

# Linear Regression



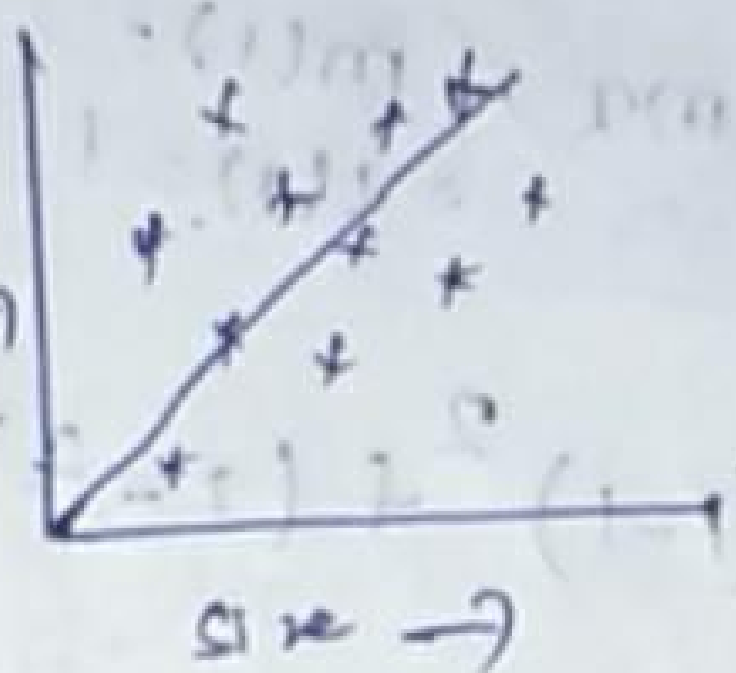
Predict by the use of known

Parameter

$$y = mx + c \rightarrow \text{line equation use}$$

this equation to find best fit line

$m$  slope,  $c$  intercept



$$S = 0$$

$$P = 0$$

$$\text{slope} = 0$$

Because pass the value by origin.

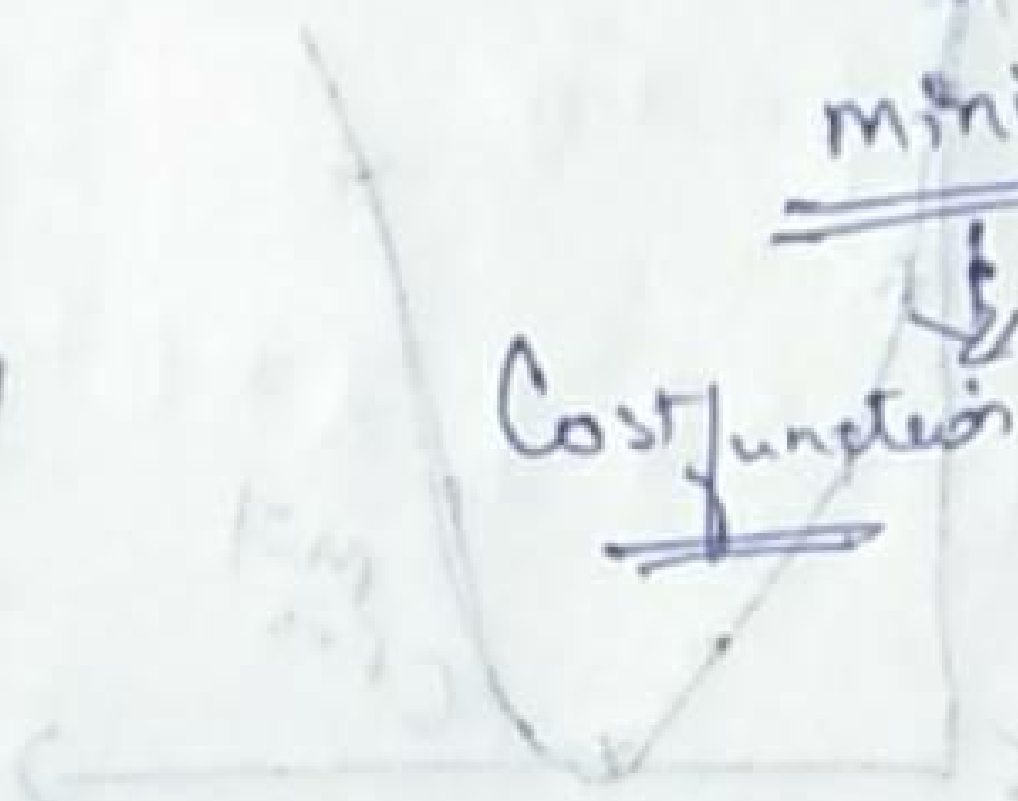
Sum of all errors

Select best fit line

through

minimal error

Cost function



distance b/w real & predicted

$$y = \frac{1}{2m} (\hat{y} - y_i)^2$$

$$\hat{y} = mx + c$$

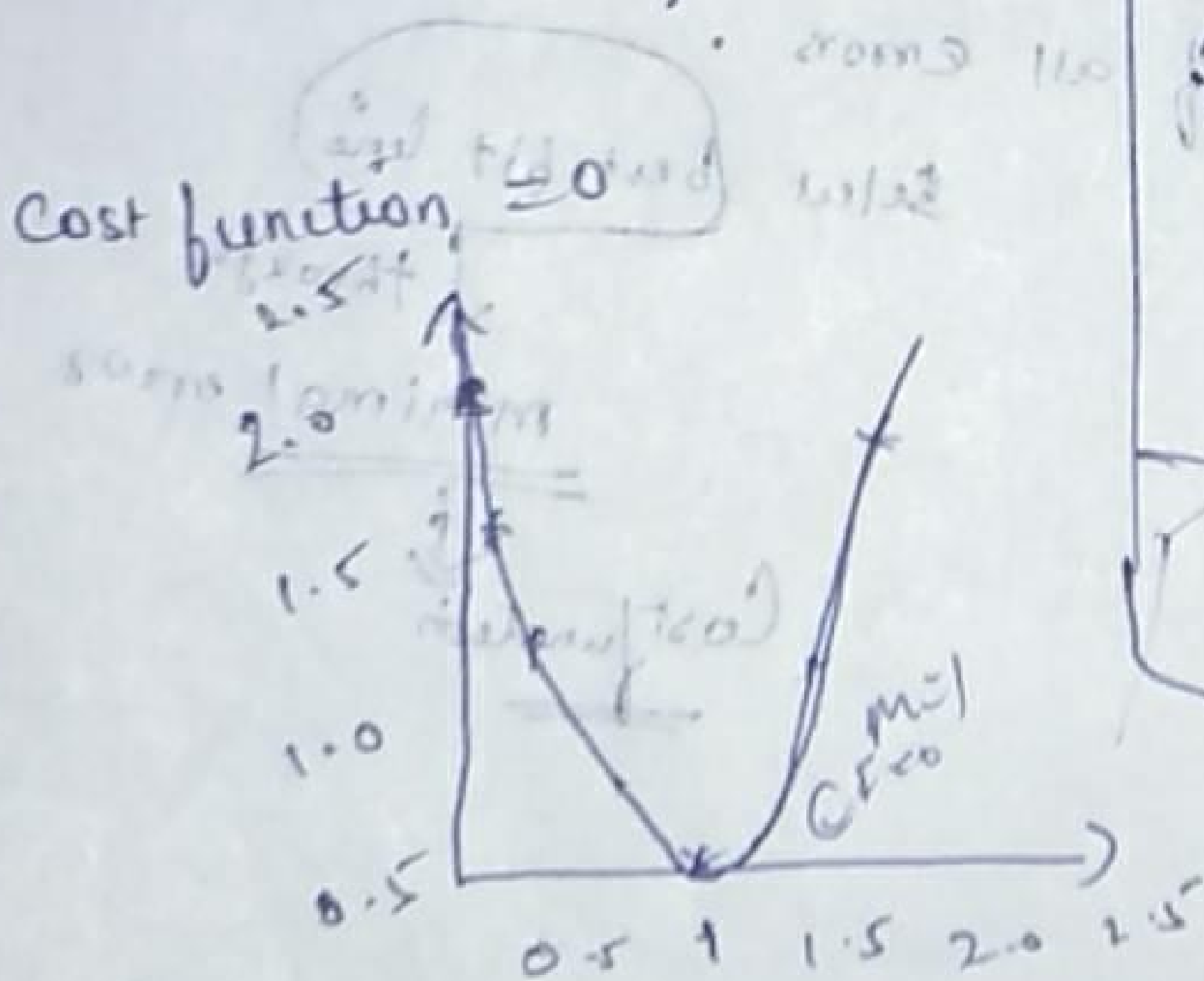
Cost function :  $\frac{1}{2m} (\hat{y} - y_i)^2$

$$= \hat{y} = y + mx + c$$

$$y = mx + m(1) = 1(1) = 1$$

$$\text{avg cost} = \frac{1}{2(3)} = \frac{1}{6} ((1-1)^2 + (2-2)^2 + (3-3)^2)$$

$$= \frac{1}{6} (0) = 0$$



$$m = 0.5$$

$$\hat{y} = mx$$

$$= 0.5(1) = 0.5$$

$$= 0.5(2) = 1.0$$

$$0.5(3) = 1.5$$

$$y = \frac{1}{2m} (\hat{y} - y)^2$$

$$= \frac{1}{2(3)}$$

$$(0.5-1)^2 +$$

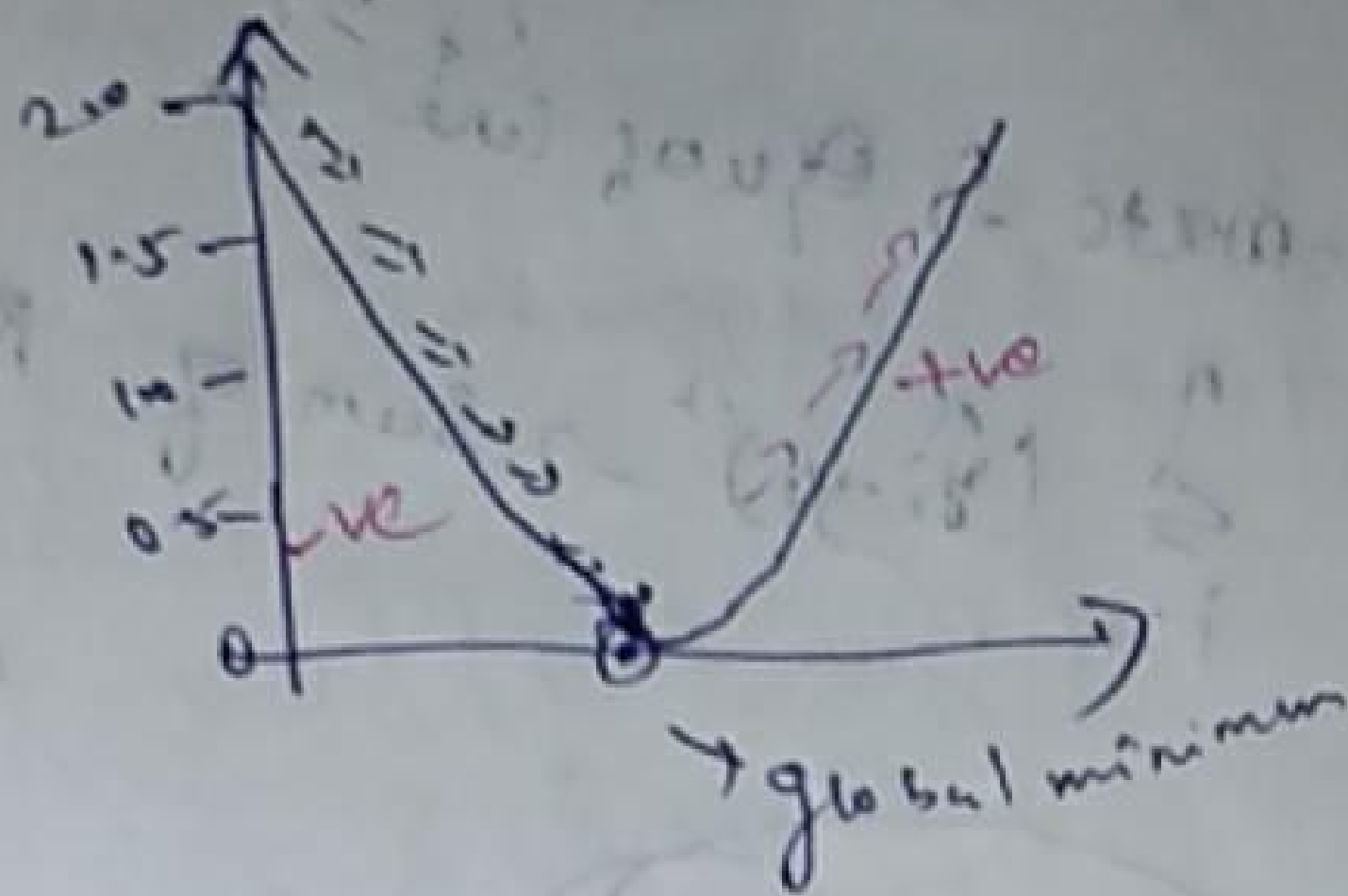
$$(1.0-2)^2 +$$

$$(1.5-3)^2$$

$$= 0.25 + 1 + 2.25$$

$$= 3.5$$

# gradient descent.



Convergence theorem → help to reach global minimum.

$$m = m - \left( \frac{dm}{dm} \right) \times \alpha$$

Subtract the slope and prod of learning rate and

$$m = m - (-ve) \times \text{smaller}$$

$$m = m + (+ve) \times \text{SR}$$

$$y = \theta_0 + \theta_1 x$$



# Ridge and Lasso Regression

$y = mx + c \rightarrow$  Quo of line

$$\sum_{i=1}^n (\hat{y}_i - y_i)^2 \rightarrow \text{Sum of Residuals}$$

↓  
Cost function

Generalized model

high Variance -  
low Variance

Ridge:

- ⇒ Reduce cost function
- ⇒ Reduce overfit

Ridge add one more parameter in cost function

$$(y - \hat{y})^2 + \lambda \times (\text{slope})^2$$

steep slope  $\rightarrow$  unit increase in x  
 steep move in y

$\lambda \rightarrow 0$  to any (true)

intercept at origin  
 residual =  $0 + 1(1.3)^2$   
 $= 0 + 1.69 = 1.69$

penalize  $\rightarrow$  along with CF are  $\lambda \times (\text{slope})^2$

high slope - low slope.

less value  $\rightarrow$  selected best fit line.

Slope line

$\rightarrow$  close to zero  
 not exactly zero.

Lasso: (magnitude of slope)

& help of feature selection

$$y = m_1x_1 + m_2x_2 + m_3x_3 + m_4x_4 + \dots c.$$

$$\lambda + |m_1 + m_2 + m_3 + m_4|$$

Ridge  $\rightarrow$  towards zero not exactly zero

Lasso  $\rightarrow$  towards zero.

Lasso  $\rightarrow$  helps to feature selection

how

$$m_1 x_1 + m_2 x_2 + m_3 x_3 + m_4 x_4$$

Slope is slow that feature will be

removed.

That removable feature not helpful

Prediction

when use magnitude moving towards

zero or atleast one time reach zero