frac{1}{21019} = .04754$

5. Don't know