

# Support Vector machine

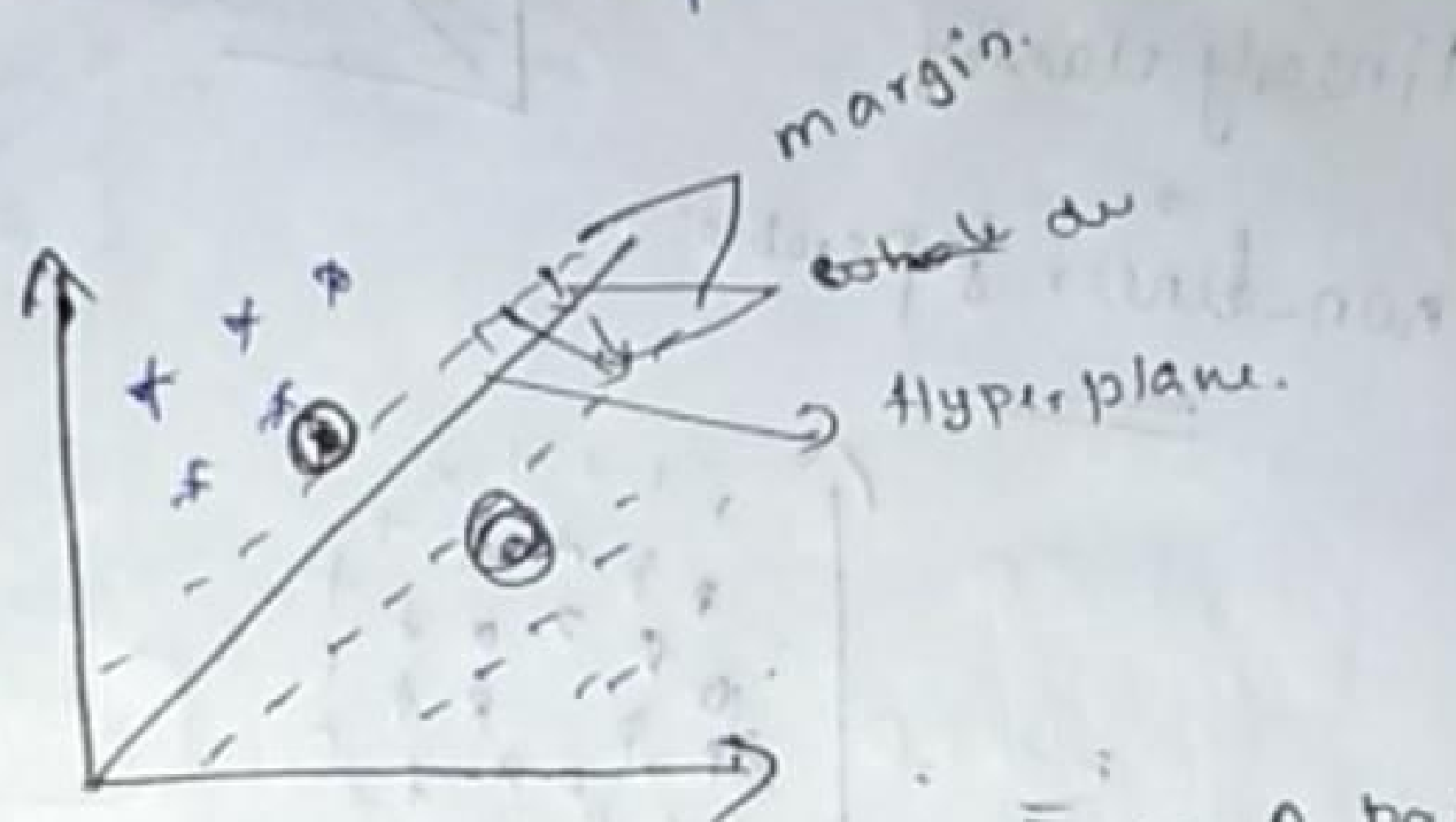
① Support Vector

② Hyper planes  $\rightarrow$  2d - straight line, 3d  $\rightarrow$  hyperplane

③ Marginal distance  $\rightarrow$  2 parallel lines are drawn  
respective nearest  
distance between them (margin)

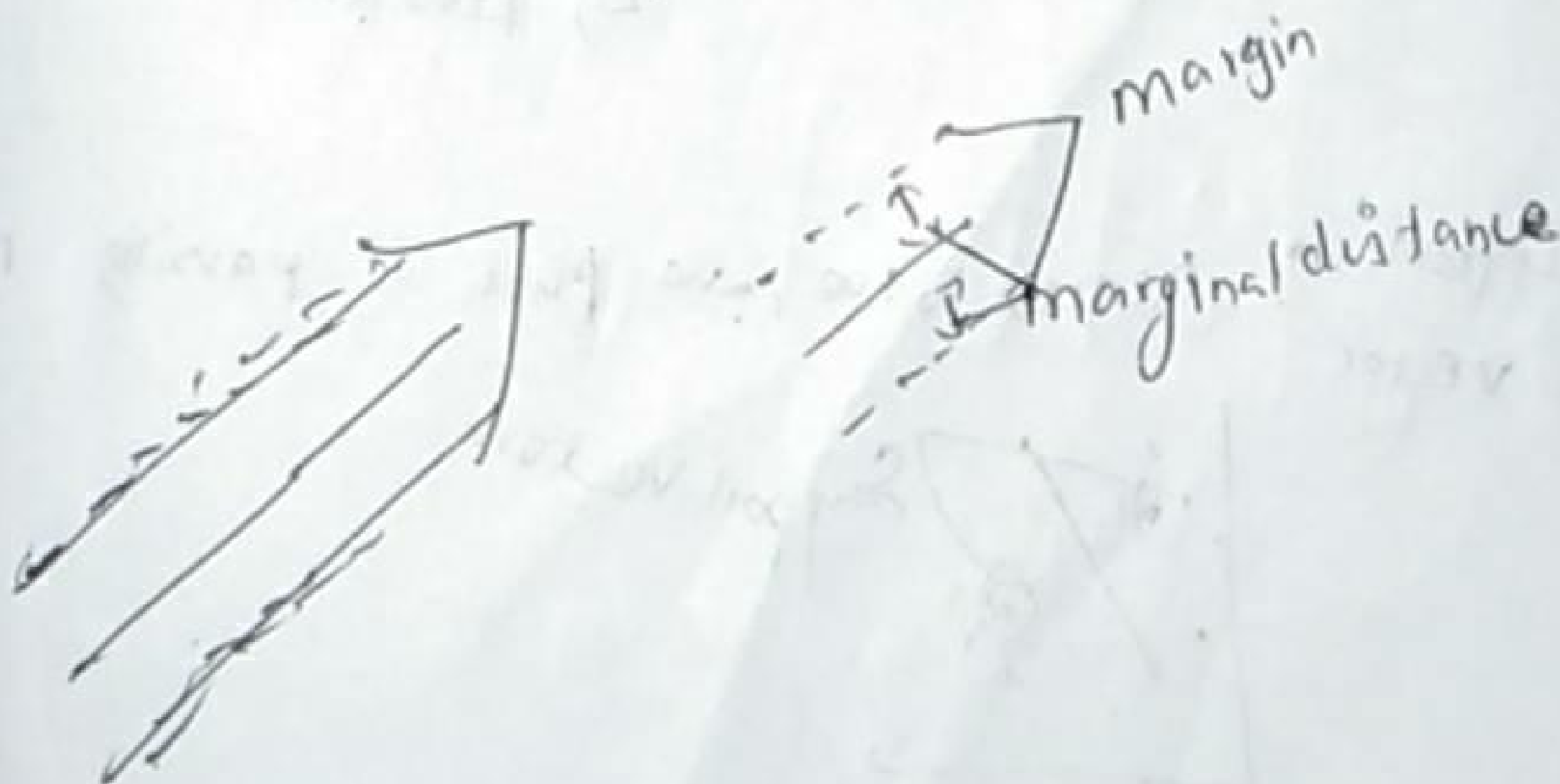
④ Linear separable  $\rightarrow$  linearly lin sep.

⑤ Non-linear separable



After create hyperplane create 2 parallel  
plane one is dot @ this is dot  
(margin)

One of Nearest (line or -ve)



aim: maximum margin plane

which has maximum plane (margin plane)

Linear separable:

linear straight actually

linearly classifiable

non-linear separable:

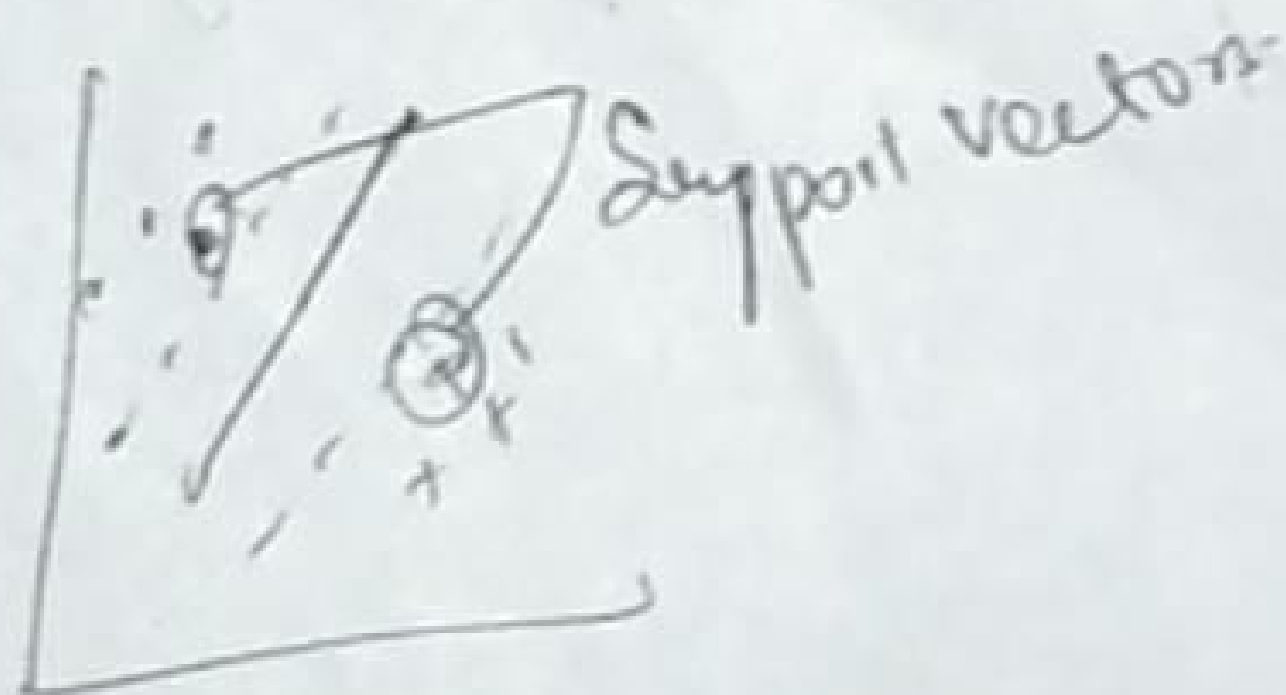


2d-line  
3d-hyperplane  
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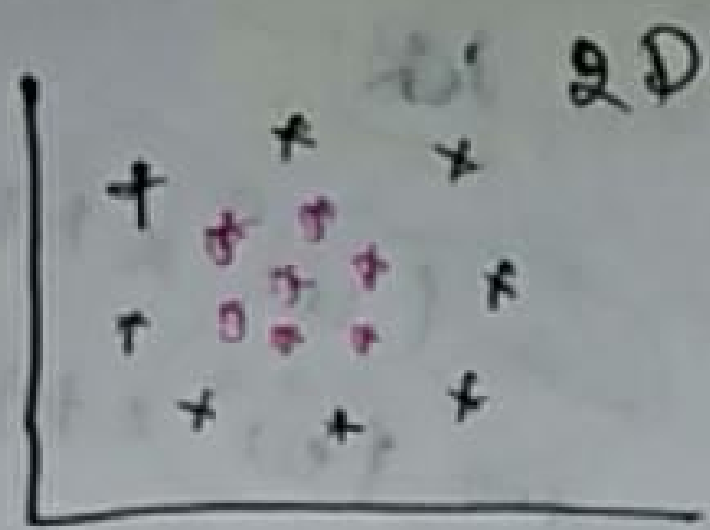
⇒ we can't draw straight line

⇒ how solve  
↳ kernel/trick

Support vector: nearest to the line that is parsing margin



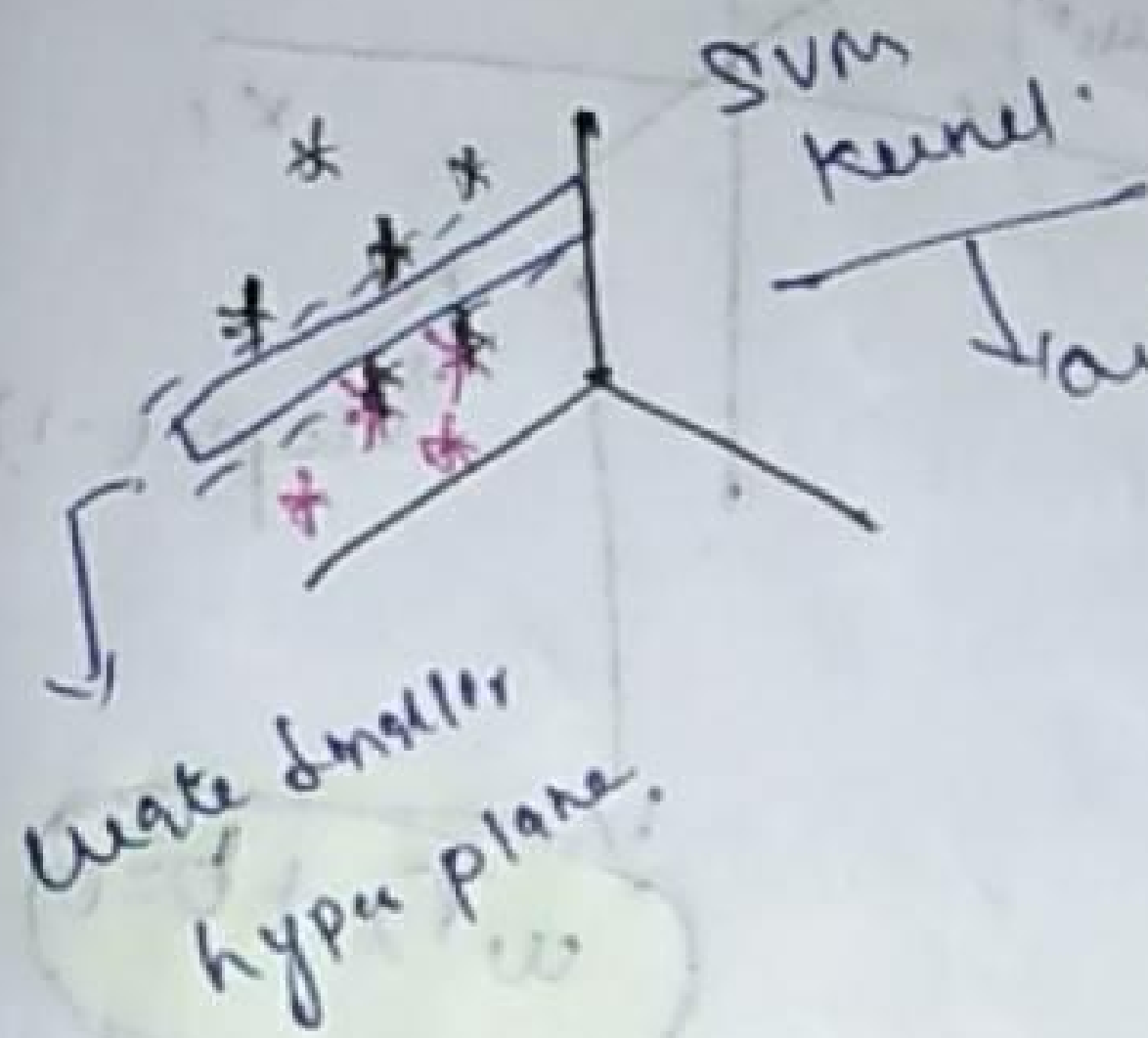
How to solve  
Non-linear?



Sum technique is SVM kernel

Low dim to  
high

2D - 3D



Low  
2D  $\rightarrow$  H.D

Higher  
margin

dis. range

more generalized  
model.

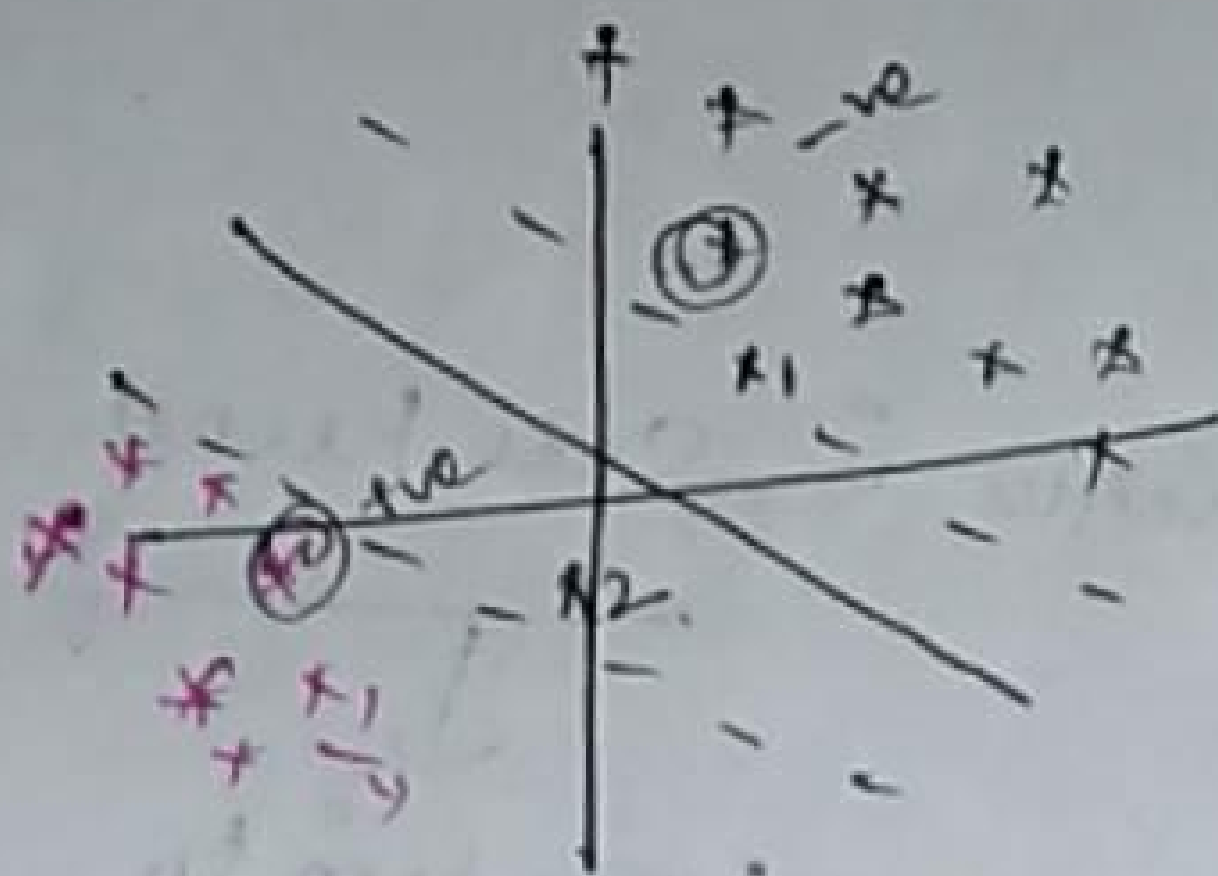




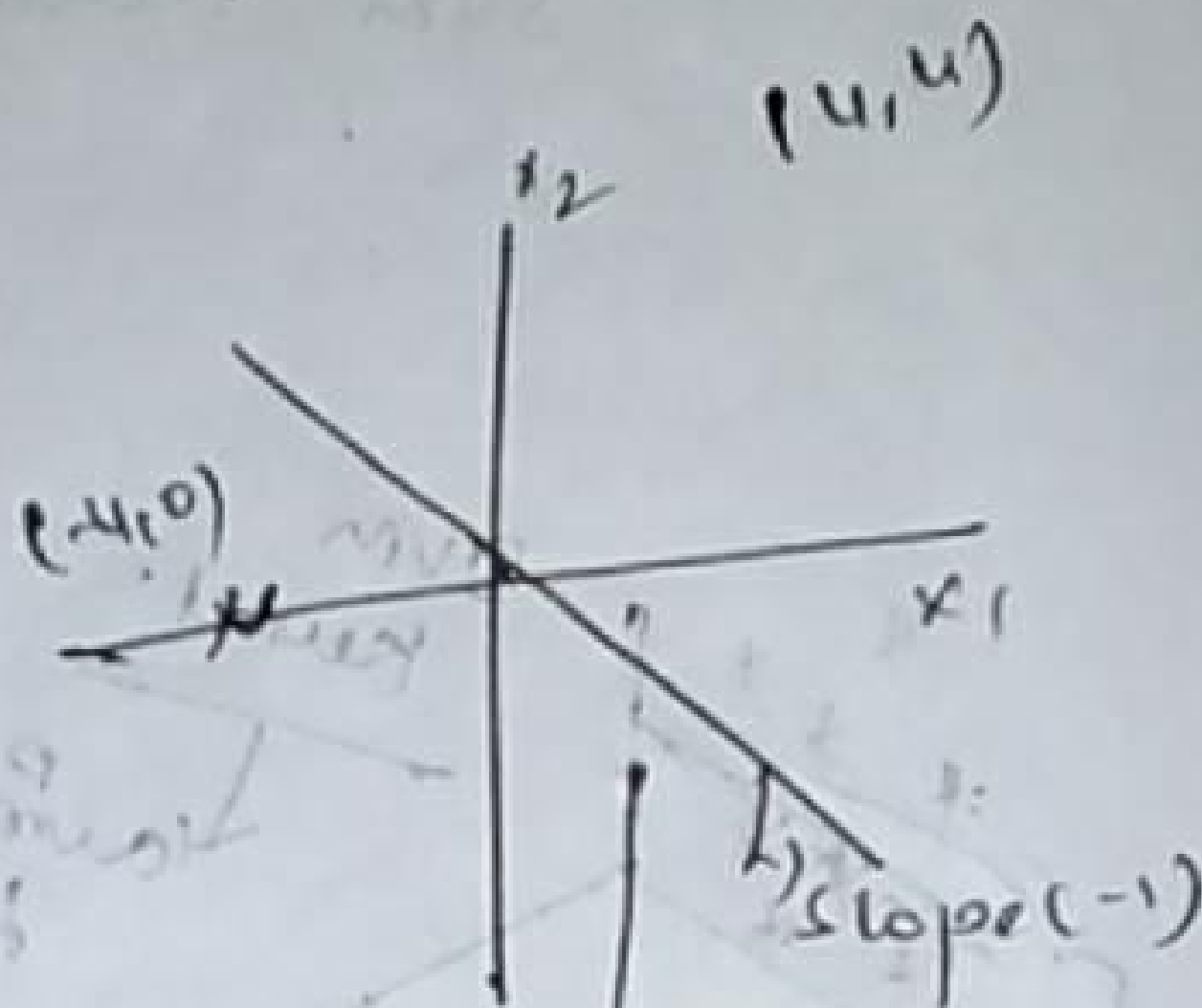
Math intuition

sum

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$$\begin{aligned} &\text{ve } (w^T x + b = -1) \\ &\text{pos } (w^T x + b = 1) \end{aligned}$$



Calculate y value:

$$m = -1$$

$$\text{cor } b = 0$$

$$y = w^T x + 0$$

$$\begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} -4 & 0 \\ 4 & 4 \end{bmatrix}$$

$$= 4 \text{ (ve)}$$

→ going to always +ve.

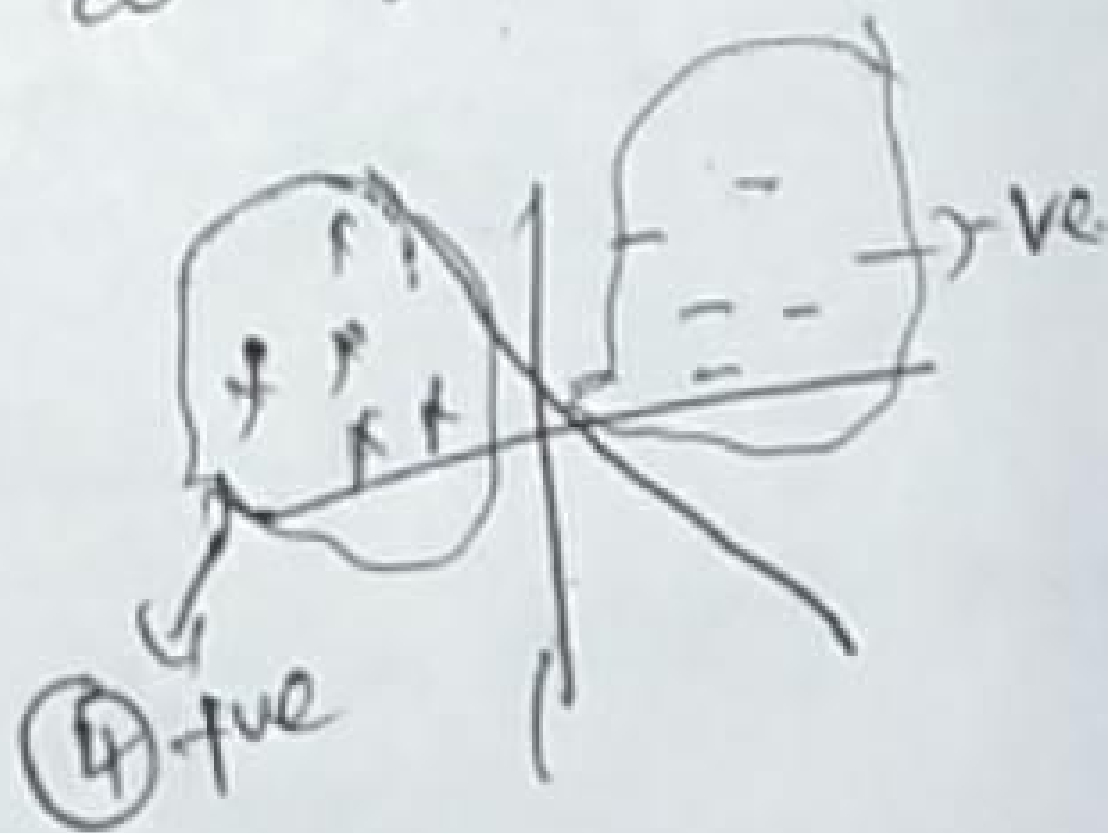
$$\begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} 4 & 4 \end{bmatrix}$$

$$= -4 \text{ //}$$

→ going to negative

$$w^T x + b = 0$$

Eqn of hyperplane



$$w^T x_1 + b = -1$$

$$w^T x_2 + b = +1$$

$$(x_2 - x_1)$$

$$w^T x_1 + b = -1$$

$$w^T x_2 + b = 1$$

$$w^T (x_2 - x_1) = 2$$

Remove help of norm  $|w|$

$$\frac{w^T}{\|w\|}$$

$$(x_2 - x_1)^T \frac{w}{\|w\|} = 2$$

optimize function

wanted to maximize

$$\text{update } (w, b) = \max \frac{2}{\|w\|}$$

such that

$y_i$

$$w^T x + b \geq 1$$

$$w^T x + b \leq -1$$

instead previous line  
 $y_i \times w^T x_i + b_i \geq 1$

That is not  $\geq 1$  that is misclassification.

apart add 2 terms,

$$w + b^* = \min \frac{\|w\|}{2} + C \sum_{i=1}^n \text{get } \eta_i \quad (\text{minimize distance})$$

how get  
 (hyperparameter  
 tuning)

(Regularization)

How many errors  
 my model.

Summation (value  
 of error)

error  
 $= C - \text{misclassified points}$

Value of error = distance b/w them  
 errors then get sum of errors

Svm

$$w + b^* = \min \frac{\|w\|}{2} + C \sum_{i=1}^n \text{get } \eta_i$$