

Graph:-

is a non-linear ds consisting of nodes & edges. nodes are also called vertex. mainly graph consist of finite set of vertices (or nodes) & a set of edges that connect a pair of nodes.

Representations:-

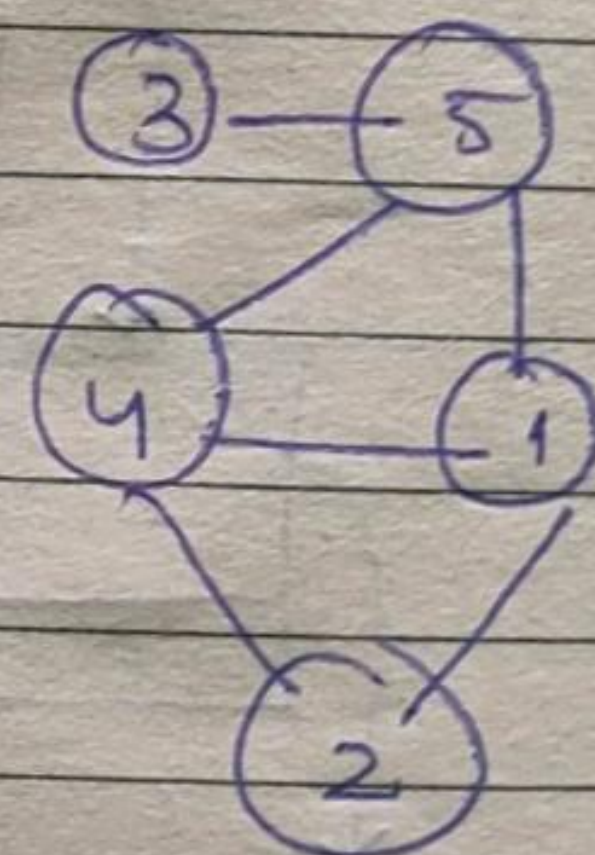
1. Adjacency Matrix

2. Adjacency List.

2D Array of size $V \times V$ where V is the number of vertices. it also used for weighted graph.
 $adj[i][j] = w$, means edge from i to j with weight w .

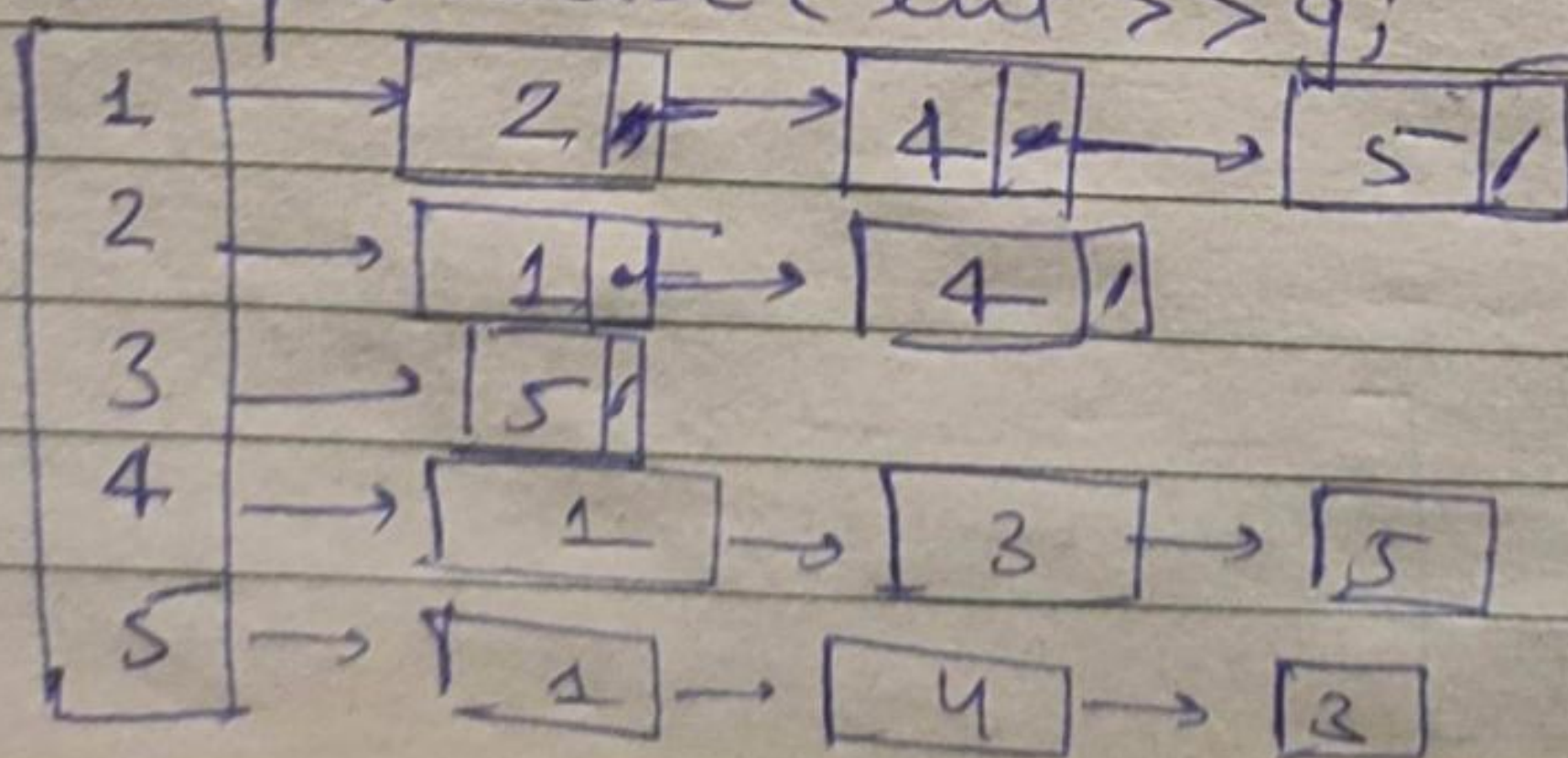
	0	1	2	3
0	0	5	10	2
1	1	0	0	1
2	0	0	5	2
3	0	1	2	3

$O(V^2)$



Adjacency List: An array of list. size of arr = no. of vertices. we can also implement

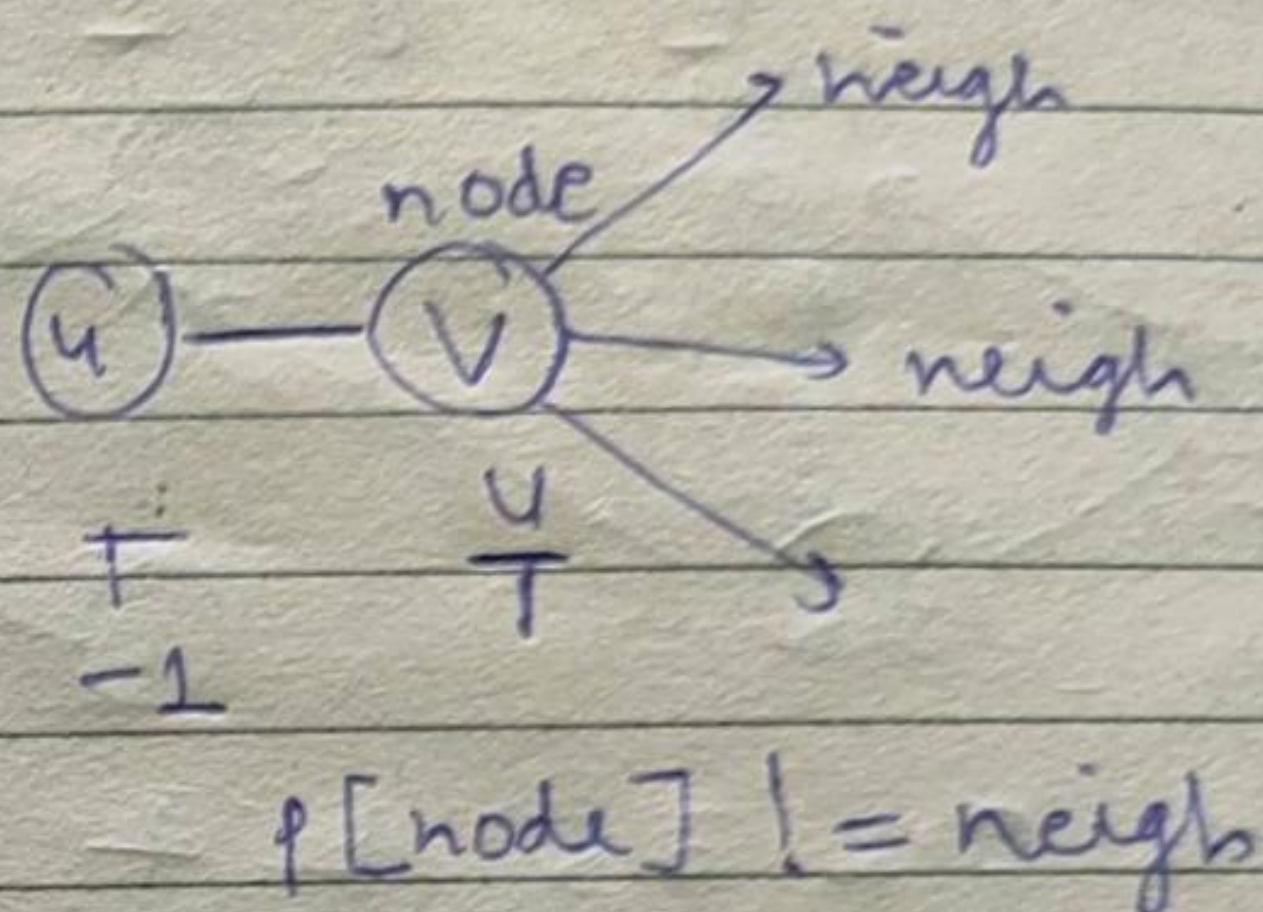
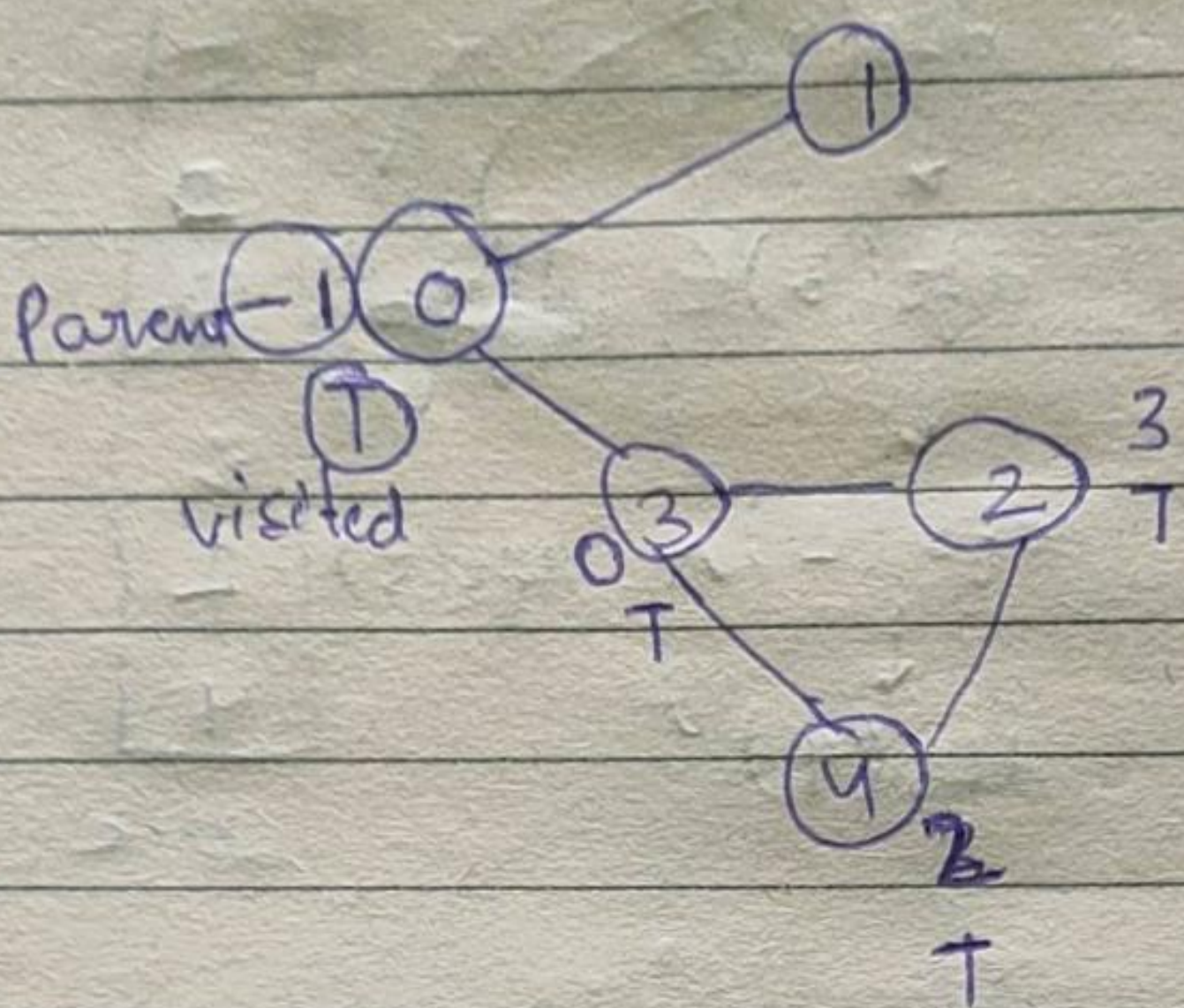
$\text{map} \langle \text{vector} \langle \text{int} \rangle \rangle g_i$ Linklist



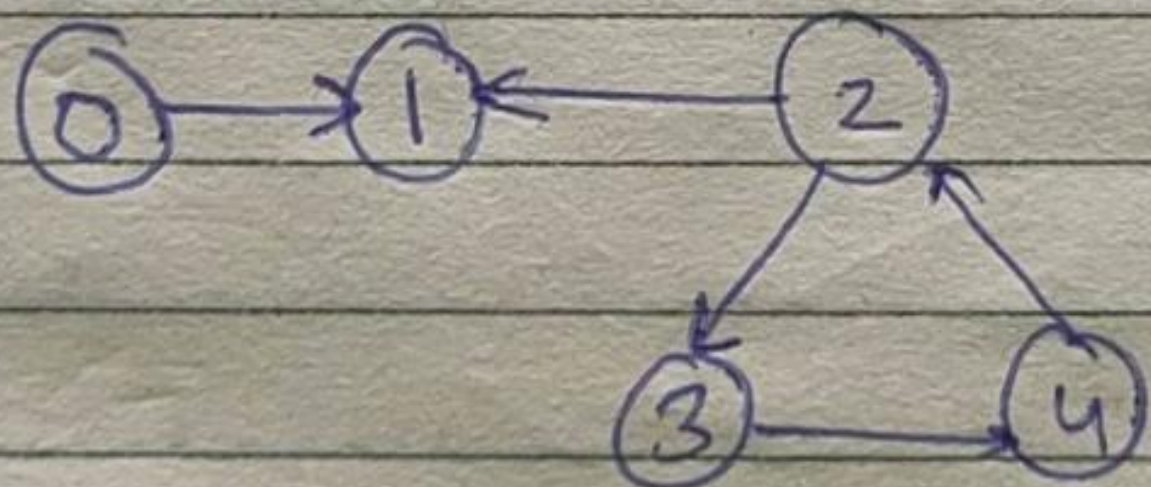
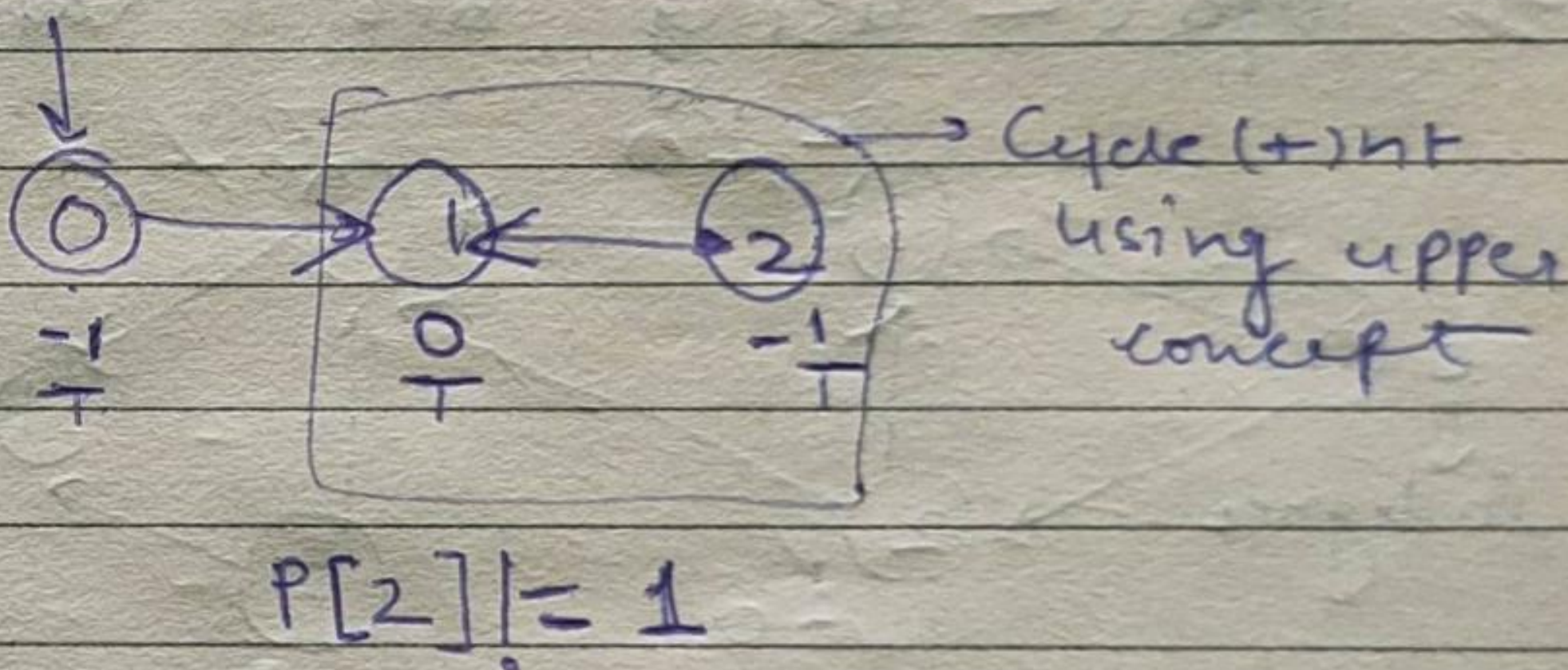
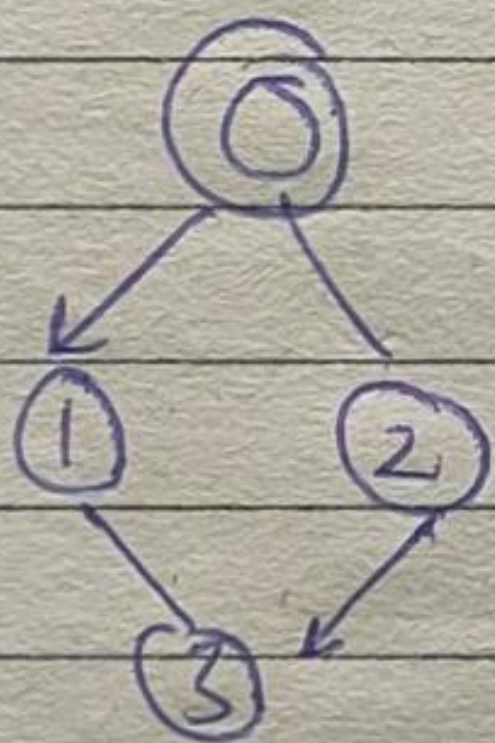
Space
 $O(2E + V)$
 $O(E + V)$

Cycle Detection :-

Undirected graph:- If we visit the same node hence cycle is there

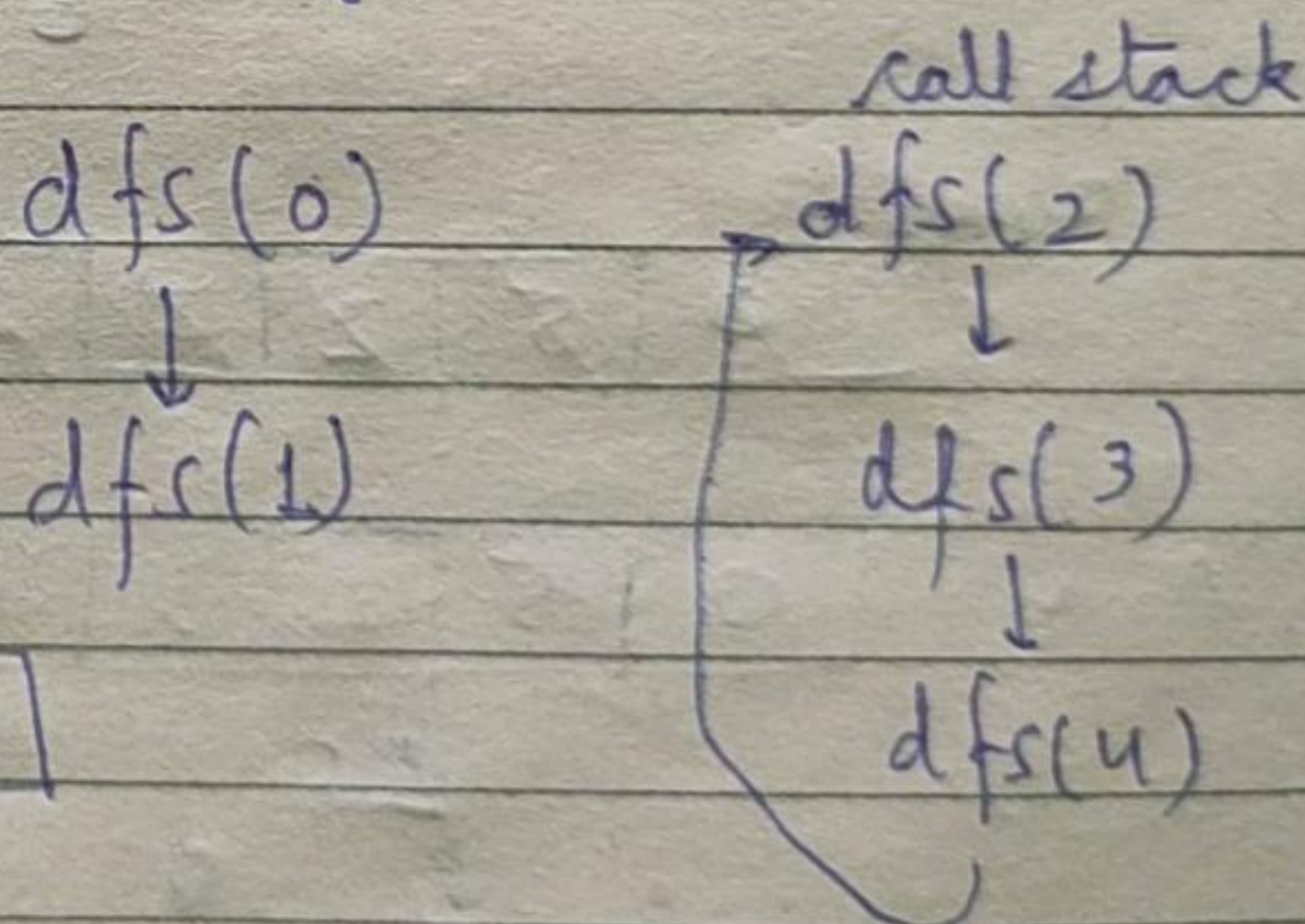


Directed Graph:-



	0	1	2	3	4
vis[] =	T	T	T	T	T

	0	1	2	3	4
res[] =	T	T	T	T	T

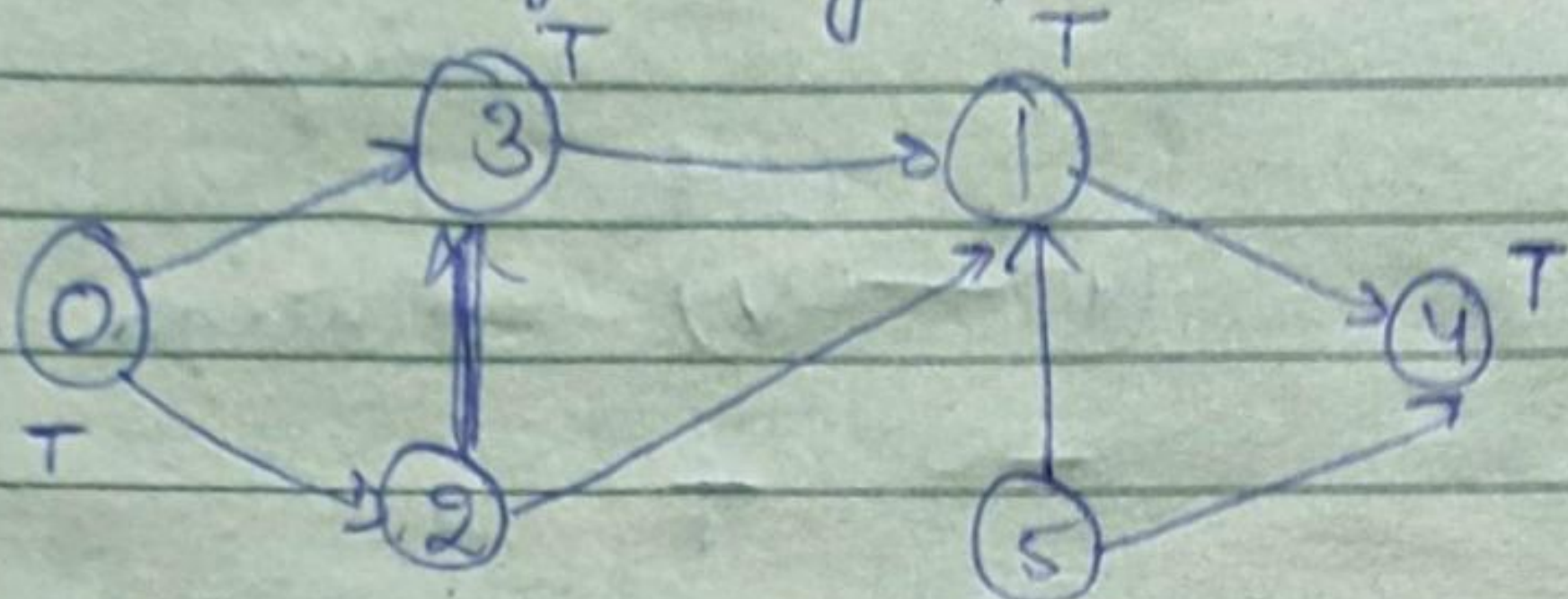


recs[neigh] = true

Topological Sort :- write in linear form such that if any edge (u, v) u appears before v .

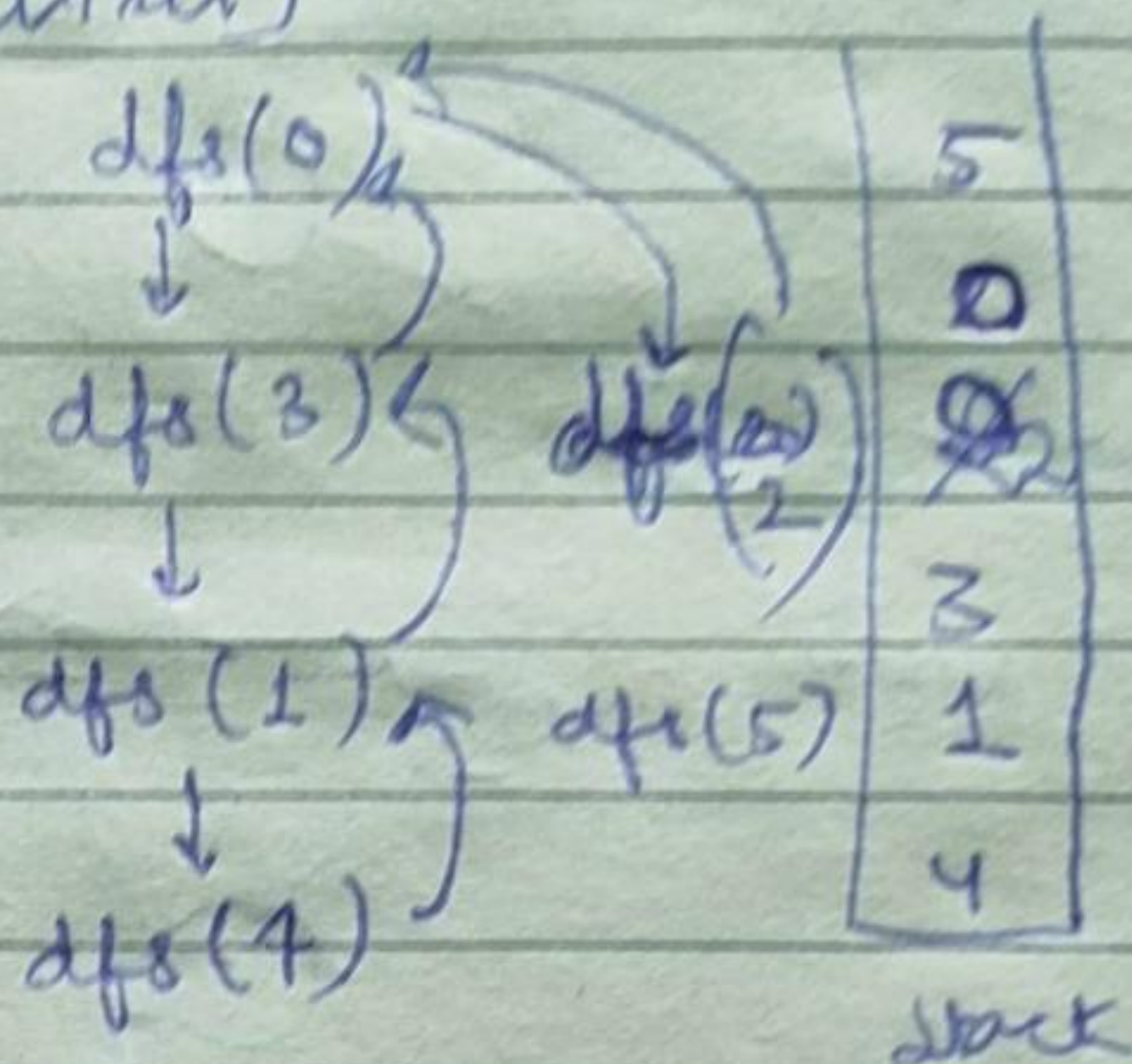
DAG

Directed Acyclic graph (means no revisit)

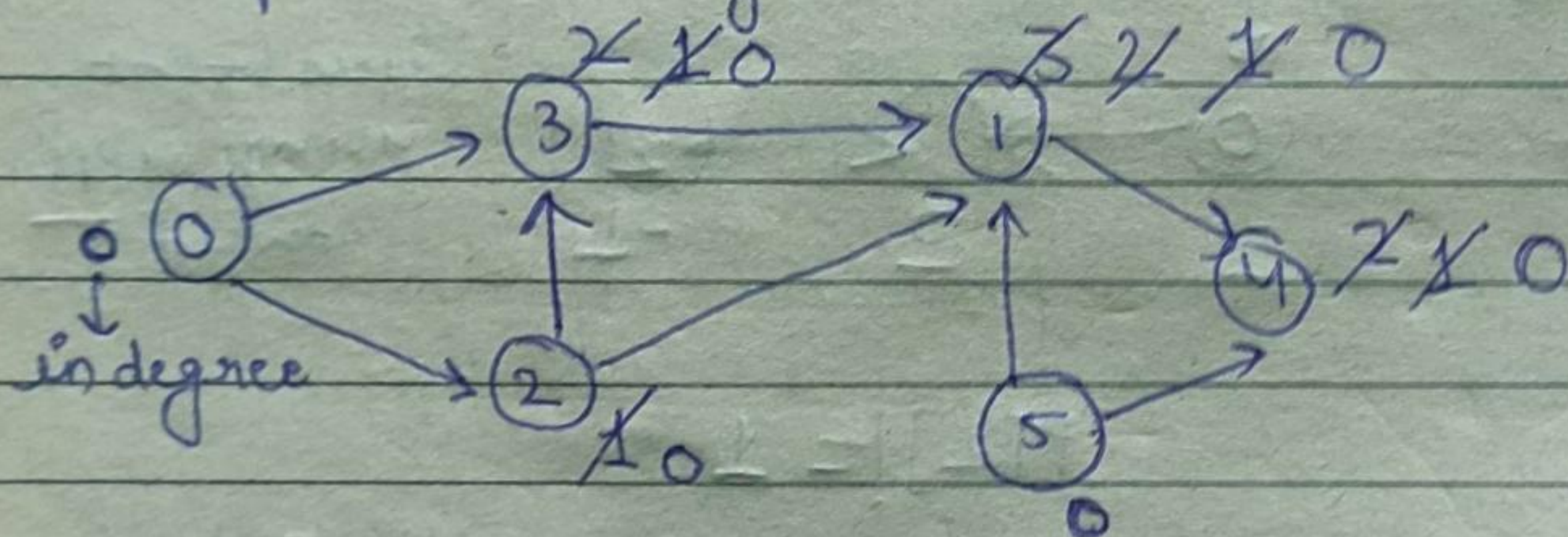


0 2 3 5 1 4
5 0 2 3 1 4 ✓

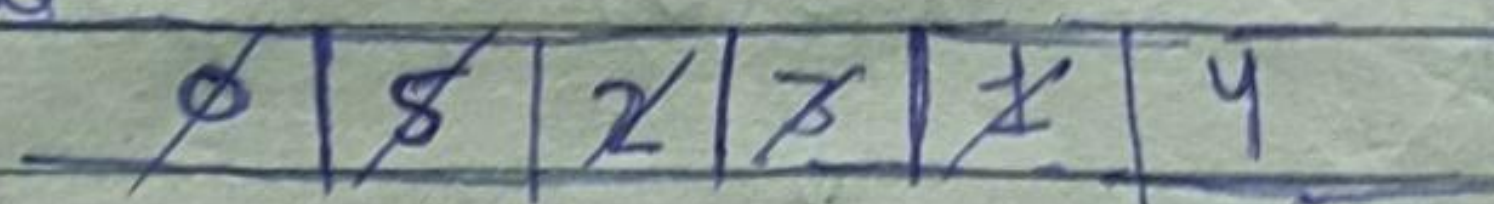
~~0 2 3 5 1 4~~



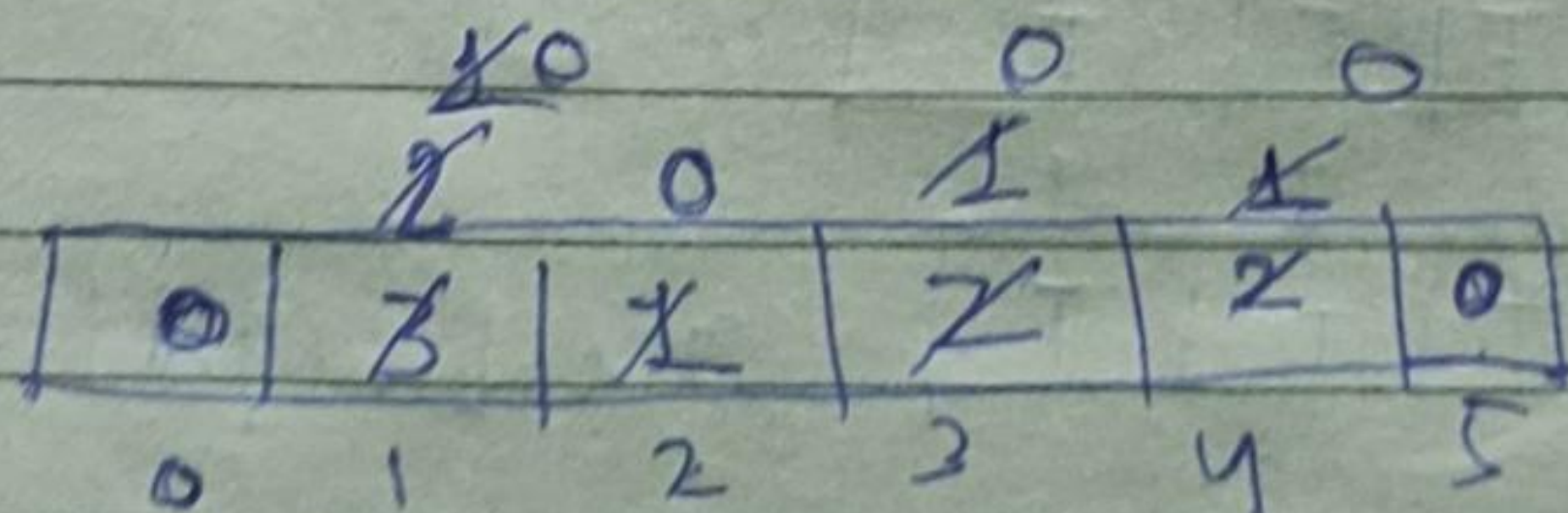
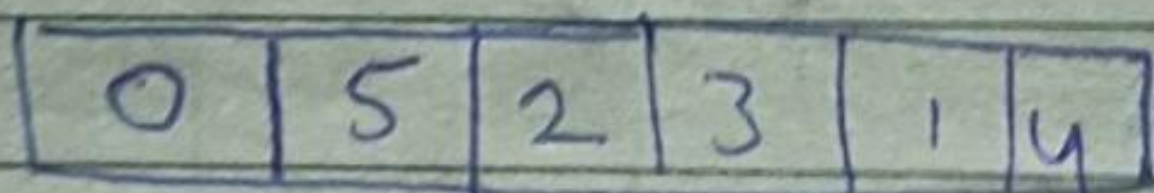
Topo s - using BFS (Kahn's algorithm)



Queue

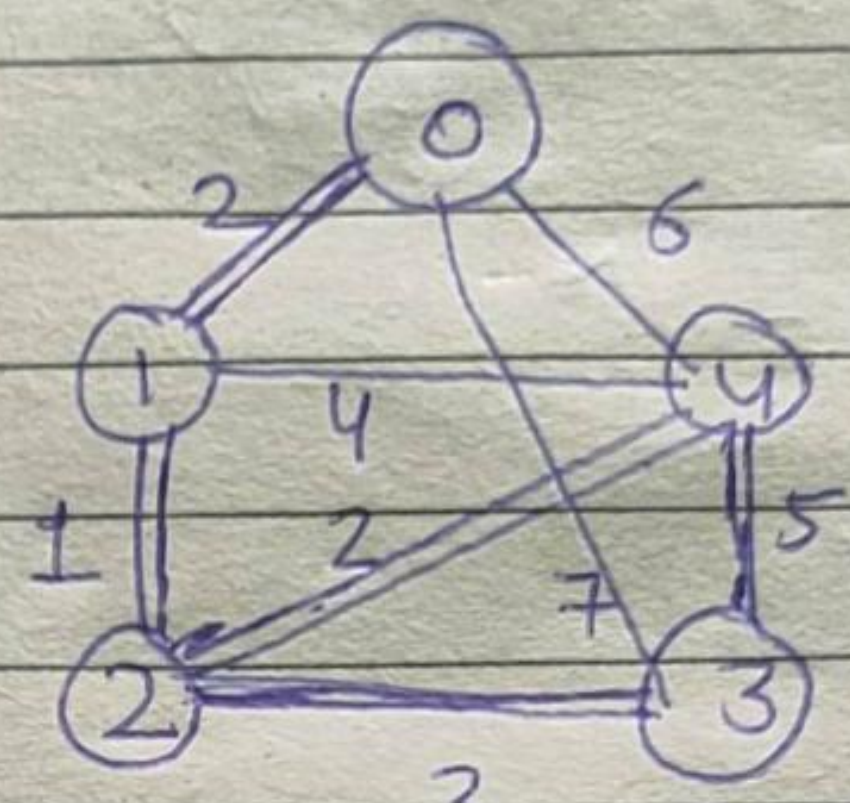


Ans



Minimum Spanning Tree - visited Prims Algorithm.

	0	1	2	3	4
vis ^(u)	T	T	T	T	T



pq (0,0) <v,wt>
pq (1,2) ✓ (4,6)
(3,7)

extract min
pq (4,6) (3,7) (2,1) (4,4) and → ~~2,3,5~~ 8

pq (4,6) (3,7) ~~(4,4)~~ (4,2) (3,3)

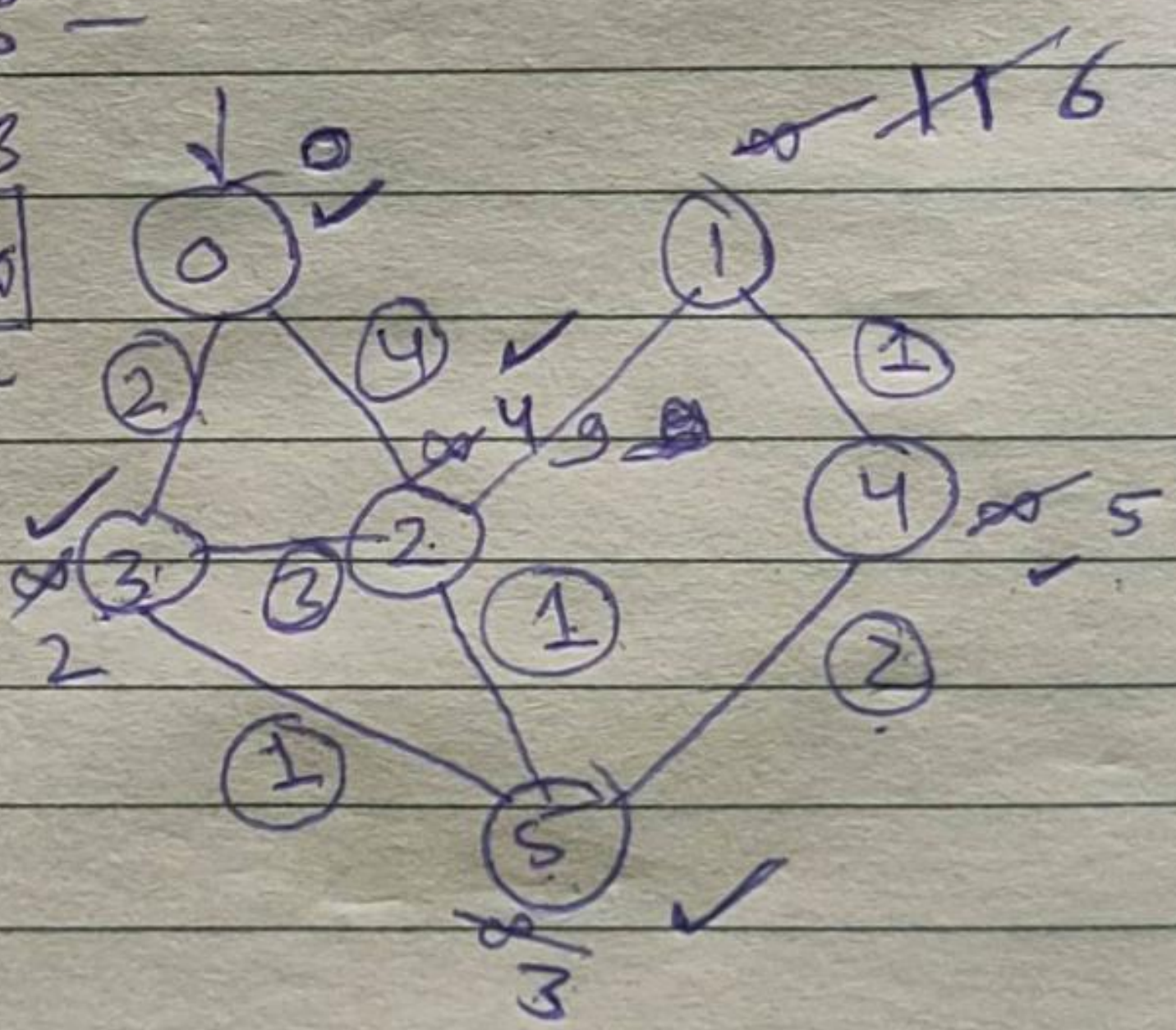
pq (4,6) (3,7) (4,4) (3,3) (3,5)

Use pq + hashmap for optimisation like
(4,2) to pq m fir bhi (4,4) dalre h apun
weight ki value modify kar sakte hn.

Dijkstra's algorithm :-

ans

	0	1	2	3	4	5
	0	6	4	2	5	3



pq (0,0) — (wt, v)

pq (2,3) ✓ (4,2)

pq (3,5) (4,2)

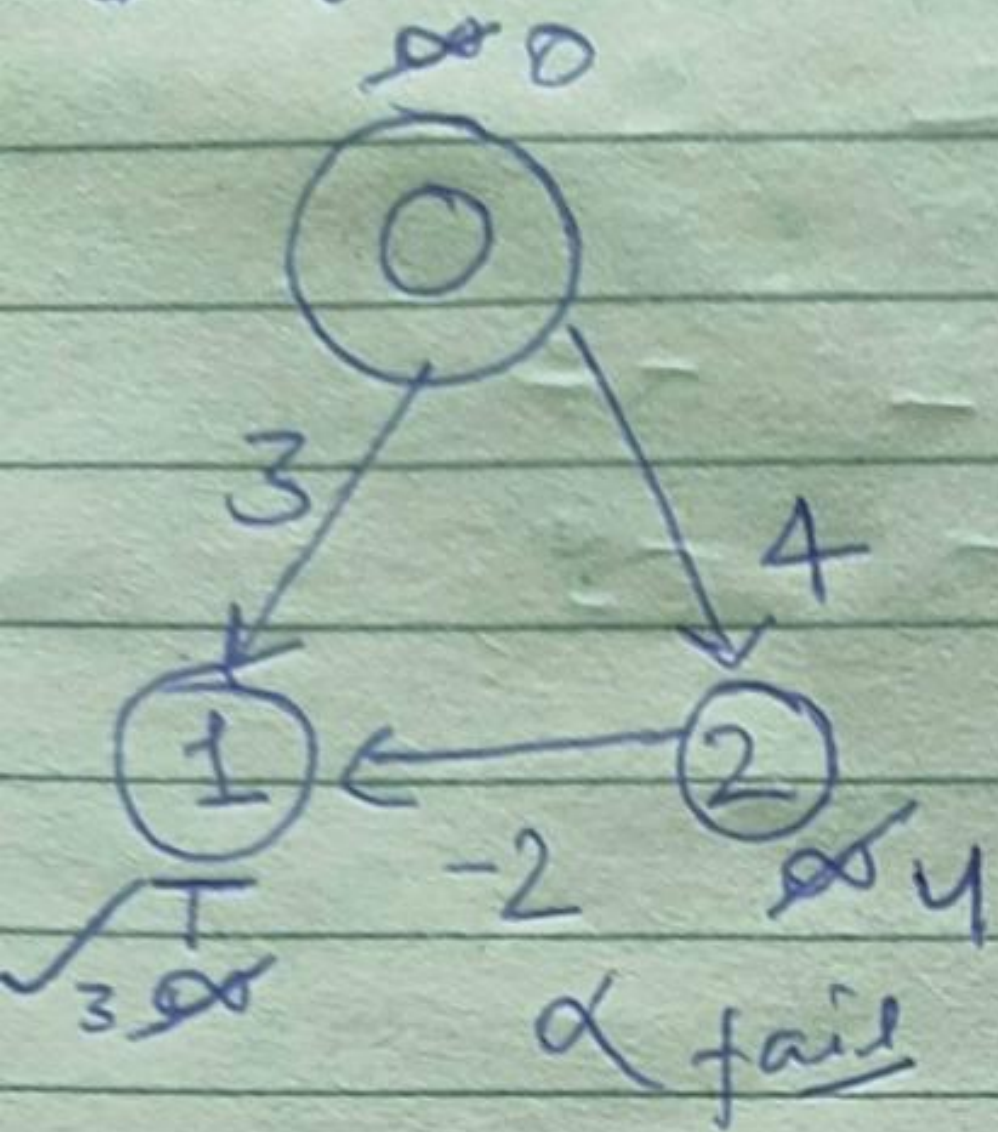
pq (4,2) (5,4)

pq (11,1) (5,4) ✓

pq (11,1) (6,1) ✓ so if (visited[4] == true) continue

pq (11,6) continue

Bellman - ford algorithm



Dijkstra
Negative edges X

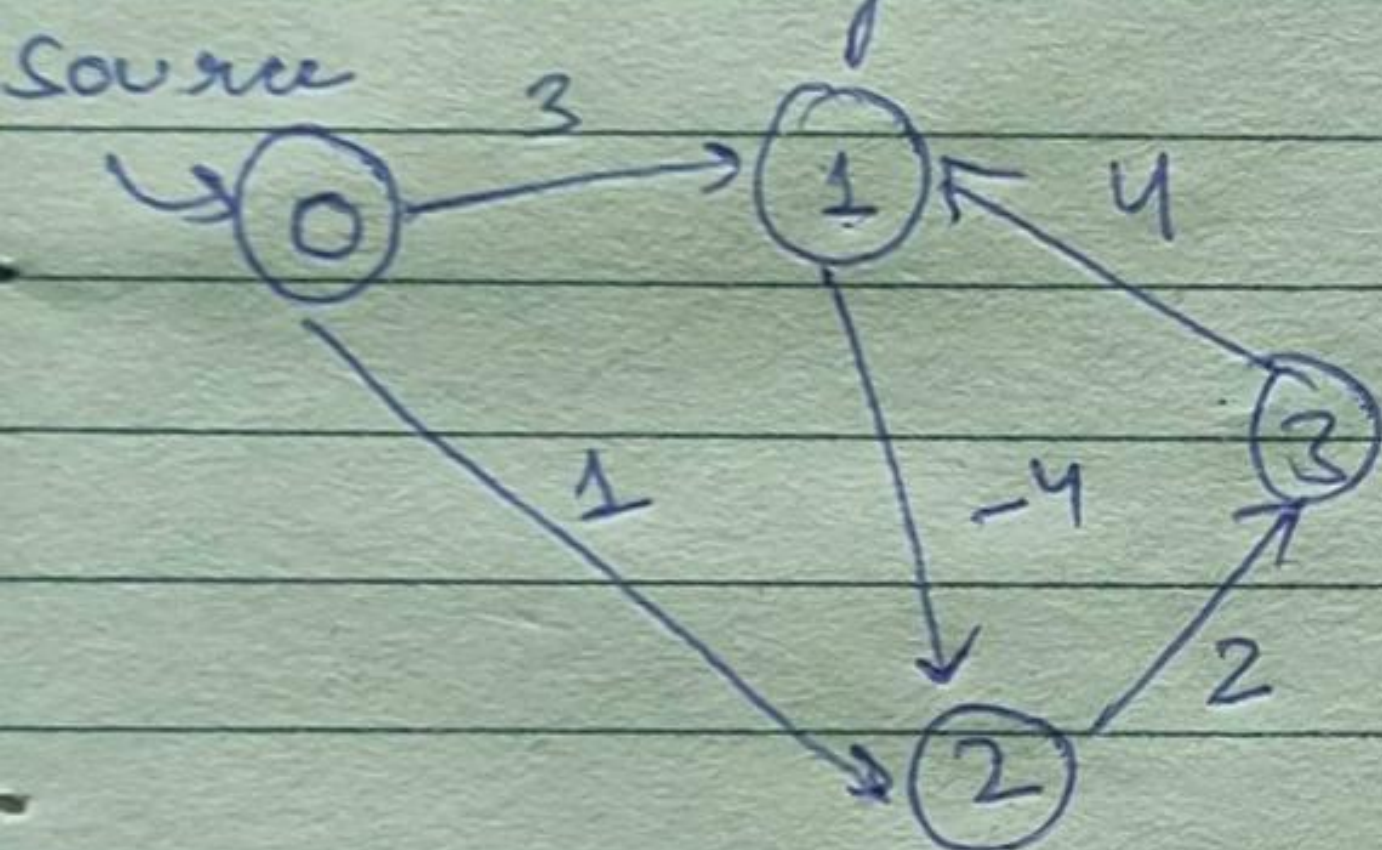
Time complex $O(E \log V)$

Bellman - ford

✓

$O(VE)$
 $(V-1)E$

Dijkstra algo not works with negative edges.
Working



V → (V-1) count	0	1	2	3	← dist
0	0	∞	∞	∞	
1	0	3	-1	1	
2		3	-1	1	
3		3	-1	1	

for every edge $(s \xrightarrow{wt} d)$
if $(dist[s] + wt < dist[d])$ {
 $dist[d] = dist[s] + wt$;
}

order of edge

0 → 1

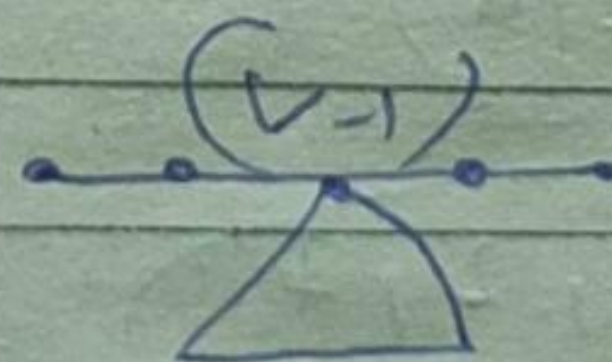
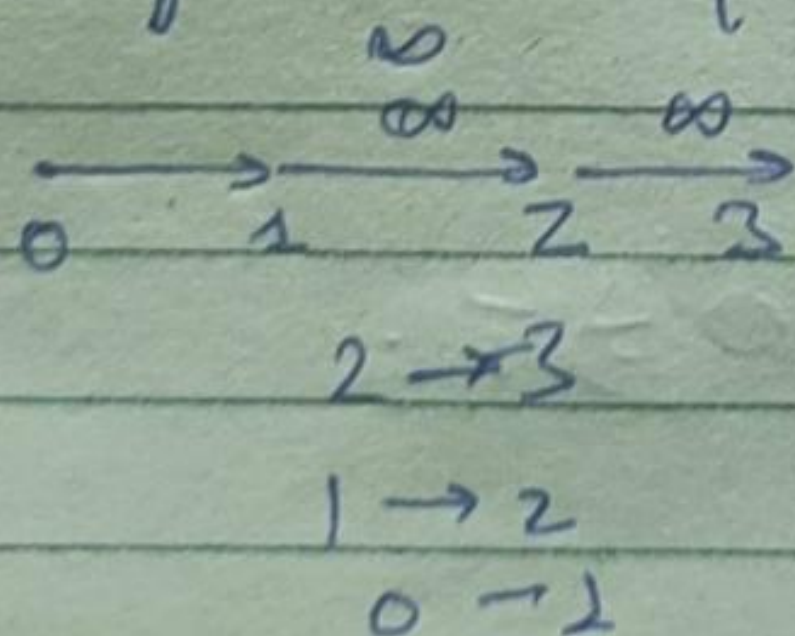
0 → 2

1 → 2

3 → 1

2 → 3

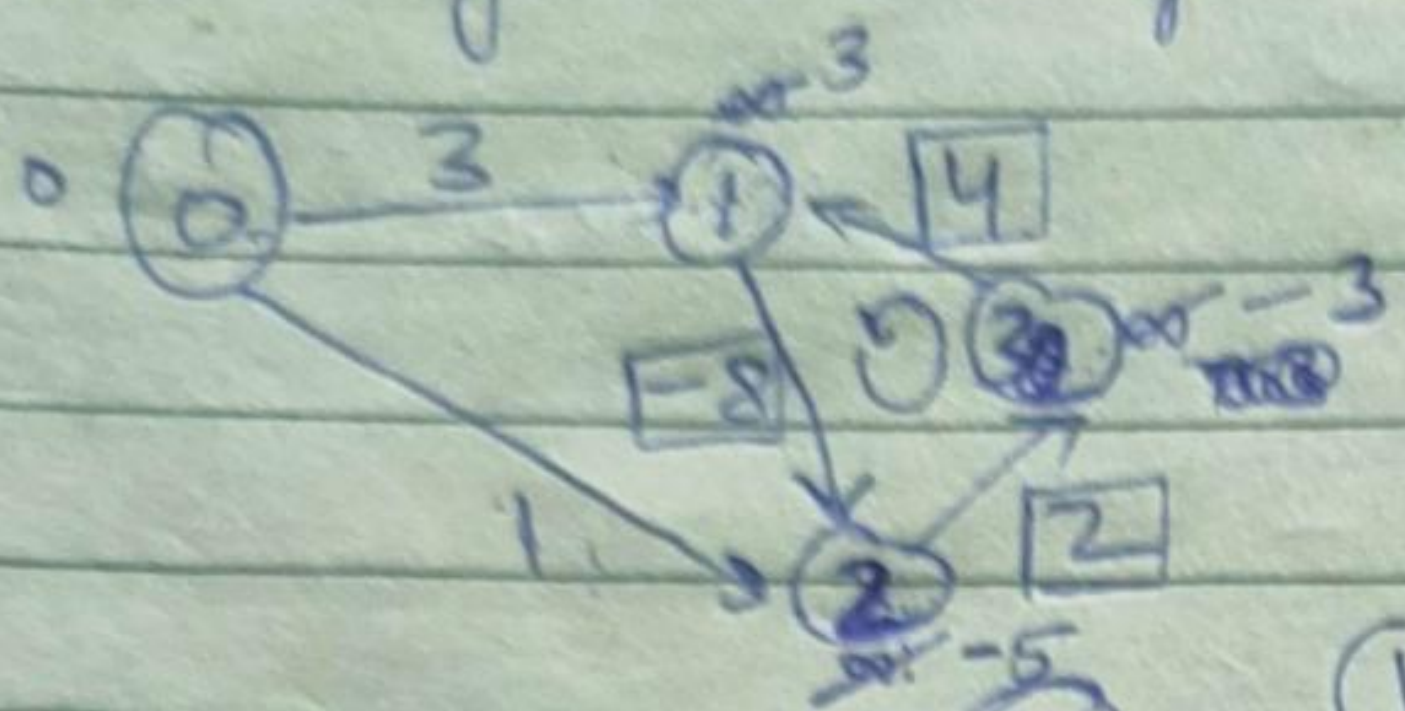
why it require $V-1$ iterations:-



max longest
edge dist $(V-1)$
edge -

$0 \rightarrow 1$ $1 \rightarrow 2$
 $0 \rightarrow 2$ $2 \rightarrow 3$
 $3 \rightarrow 1$

Negative edge cycle:-



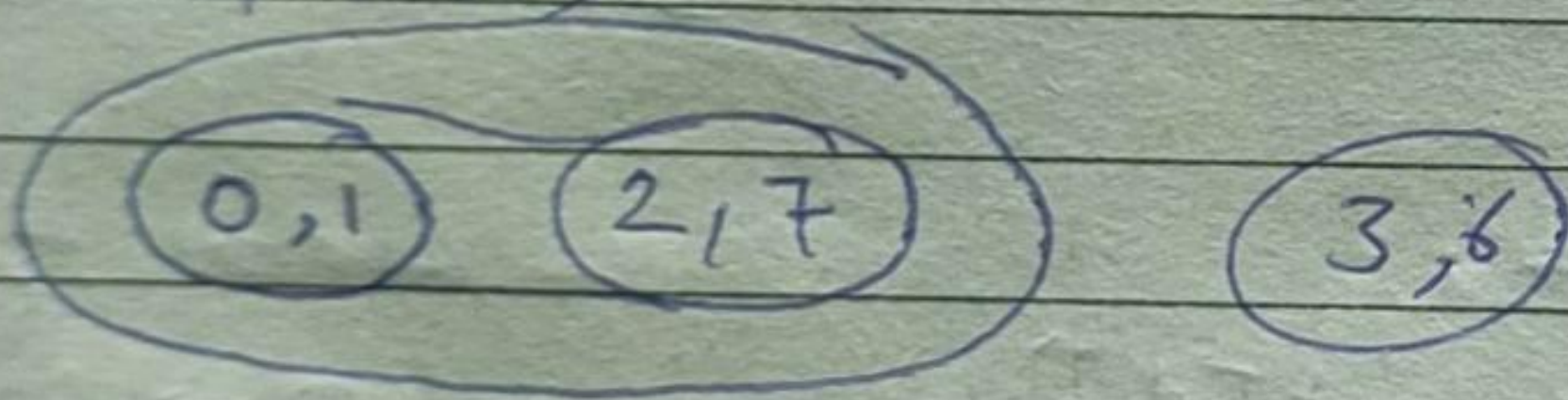
V →	0	1	2	3
0	0	∞	∞	∞
1	0	3	1	-7
2		-3	-11	-9

$-8 + 4 + 2 = -2$ (negative) \rightarrow changes

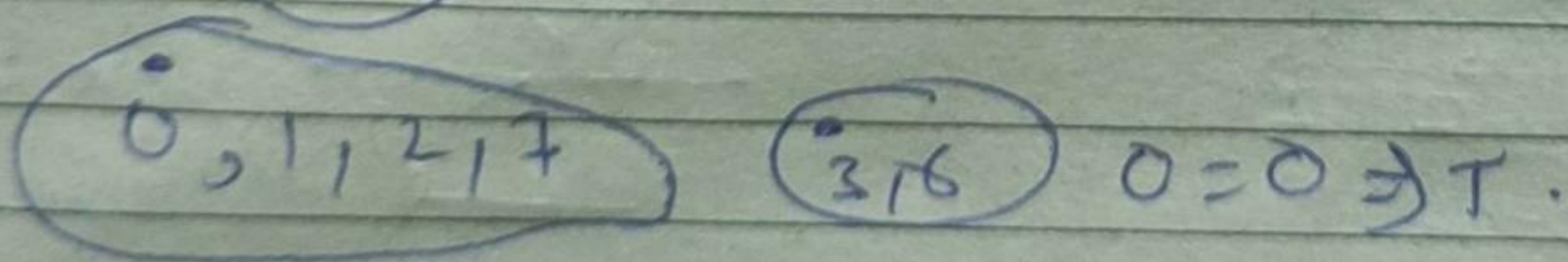
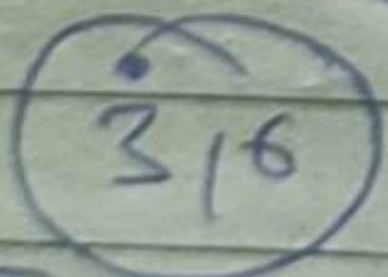
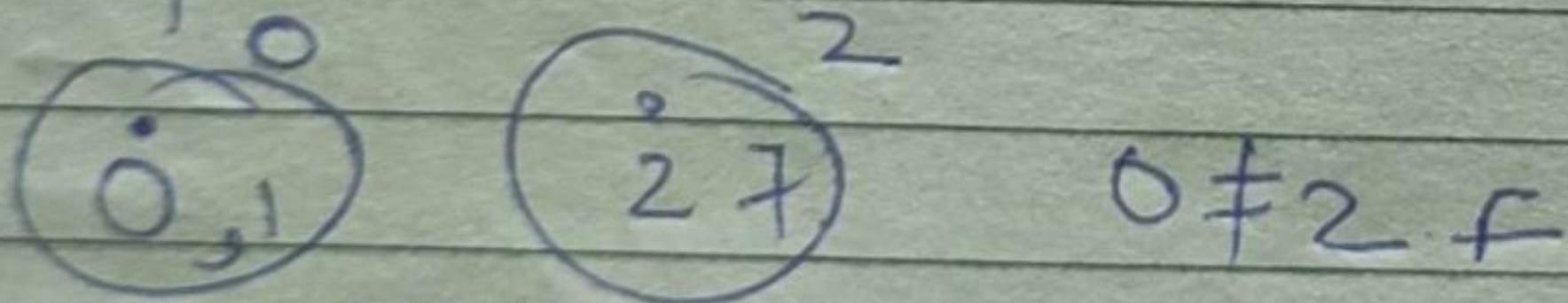
Disjoint Sets:-

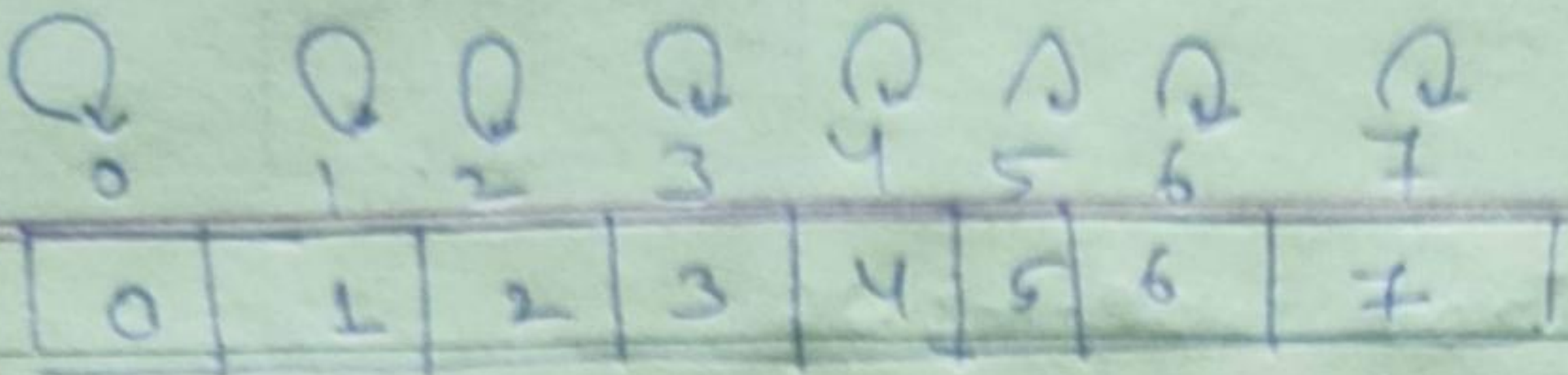
People: 0 1 7 mf(0,1)
 4 3 2 mf(2,7)
 5 6 mf(3,6)
 af(0,2) → F
 mf(0,7)
 af(0,2)

Operation
 → makefriend(a,b)
 → a & b friend(a,b)

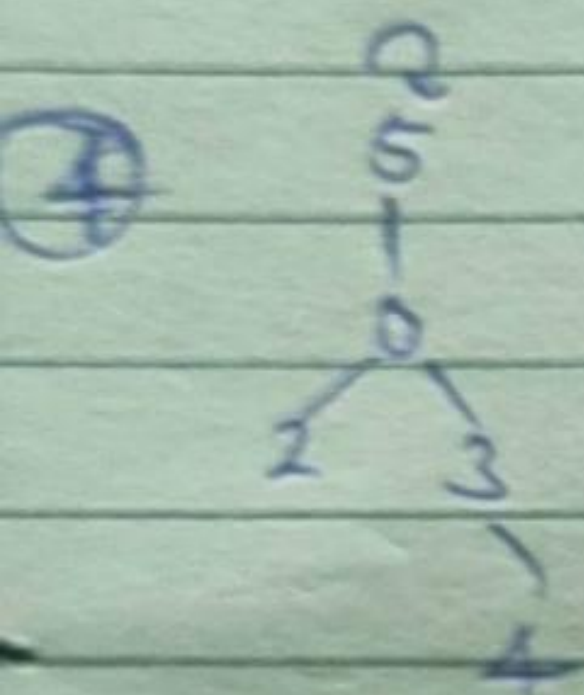
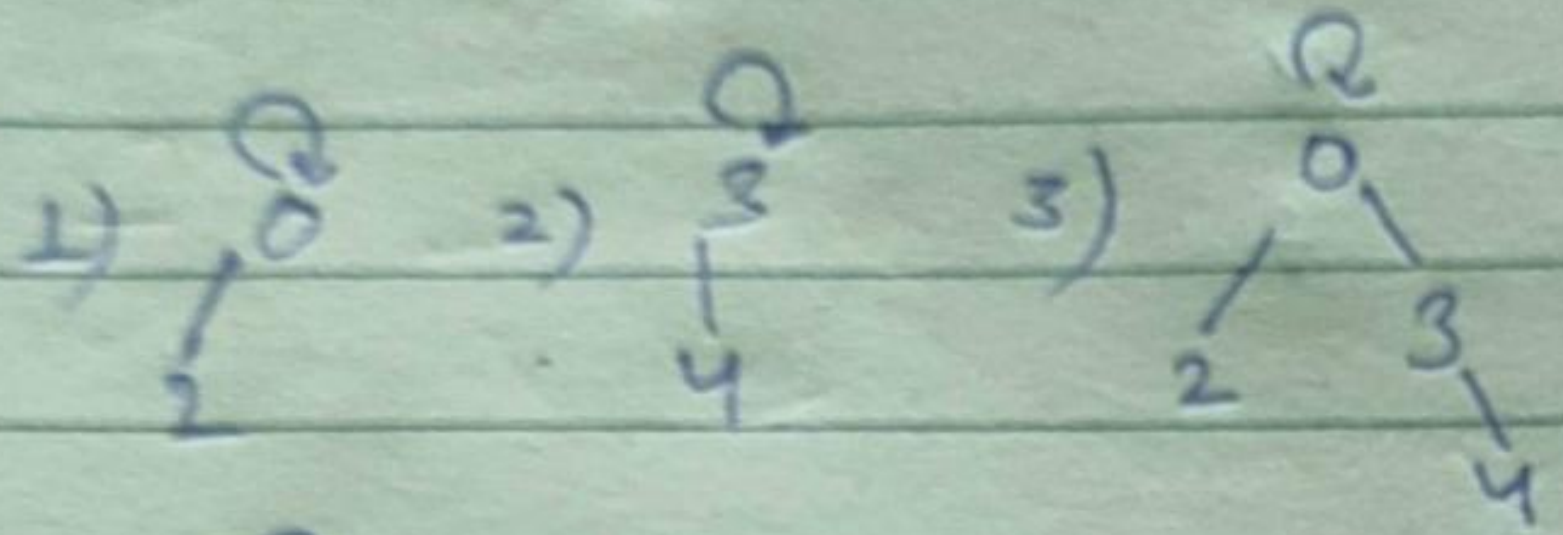


make representative



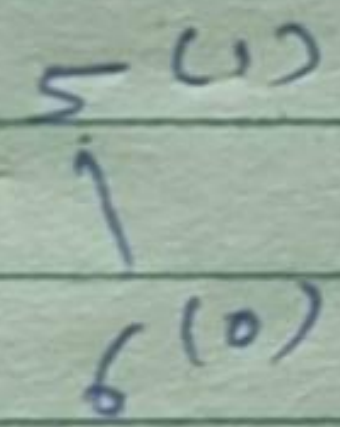
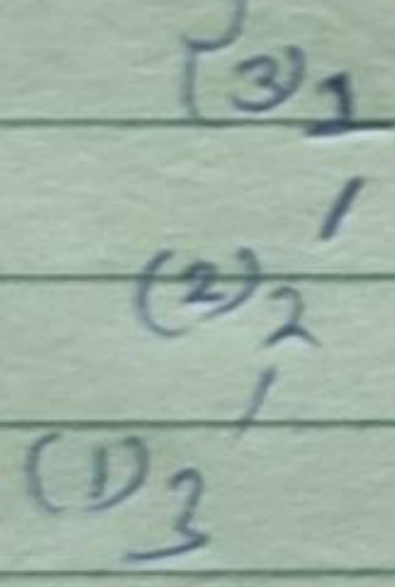


$p \rightarrow$
 1) union(0, 2), 2) union(3, 4)
 3) union(2, 4) 4) union(5, 4)
 $2 \rightarrow 0, 4 \rightarrow 3$ $5 \rightarrow 0$



complexity depends
of tree height.

so, make rank use while making parent.



Aiski rank Badi h vo parent

(0)4

Kruskal also

```

int P[] = new int[n]
initialize() {
    for (int i = 0; i < n; i++) {
        P[i] = i;
    }
}

```

```

int find (int x) {
    if (P[x] == x) return x;
    return find(P[x]);
}

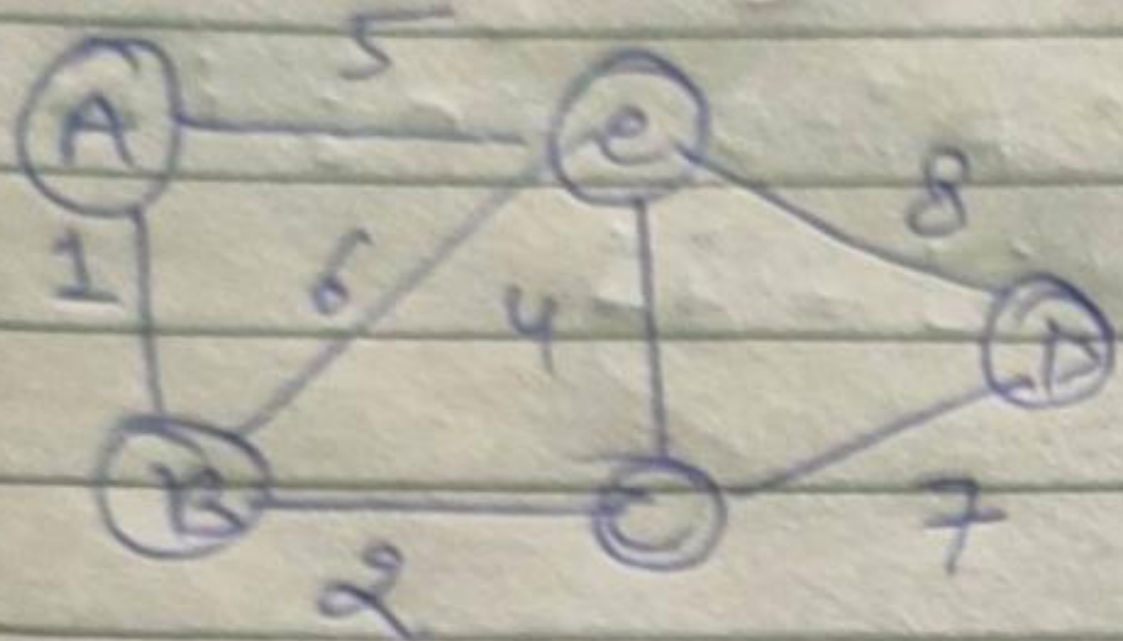
```

```

void union (int a, int b) {
    int x = find(a);
    int y = find(b);
    if (x == y) return;
    P[y] = x;
}

```


MST (Kruskal algo) connected VG



(V-1) edge

- ✓ A → B 1
- ✓ B → C 2
- ✓ C → E 4
- ✓ C → D 7

sorted edge weight

AB	1
BC	2
CE	4
X AE	5
X BE	6
CD	7
X ED	8

