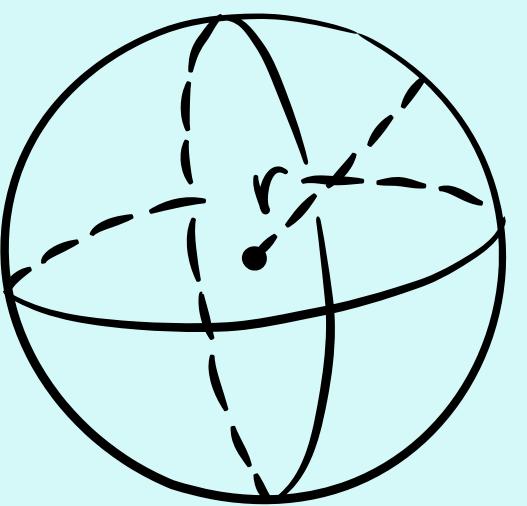


INTRODUCTION

Correlation is a statistical method used to measure the strength and direction of the relationship between two variables, commonly applied in mathematics, statistics, economics, and research.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



$$V = \frac{4}{3} \pi r^3$$

CONCEPT OF REGRESSION

- Regression shows the functional relationship between variables.
- Simple linear regression uses one independent variable (x) to predict dependent variable (y).

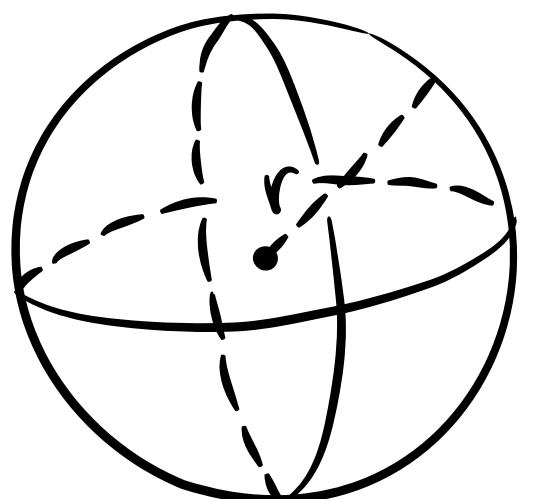
General equation:

$$\hat{y} = a + bx$$

- a = intercept
- b = slope (rate of change)

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



$$V = \frac{4}{3} \pi r^3$$

FORMULA OF REGRESSION

To compute regression coefficients:

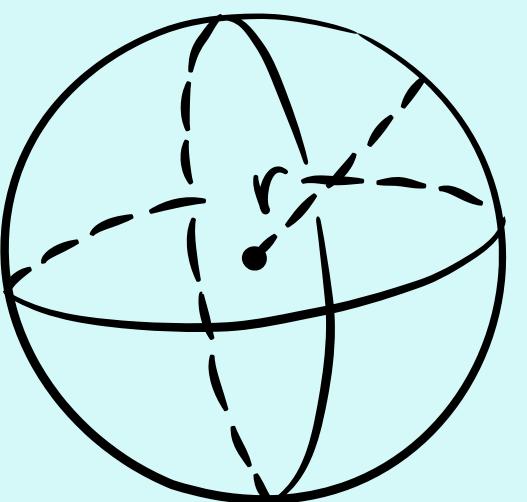
- $b = [n\sum xy - (\sum x)(\sum y)] \div [n\sum x^2 - (\sum x)^2]$
- $a = \bar{y} - b(\bar{x})$

Regression equation:

- $\hat{y} = a + bx$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



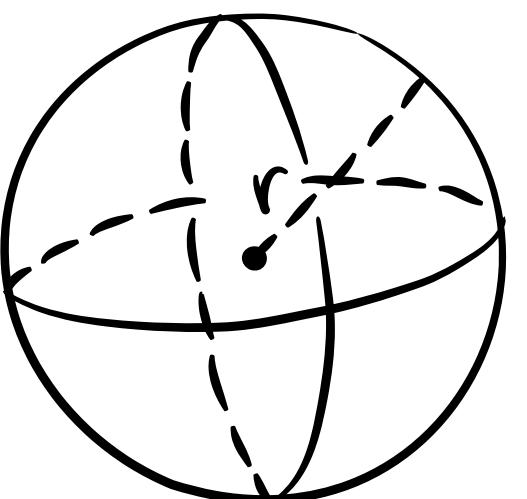
$$V = \frac{4}{3} \pi r^3$$

PROCESS OF REGRESSION

- Calculate Σx , Σy , Σxy , Σx^2 .
- Find slope b .
- Find intercept a .
- Form regression equation $\hat{y} = a + bx$.
- Use equation to predict values of y given x .

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



$$V = \frac{4}{3} \pi r^3$$

CONCEPT OF CORRELATION

Correlation measures how strongly two variables are related.

Types:

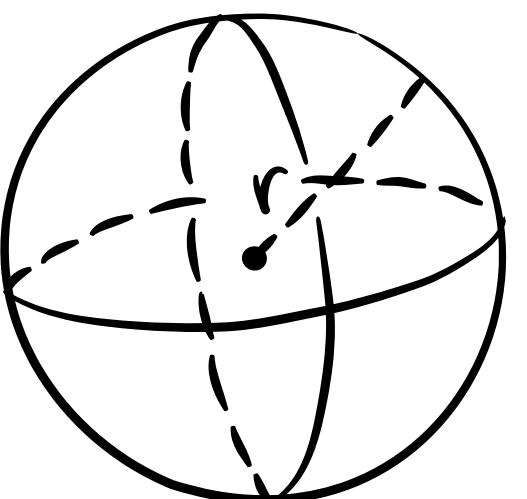
- Positive correlation → both variables increase together.
- Negative correlation → one increases while the other decreases.
- Zero correlation → no relationship.

Values of correlation coefficient (r):

- $r = +1 \rightarrow$ perfect positive correlation
- $r = -1 \rightarrow$ perfect negative correlation
- $r = 0 \rightarrow$ no correlation

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



$$V = \frac{4}{3} \pi r^3$$

FORMULA OF CORRELATION

Pearson's Correlation Coefficient (r):

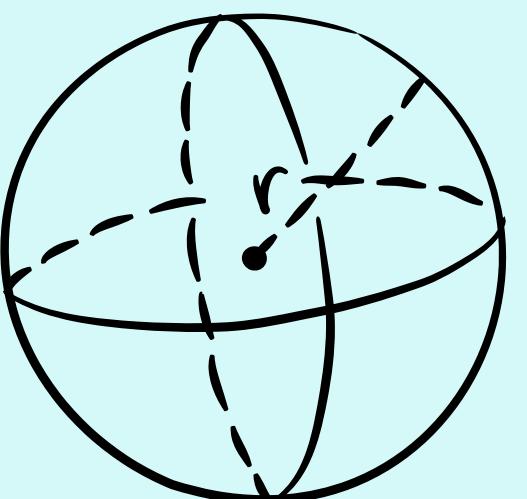
$$\bullet r = \frac{\sum[(x - \bar{x})(y - \bar{y})]}{\sqrt{[\sum(x - \bar{x})^2] [\sum(y - \bar{y})^2]}}$$

Alternate formula:

$$\bullet r = \frac{[n\sum xy - (\sum x)(\sum y)]}{\sqrt{[(n\sum x^2 - (\sum x)^2)(n\sum y^2 - (\sum y)^2)]}}$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



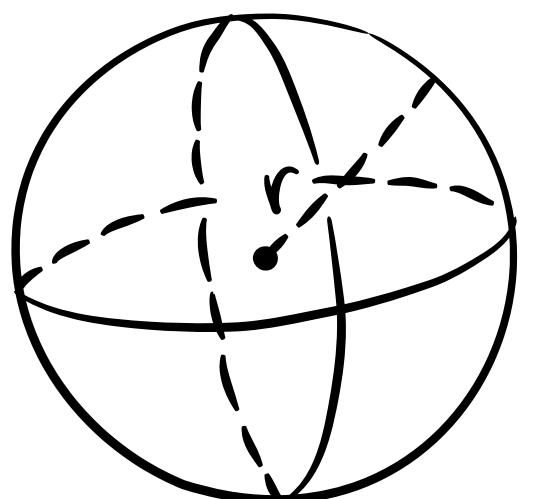
$$V = \frac{4}{3} \pi r^3$$

PROCESS OF CORRELATION

- Collect paired data (x, y).
- Calculate $\Sigma x, \Sigma y, \Sigma x^2, \Sigma y^2, \Sigma xy$.
- Substitute into the formula.
- Solve numerator and denominator.
- Compute r .
- Interpret: strength and direction of relationship.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



$$V = \frac{4}{3} \pi r^3$$

EXAMPLE OF THE PROBLEM

Data:

- $x = [2, 4, 6, 8, 10]$
- $y = [3, 5, 7, 9, 11]$

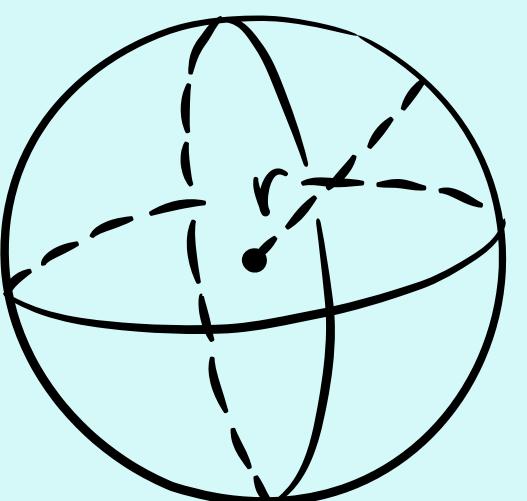
Correlation: $r = 1 \rightarrow$ perfect positive correlation.

Regression:

- $b = 1, a = 1$
- Equation: $\hat{y} = 1 + 1x = x + 1$
- If $x = 12, \hat{y} = 13$.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



$$V = \frac{4}{3} \pi r^3$$

APPLICATION

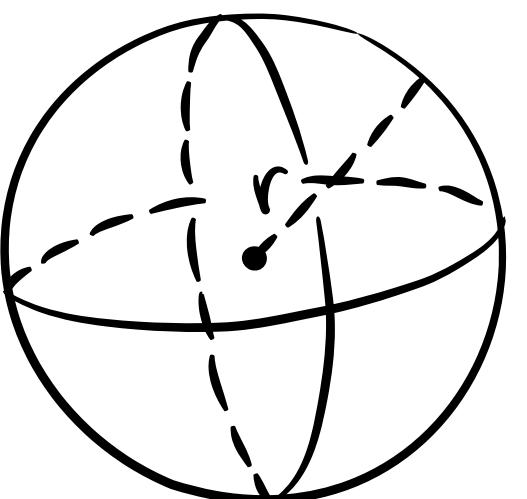
- Correlation: measures association between variables.
- Regression: predicts outcomes and trends.

Fields of use:

- Business → sales prediction
- Economics → income vs. spending
- Science → experimental data modeling
- Education → study hours vs. test scores

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



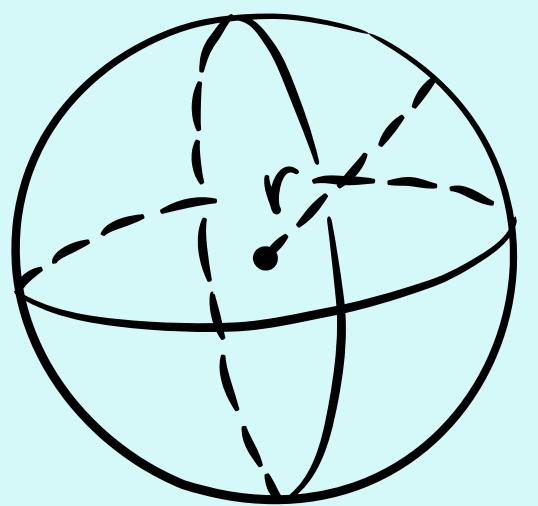
$$V = \frac{4}{3} \pi r^3$$

CRITICAL THINKING

- Correlation does not imply causation.
- Regression builds prediction, but accuracy depends on data quality.
- Example: A high correlation between shoe size and reading skills is due to age, not causation.
- Always check for hidden variables before making conclusions.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



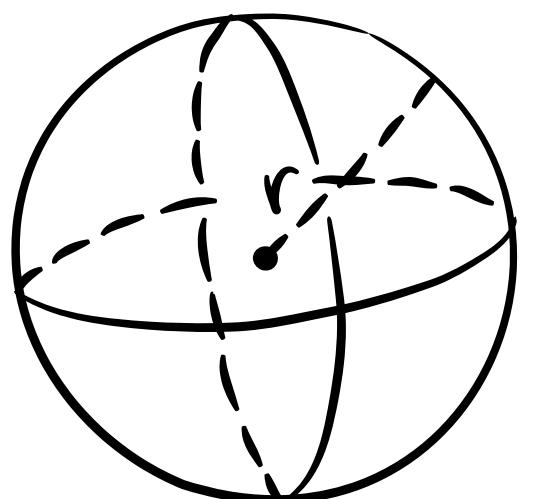
$$V = \frac{4}{3} \pi r^3$$

CONCLUSION

- Correlation explains the strength and direction of relationships.
- Regression provides a predictive model using those relationships.
- Both are powerful tools in mathematics and statistics.
- Correct application leads to better analysis, prediction, and decision-making.

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$y = mx + b$$



$$V = \frac{4}{3} \pi r^3$$