Question 5

Edward is a probabilistic modeling library built on top of TensorFlow and written in python. Edward's design reflects an iterative process pioneered by Edward Box:

- Build a model of a phenomenon. The model consists of probability distributions, observed data, and graphical models.
 - The data can be preloaded, fed into the program during runtime using TensorFlow placeholders, or directly read from files in case of large size.
 - A probabilistic model is a joint distribution p(x, z) of data x and latent variables z. Random variables are generated on the fly when the graph is initiated.
- Make inferences about the model given the data. Edward has many inference algorithms, including variational and black-box inference, Markov Chain Monte Carlo(MCMC), and a symbolic library in production, which will help in exact inference with symbolic probability distributions and closed form solutions.
- Criticize the model's fit to the data.

 Edward explores model criticism using point estimates of latent variables, and posterior predictive checks

In the following section, we use Edward to model data using end-to-end Bayesian linear regression, using weight \boldsymbol{w} and intercept \boldsymbol{b}

$$p(\boldsymbol{w}) = \mathcal{N}(\boldsymbol{w}|\boldsymbol{0}, \sigma_w^2 \boldsymbol{I})$$

$$p(b) = \mathcal{N}(b|0, \sigma_b^2)$$

$$p(\boldsymbol{y}|\boldsymbol{w}, b, \boldsymbol{X}) = \prod_{n=1}^{N} \mathcal{N}(y_n|\boldsymbol{x}_n^T \boldsymbol{w} + b, \sigma_y^2)$$

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Fixing \sigma_w, \sigma_b, \sigma_y = 1,
import numpy as np
import edward as ed
import tensorflow as tf
#Import the Normal distribution
from edward.models import Normal
N = 40 #Number of data points
D = 10 #Number of features
#Initializing variables using TensorFlow variables and placeholders, defining models
X = tf.placeholder(tf.float32, [N, D])
w = Normal(mu=tf.zeros(D), sigma=tf.ones(D))
b = Normal(mu=tf.zeros(1), sigma=tf.ones(1))
y = Normal(mu=ed.dot(X, w) + b, sigma=tf.ones(N))
#Building a toy dataset
def build_toy_dataset(N, w, noise_std=0.1):
 D = len(w)
 x = np.random.randn(N, D).astype(np.float32)
  y = np.dot(x, w) + np.random.normal(0, noise_std, size=N)
 return x, y
w_true = np.random.randn(D)
X_train, y_train = build_toy_dataset(N, w_true)
X_test, y_test = build_toy_dataset(N, w_true)
#Inference part - using Variational Inference
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qw = Normal(mu=tf.Variable(tf.random_normal([D])),
            sigma=tf.nn.softplus(tf.Variable(tf.random_normal([D])))) #Initializing required w with
            #a random mean and diagonal covariance matrix.
qb = Normal(mu=tf.Variable(tf.random_normal([1])),
            sigma=tf.nn.softplus(tf.Variable(tf.random_normal([1])))) #Initializes the bias
            #with random mean and variance
#Run Variational Inference using Kullback-Leibler divergence, using a default of 500 iterations.
inference = ed.KLqp({w: qw, b: qb}, data={X: X_train, y: y_train}) #Data fed into dicts into the
                                                                   #KLqp inference method of Edward
inference.run() #Initializes the back-end TensorFlow graph
#Criticism part - We test our model by point based evaluations on test data.
#Form the Posterior predictive distribution
y_post = Normal(mu=ed.dot(X, qw.mean()) + qb.mean(), sigma=tf.ones(N))
#We can evaluate various point based quantities using PPD.
print("Mean squared error on test data:")
print(ed.evaluate('mean_squared_error', data={X: X_test, y_post: y_test}))#Prints a value of 0.012
```