• Recursive Program to find sibling of node, given the tree and the node key

• Write a program to count the number of leaf nodes in a binary tree.

CS 103

BST

```
Write a program to insert a new node to Binary Search Tree (BST)
Main() {
  insertBST(root, val) // root = newnode{
insertBST(node, val) {
  while (true) {
   if (node.val < val ) {
              if (node.right == null) { insert new node.....node.right = nd.; return }
              node = node.right;
   if (node.val > val) {
            if (node.left == null ) { insert .....node.left = nd; return }
             node = node.left;
```

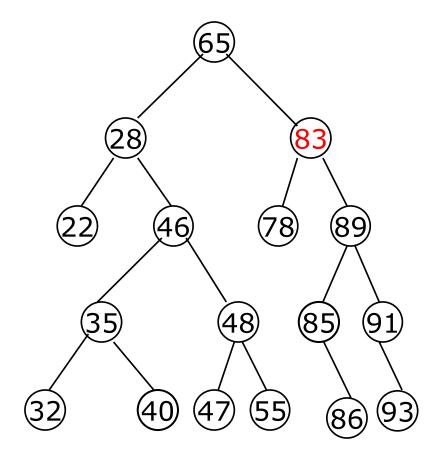
CS 103 3

BST

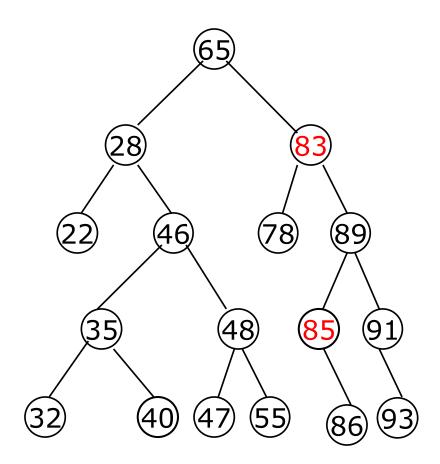
```
Write a program to insert a new node to Binary Search Tree (BST)
Main() {
  rinsertBST(root, val){
rinsertBST(node, val) {
    if (node.val < val ) {
              if (node.right == null) { insert .....; return; }
              else { return rinsertBST(node.right, val); }
   if (node.val > val) {
             if (node.left == null ) { insert .....; return; }
              else { return rinsertBST(node.left, val); }
```

CS 103 4

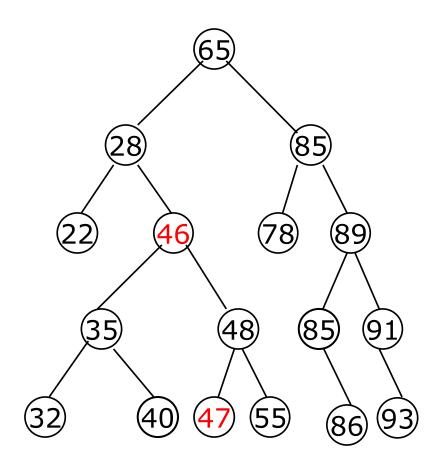
- Program to delete node from BST
- Delete 83



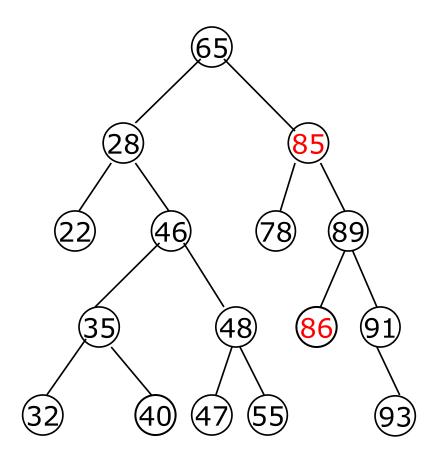
- Program to delete node from BST
- Delete 83



- Program to delete node from BST
- Delete 83



- Program to delete node from BST
- Delete 83



- DFS Depth First Search
 - Visit Node, left subtree, right subtree
- BFS Breadth First Search
 - Visit each node at the same level, then go down a level

Pre Order A B D E H L N I O P C F G J K Q

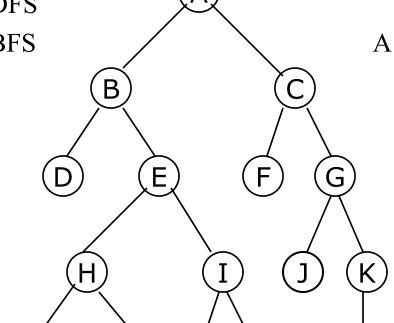
Post order D L N H O P I E B F J Q K G C A Inorder DBLHNEOIPAFCJGQK ABCDEFGHIJKLNOPQB BFS

Pre Order Traversal

Post order

• DFS

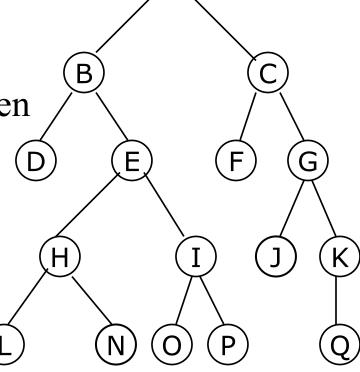
• BFS



ABDEHLNIOPCFGJKQ DLNHOPIEBFJQKGCA

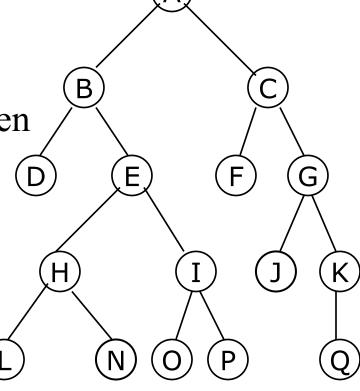
ABCDEFGHIJKLNOPQ

- BFS; not recursive; why?
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while



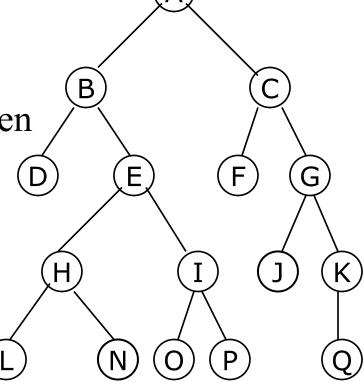
- BFS Visited = {}
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{\}$$



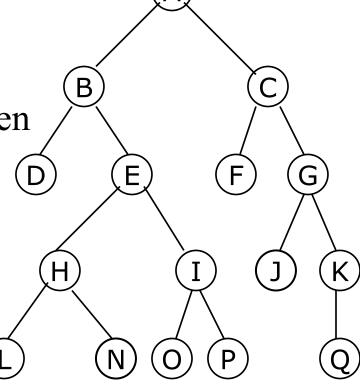
- BFS Visited = {}
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{A\}$$



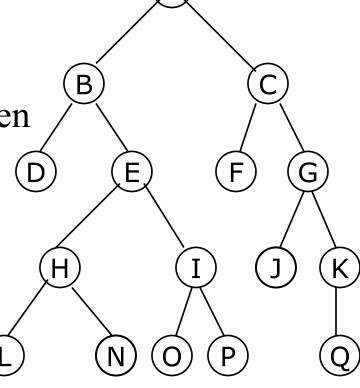
- BFS Visited = $\{A\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{\}$$



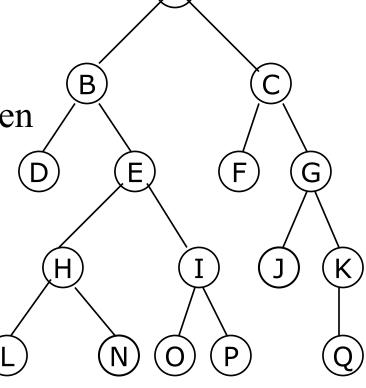
- BFS Visited = $\{A\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{B\}$$



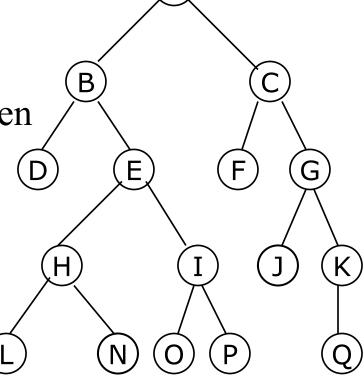
- BFS Visited = $\{A\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{C, B\}$$



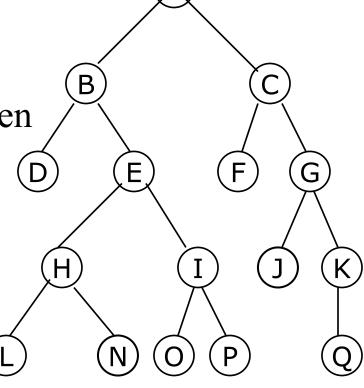
- BFS Visited = $\{A,B\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{C\}$$



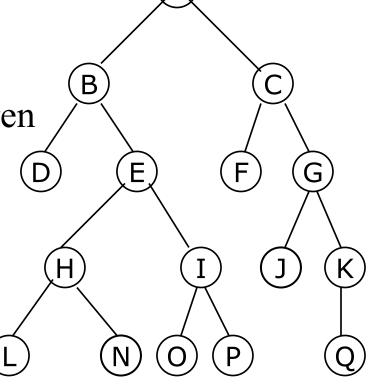
- BFS Visited = $\{A,B\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{D,C\}$$



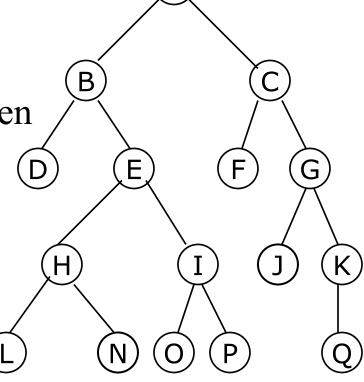
- BFS Visited = $\{A,B\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{E,D,C\}$$



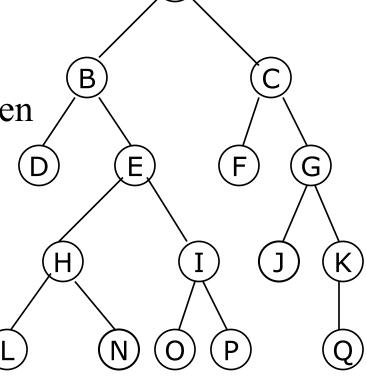
- BFS Visited = $\{A,B,C\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{E,D\}$$



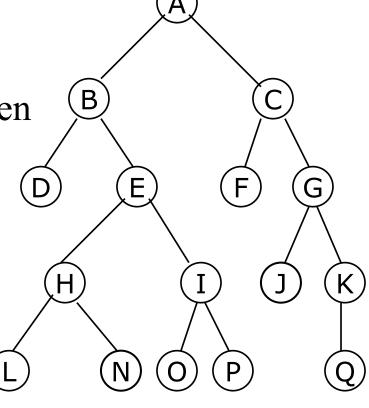
- BFS Visited = $\{A,B,C\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{F,E,D\}$$



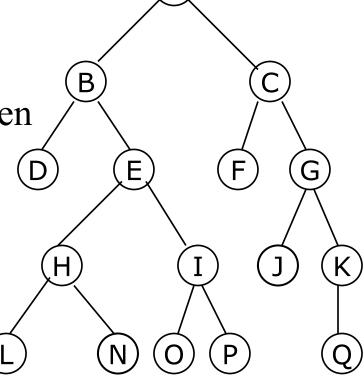
- BFS Visited = $\{A,B,C\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{G,F,E,D\}$$



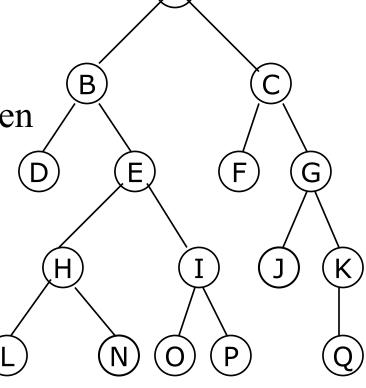
- BFS Visited = $\{A,B,C,D\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{G,F,E\}$$



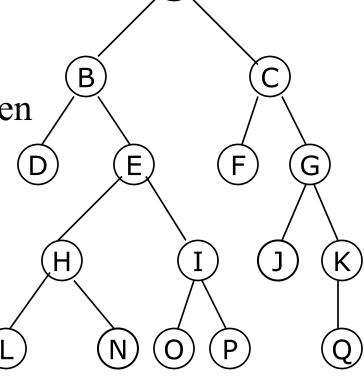
- BFS Visited = $\{A,B,C,D,E\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{G,F\}$$



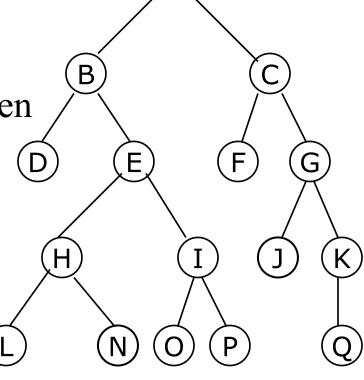
- BFS Visited = $\{A,B,C,D,E\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{I,H,G,F\}$$



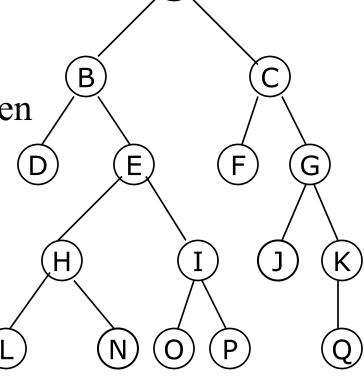
- BFS Visited = $\{A,B,C,D,E,F\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{I,H,G\}$$



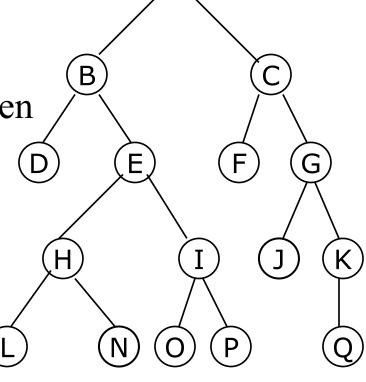
- BFS Visited = $\{A,B,C,D,E,F,G\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{I,H\}$$



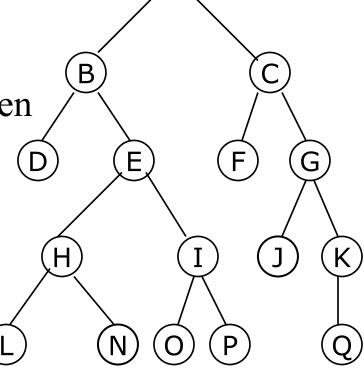
- BFS Visited = $\{A,B,C,D,E,F,G\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{J,I,H\}$$



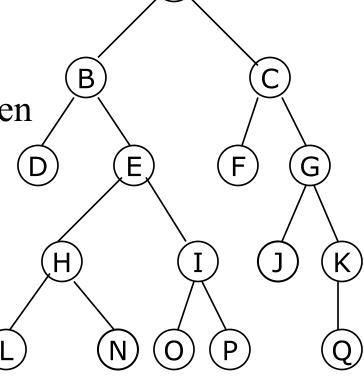
- BFS Visited = $\{A,B,C,D,E,F,G\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{K,J,I,H\}$$



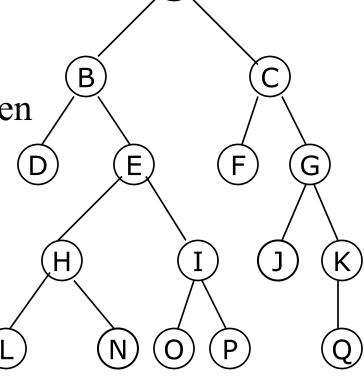
- BFS Visited = $\{A,B,C,D,E,F,G,H\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{K,J,I\}$$



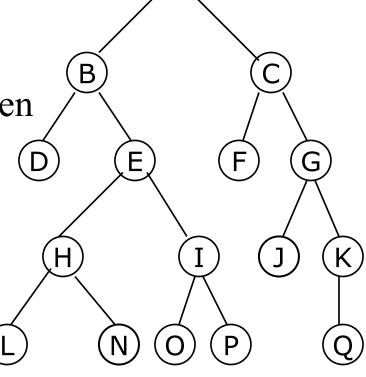
- BFS Visited = $\{A,B,C,D,E,F,G,H\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{L,K,J,I\}$$



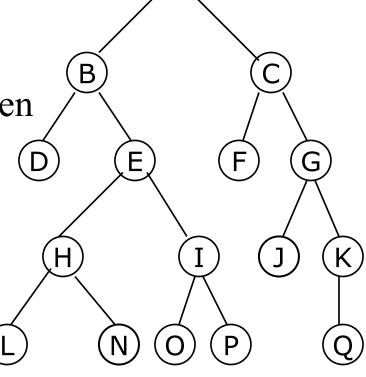
- BFS Visited = $\{A,B,C,D,E,F,G,H\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

 $Q = \{N,L,K,J,I\}$



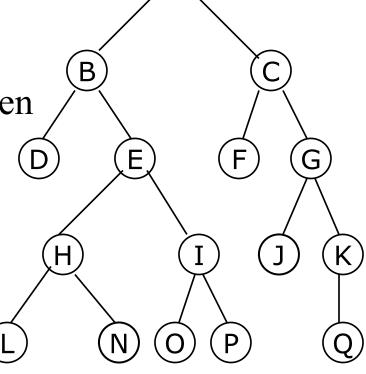
- BFS Visited = $\{A,B,C,D,E,F,G,H,I\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

 $Q = \{N,L,K,J\}$



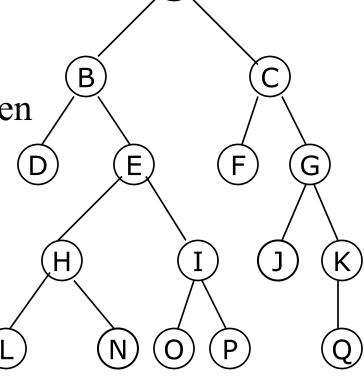
- BFS Visited = $\{A,B,C,D,E,F,G,H,I\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

 $Q = \{O, N, L, K, J\}$



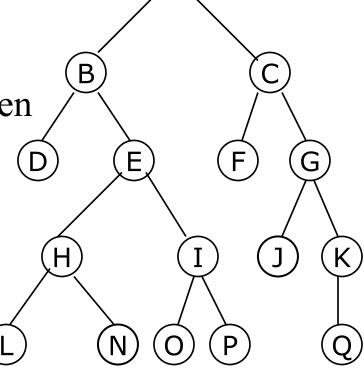
- BFS Visited = $\{A,B,C,D,E,F,G,H,I\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

 $Q = \{P,O,N,L,K,J\}$



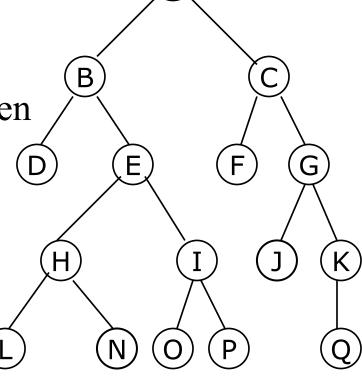
- BFS Visited = $\{A,B,C,D,E,F,G,H,I,J\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

 $Q = \{P,O,N,L,K\}$



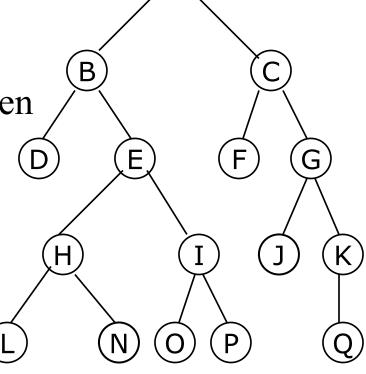
- BFS Visited = $\{A,B,C,D,E,F,G,H,I,J,K\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{P,O,N,L\}$$



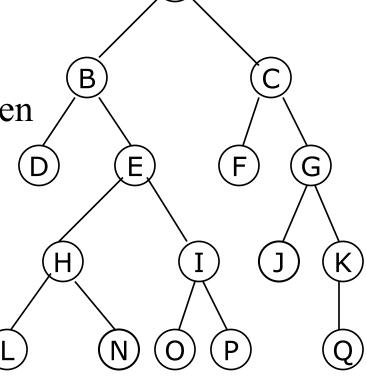
- BFS Visited = $\{A,B,C,D,E,F,G,H,I,J,K\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{Q,P,O,N,L\}$$



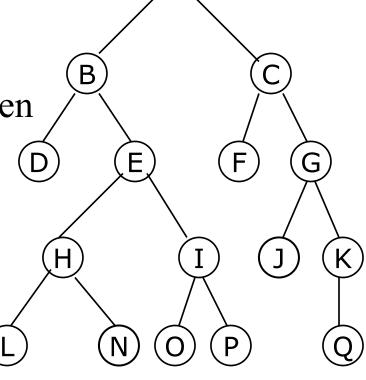
- BFS Visited = $\{A,B,C,D,E,F,G,H,I,J,K,L\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

 $Q = \{Q,P,O,N\}$



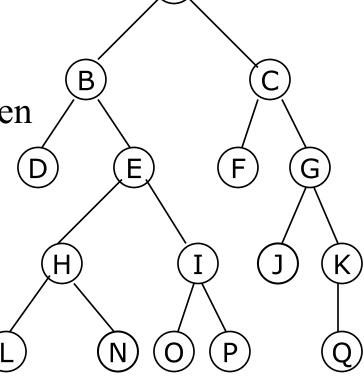
- BFS; Visited = {A,B,C,D,E,F,G,H,I,J,K,L,N}
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{Q,P,O\}$$



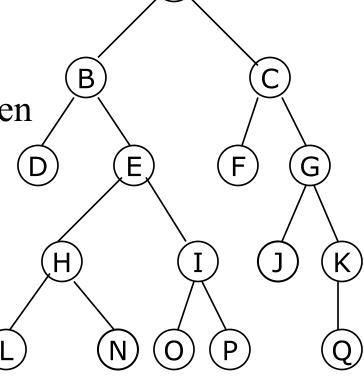
- BFS; Visited = $\{A,B,C,D,E,F,G,H,I,J,K,L,N,O\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{Q,P\}$$



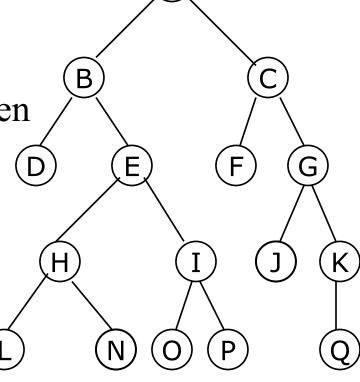
- BFS; Visited = {A,B,C,D,E,F,G,H,I,J,K,L,N,O,P}
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{Q\}$$



- BFS; $Visit = \{A,B,C,D,E,F,G,H,I,J,K,L,N,O,P,Q\}$
 - Enqueue root
 - While Q not empty
 - Dequeue
 - Enqueue all children
 - End while

$$Q = \{\}$$

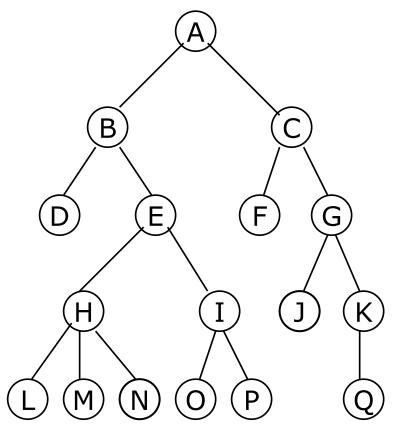


Trees

- Tree Traversal
 - Pre Order
 - Post Order
 - inorder
 - DFS
 - BFS

Trees

- Tree Traversal
 - Pre Order
 - Post Order
 - DFS
 - BFS



Representing Trees

Linked list Based representation

```
Node {
int Data;
Node *leftChild;
Node *rightSibling;
Node *parent;
}
```

regular trees

- Inserting a node .. How to specify
- Program to insert a node
- Program to find a key?

regular trees

• Tree traversal – modify the binary tree traversal.