



DeepLearning.AI

Math for Machine Learning

Probability and Statistics - Week 4

W4 Lesson 1



DeepLearning.AI

Confidence Interval

Confidence Interval (Known Standard Deviation)

Confidence Interval - Intuition

Confidence Interval - Intuition

Statistopia

10,000 people

Confidence Interval - Intuition

Statistopia

10,000 people

Estimate μ

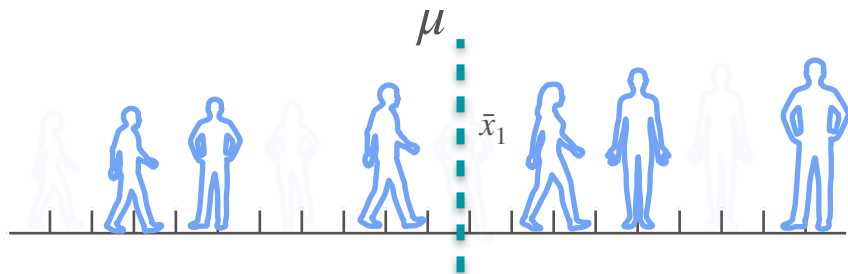
Confidence Interval - Intuition

Statistopia

10,000 people

Estimate μ
(mean height of the population)

Confidence Interval - Intuition

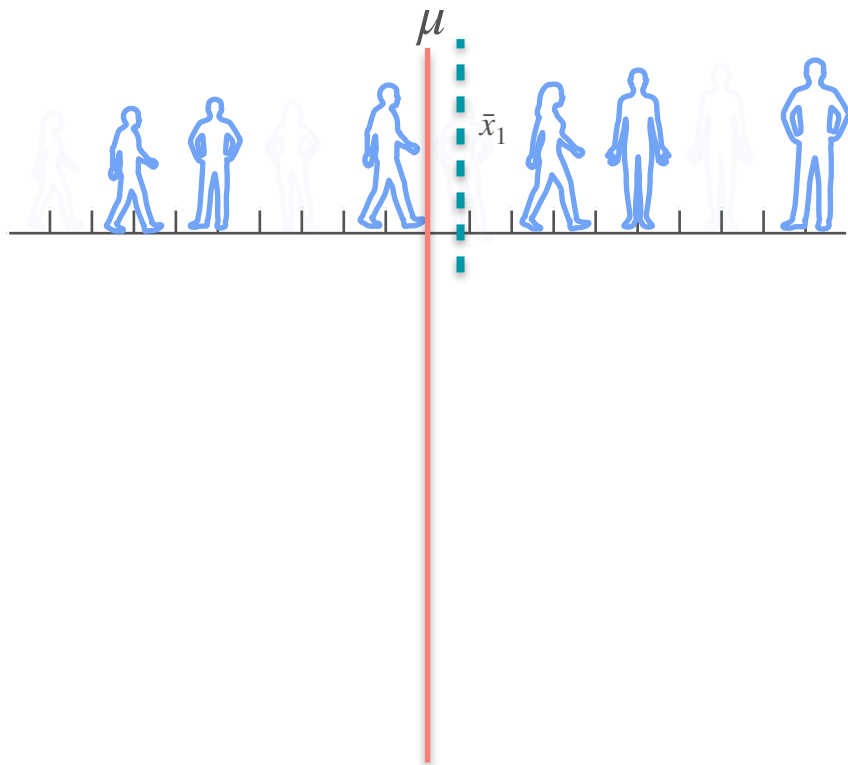


Statistopia

10,000 people

Estimate μ
(mean height of the population)

Confidence Interval - Intuition

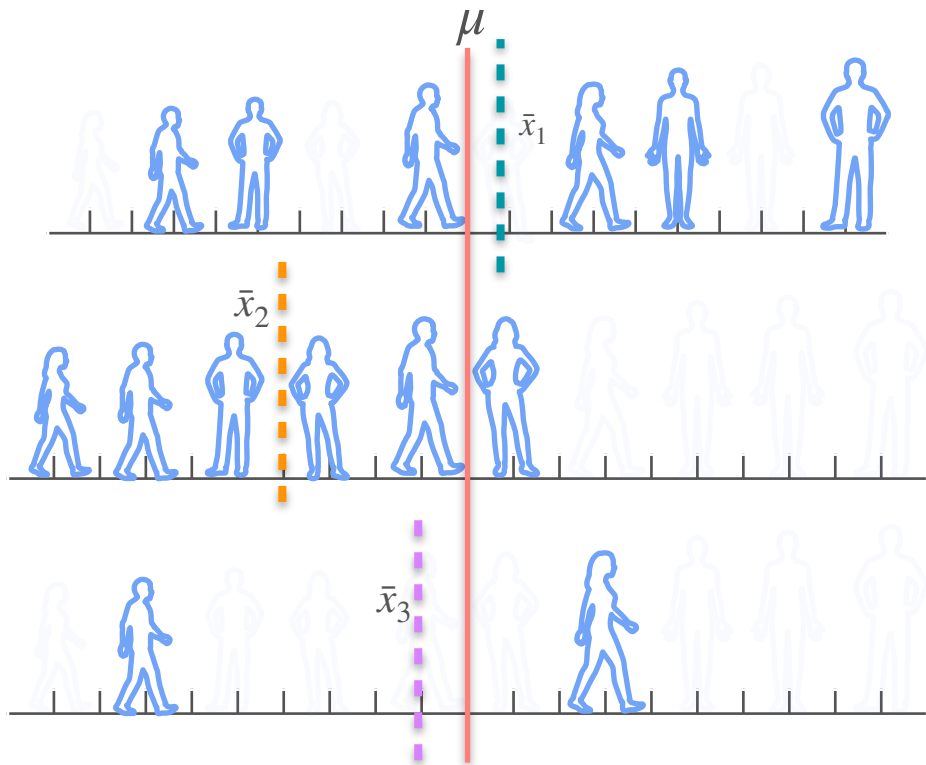


Statistopia

10,000 people

Estimate μ
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Confidence Interval - Intuition

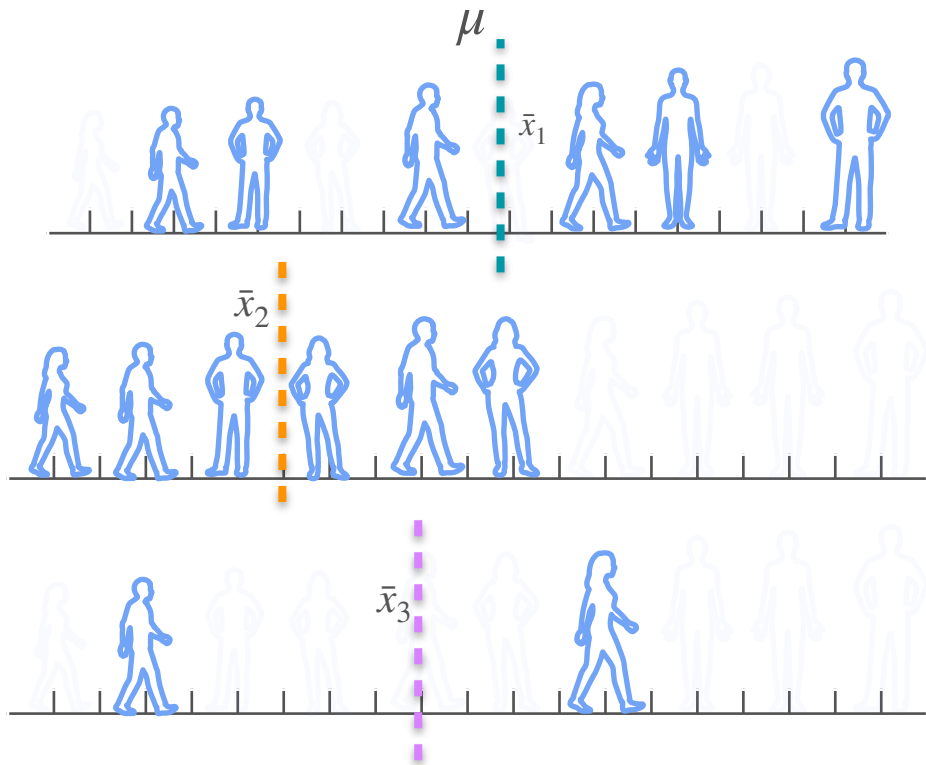


Statistopia

10,000 people

Estimate μ
(mean height of the population)

Confidence Interval - Intuition

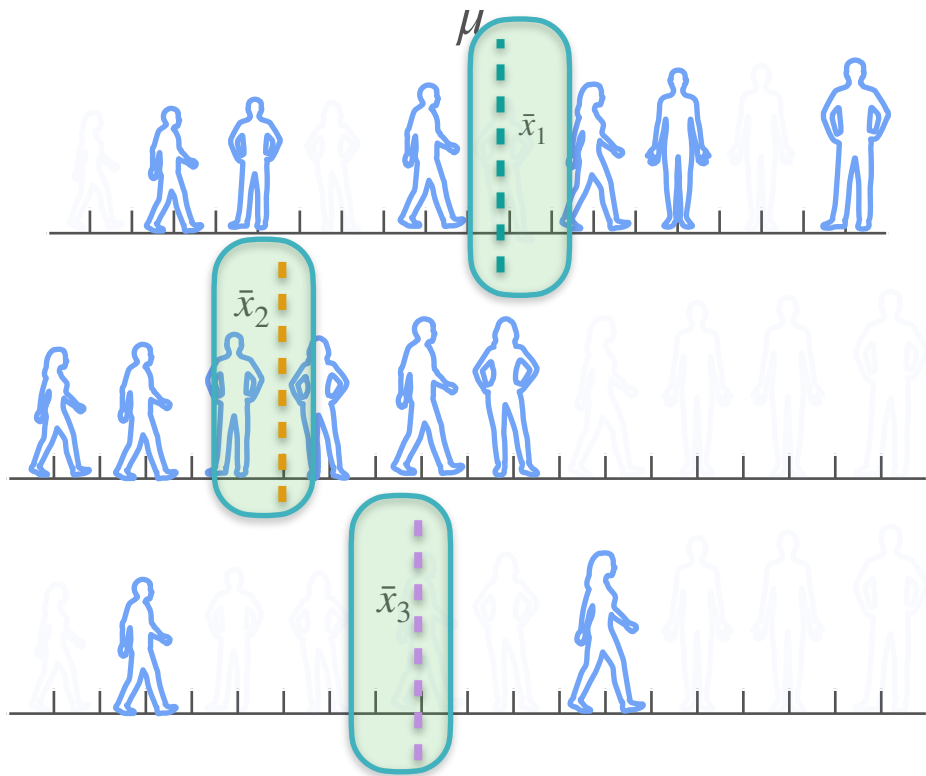


Statistopia

10,000 people

Estimate μ
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Confidence Interval - Intuition



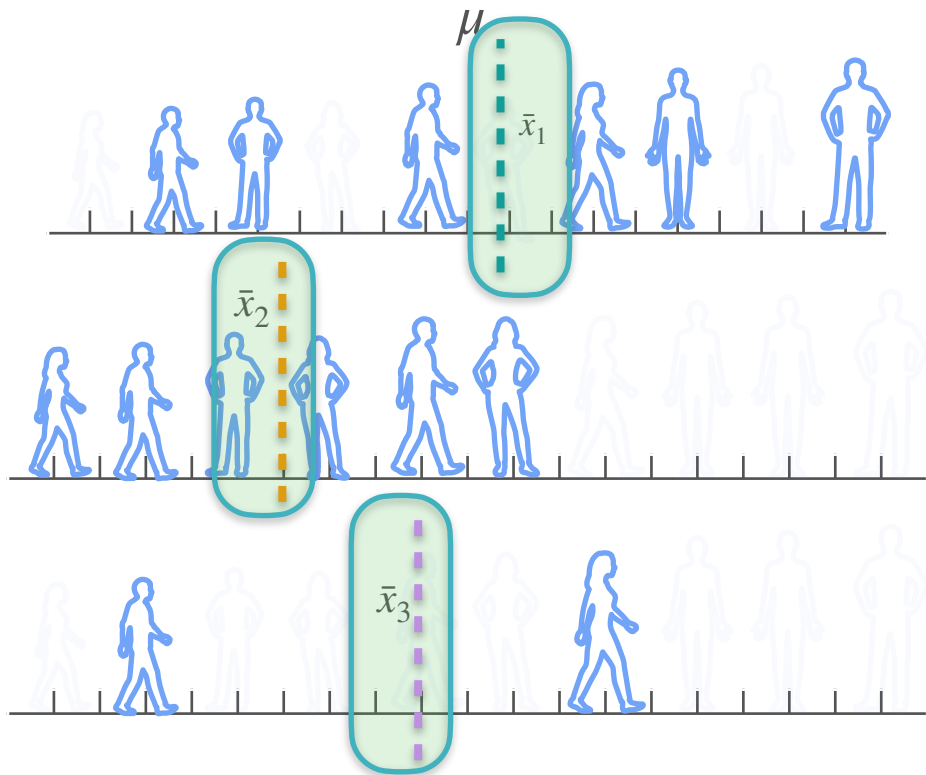
Statistopia

10,000 people

Estimate μ
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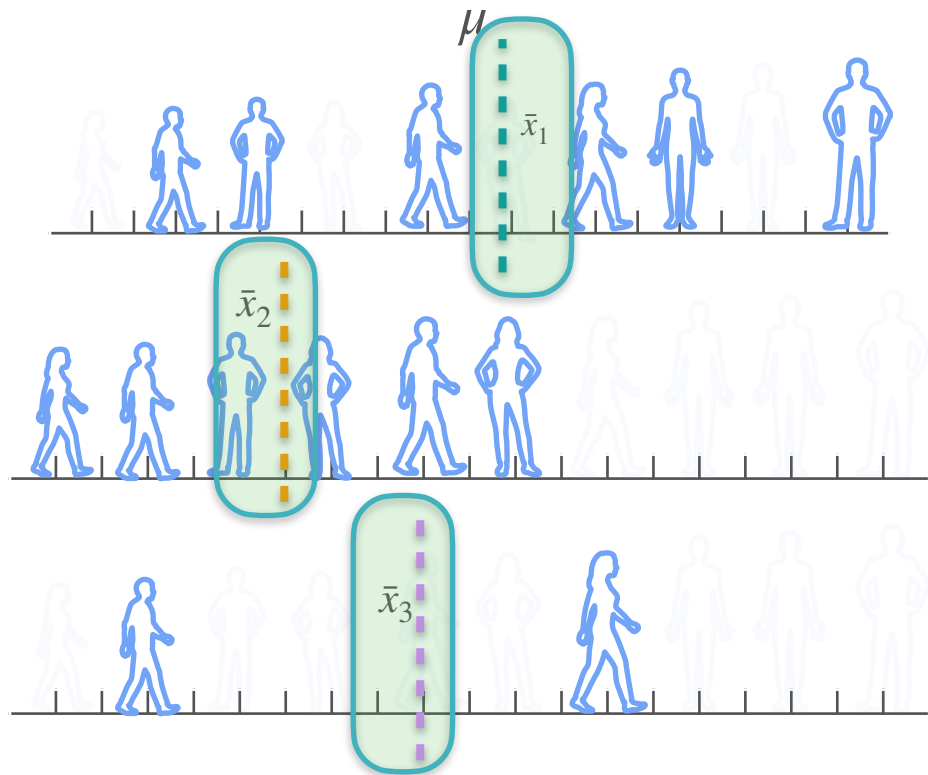
Can you use these sample means with
some degree of certainty?

Confidence Interval - Intuition



Can you use these sample means with some degree of certainty?

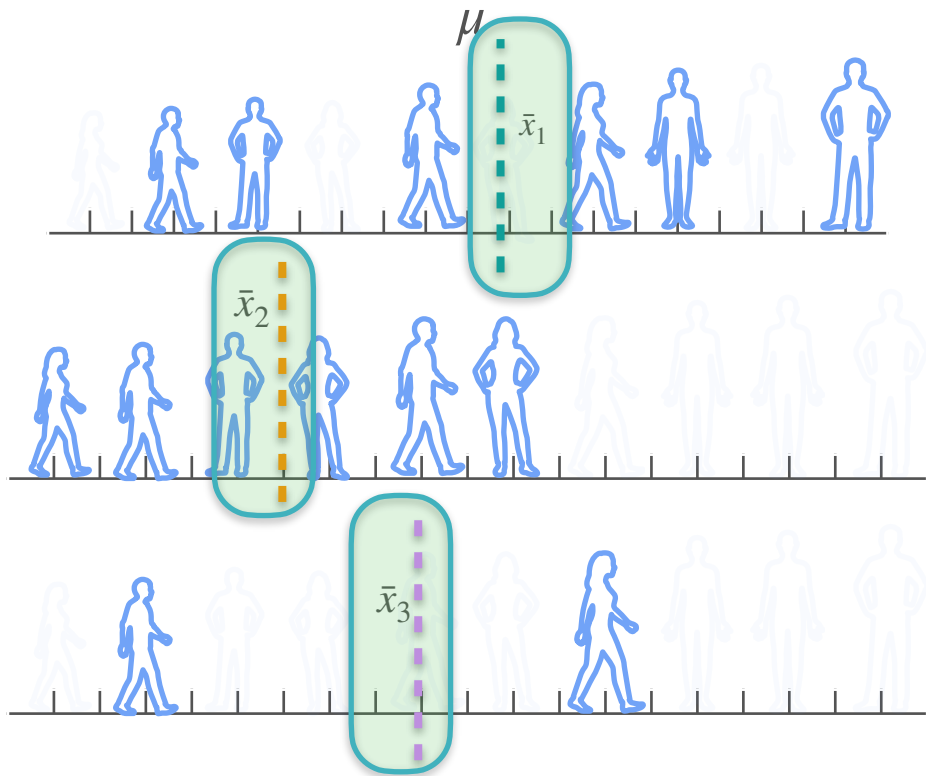
Confidence Interval - Intuition



Can you use these sample means with some degree of certainty?

Confidence Interval

Confidence Interval - Intuition



Can you use these sample means with some degree of certainty?

Confidence Interval

lower limit $< \bar{x} <$ upper limit

Confidence Interval - Intuition

Confidence Interval - Intuition

$$n = 1$$



Confidence Interval - Intuition

$$n = 1$$



$$\bar{x}$$

Confidence Interval - Intuition

$$n = 1$$



$$\bar{x}$$

Central Limit Theorem

Confidence Interval - Intuition

$$n = 1$$

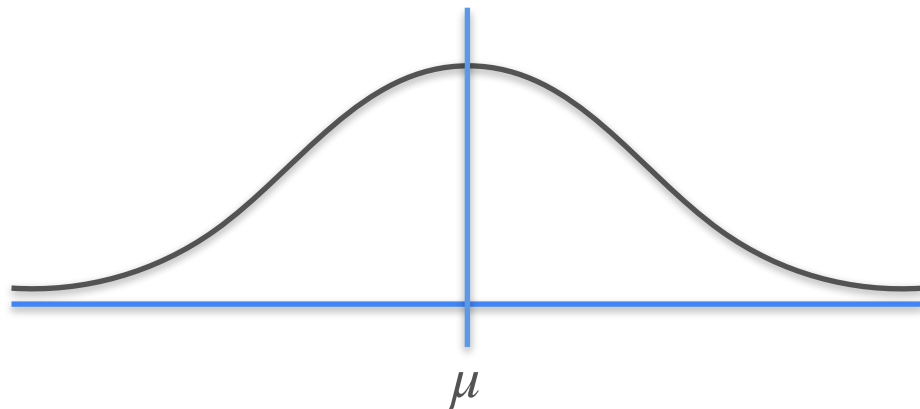


$$\bar{x}$$

Central Limit Theorem

population standard deviation (σ)

$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



Confidence Interval - Intuition

$$n = 1$$

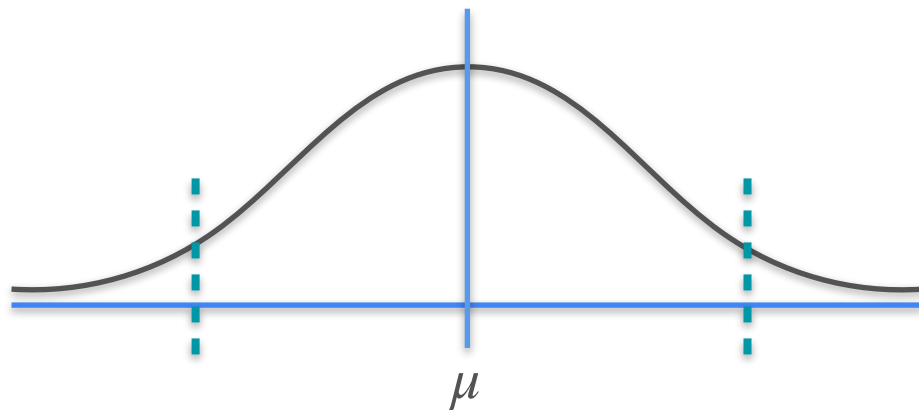


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Central Limit Theorem

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Confidence Interval - Intuition

$$n = 1$$

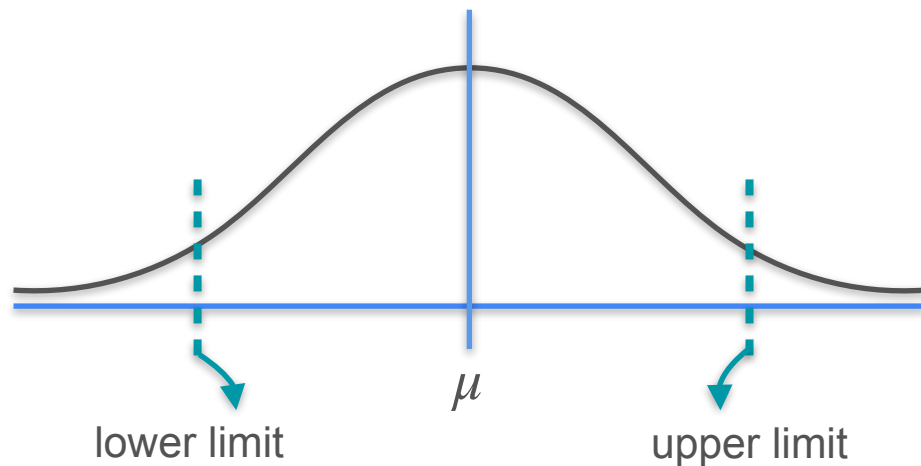


$$\bar{x}$$

Central Limit Theorem

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Confidence Interval - Intuition

$$n = 1$$



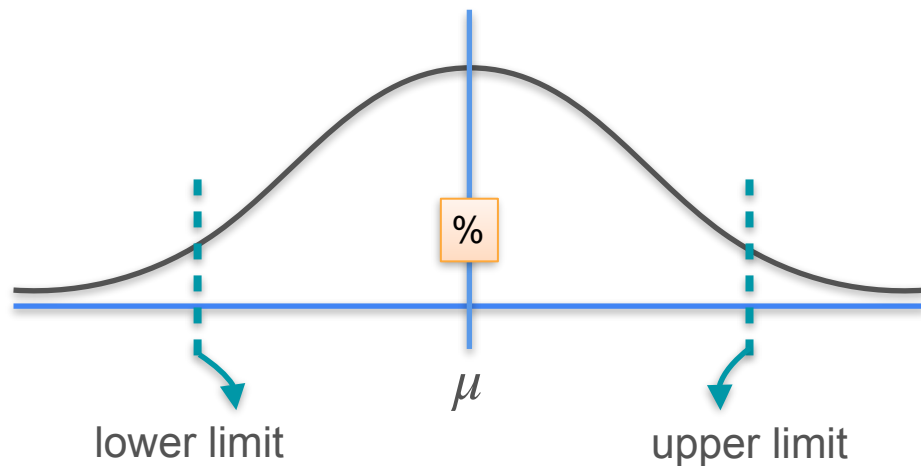
$$\bar{x}$$

%

Central Limit Theorem

population standard deviation (σ)

$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



Confidence Interval - Intuition

$$n = 1$$



$$\bar{x}$$

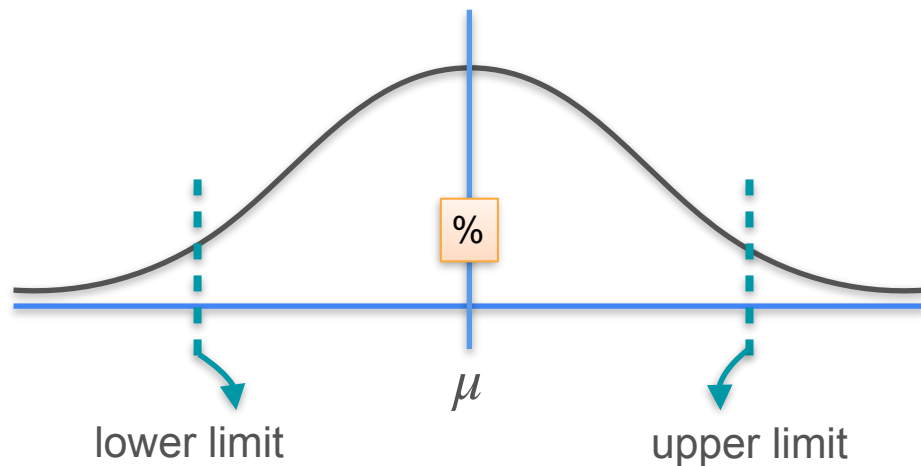
%

α
significance level

Central Limit Theorem

population standard deviation (σ)

$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



Confidence Interval - Intuition

$$n = 1$$



$$\bar{x}$$

α
significance level

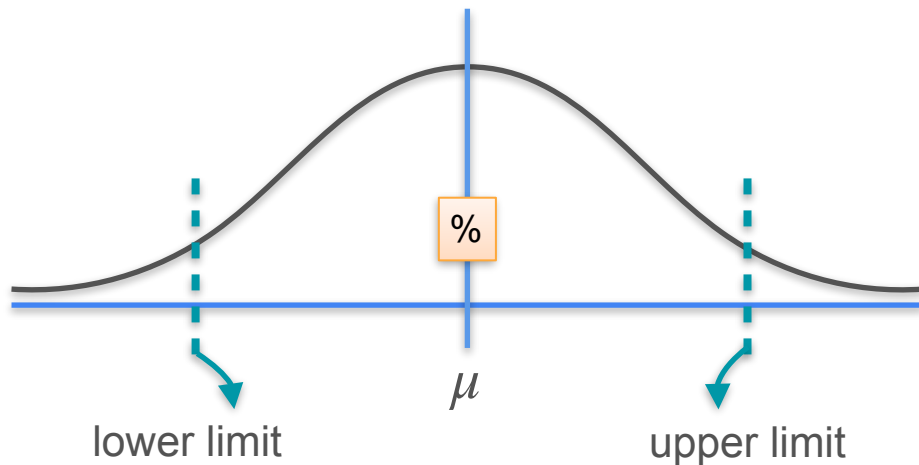
%

$$1 - \alpha$$

Central Limit Theorem

population standard deviation (σ)

$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



Confidence Interval - Intuition

$$n = 1$$



$$\bar{x}$$

Confidence level

%

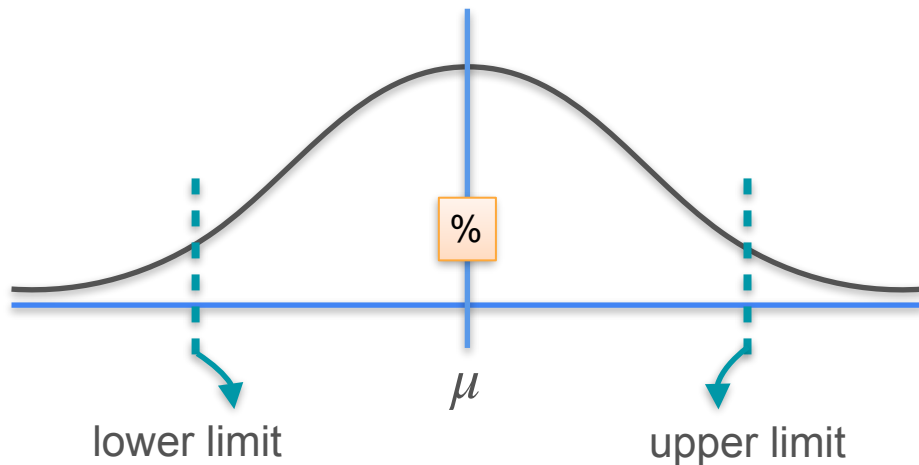
$$1 - \alpha$$

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significance level

Central Limit Theorem

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Confidence Interval - Intuition

$$n = 1$$



$$\bar{x}$$

Confidence level

%

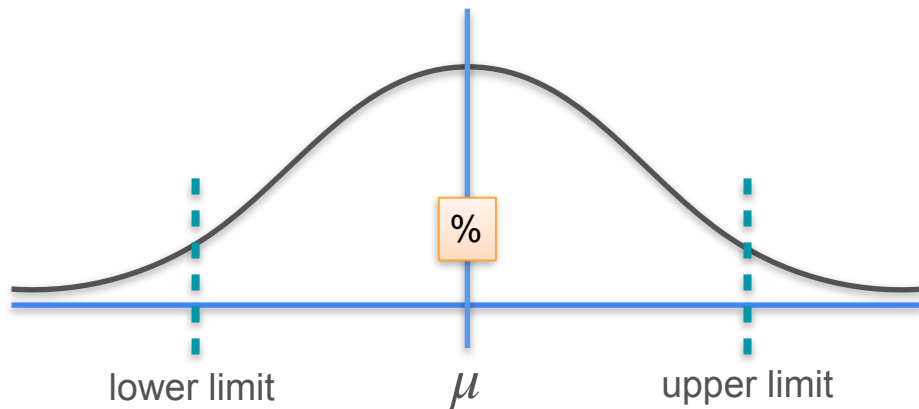
$$1 - \alpha$$

α
significance level

Central Limit Theorem

population standard deviation (σ)

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Confidence Interval - Intuition

$$n = 1$$



$$\bar{x}$$

Confidence level

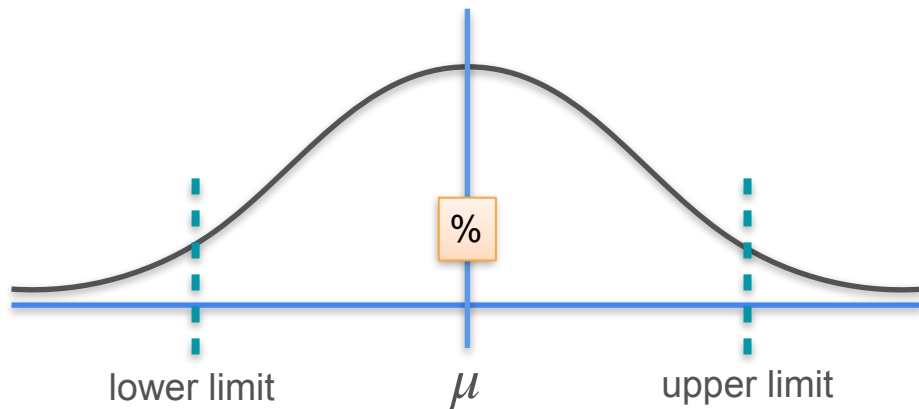
%

$$1 - \alpha$$

Central Limit Theorem

population standard deviation (σ)

$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



$\alpha = 0.05$
significance level

Confidence Interval - Intuition

$$n = 1$$



\bar{x}

Confidence level

%

$$1 - \alpha$$

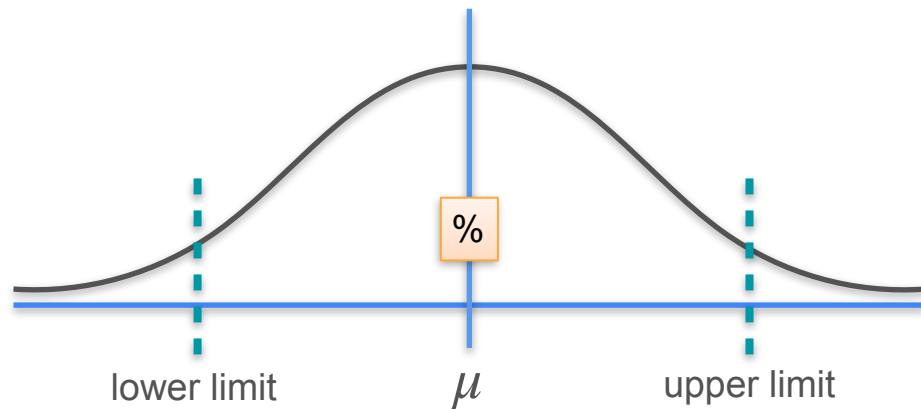
$$1 - 0.05 = 0.95$$

$\alpha = 0.05$
significance level

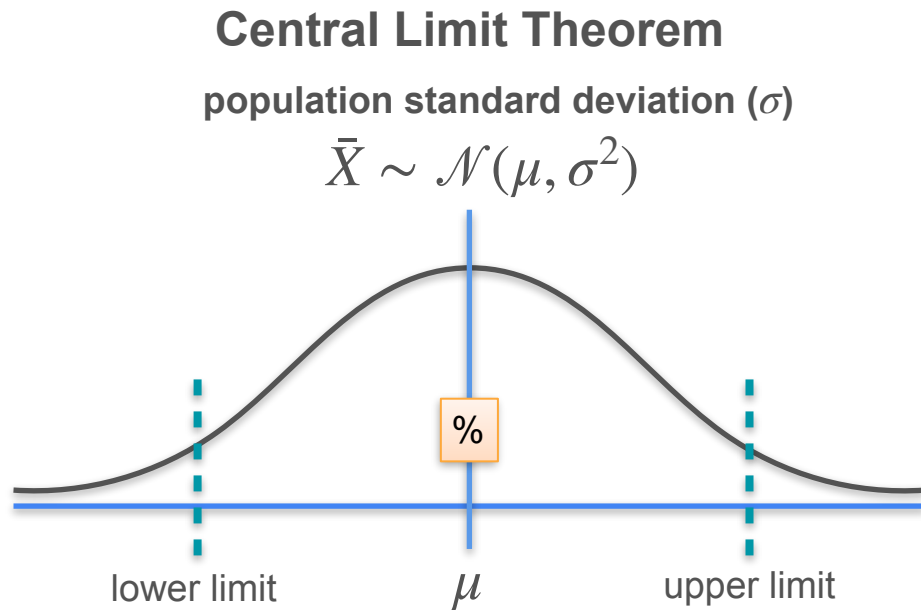
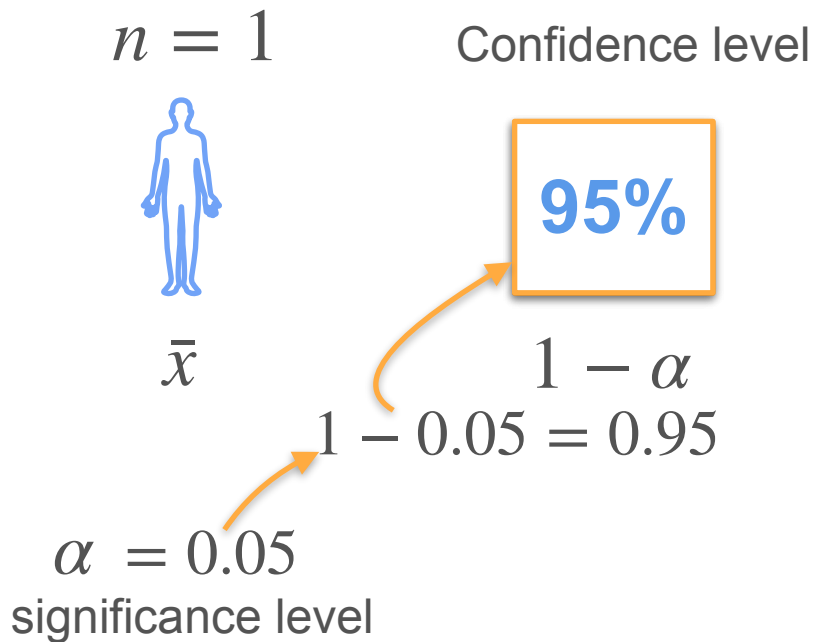
Central Limit Theorem

population standard deviation (σ)

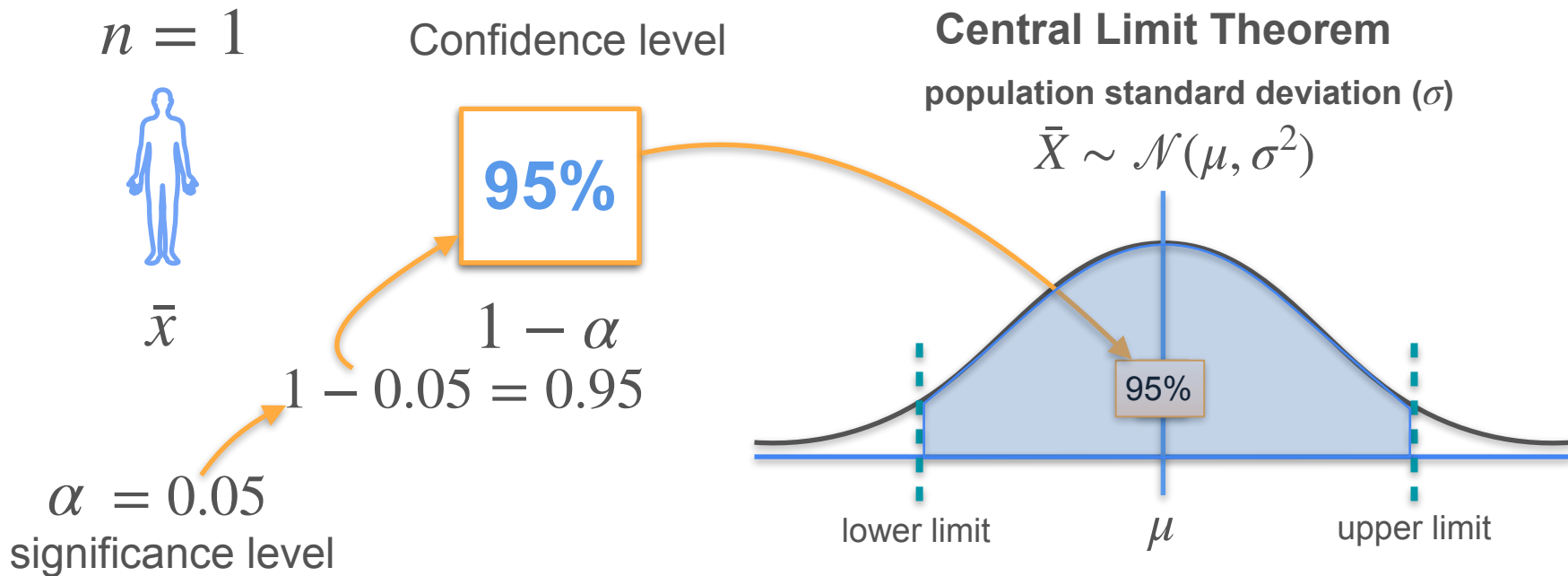
$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



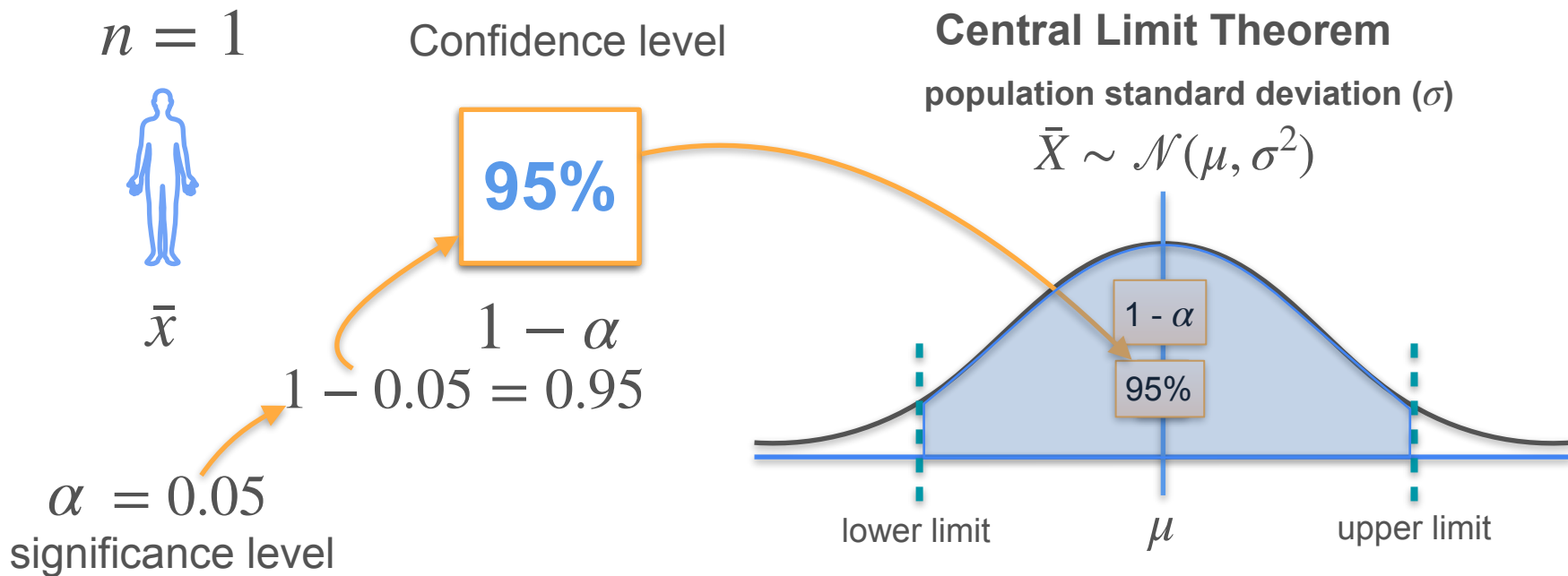
Confidence Interval - Intuition



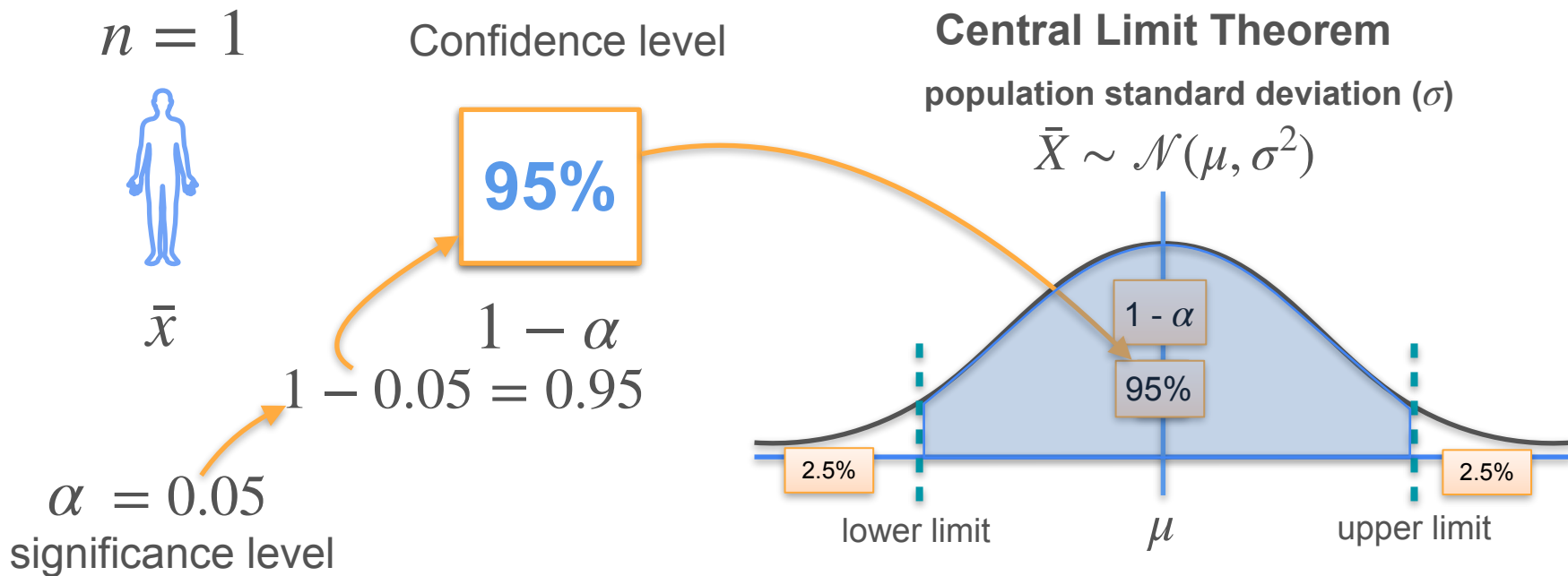
Confidence Interval - Intuition



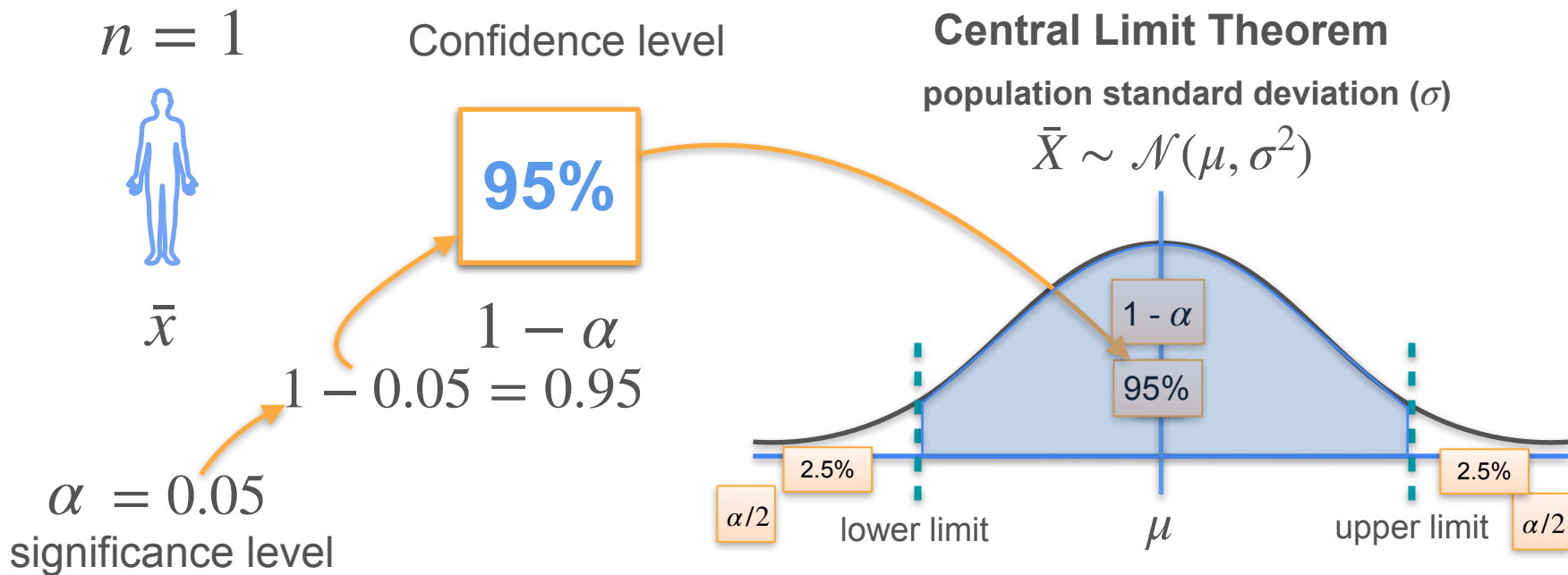
Confidence Interval - Intuition



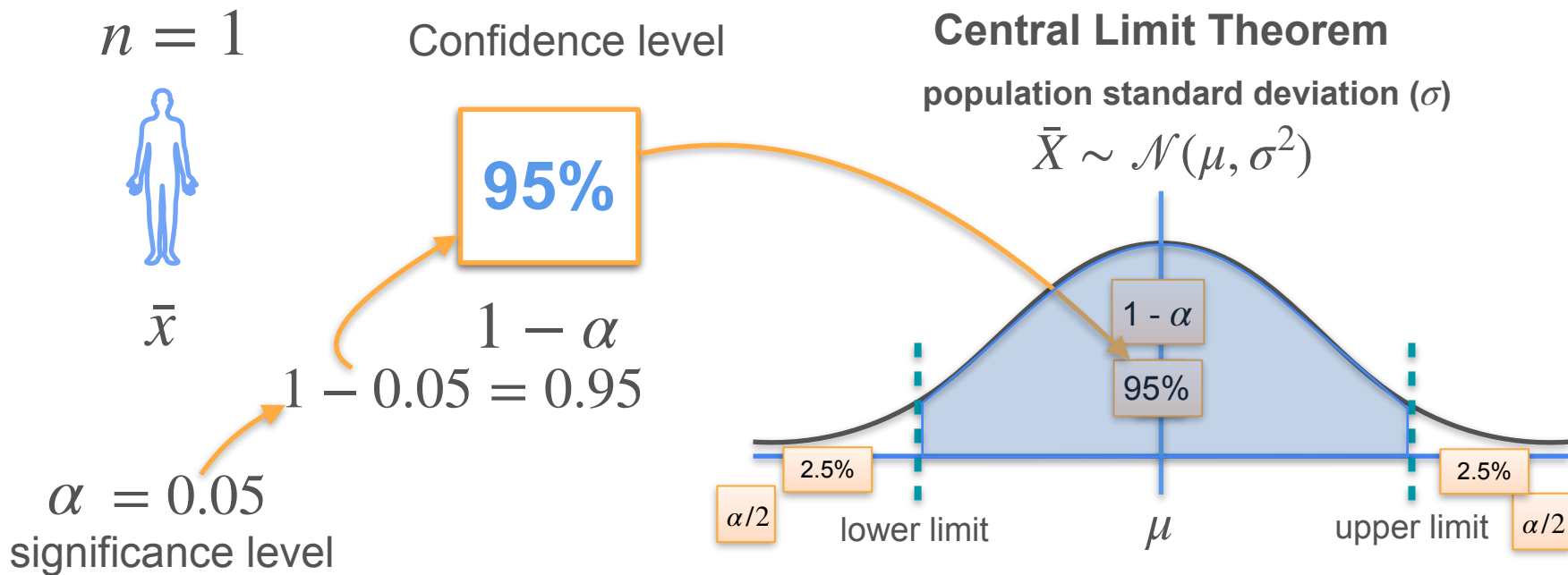
Confidence Interval - Intuition



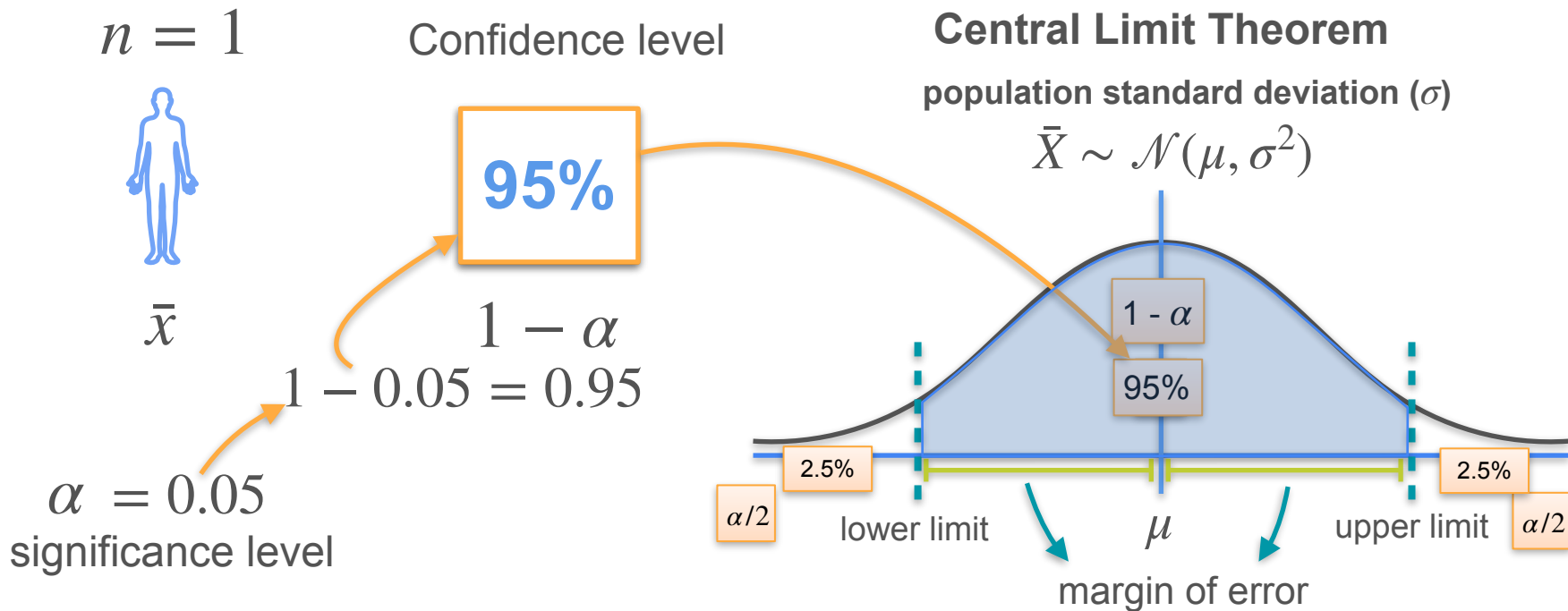
Confidence Interval - Intuition



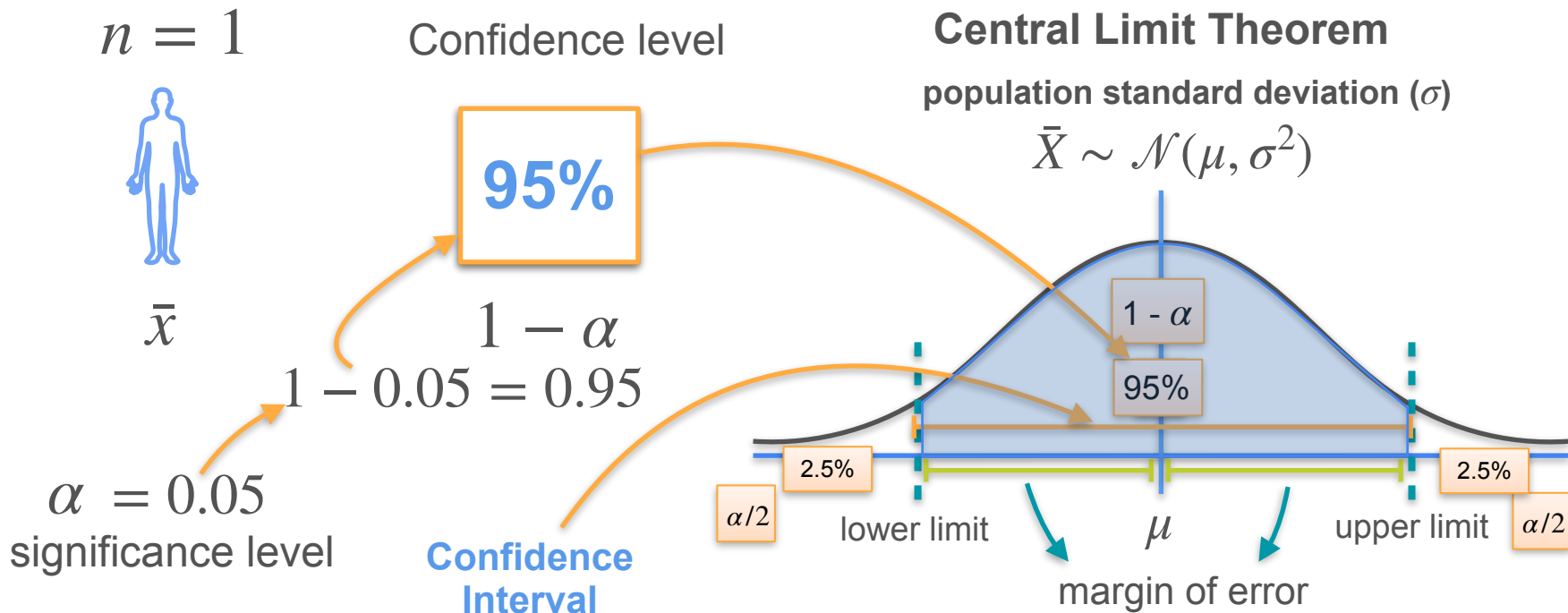
Confidence Interval - Intuition



Confidence Interval - Intuition



Confidence Interval - Intuition



Confidence Interval - Intuition

$$n = 1$$

Known σ

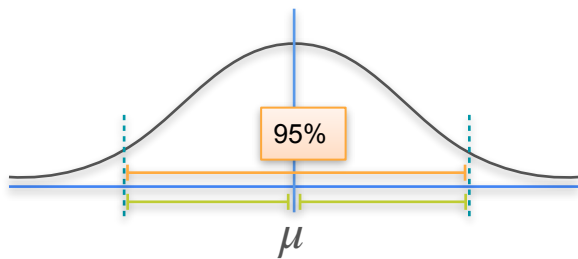
95%

Confidence Interval - Intuition

$$n = 1$$

Known σ

95%



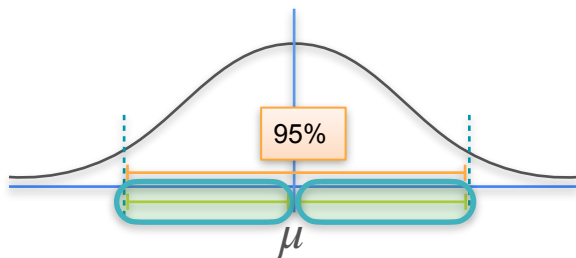
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



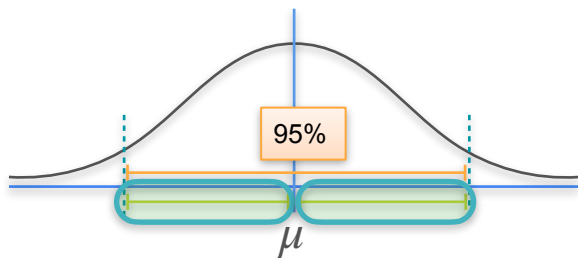
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



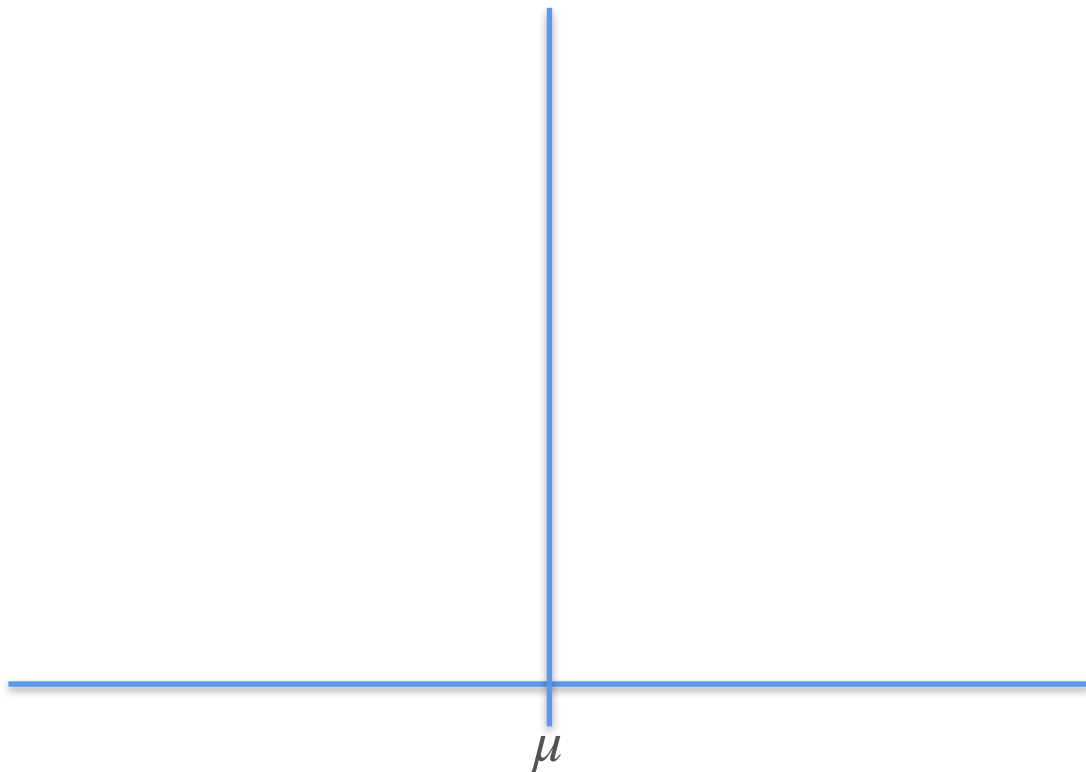
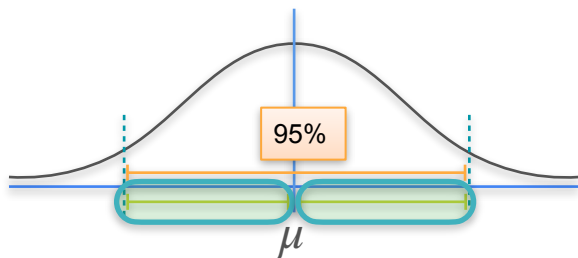
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



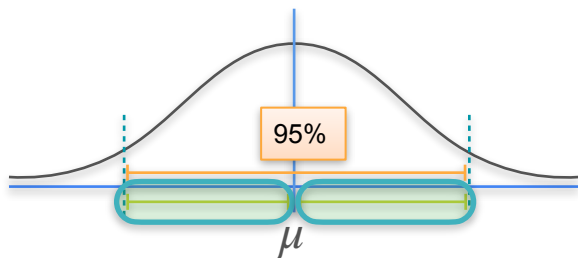
Confidence Interval - Intuition

$$n = 1$$

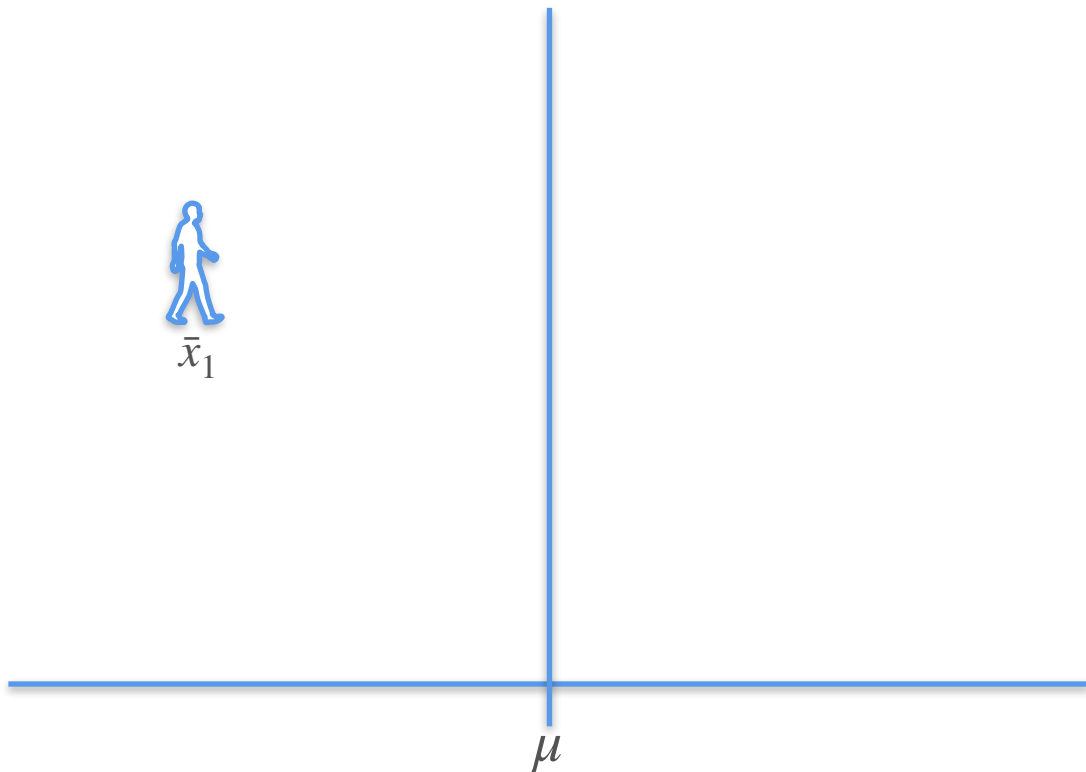
Known σ

95%

Margin of error



\bar{x}_1



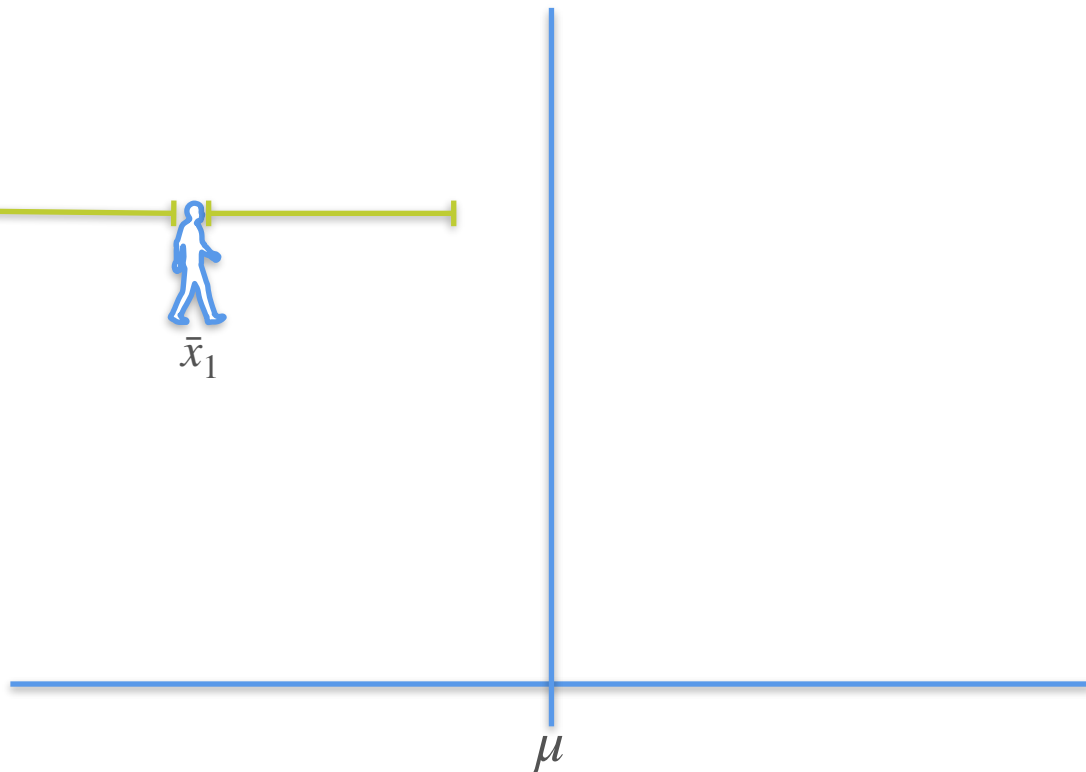
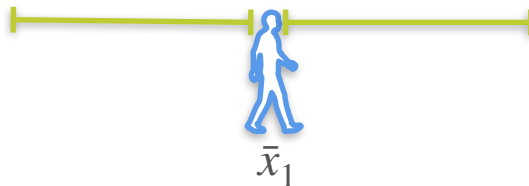
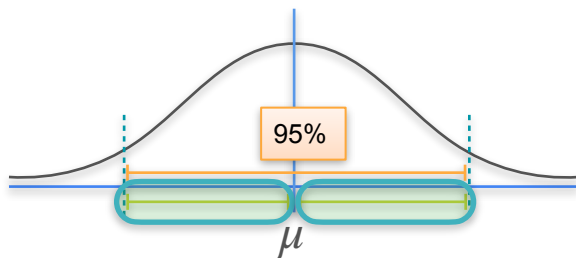
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



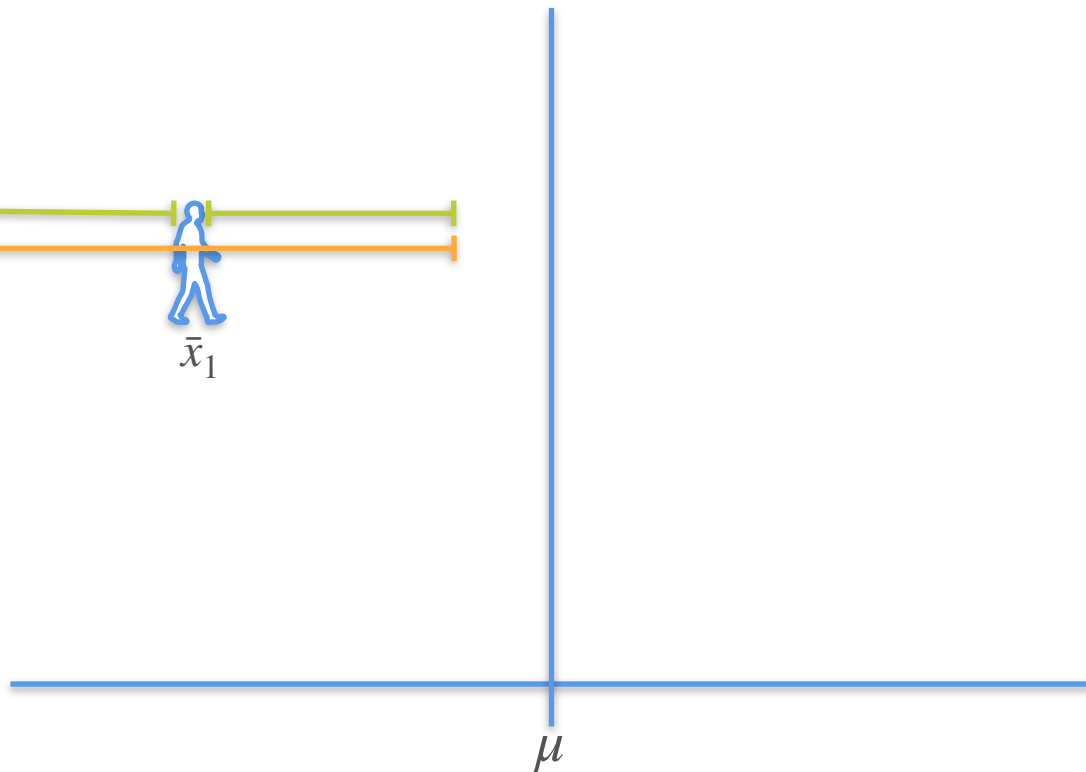
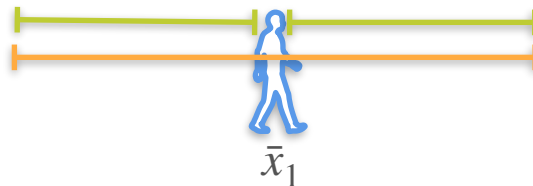
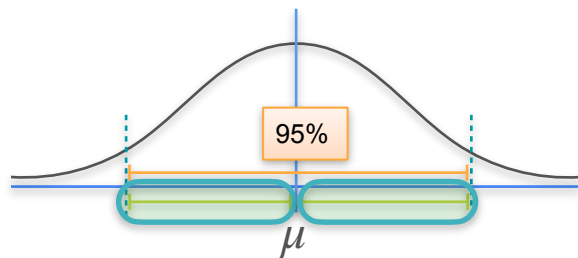
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



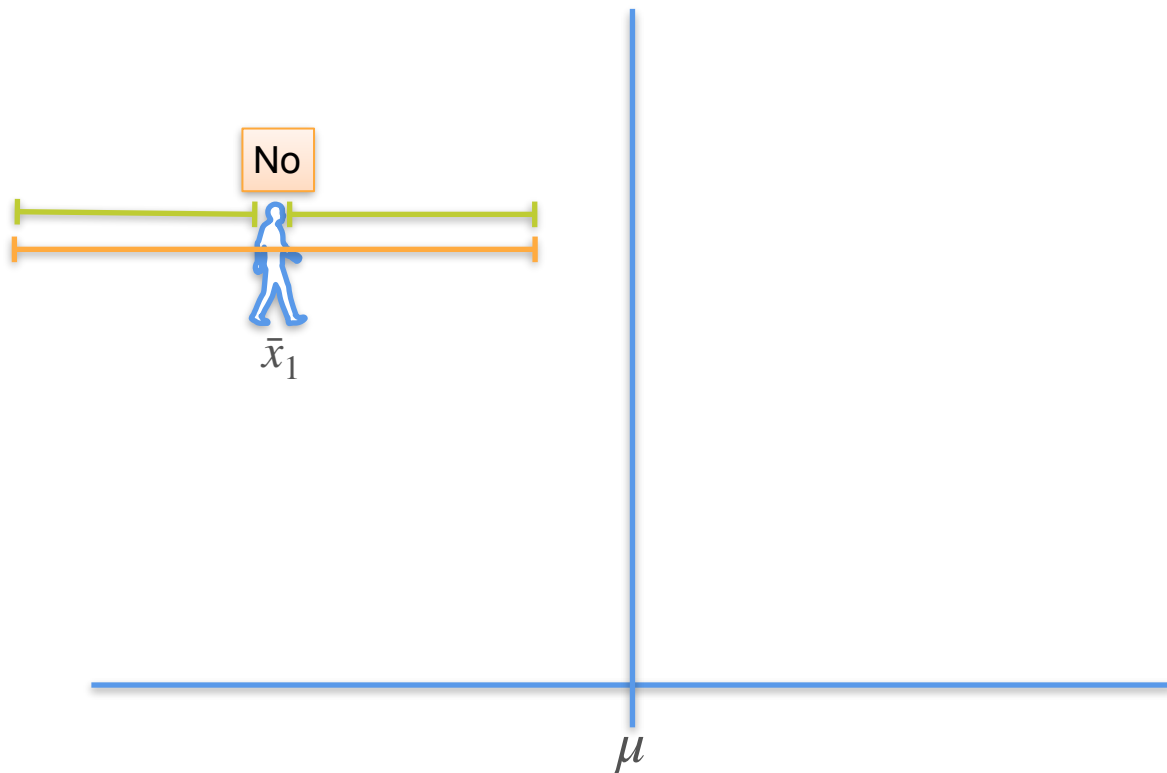
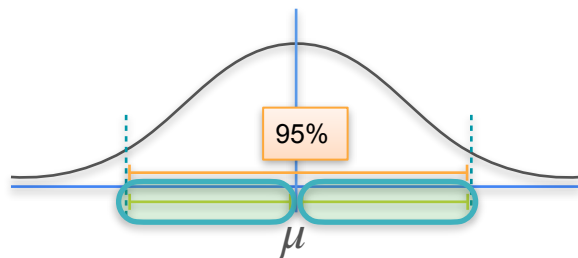
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



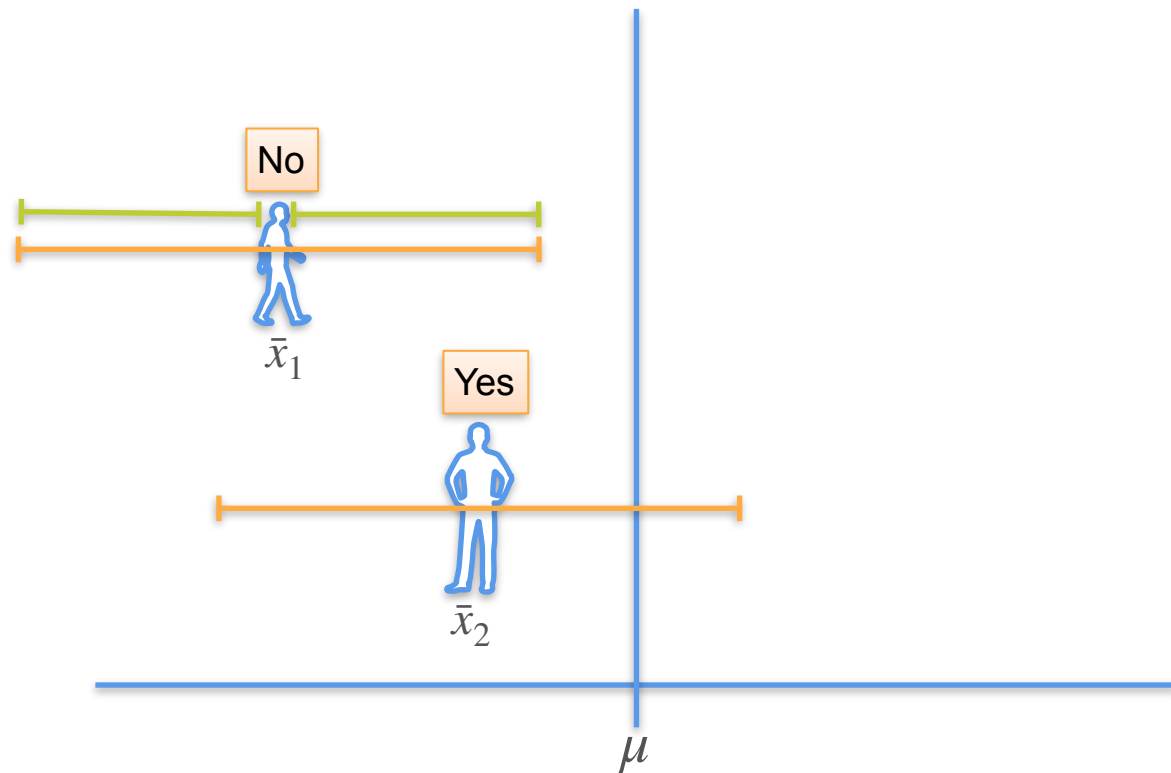
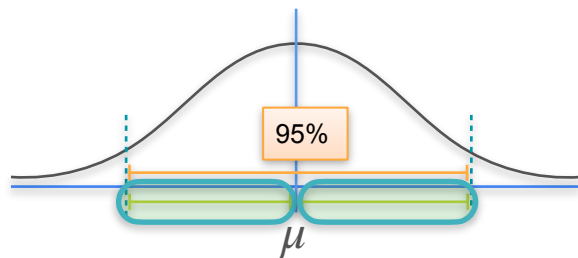
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



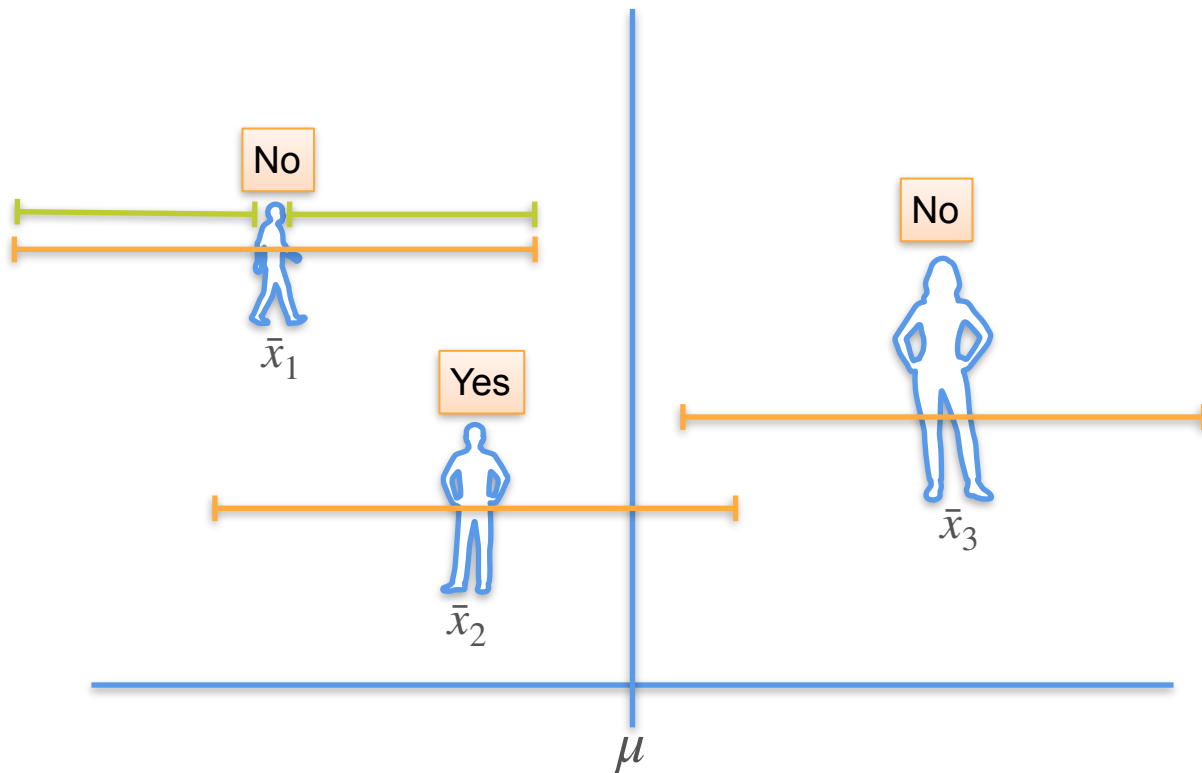
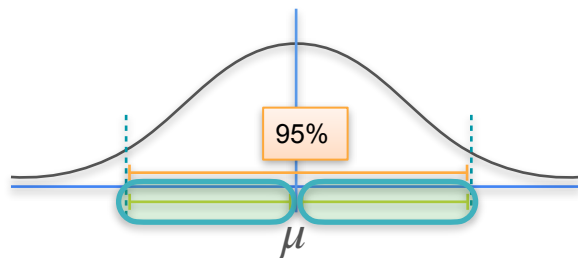
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



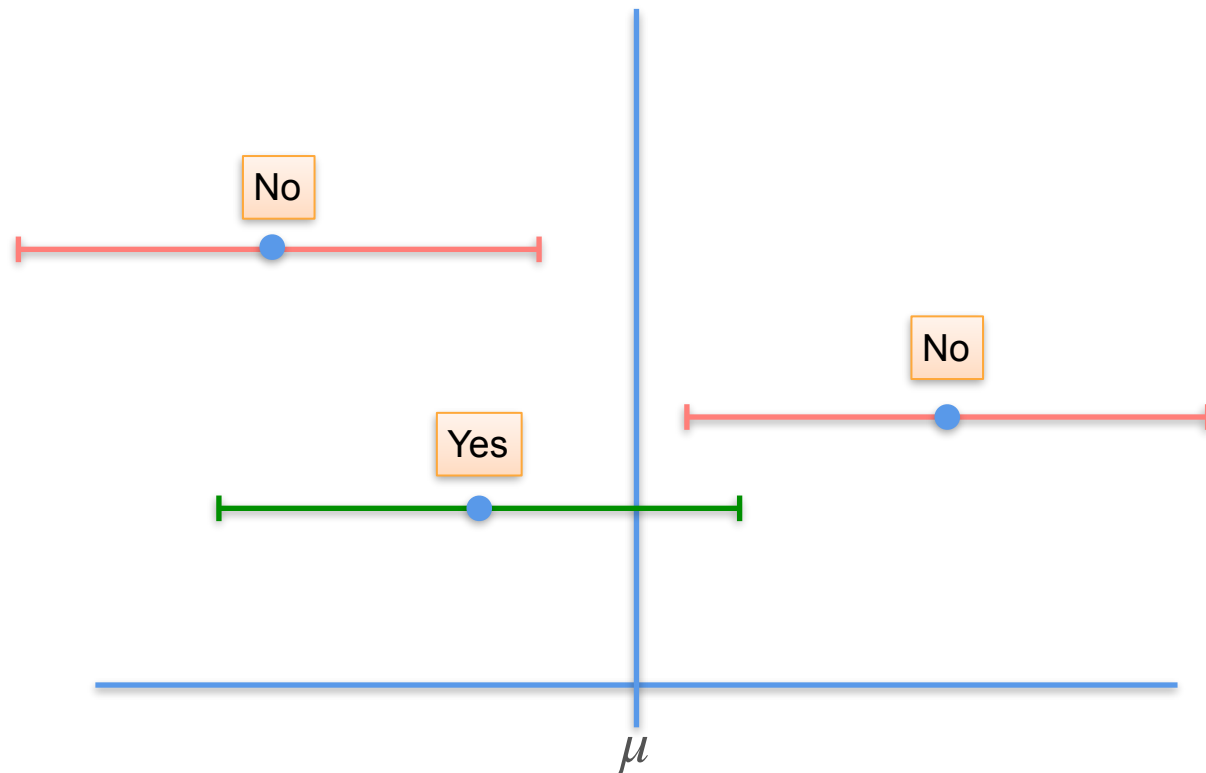
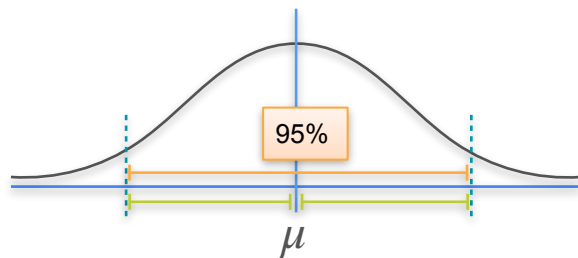
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



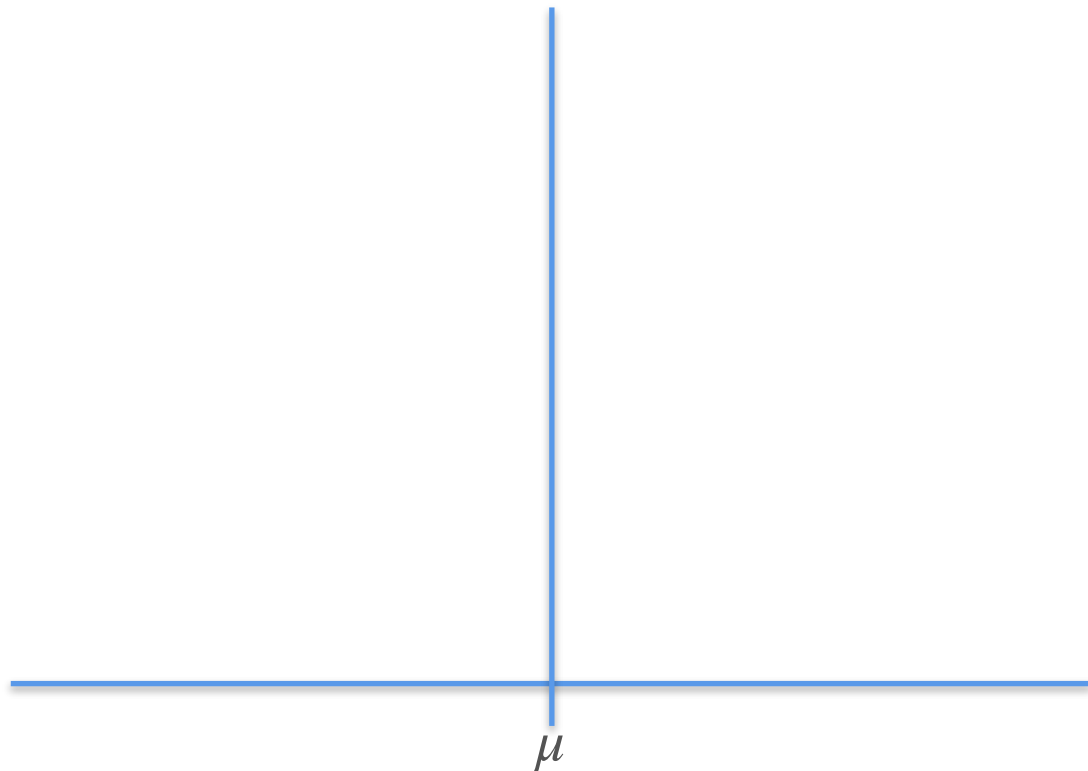
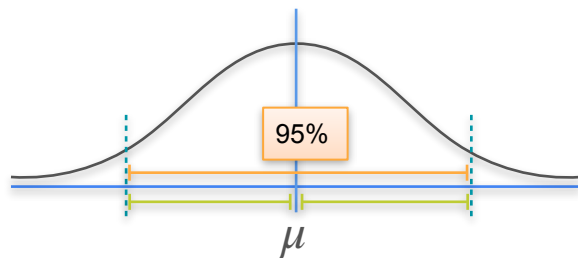
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



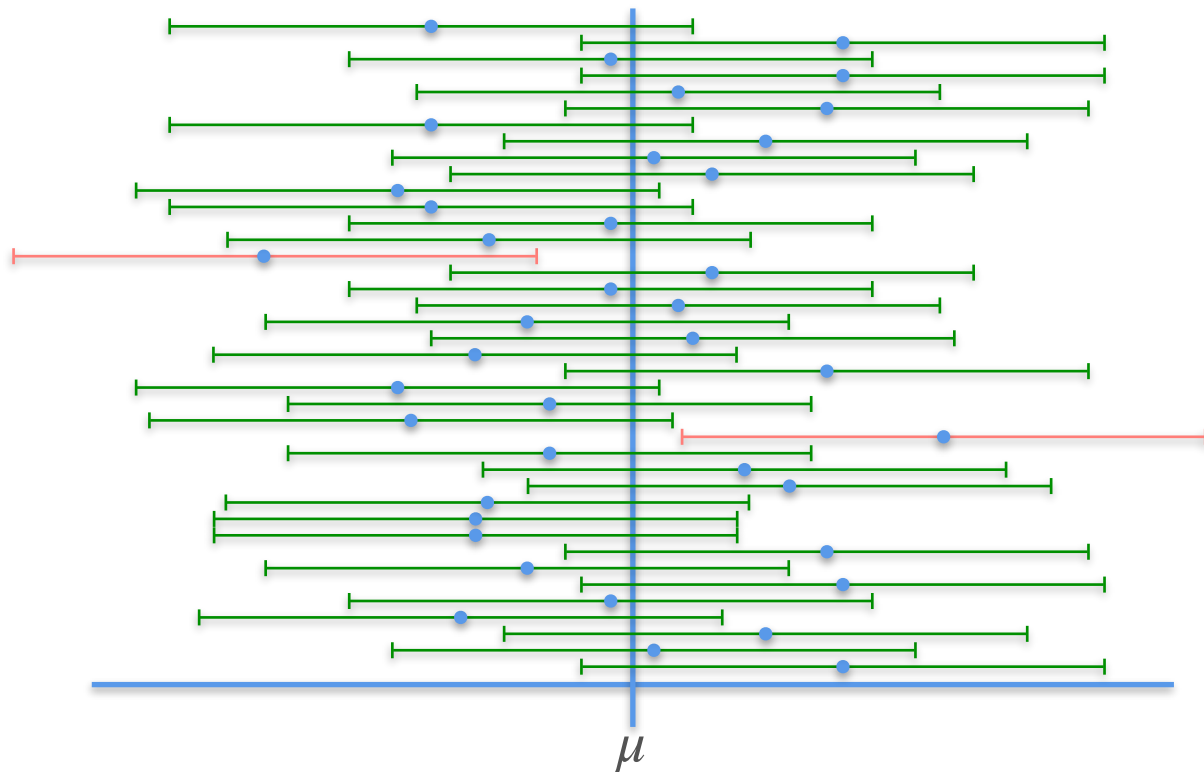
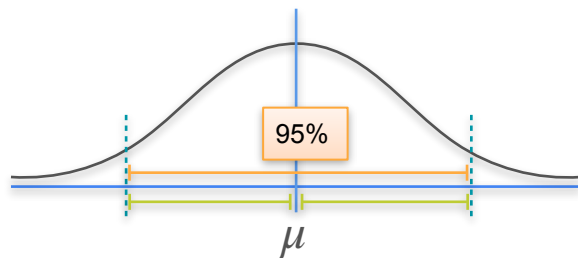
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



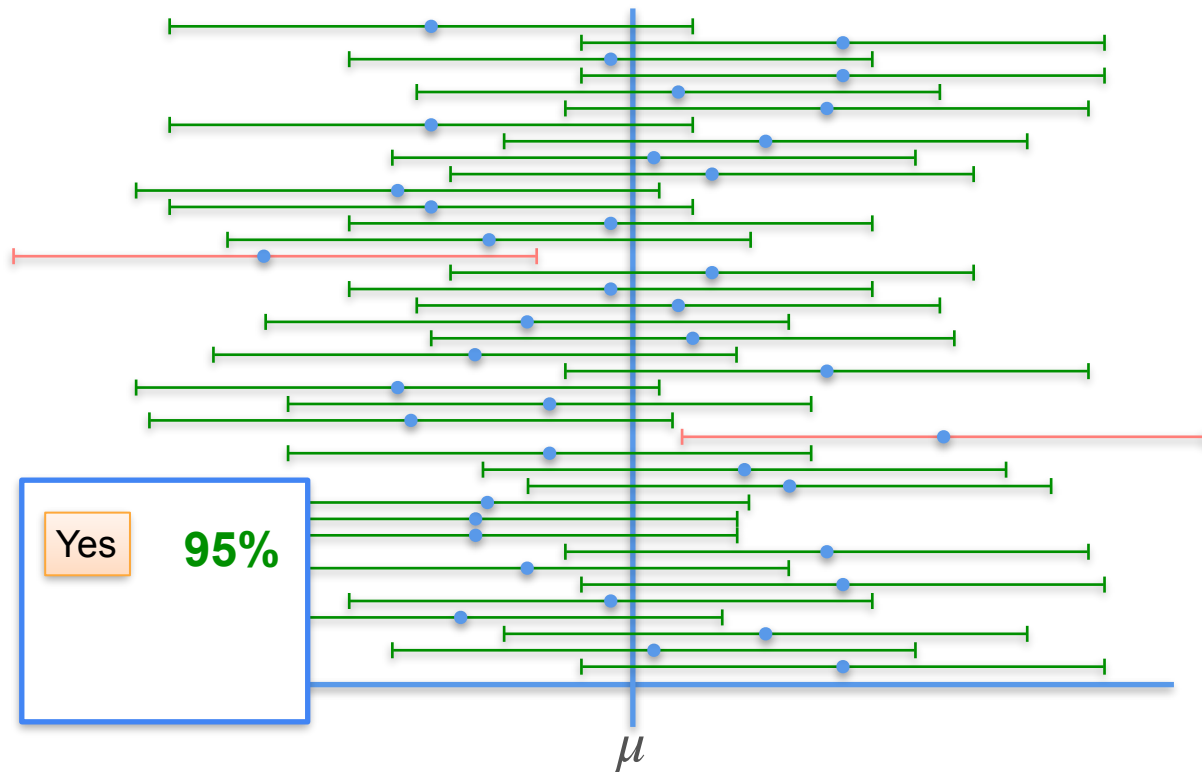
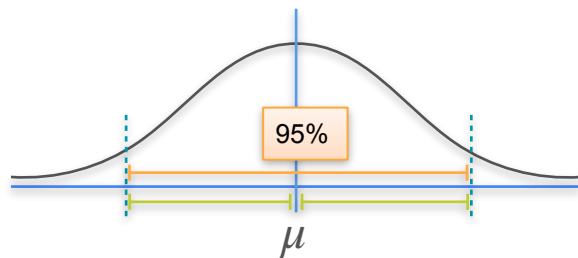
Confidence Interval - Intuition

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Known σ

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Margin of error



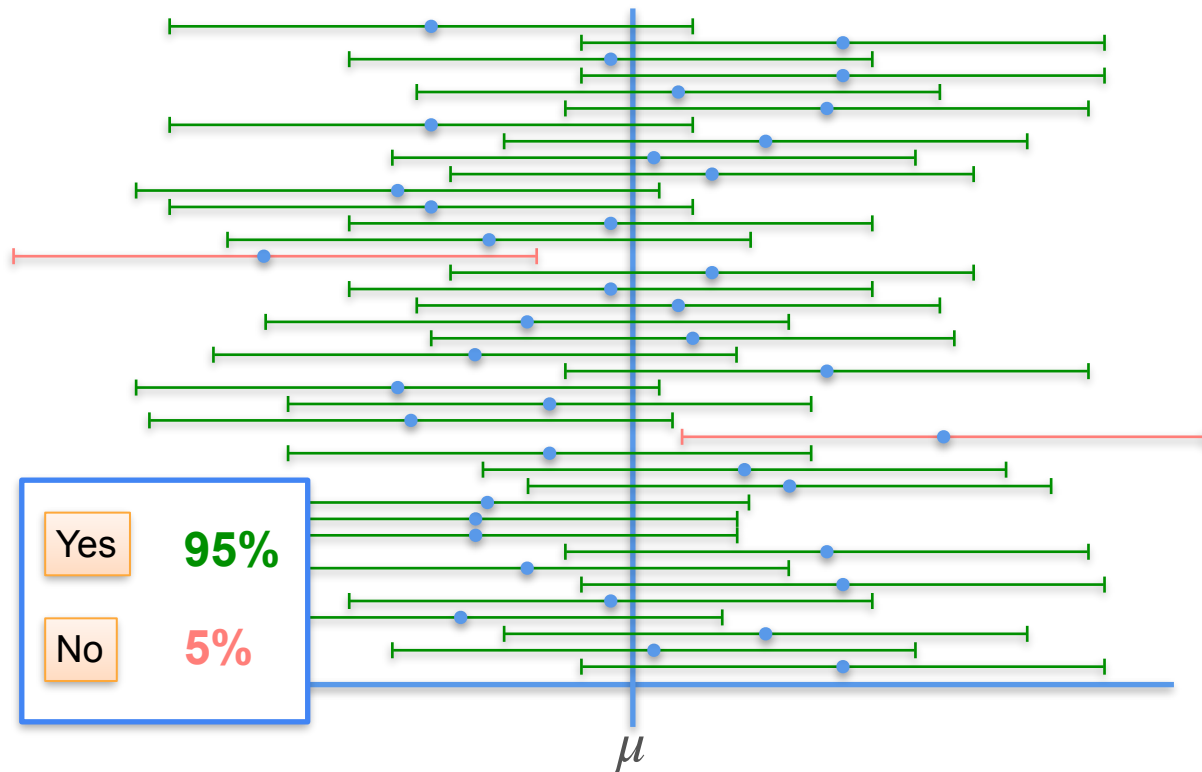
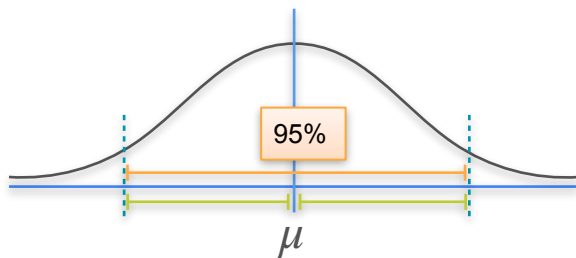
Confidence Interval - Intuition

$$n = 1$$

Known σ

95%

Margin of error



Confidence Interval - Intuition

$$n = 1$$



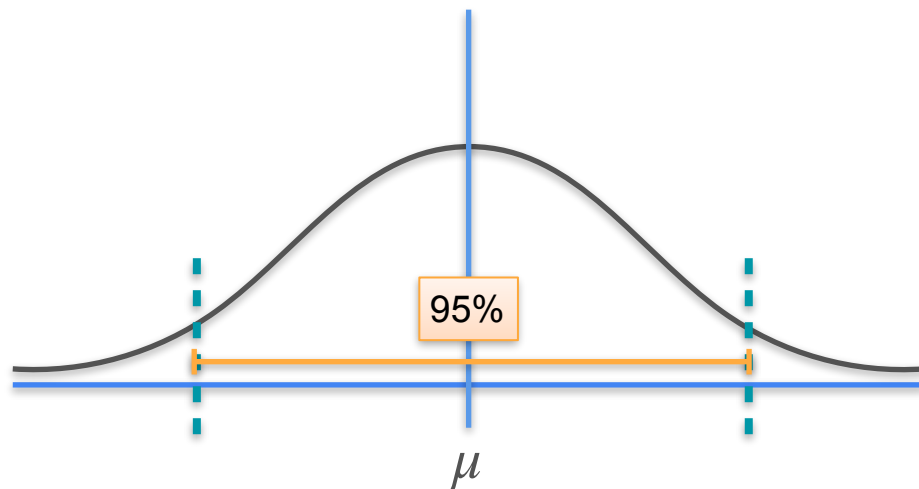
$$\bar{x}$$

Confidence Interval - Intuition

$$n = 1$$



\bar{x}



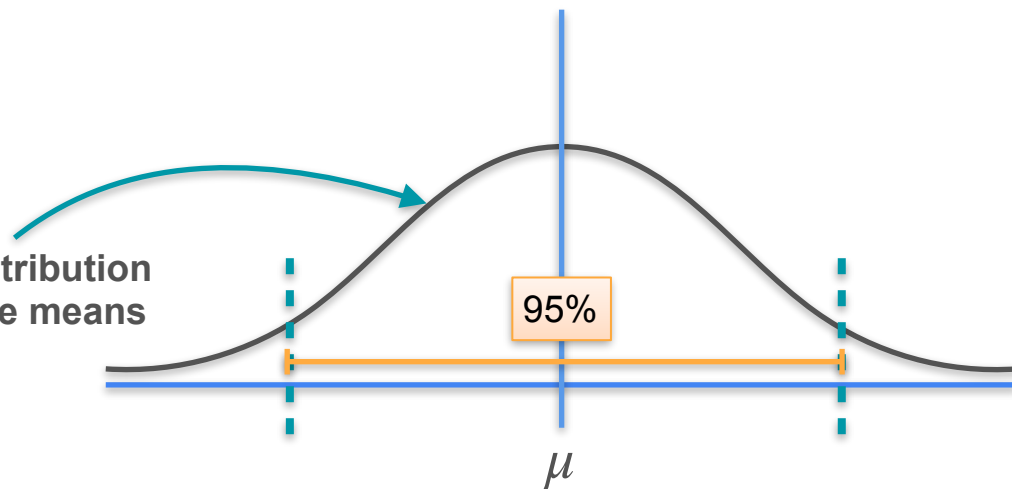
Confidence Interval - Intuition

$$n = 1$$



\bar{x}

sampling distribution
of the sample means



Confidence Interval - Intuition

$$n = 1$$

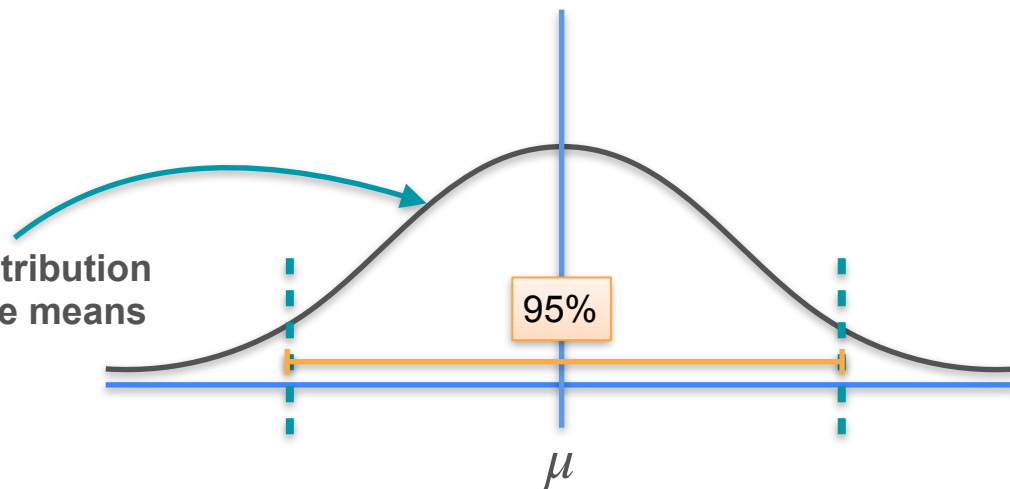
Central Limit Theorem

$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



\bar{x}

sampling distribution
of the sample means



Confidence Interval - Intuition

$$n = 1$$

Central Limit Theorem

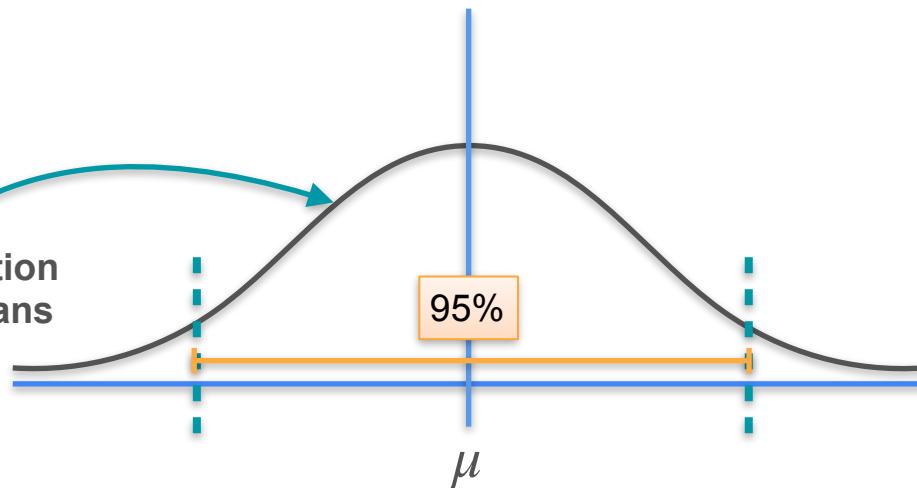
$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$

$$\mu_{\bar{x}} = \mu$$



\bar{x}

sampling distribution
of the sample means



Confidence Interval - Intuition

$n = 1$

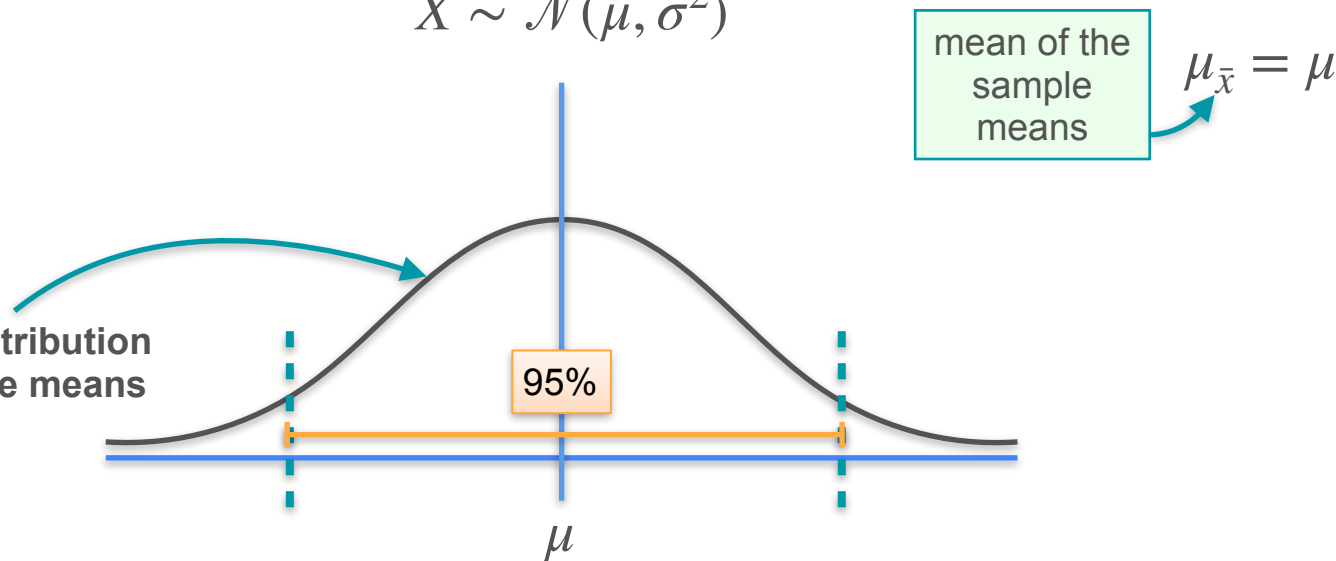
Central Limit Theorem

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\bar{x}

sampling distribution
of the sample means



Confidence Interval - Intuition

$n = 1$

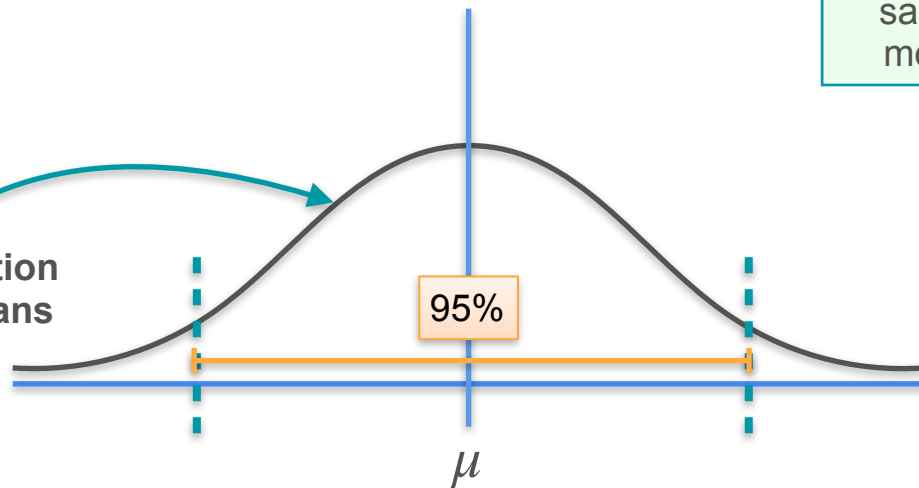
Central Limit Theorem

$$\bar{X} \sim \mathcal{N}(\mu, \sigma^2)$$



\bar{x}

sampling distribution
of the sample means



mean of the
sample
means

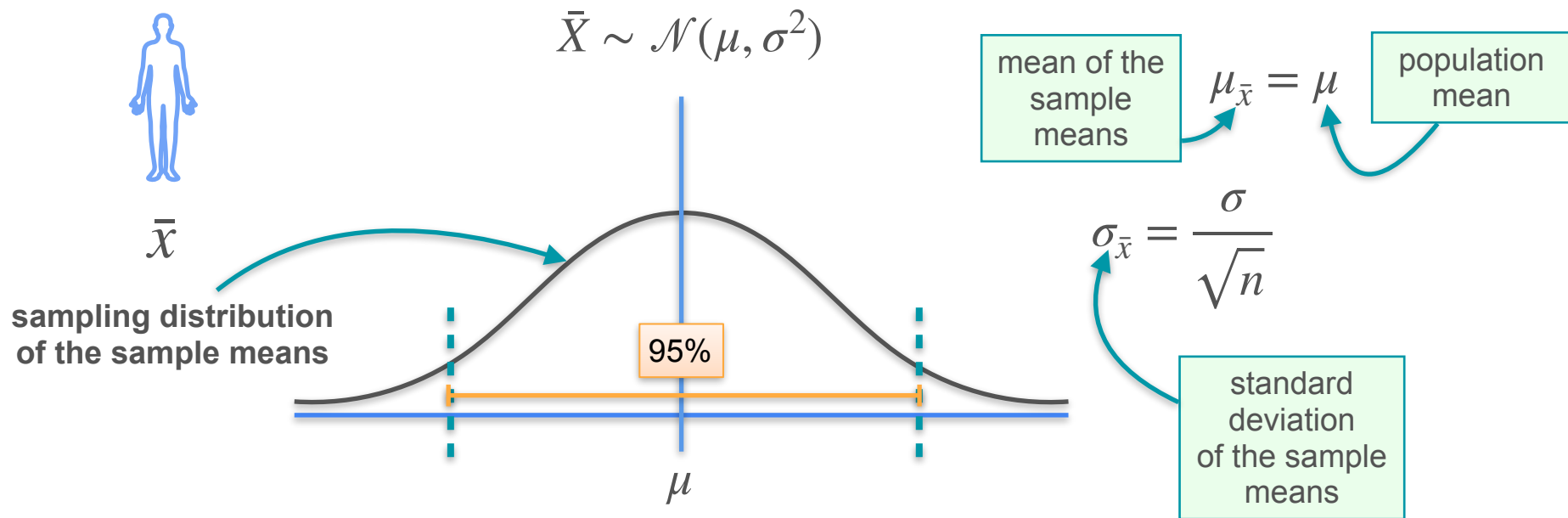
$$\mu_{\bar{x}} = \mu$$

population
mean

Confidence Interval - Intuition

$n = 1$

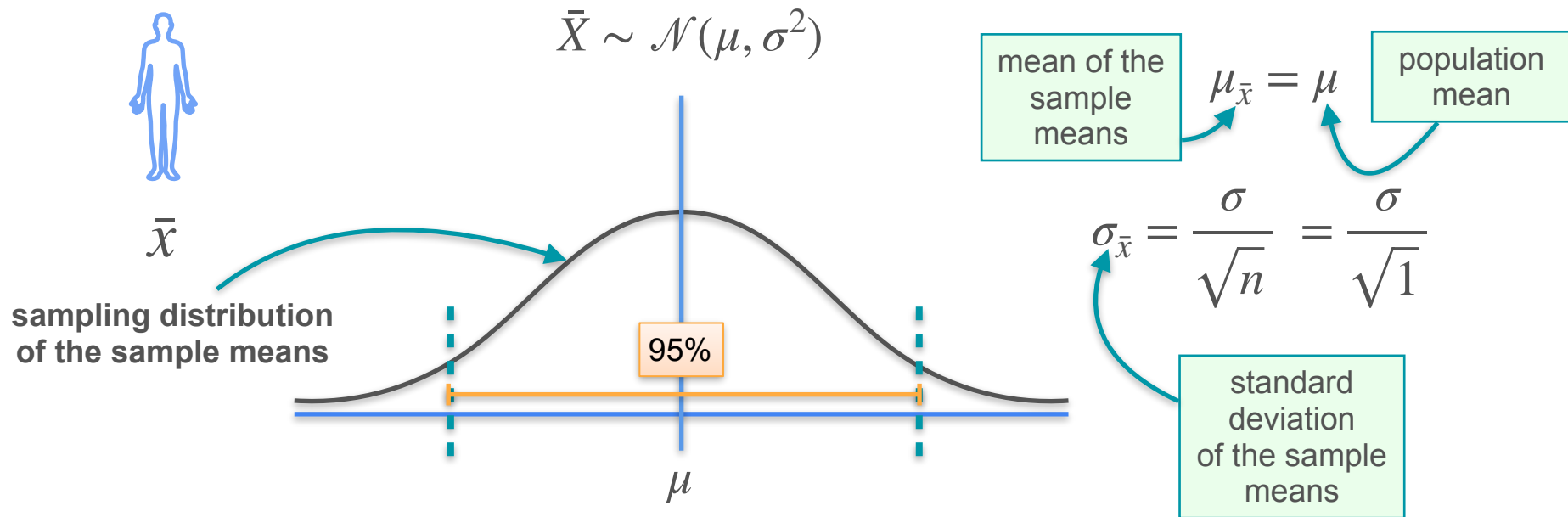
Central Limit Theorem



Confidence Interval - Intuition

$n = 1$

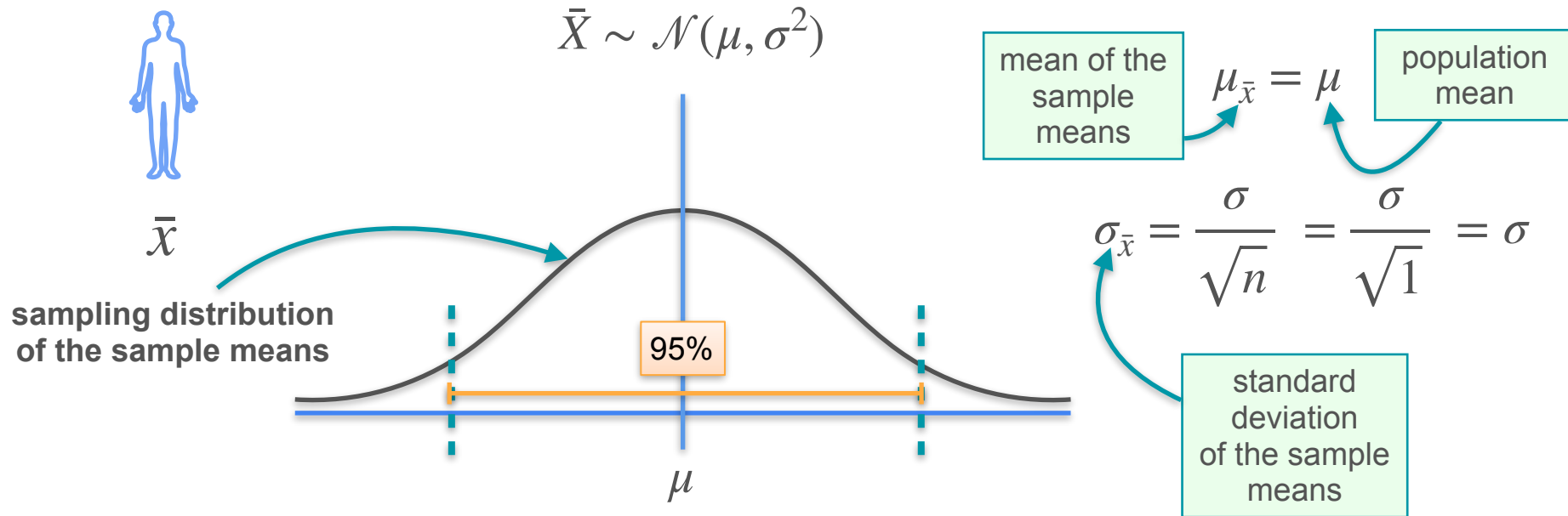
Central Limit Theorem



Confidence Interval - Intuition

$n = 1$

Central Limit Theorem

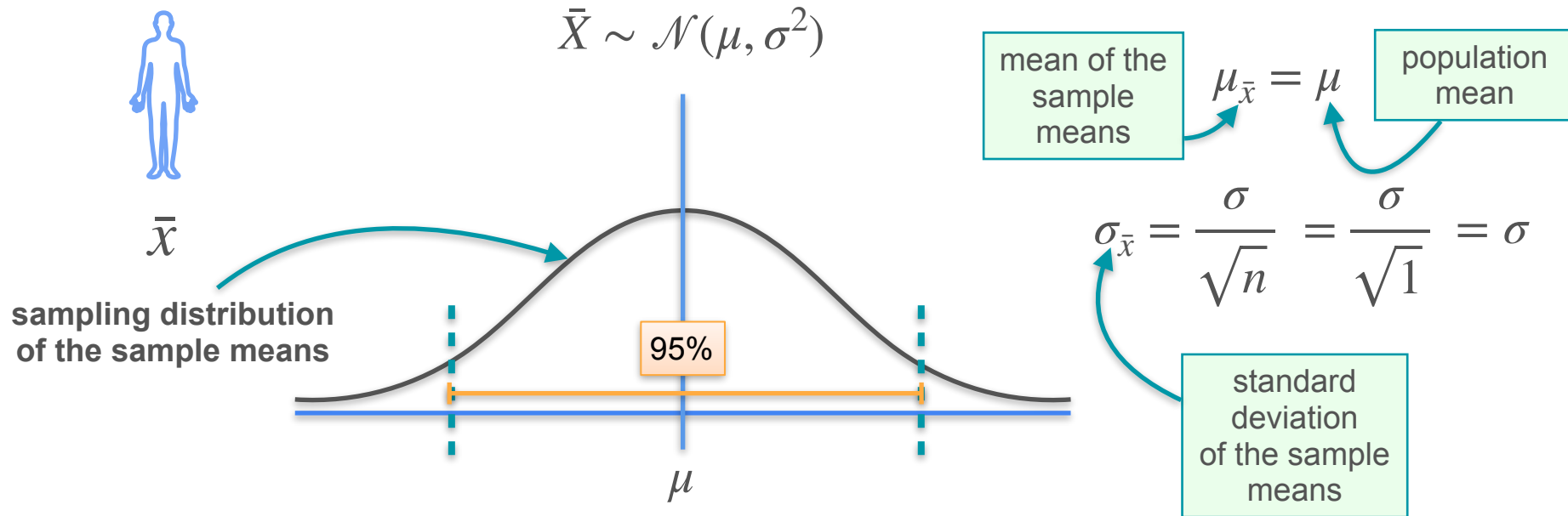


Confidence Interval - Intuition

$n = 1$

Central Limit Theorem

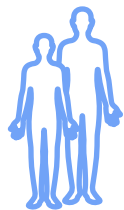
Population standard deviation (σ)



Confidence Interval - Intuition

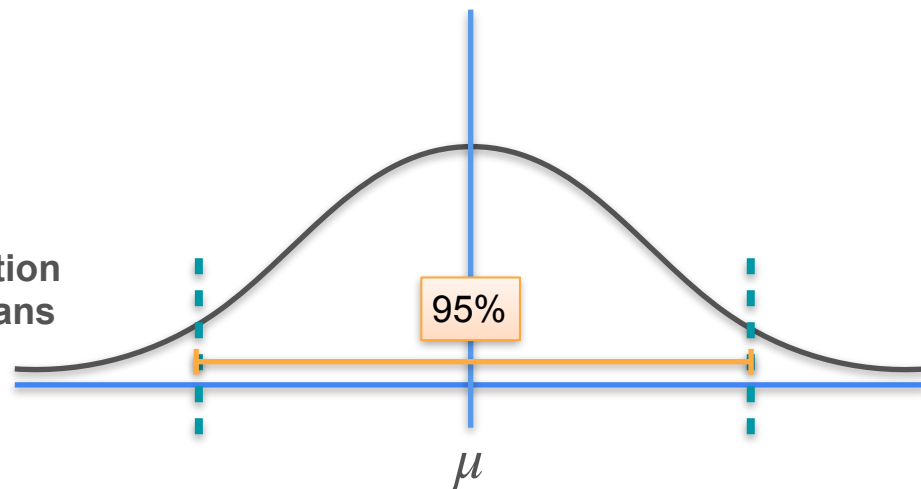
Central Limit Theorem

Population standard deviation (σ)



\bar{x}

sampling distribution
of the sample means

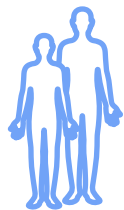


Confidence Interval - Intuition

$$n = 2$$

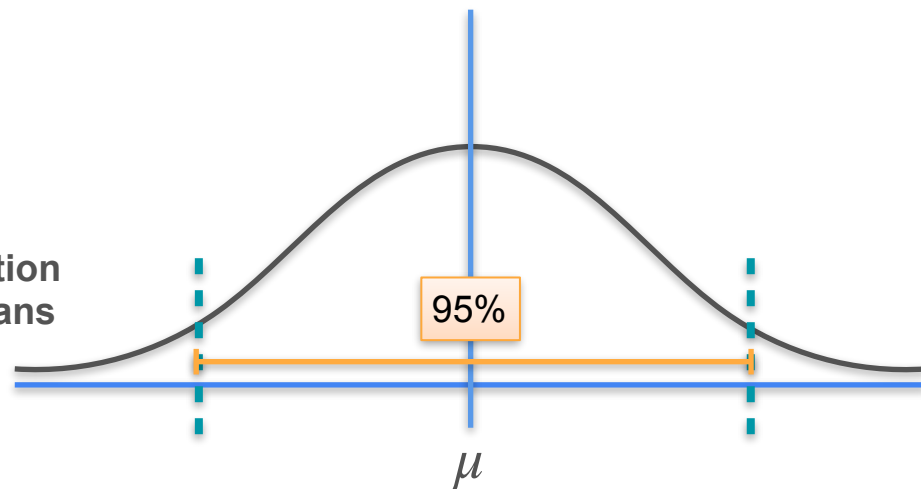
Central Limit Theorem

Population standard deviation (σ)



$$\bar{x}$$

sampling distribution
of the sample means

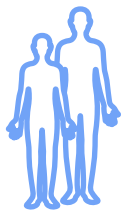


Confidence Interval - Intuition

$$n = 2$$

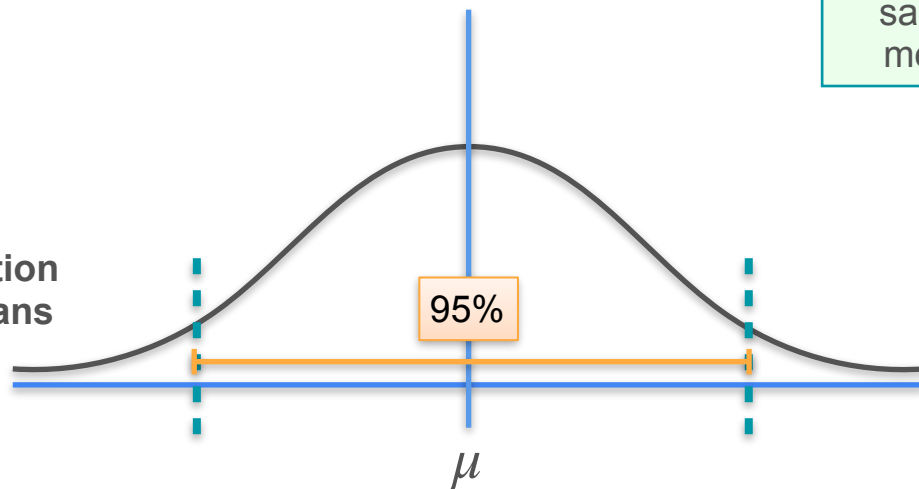
Central Limit Theorem

Population standard deviation (σ)



$$\bar{x}$$

sampling distribution
of the sample means



mean of the
sample
means

$$\mu_{\bar{x}} = \mu$$

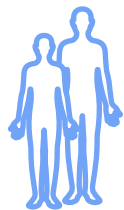
population
mean

Confidence Interval - Intuition

$$n = 2$$

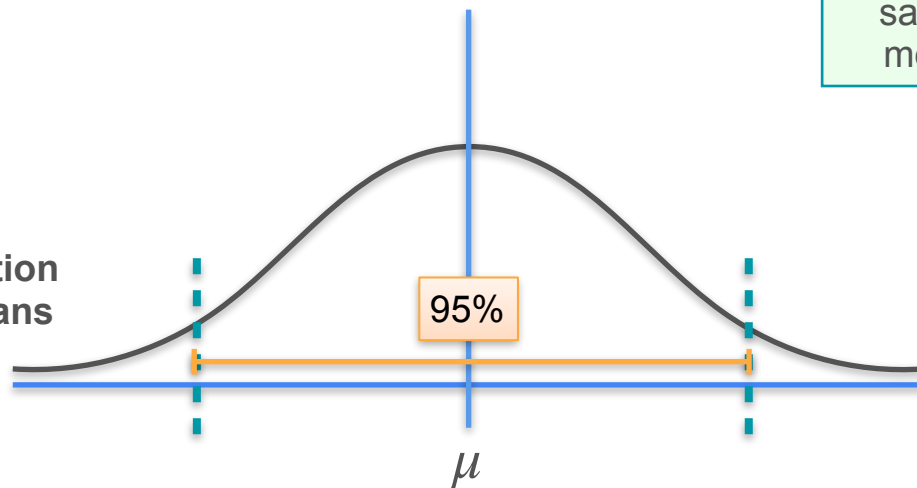
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mean of the
sample
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population
mean

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

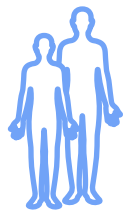
standard
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Confidence Interval - Intuition

$$n = 2$$

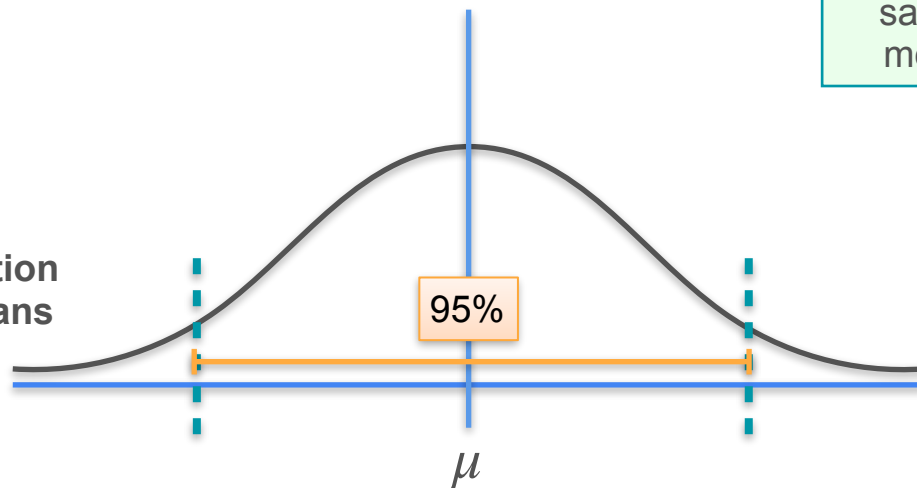
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population
mean

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{\sigma}{\sqrt{2}}$$

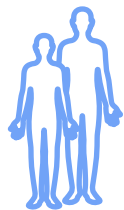
standard
deviation
of the sample
means

Confidence Interval - Intuition

$$n = 2$$

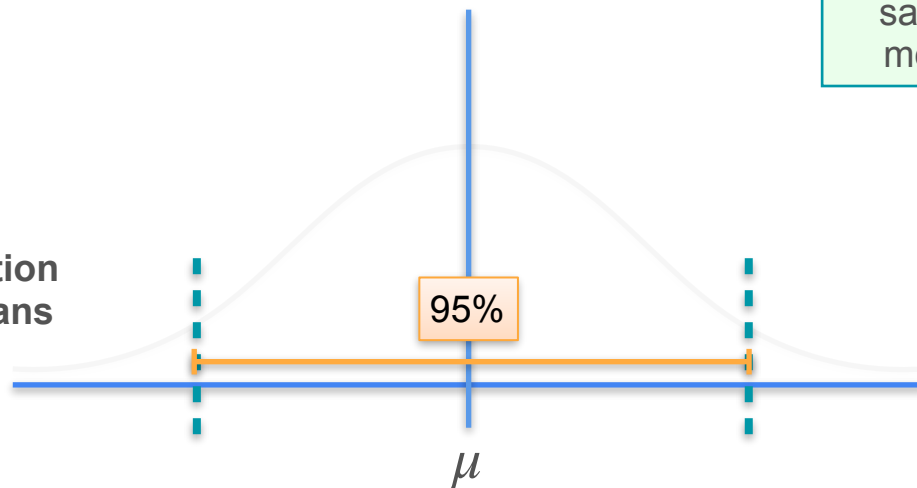
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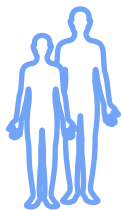
standard
deviation
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Confidence Interval - Intuition

$$n = 2$$

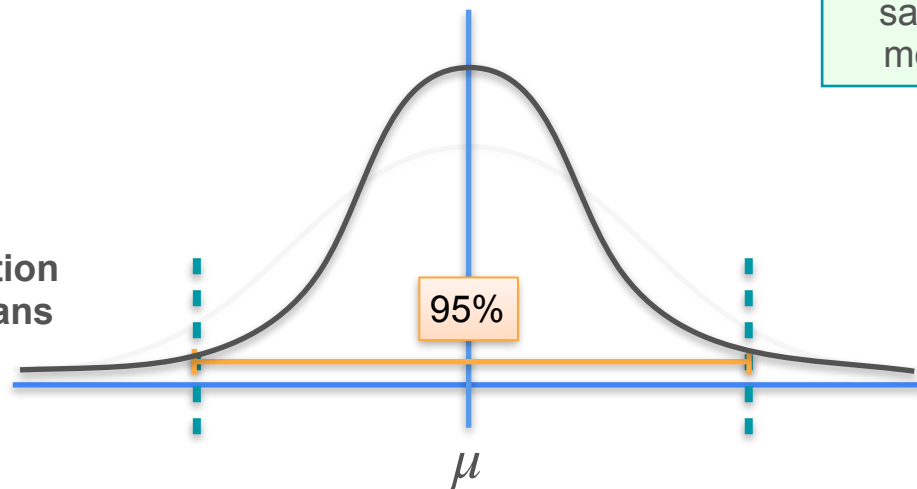
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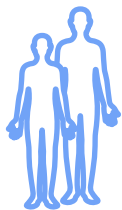
population
mean

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{\sigma}{\sqrt{2}}$$

standard
deviation
of the sample
means

Confidence Interval - Intuition

$$n = 2$$

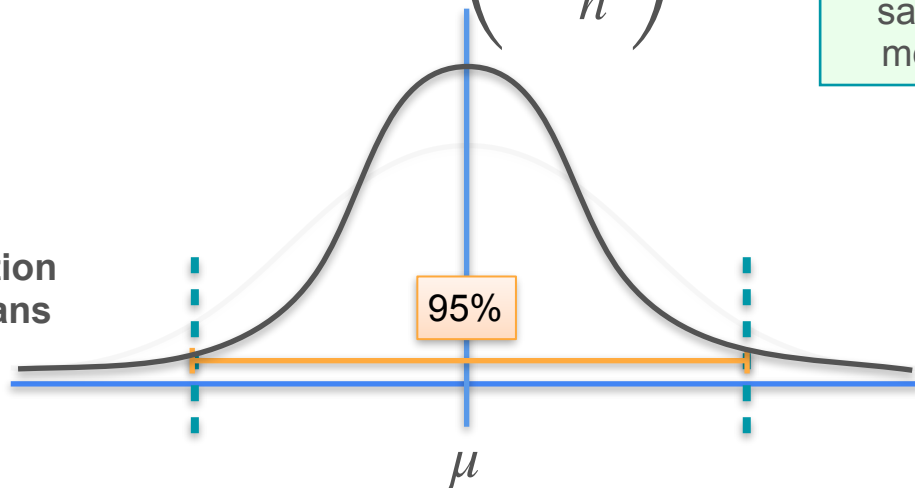


$$\bar{x}$$

sampling distribution
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Central Limit Theorem

$$\bar{X} \sim \mathcal{N}\left(\mu, \frac{\sigma^2}{n}\right)$$



Population standard deviation (σ)

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sample
means

$$\mu_{\bar{x}} = \mu$$

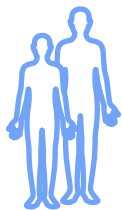
population
mean

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{\sigma}{\sqrt{2}}$$

standard
deviation
of the sample
means

Confidence Interval - Intuition

$$n = 2$$

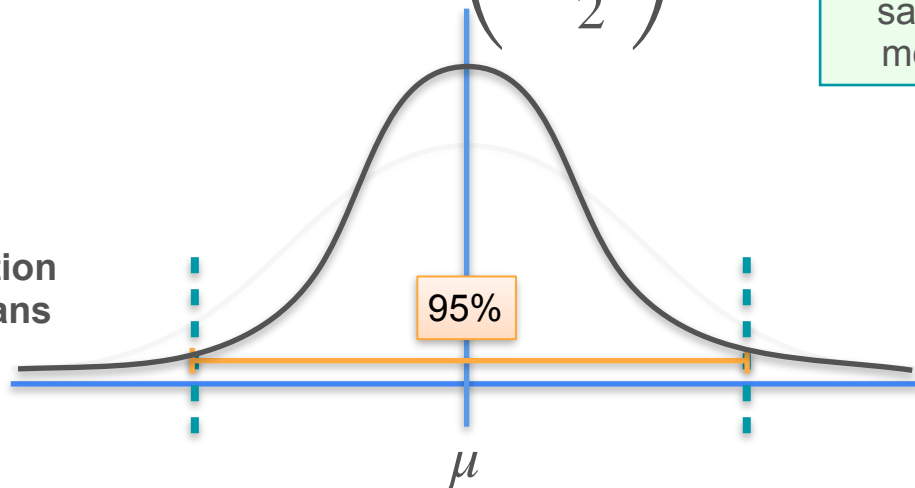


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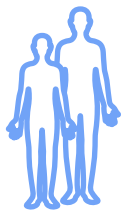
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standard
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Confidence Interval - Intuition

$$n = 2$$

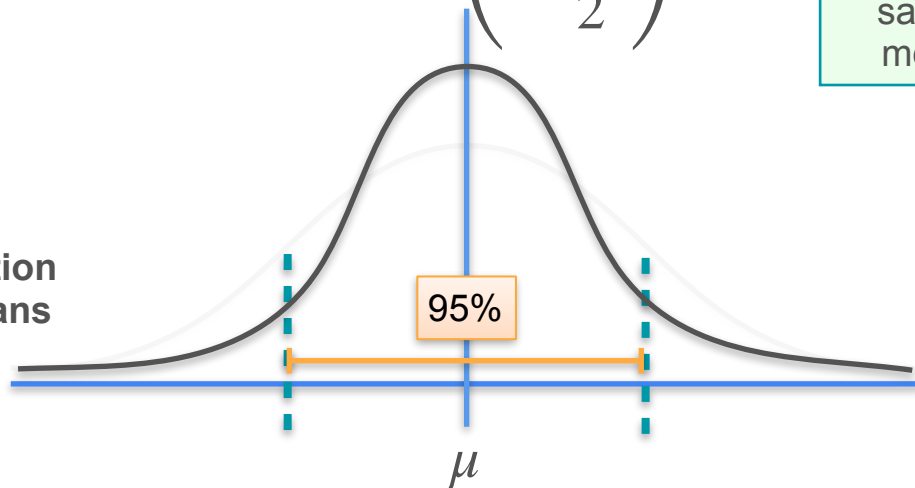


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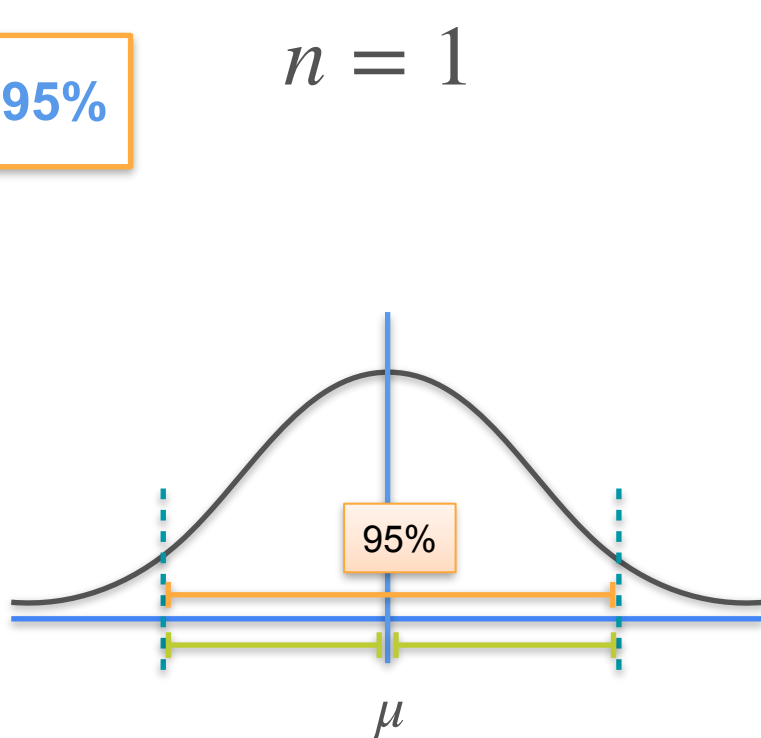
$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{\sigma}{\sqrt{2}}$$

standard
deviation
of the sample
means

Confidence Interval - Intuition

95%

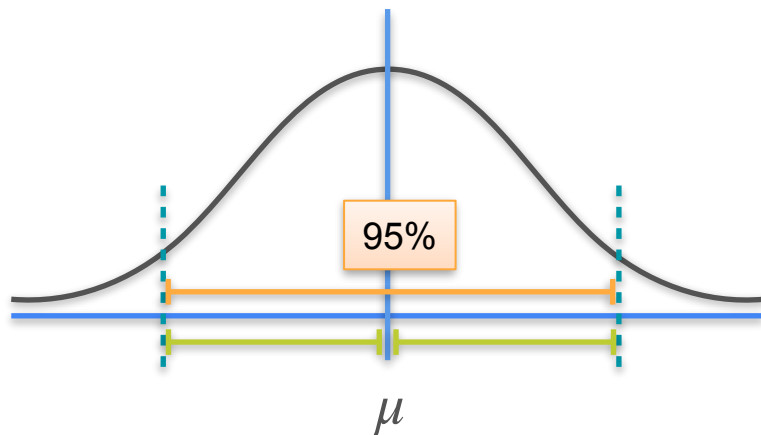
$n = 1$



Confidence Interval - Intuition

95%

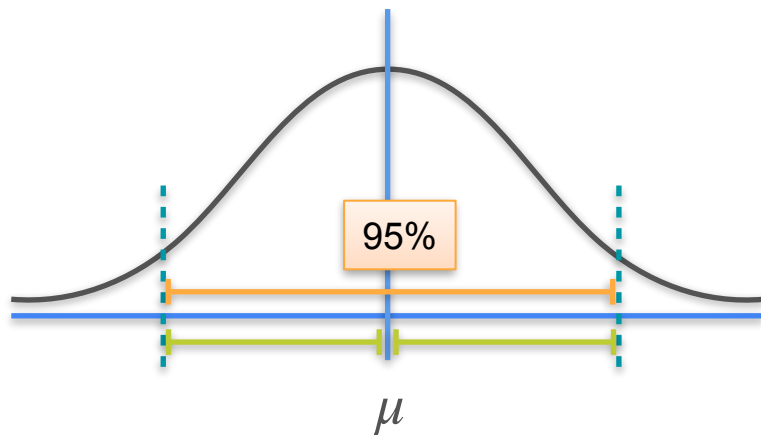
$$n = 1$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



Confidence Interval - Intuition

95%

$$n = 1$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$

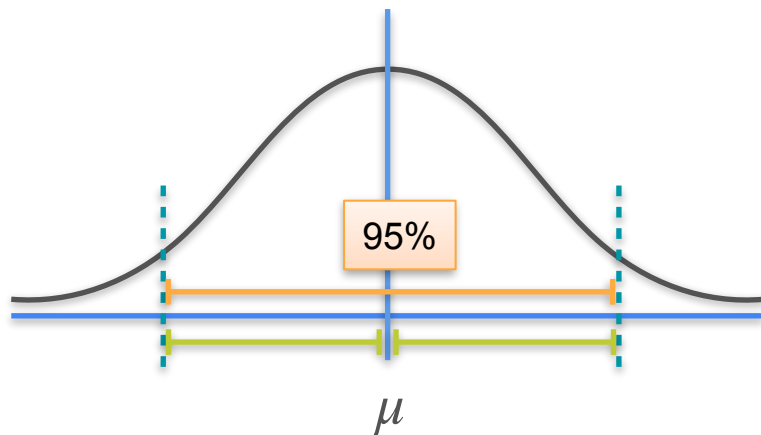


$$n = 2$$

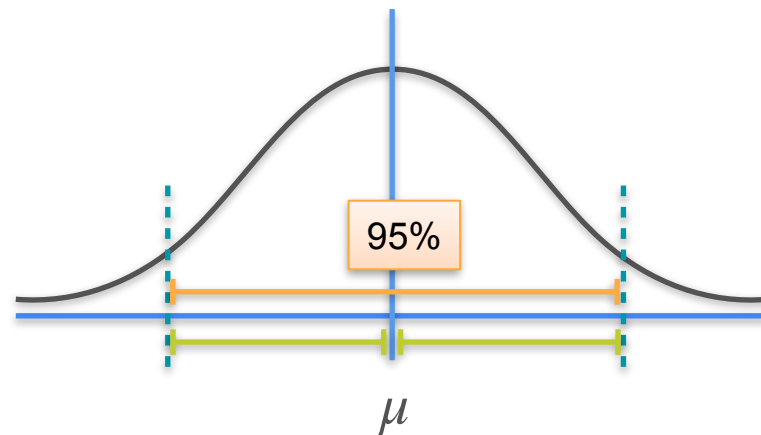
Confidence Interval - Intuition

95%

$$n = 1$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



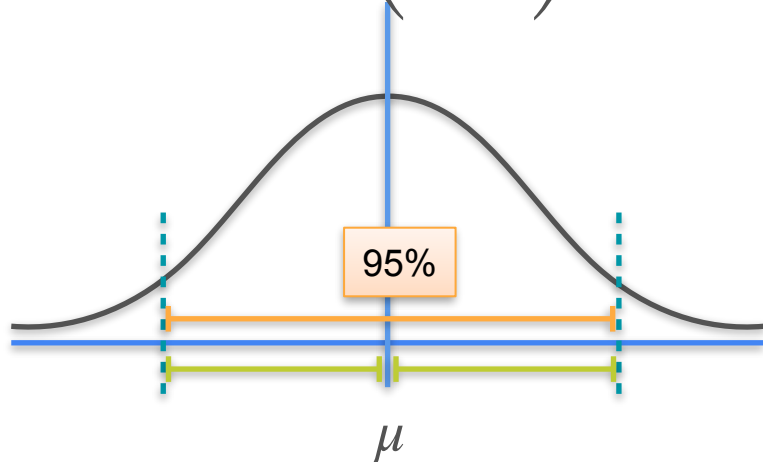
$$n = 2$$



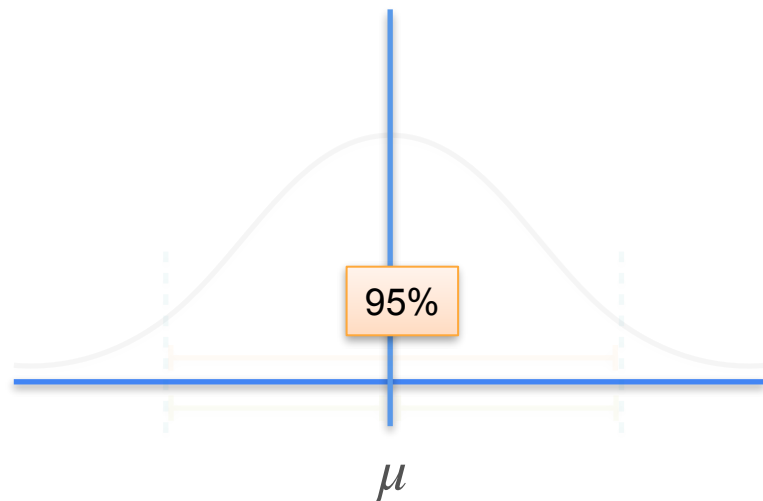
Confidence Interval - Intuition

95%

$$n = 1$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



$$n = 2$$

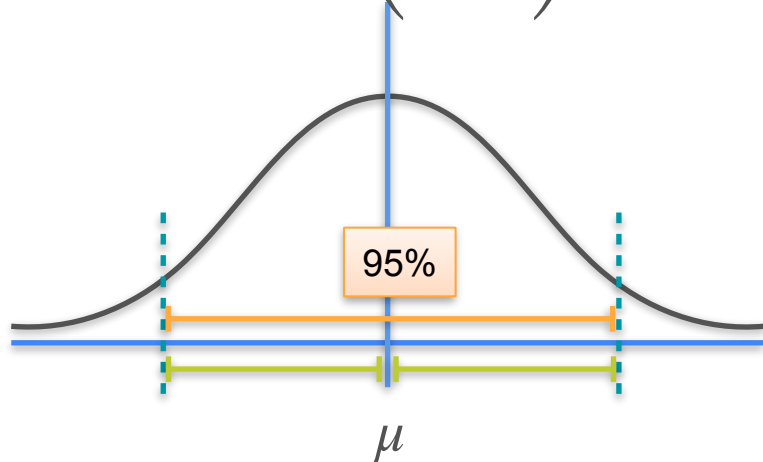


Confidence Interval - Intuition

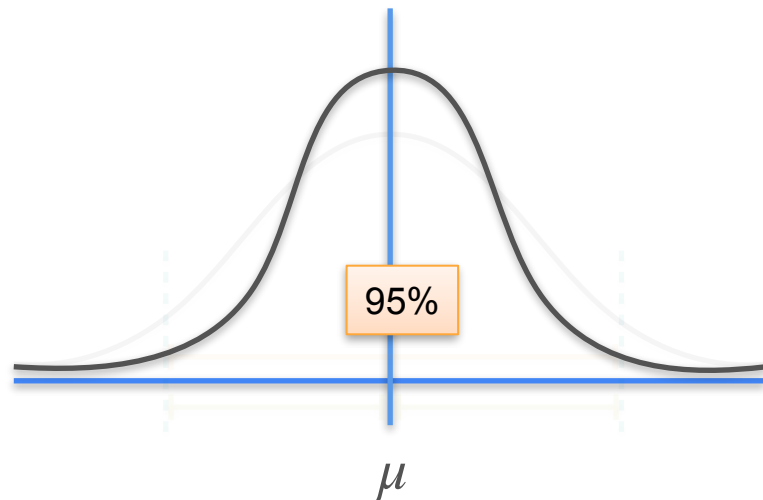
95%

$n = 1$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



$n = 2$

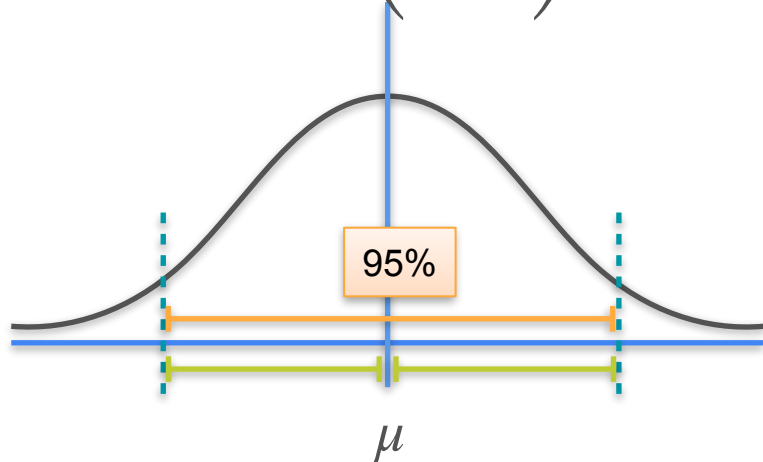


Confidence Interval - Intuition

95%

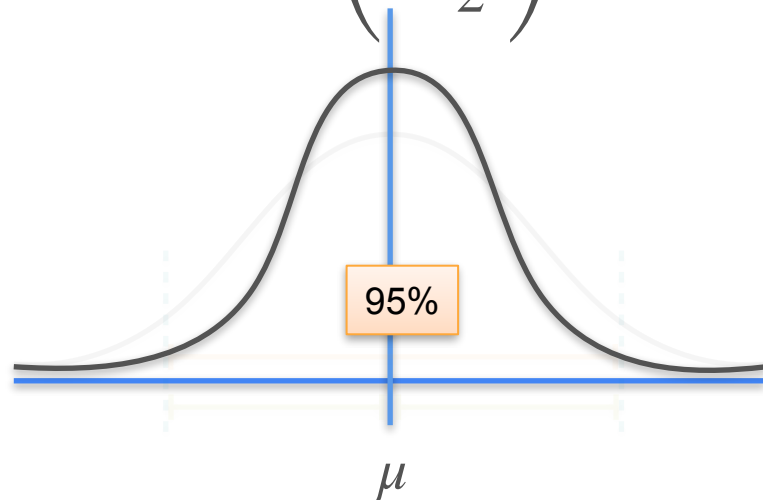
$n = 1$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



$n = 2$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{2}\right)$$

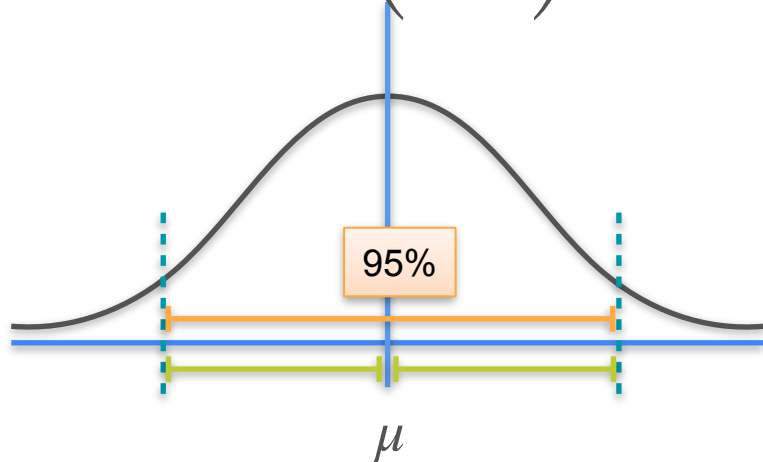


Confidence Interval - Intuition

95%

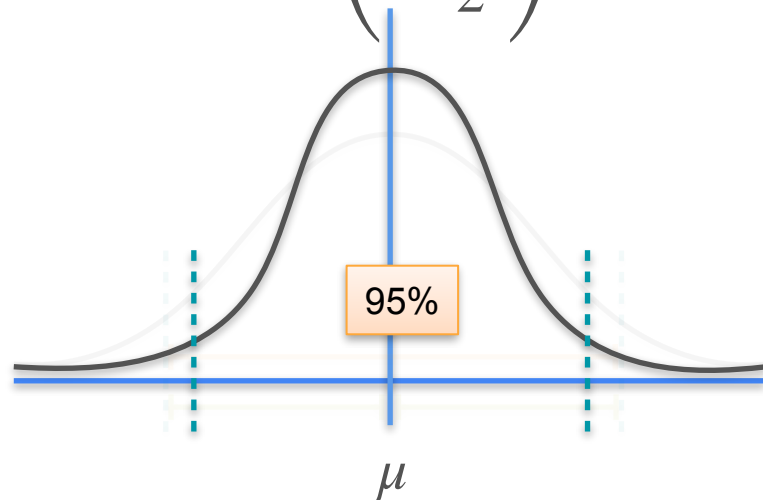
$n = 1$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



$n = 2$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{2}\right)$$

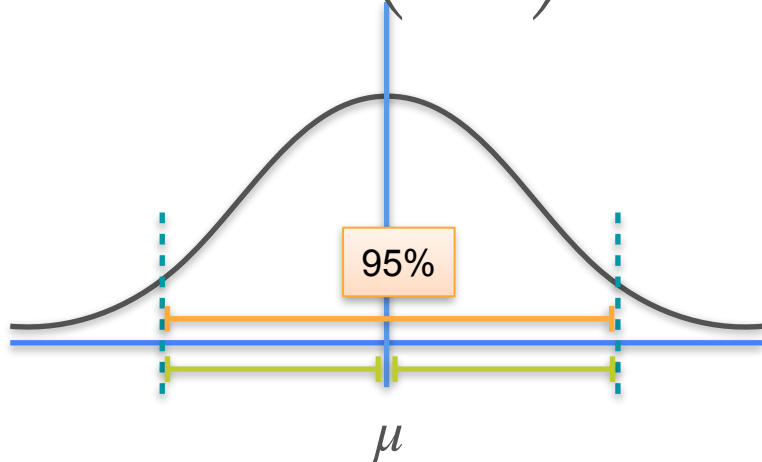


Confidence Interval - Intuition

95%

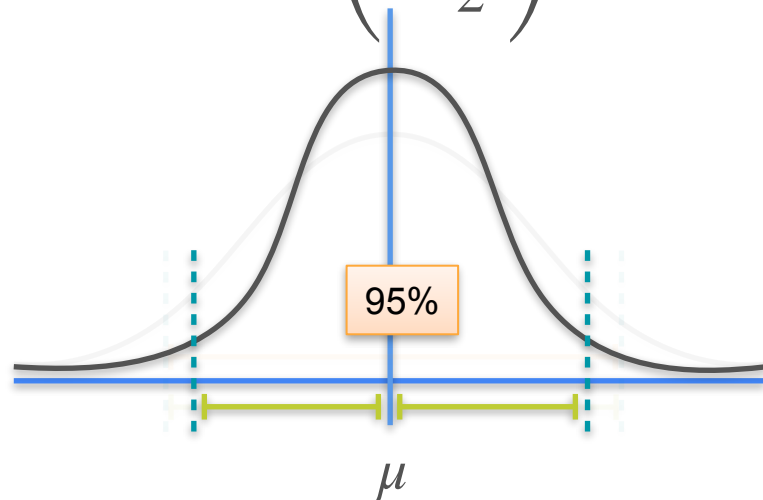
$n = 1$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



$n = 2$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{2}\right)$$

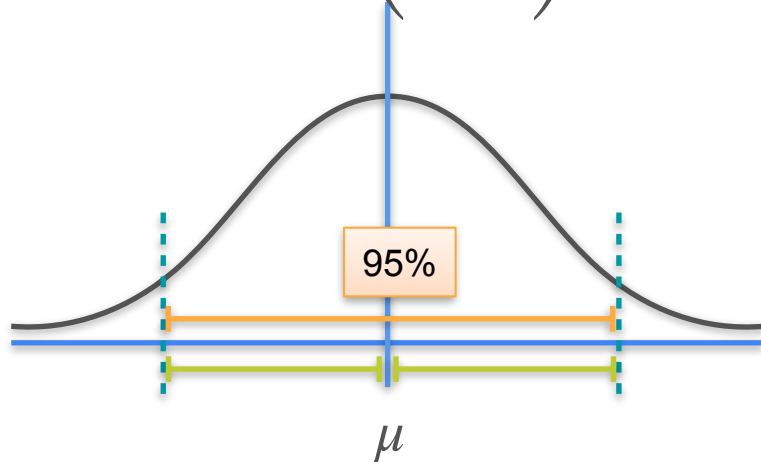


Confidence Interval - Intuition

95%

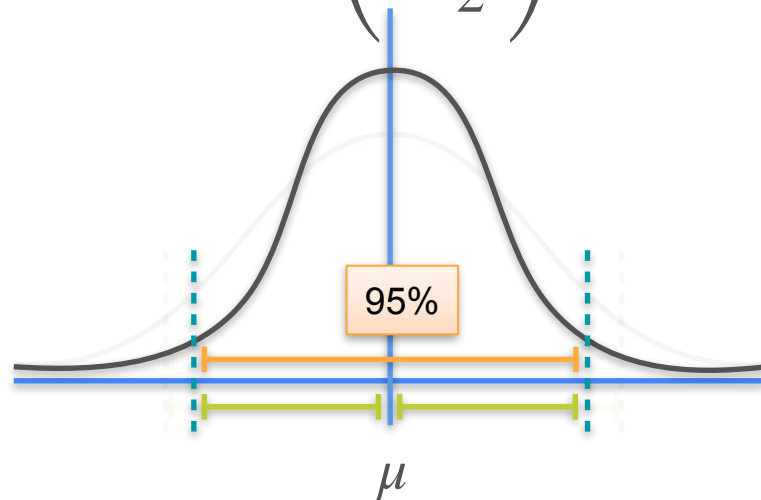
$n = 1$

$$\mathcal{N}\left(\mu, \frac{\sigma^2}{1}\right)$$



$n = 2$

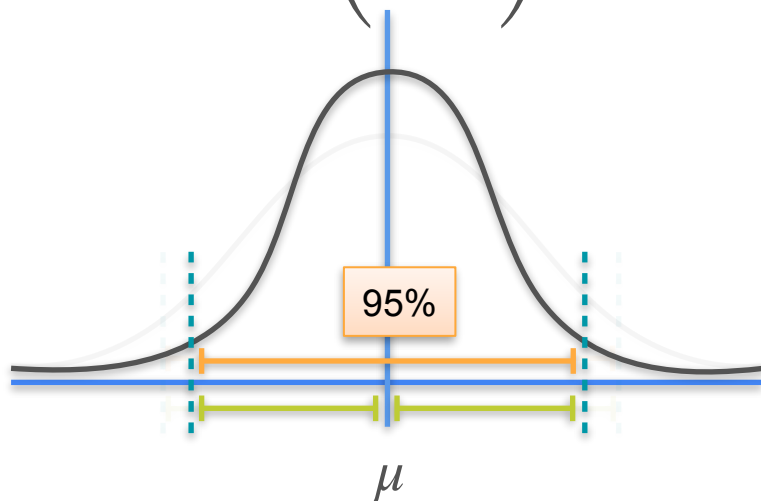
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{2}\right)$$



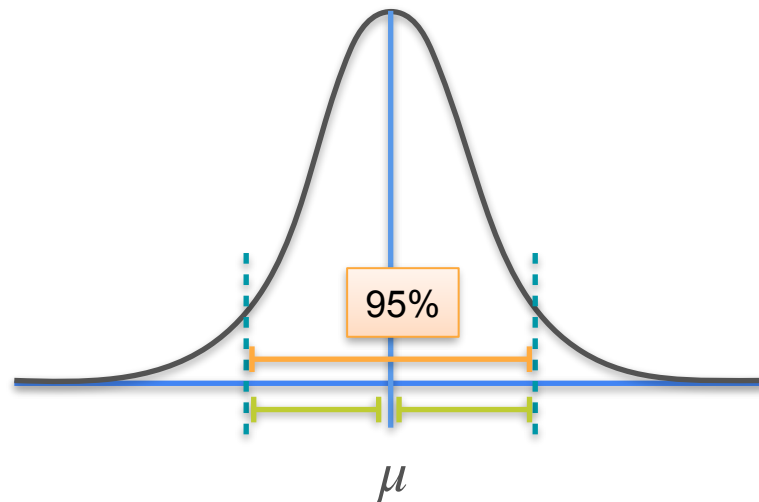
Confidence Interval - Intuition

95%

$$n = 2$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{2}\right)$$



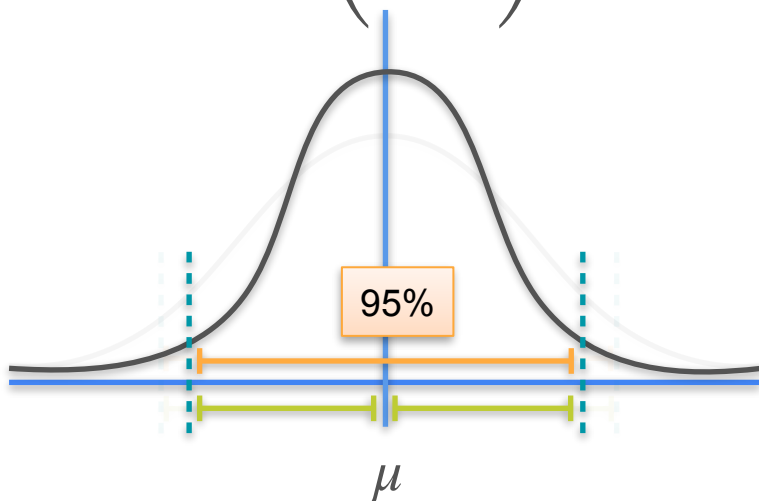
$$n = 10$$



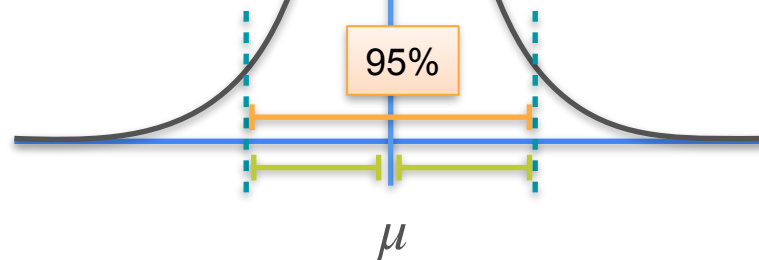
Confidence Interval - Intuition

95%

$$n = 2$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{2}\right)$$



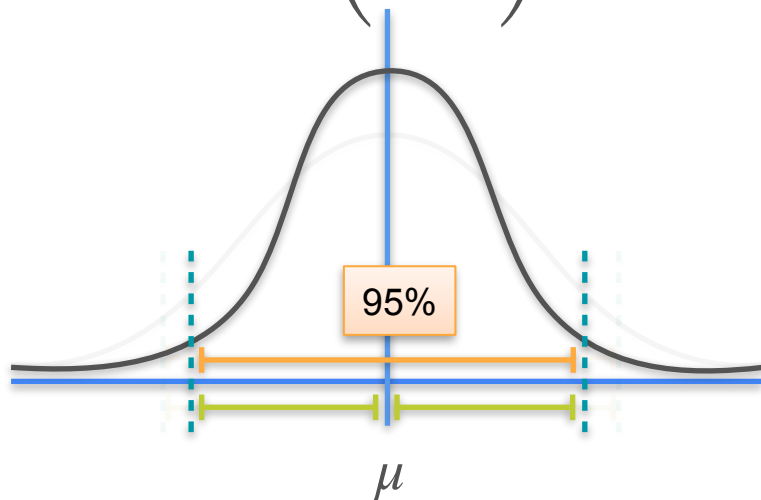
$$n = 10$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{10}\right)$$



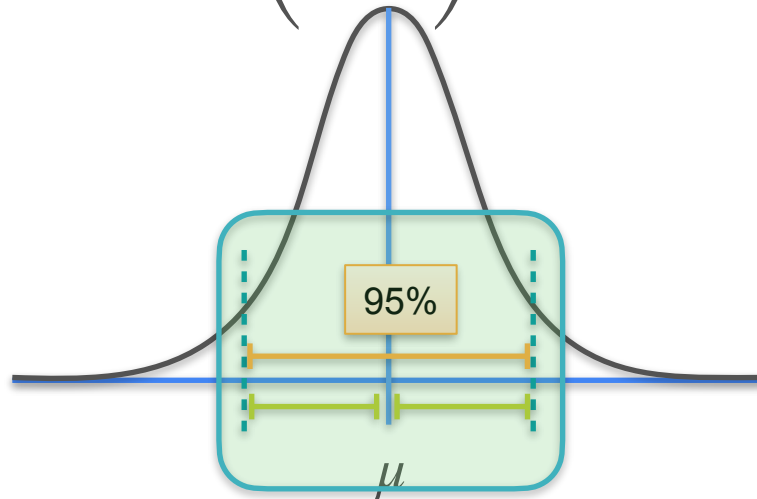
Confidence Interval - Intuition

95%

$$n = 2$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{2}\right)$$



$$n = 10$$
$$\mathcal{N}\left(\mu, \frac{\sigma^2}{10}\right)$$



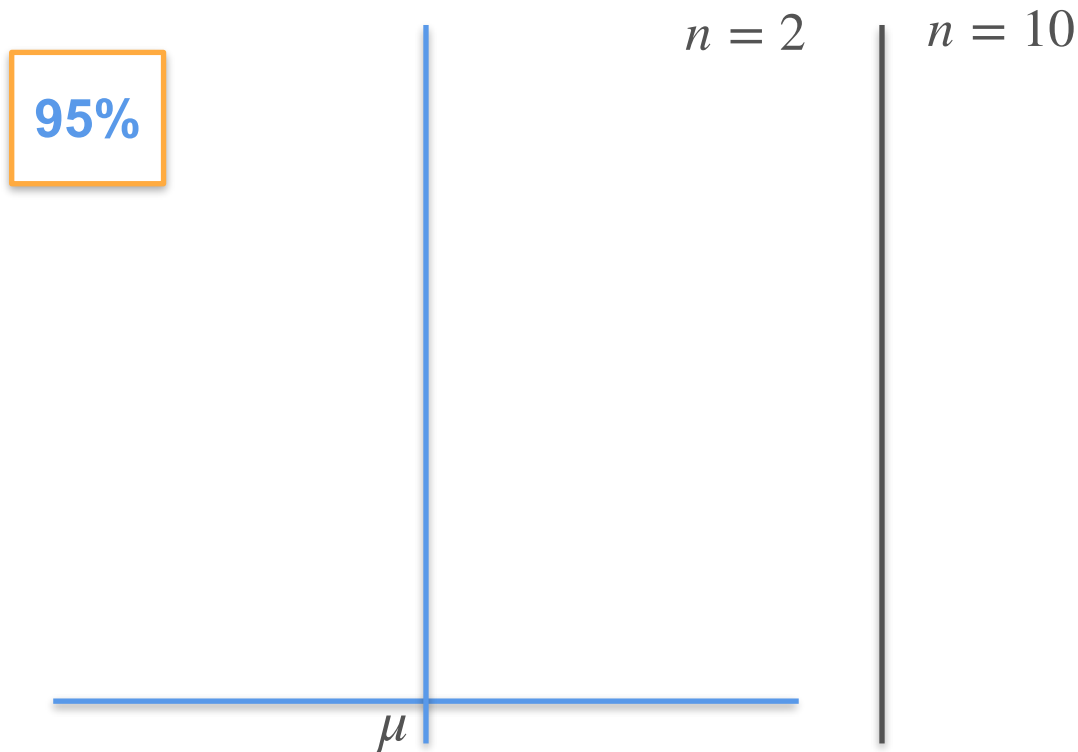
Confidence Interval - Intuition

95%

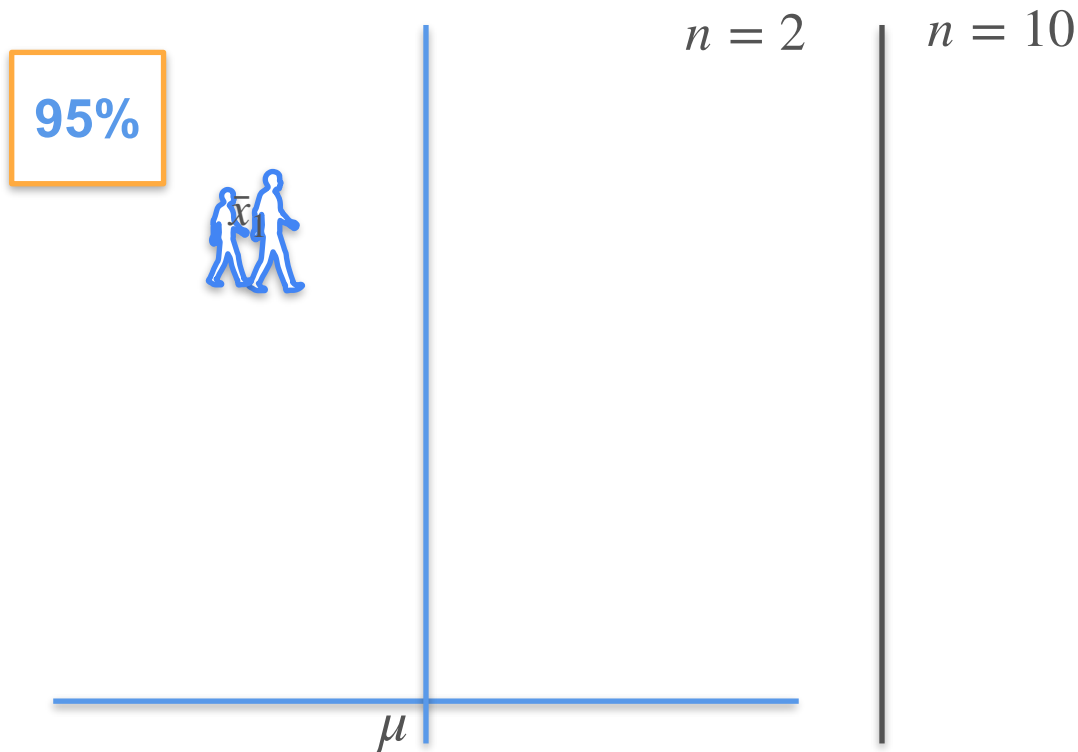
$n = 2$

$n = 10$

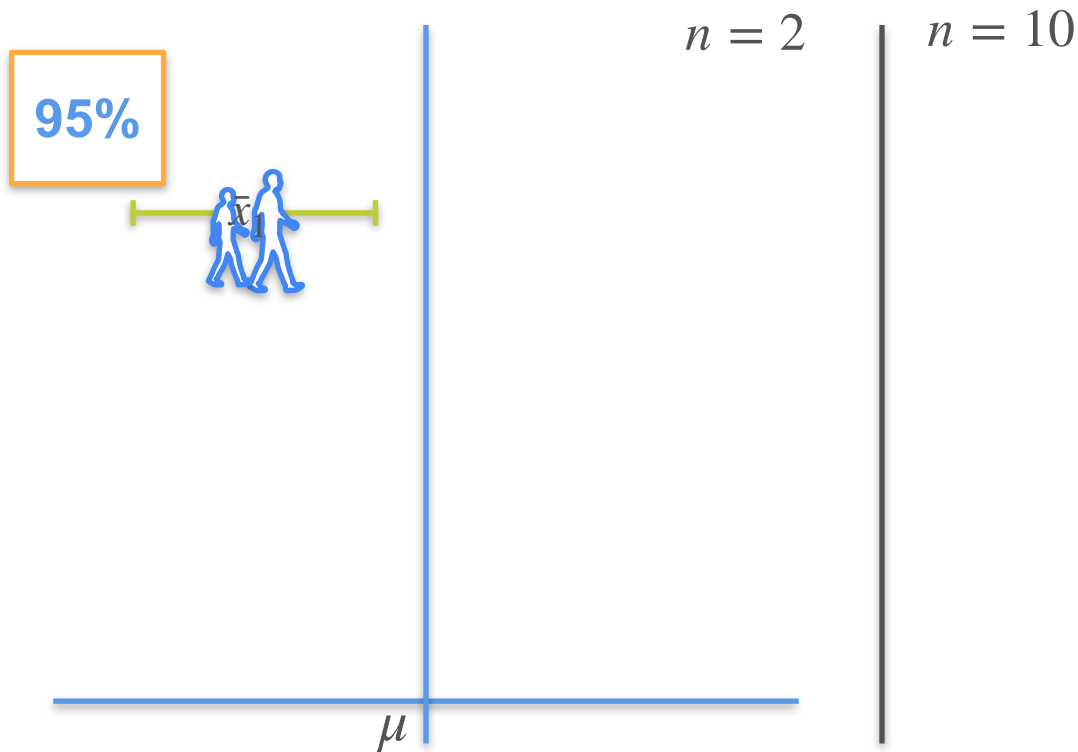
Confidence Interval - Intuition



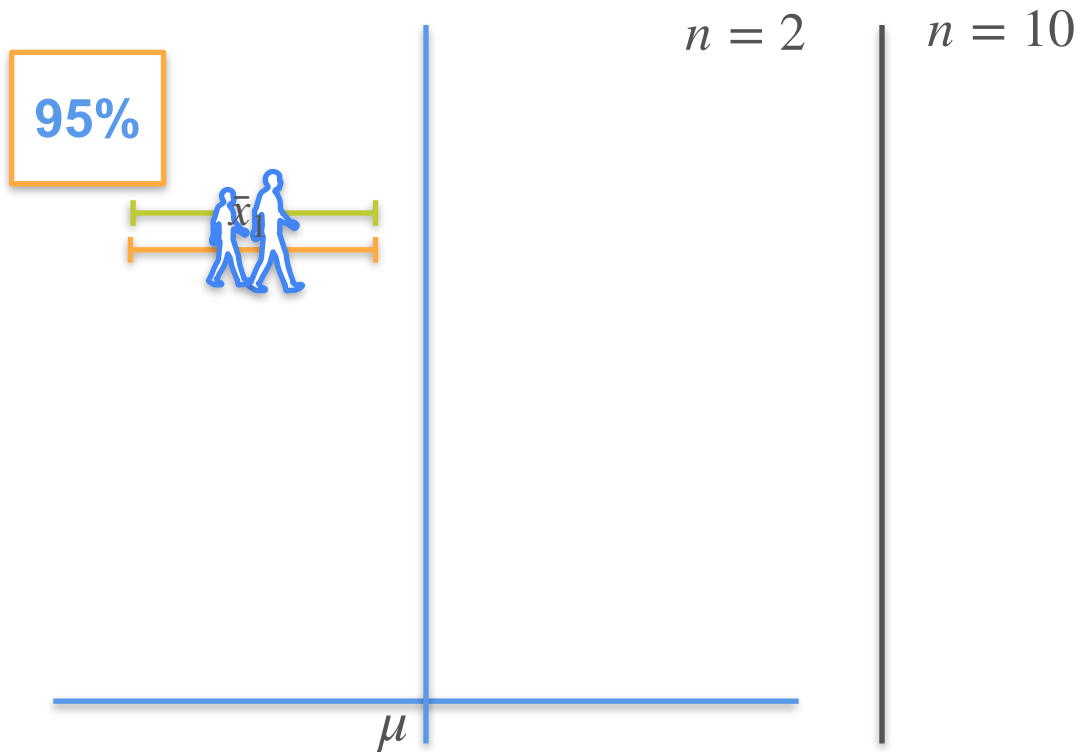
Confidence Interval - Intuition



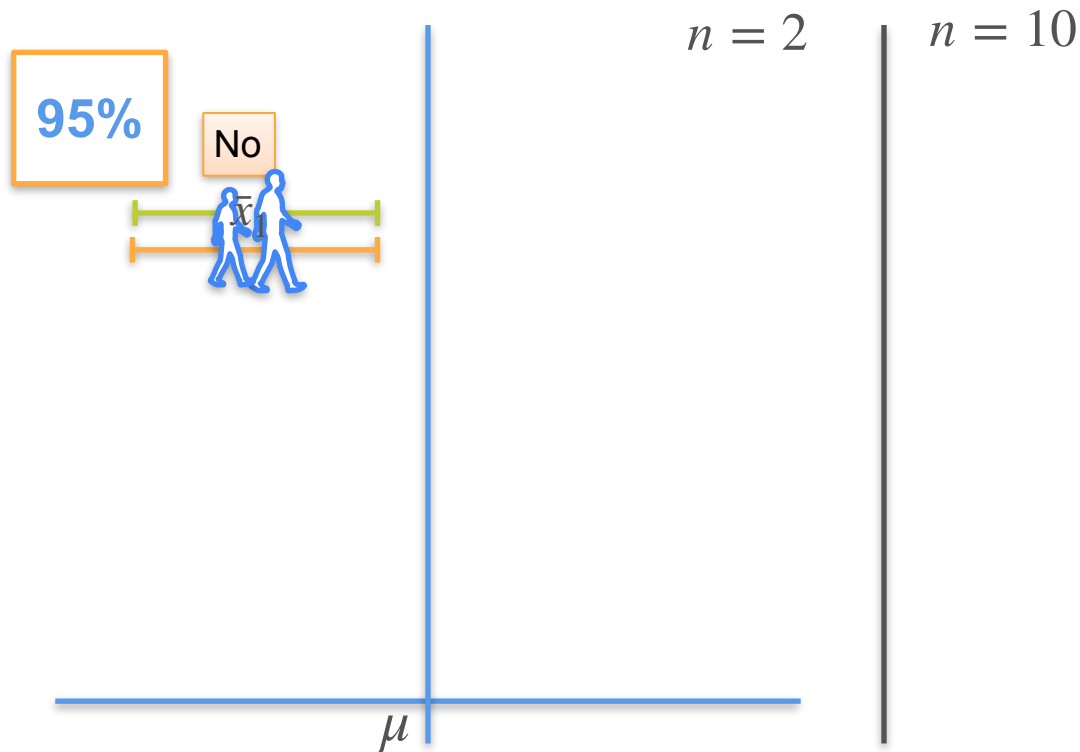
Confidence Interval - Intuition



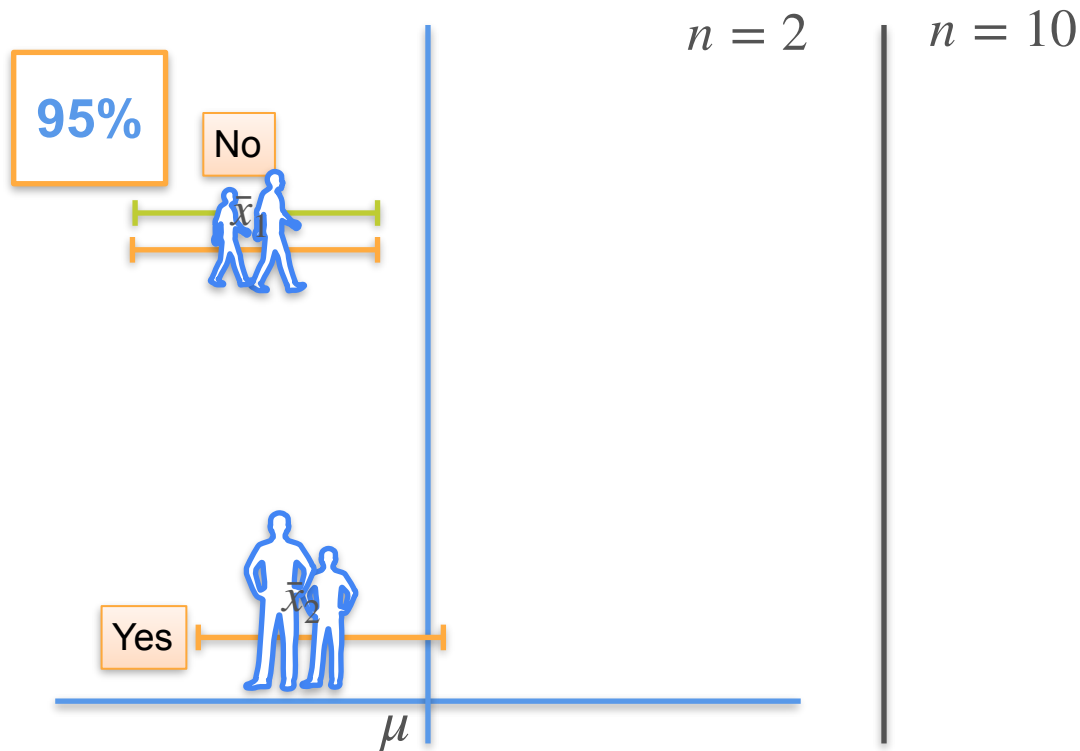
Confidence Interval - Intuition



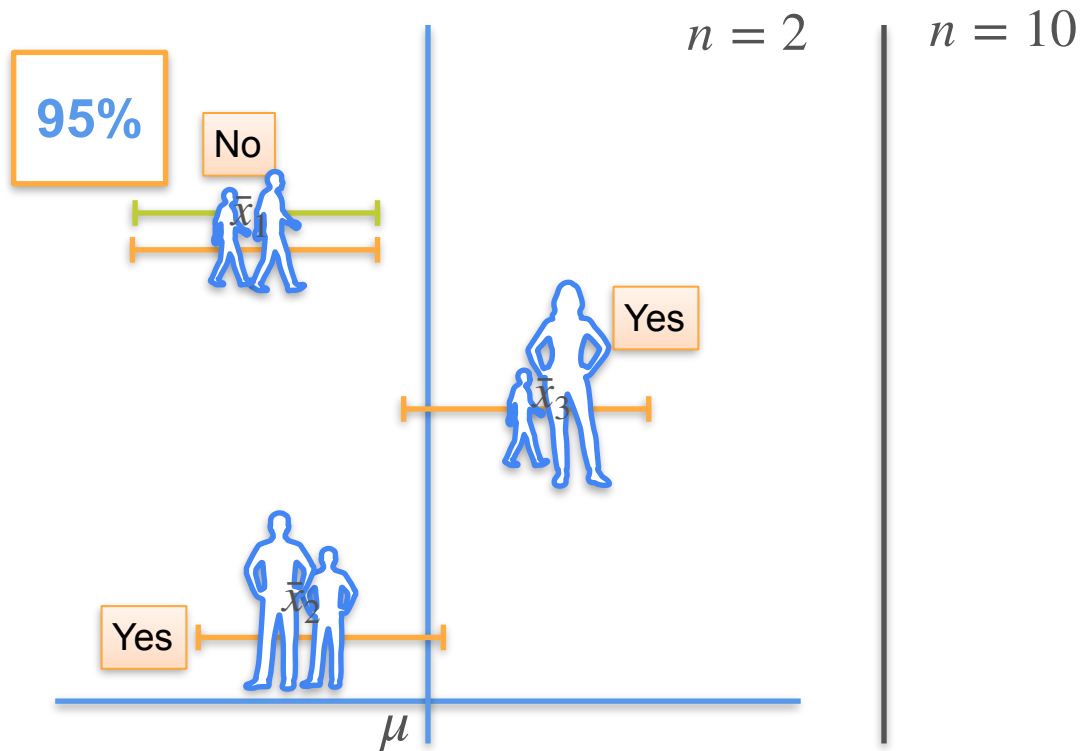
Confidence Interval - Intuition



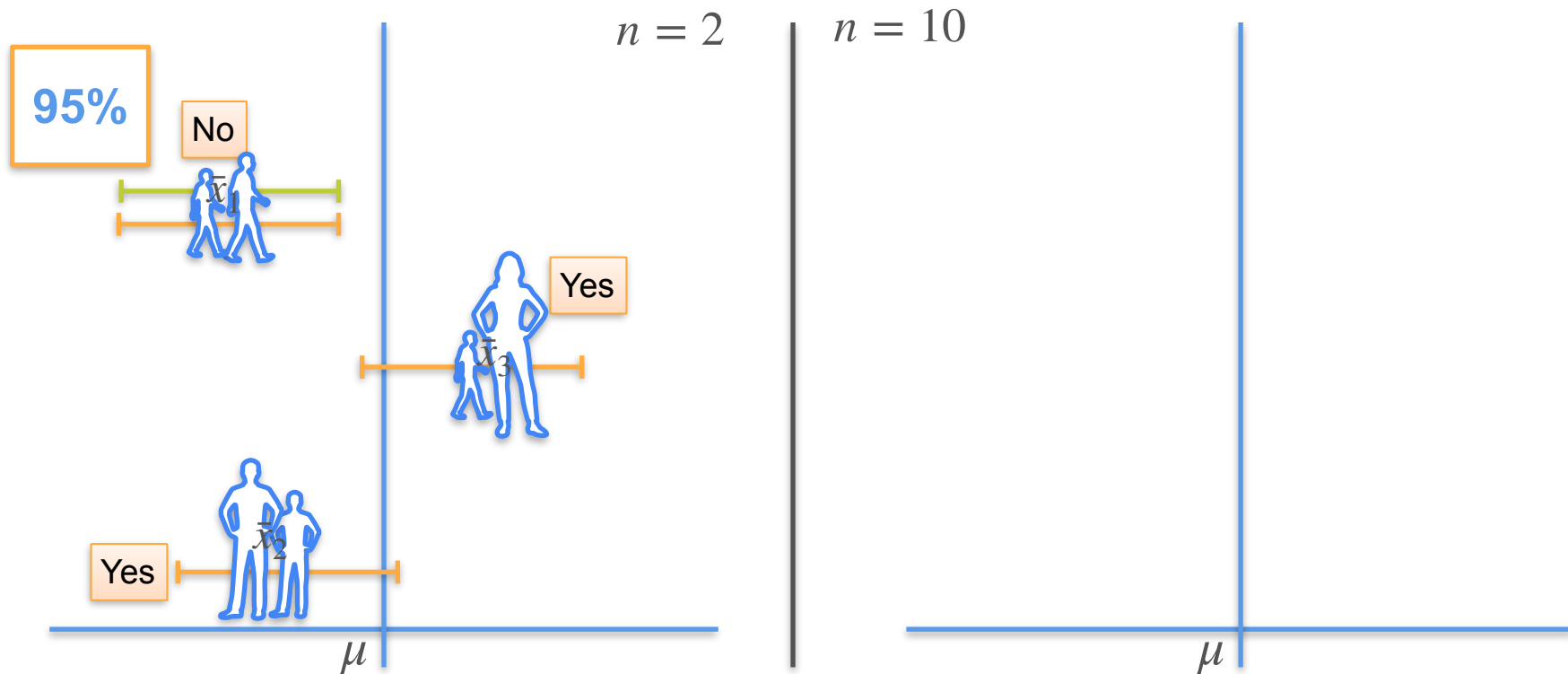
Confidence Interval - Intuition



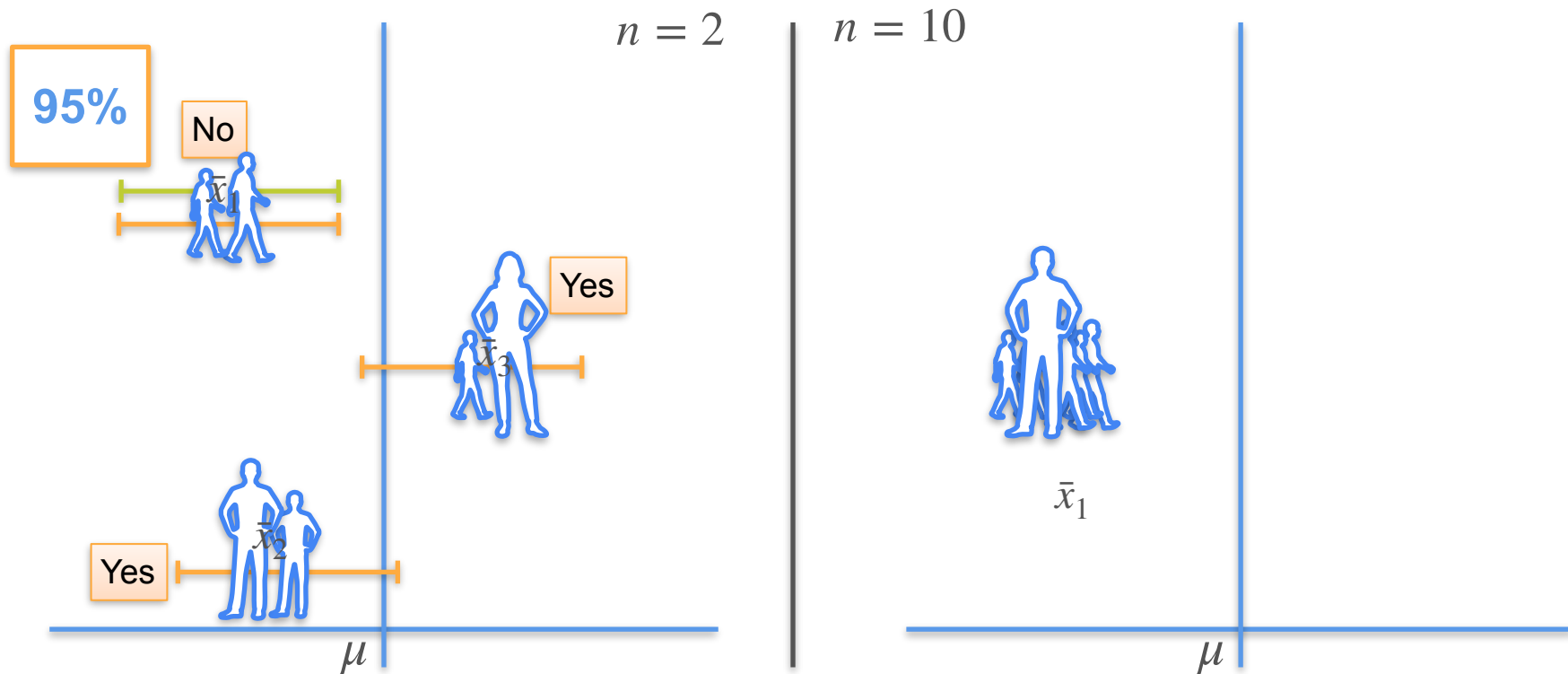
Confidence Interval - Intuition



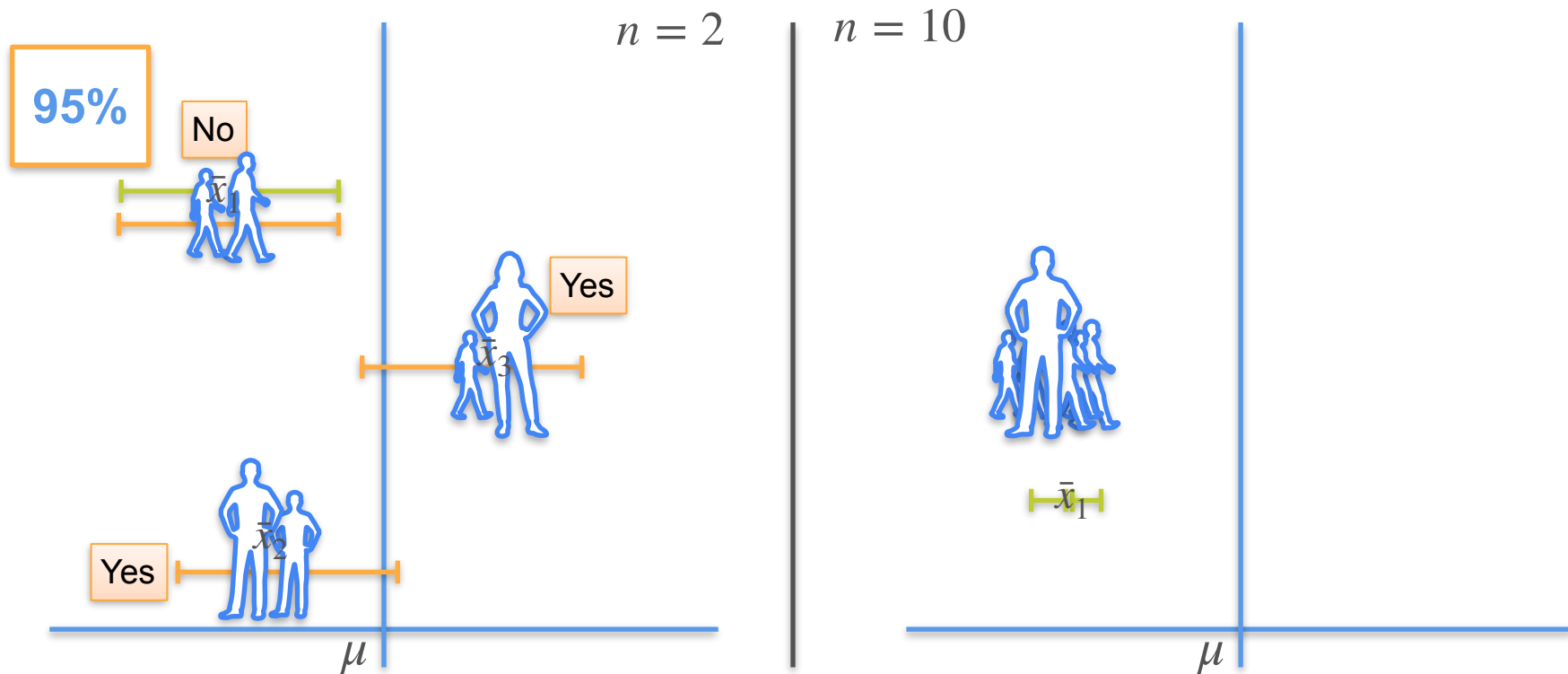
Confidence Interval - Intuition



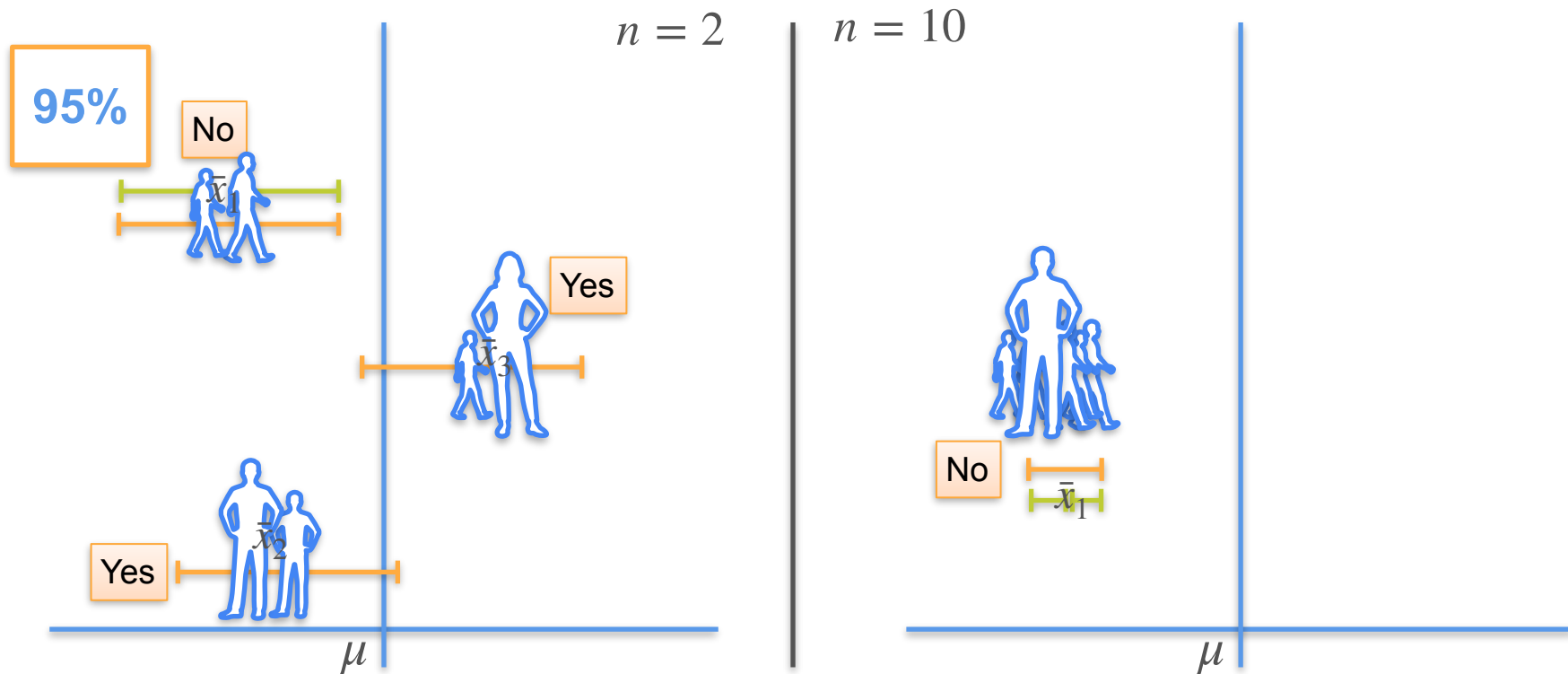
Confidence Interval - Intuition



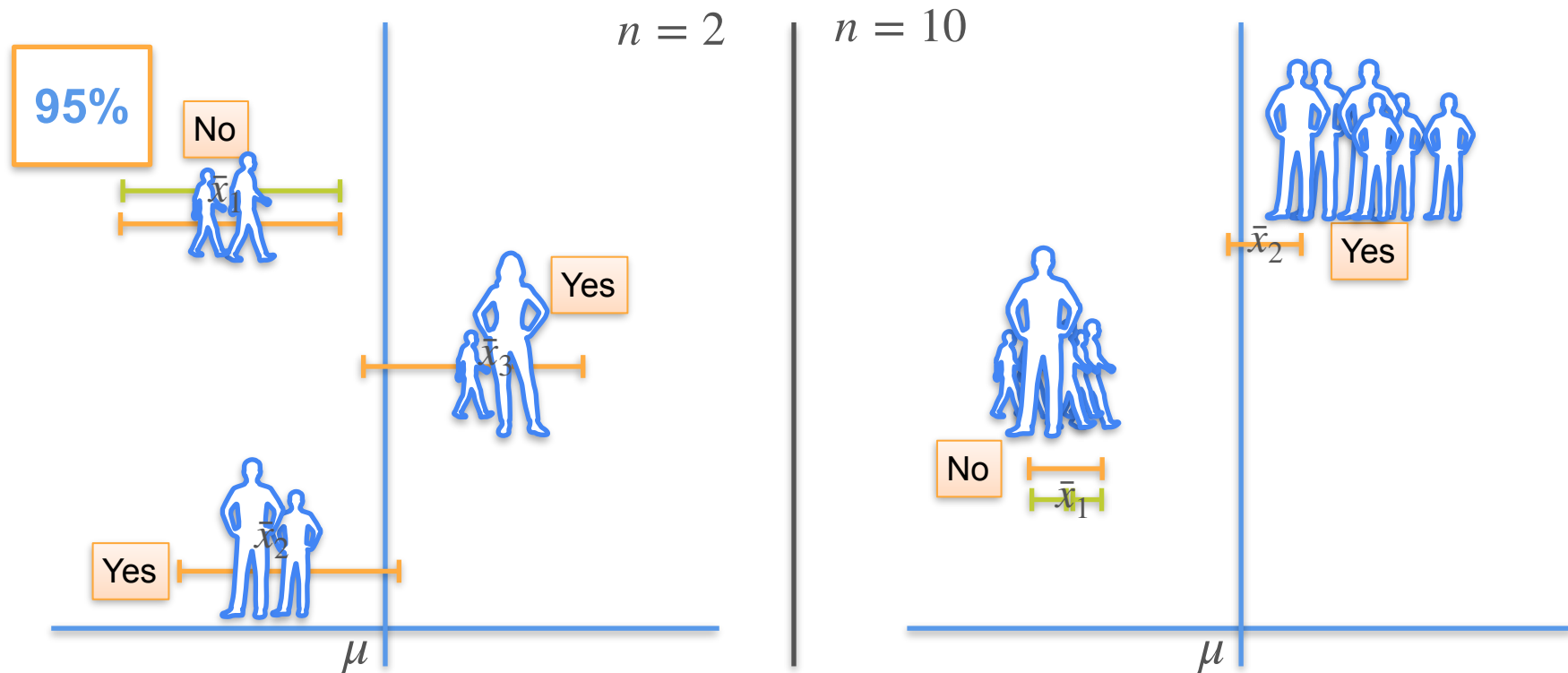
Confidence Interval - Intuition



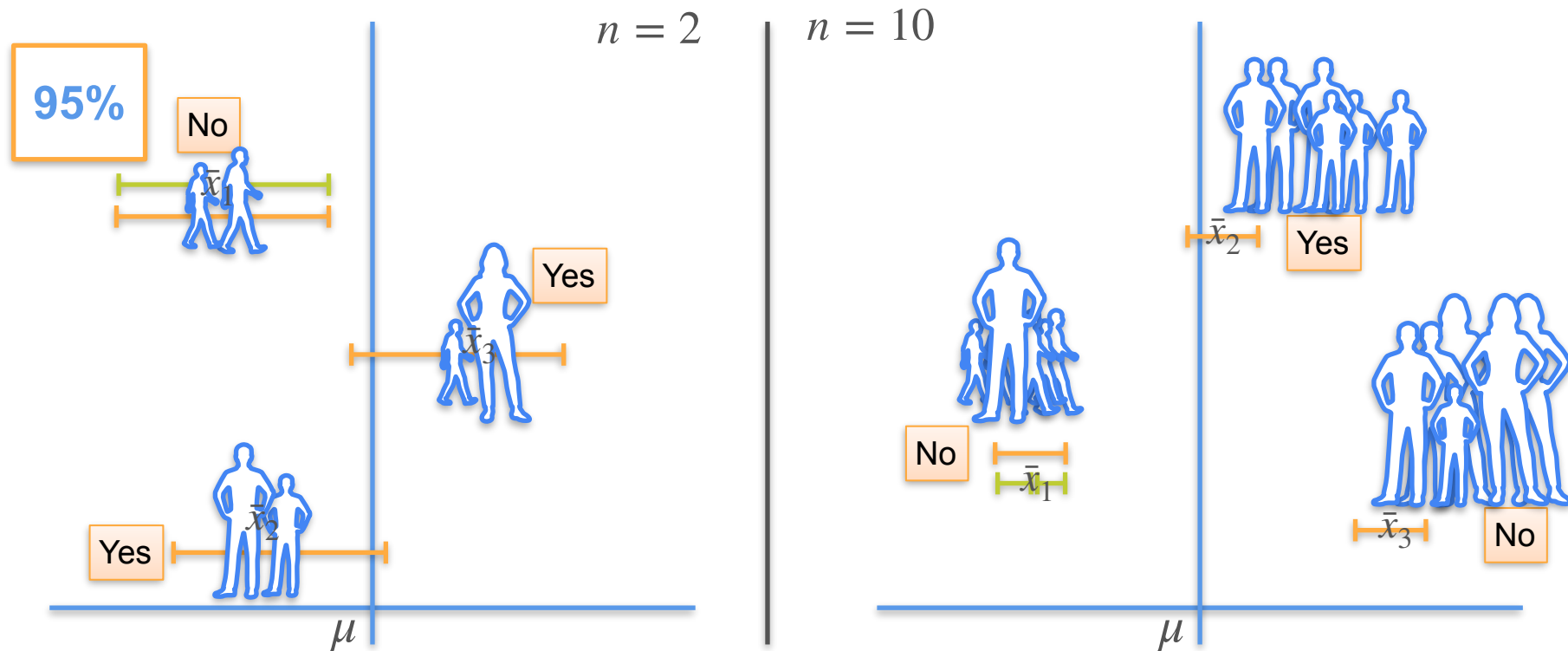
Confidence Interval - Intuition



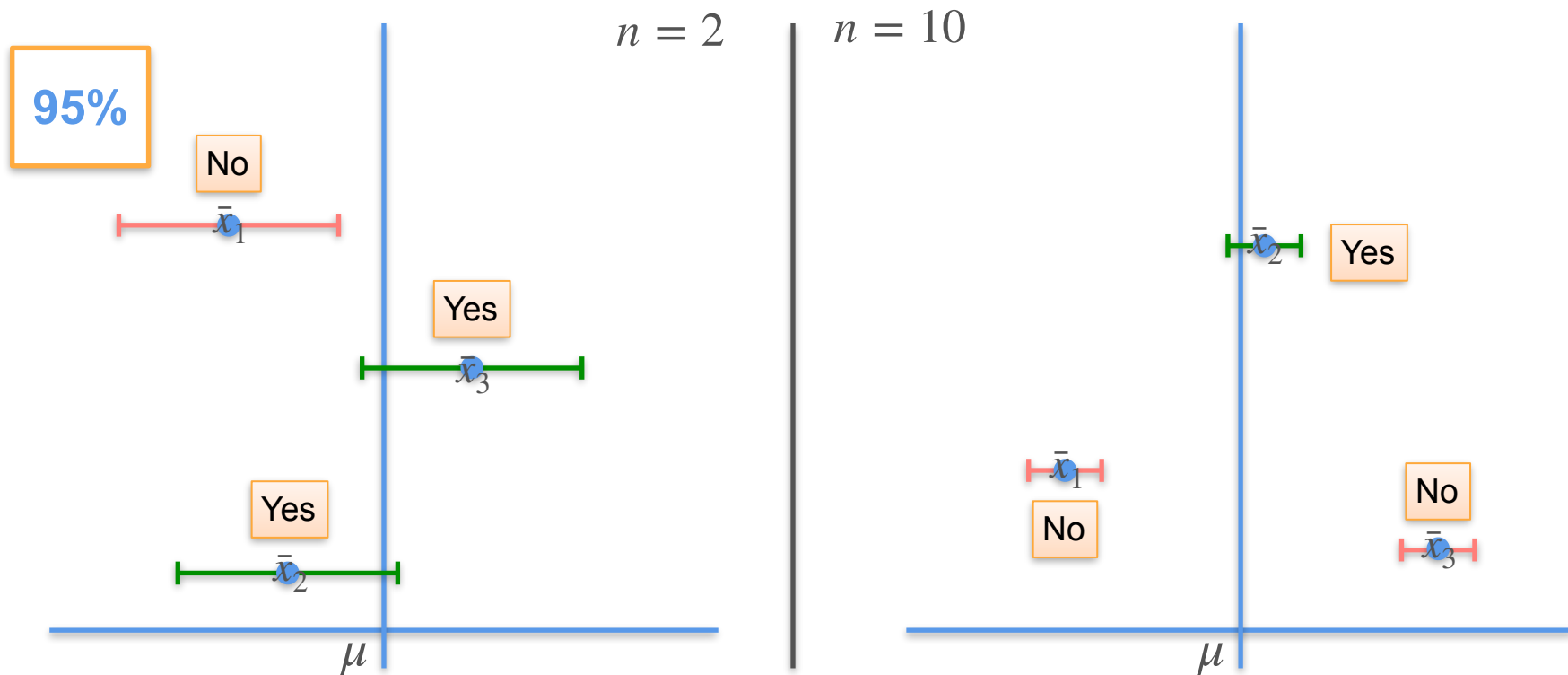
Confidence Interval - Intuition



Confidence Interval - Intuition



Confidence Interval - Intuition

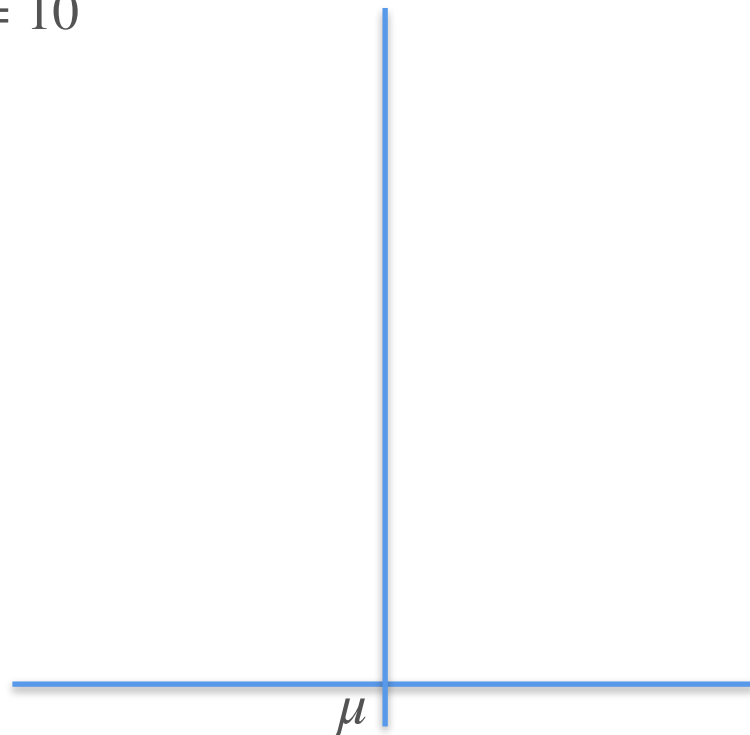
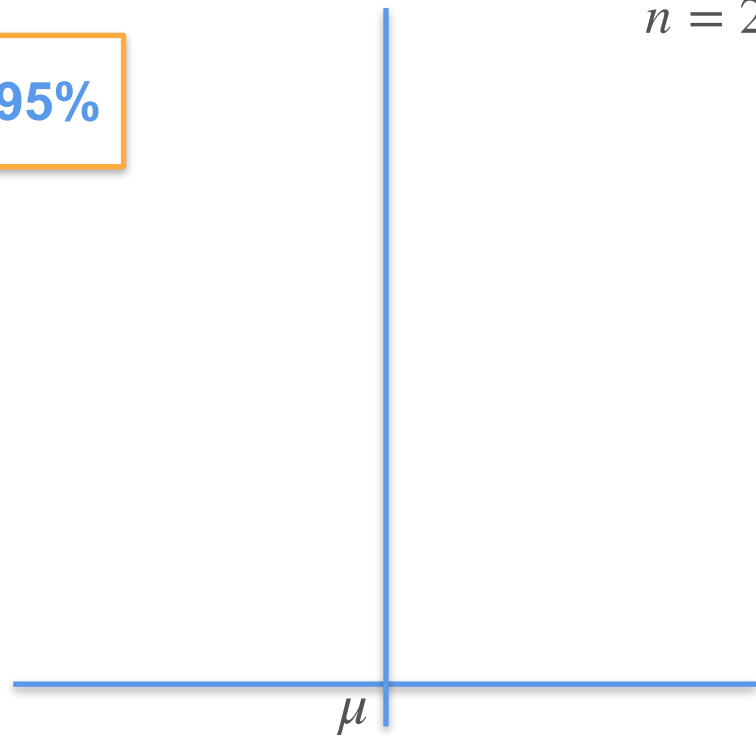


Confidence Interval - Intuition

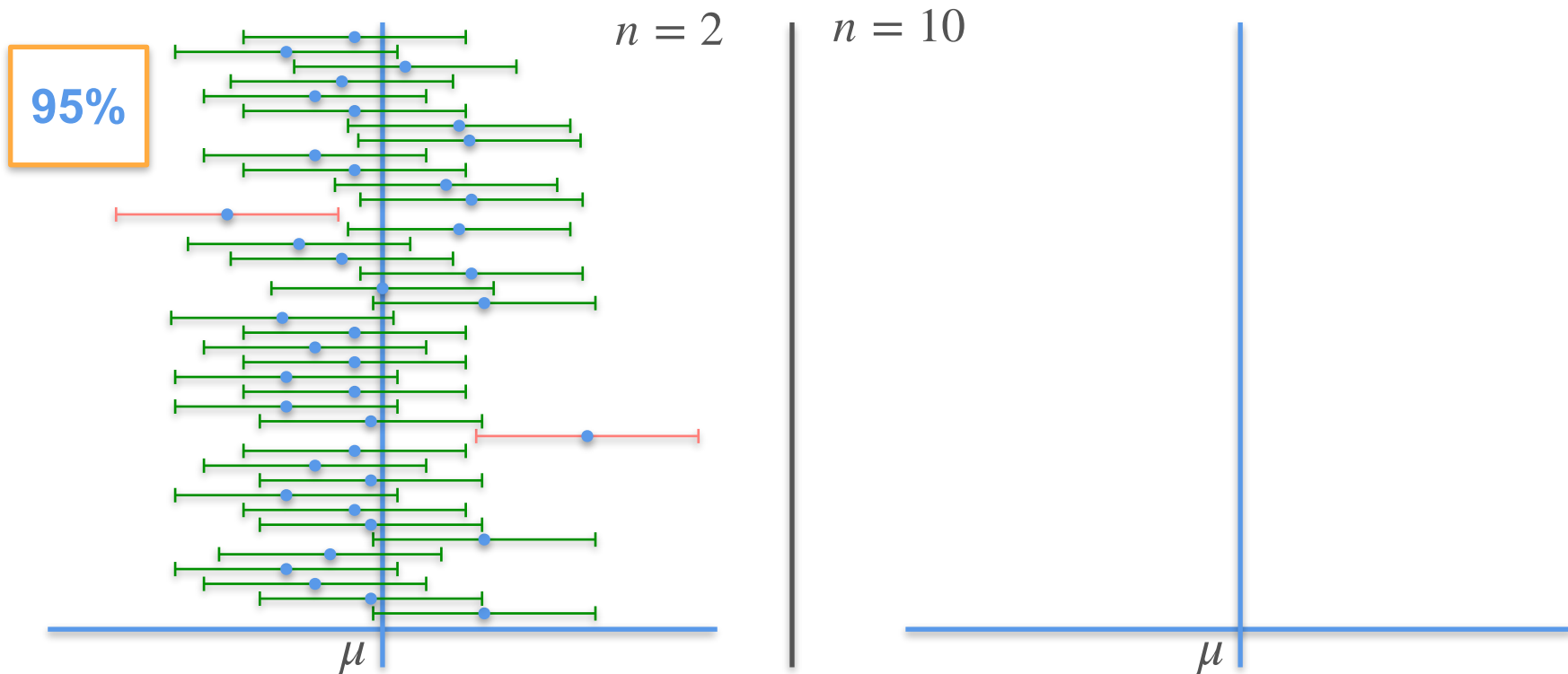
95%

$n = 2$

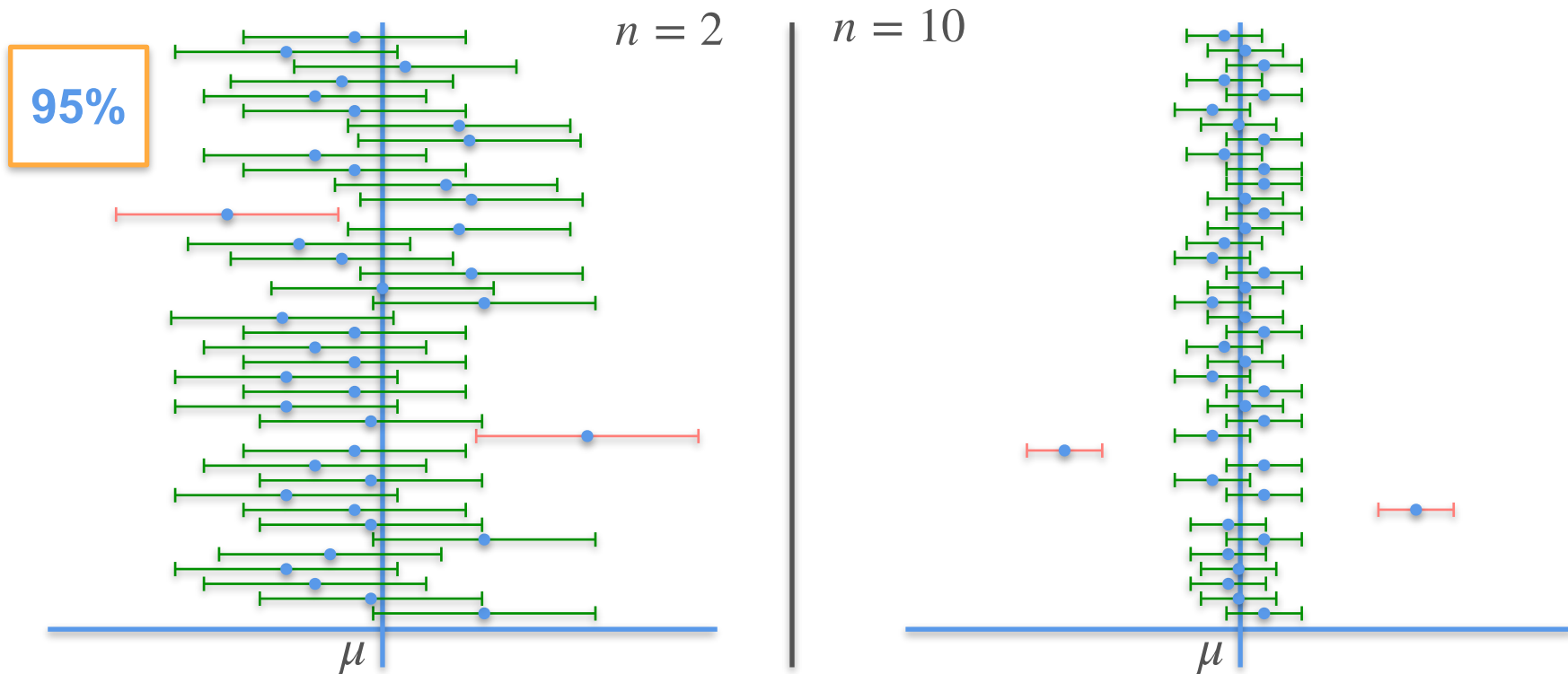
$n = 10$



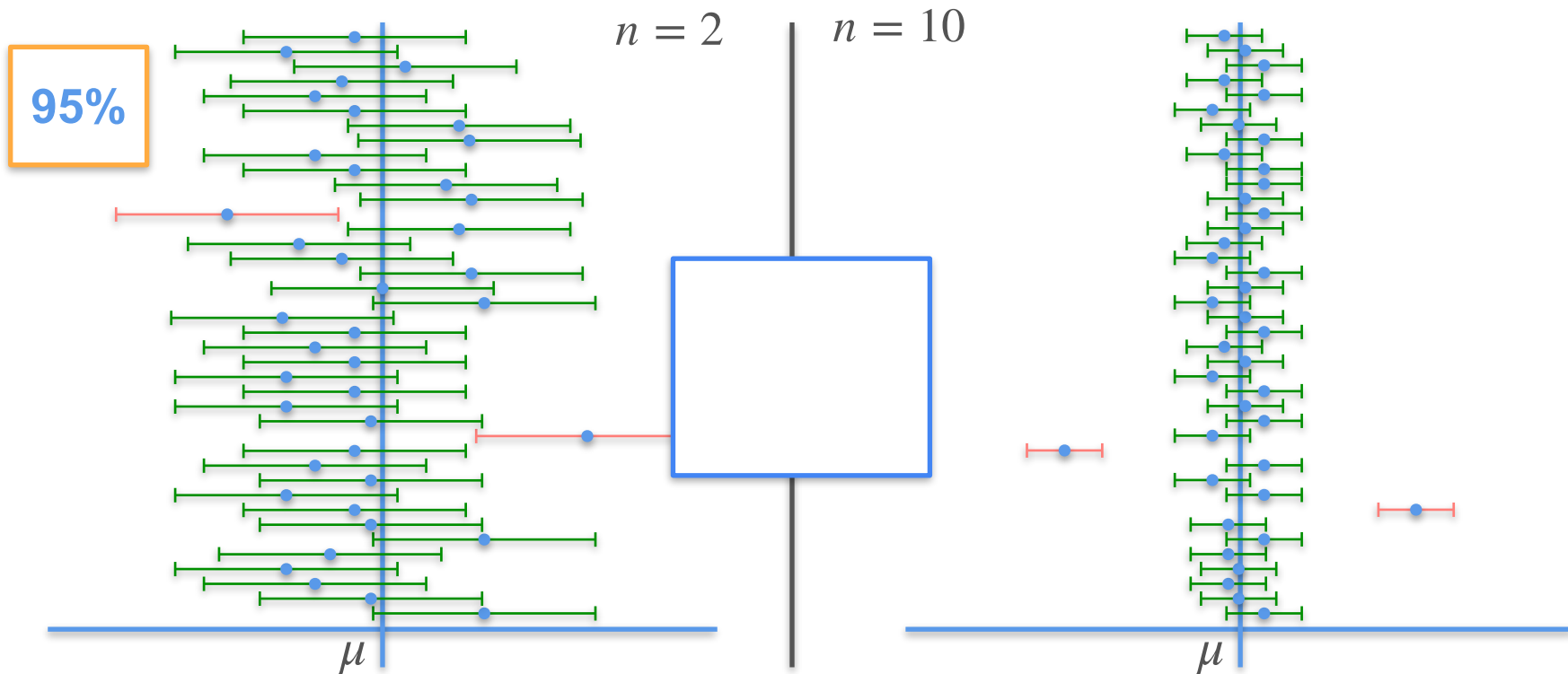
Confidence Interval - Intuition



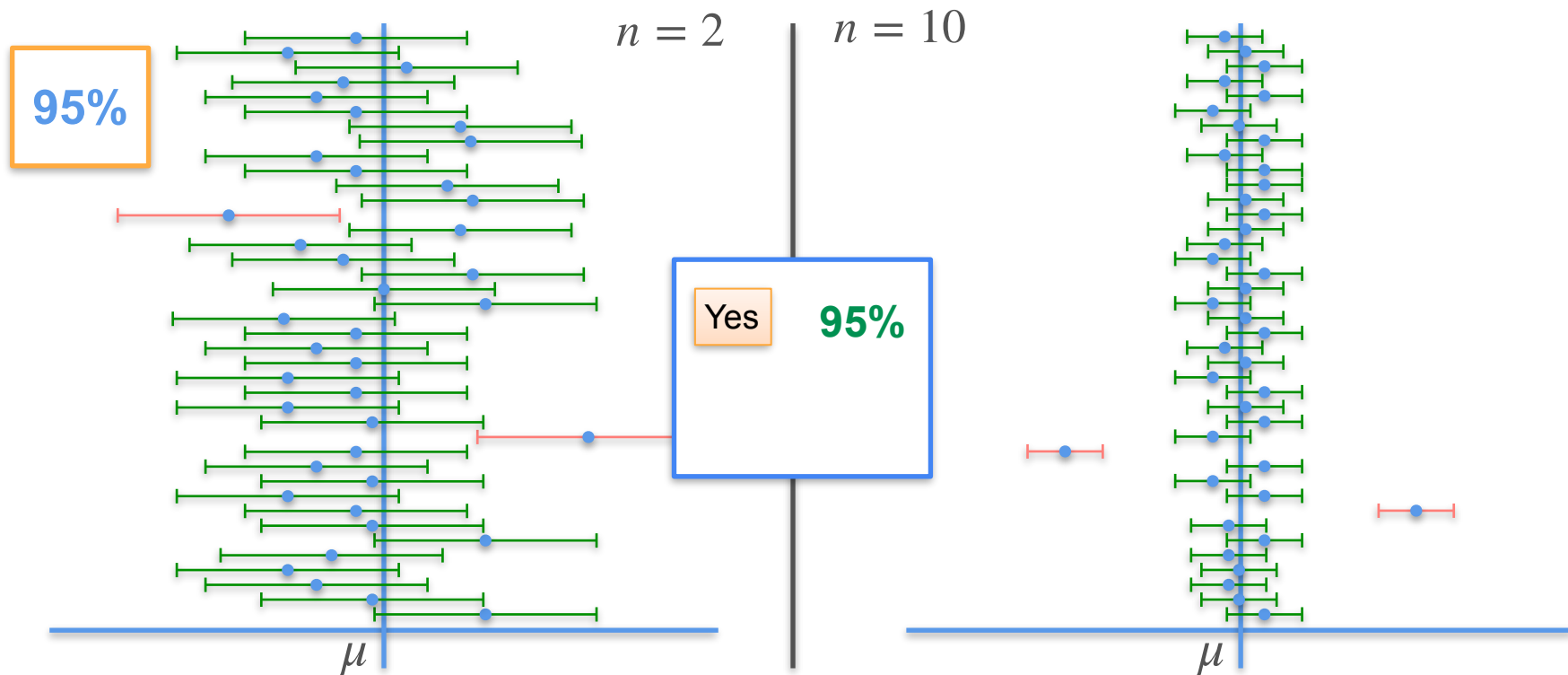
Confidence Interval - Intuition



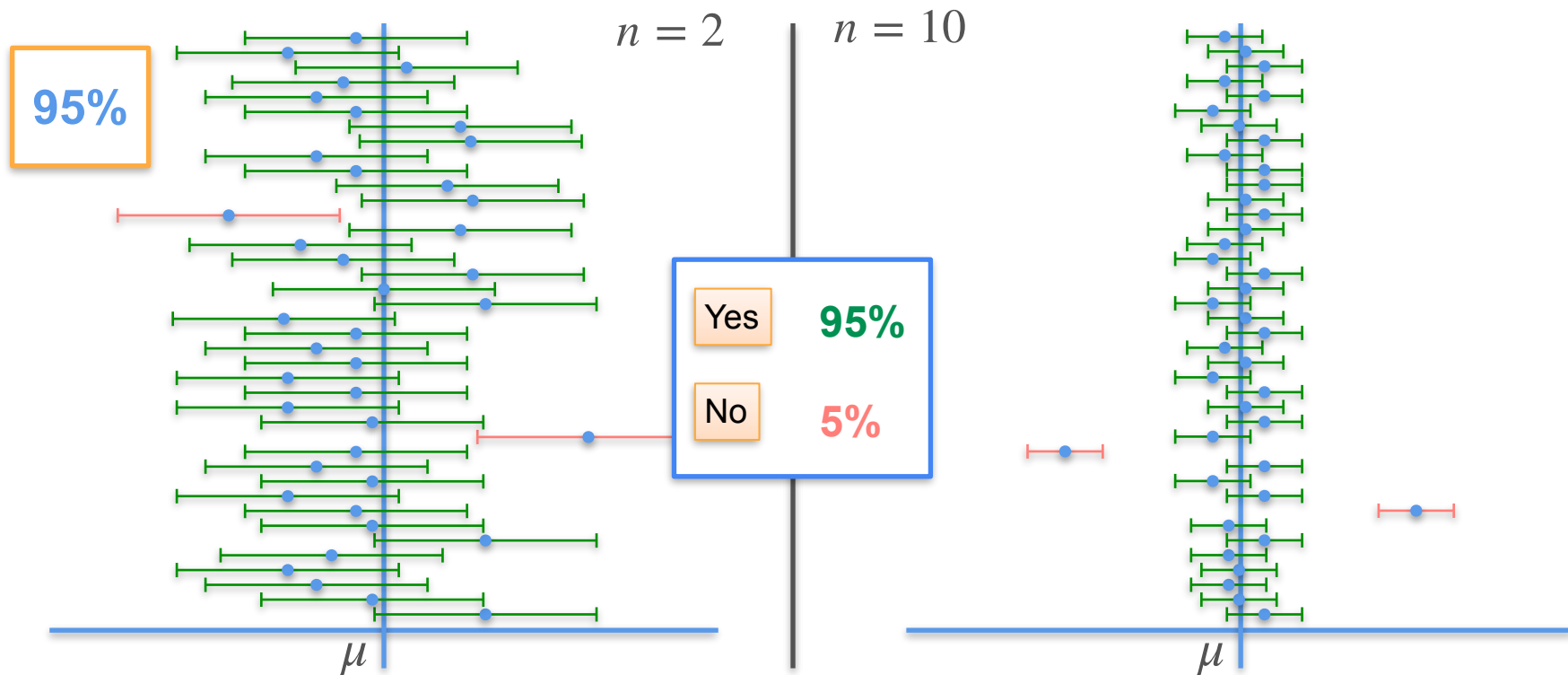
Confidence Interval - Intuition



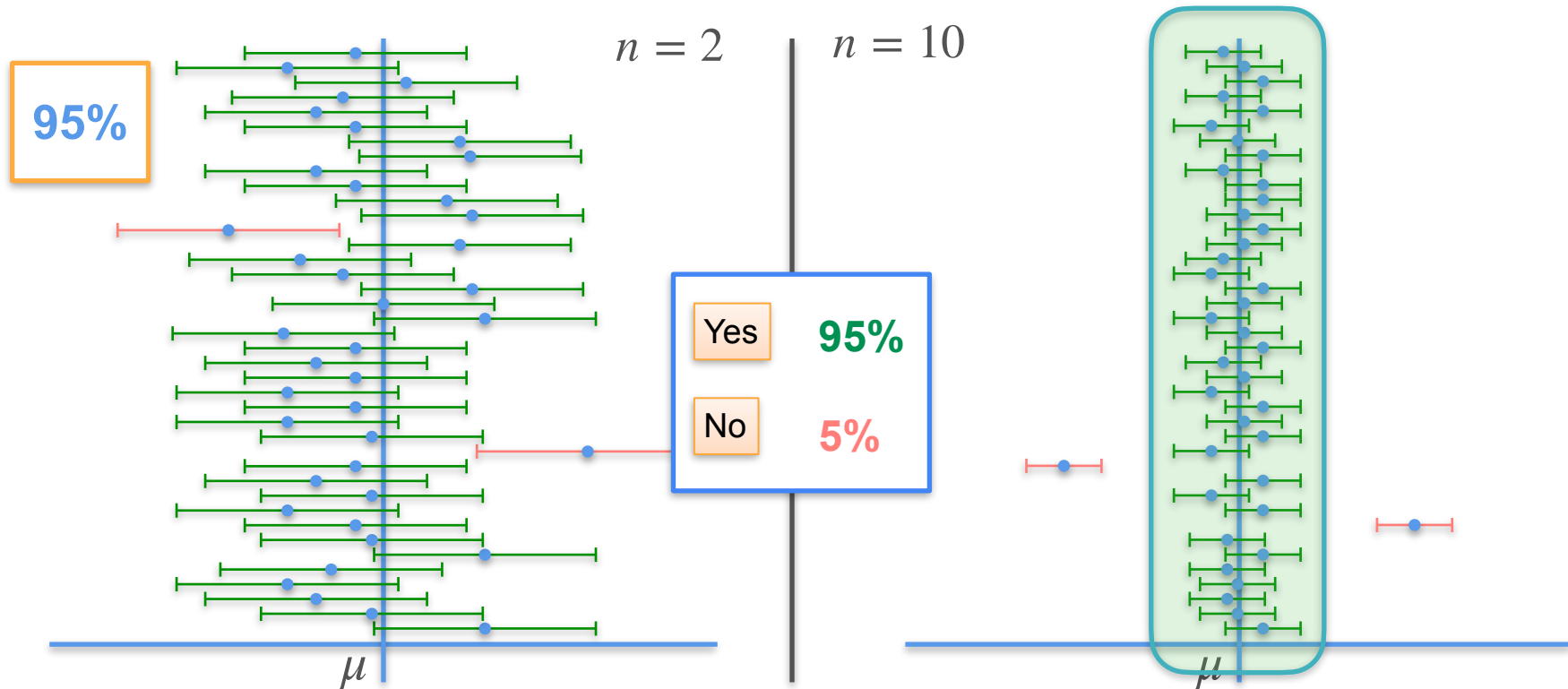
Confidence Interval - Intuition



Confidence Interval - Intuition



Confidence Interval - Intuition



Effect of the Sample Size

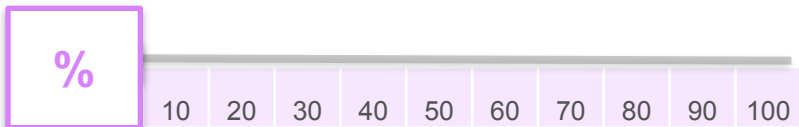


Effect of the Sample Size

sample size



Confidence level

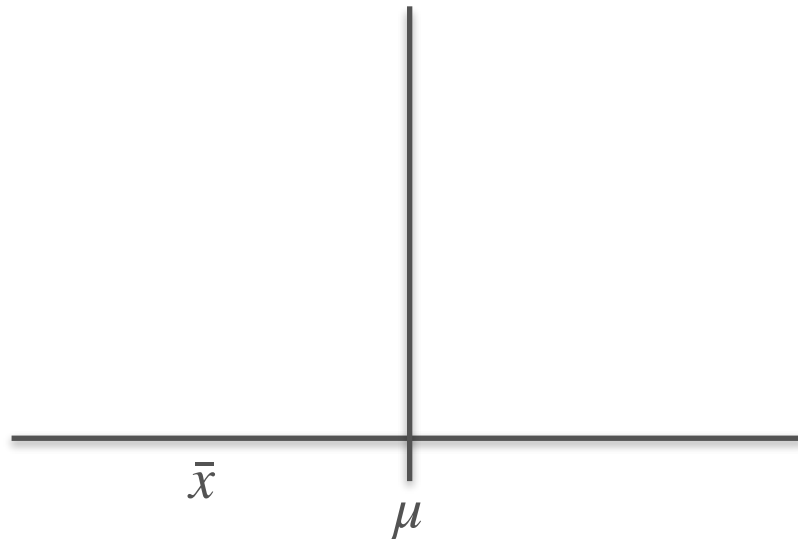
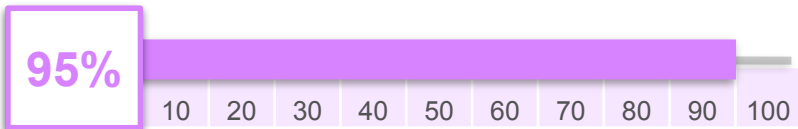


Effect of the Sample Size

sample size



Confidence level

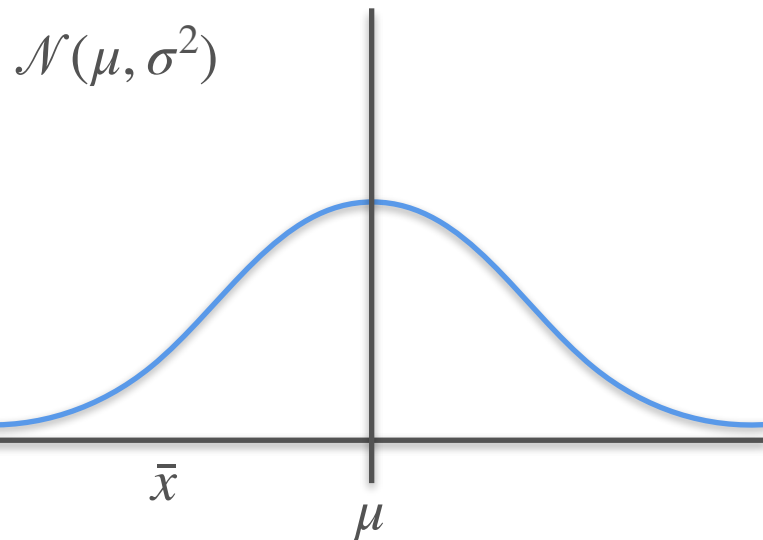
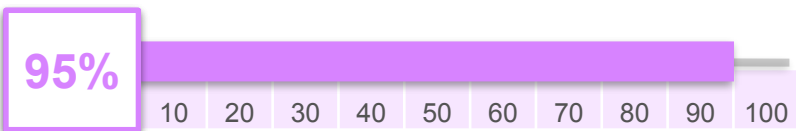


Effect of the Sample Size

sample size



Confidence level

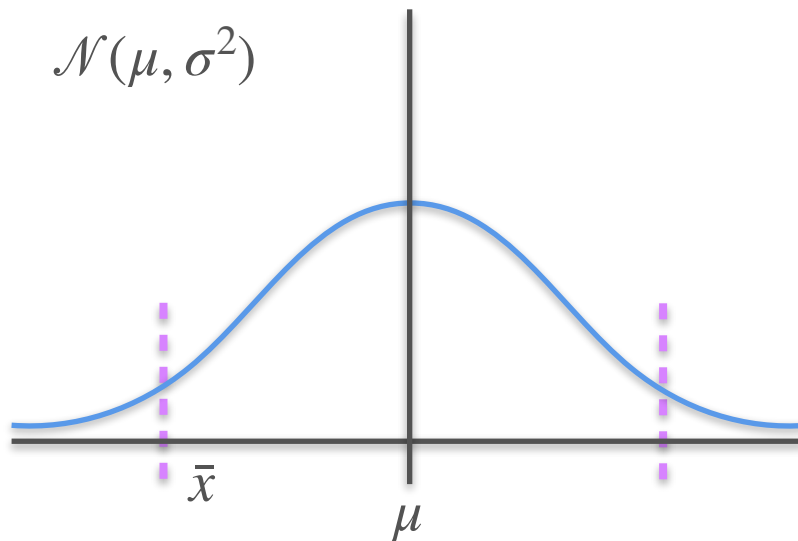
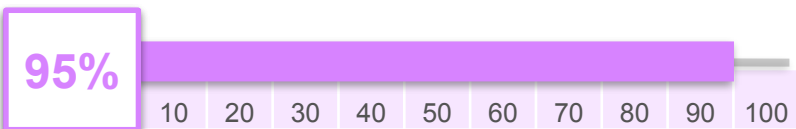


Effect of the Sample Size

sample size



Confidence level

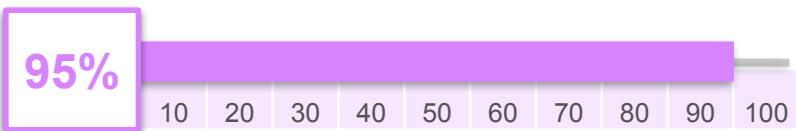


Effect of the Sample Size

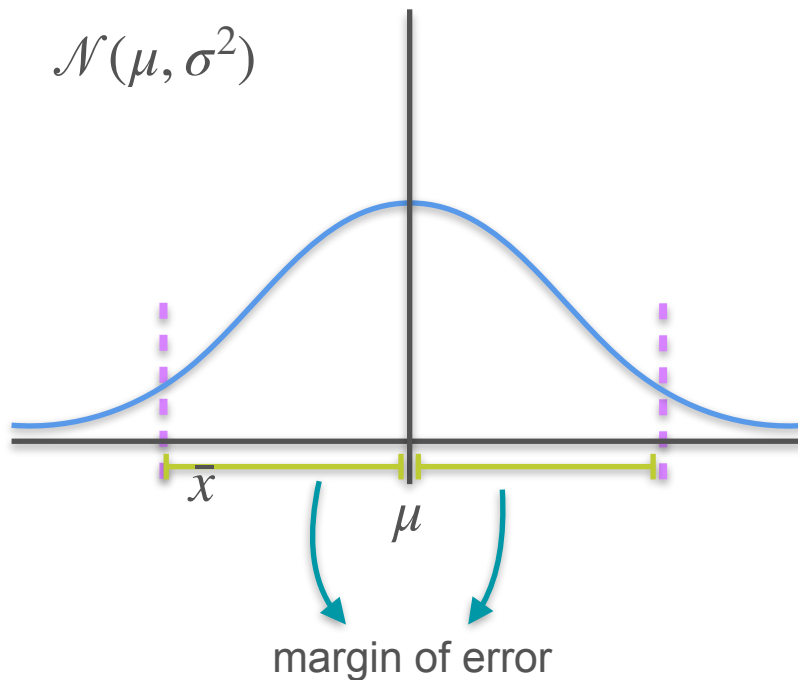
sample size



Confidence level

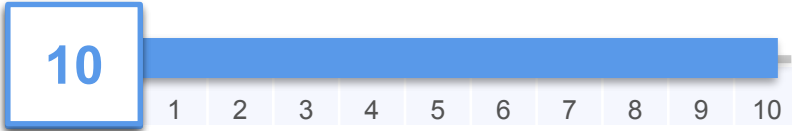


$$\mathcal{N}(\mu, \sigma^2)$$

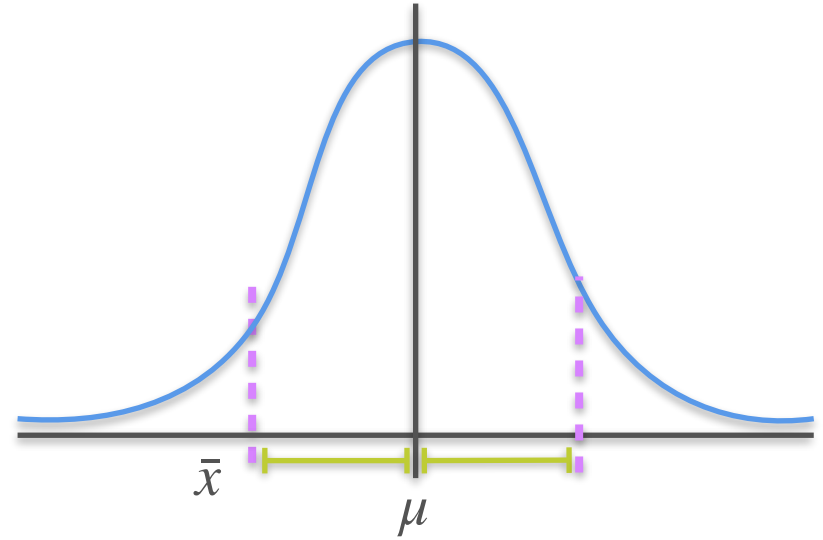
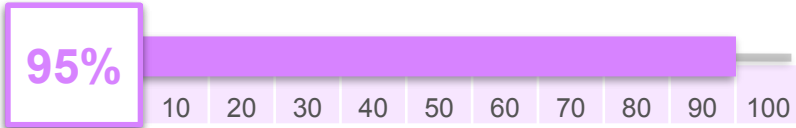


Effect of the Sample Size

sample size

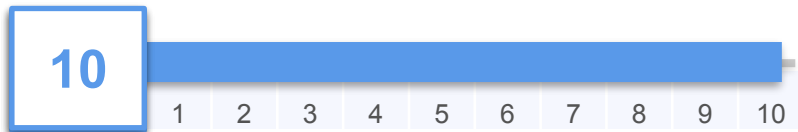


Confidence level

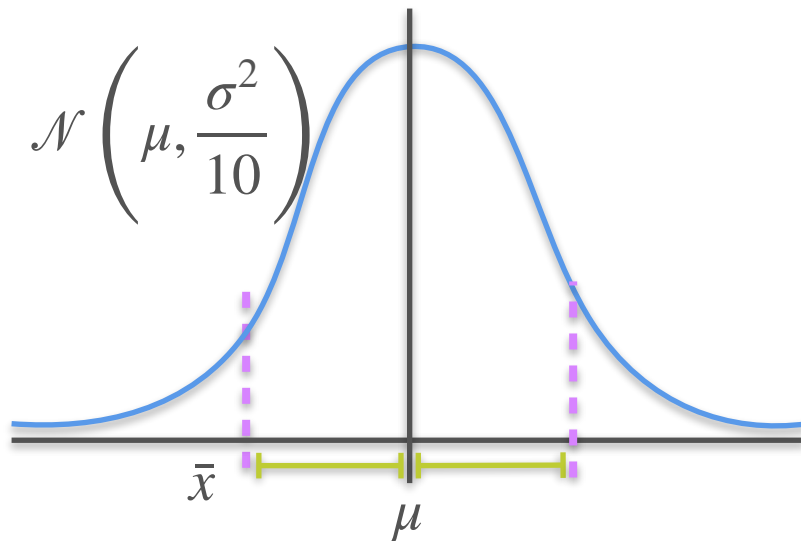
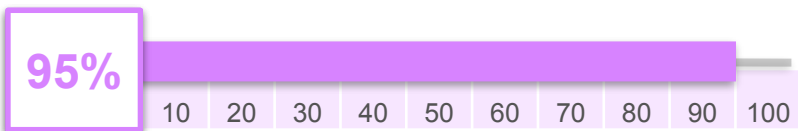


Effect of the Sample Size

sample size

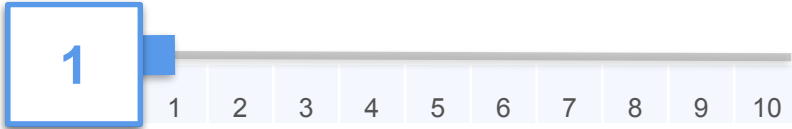


Confidence level

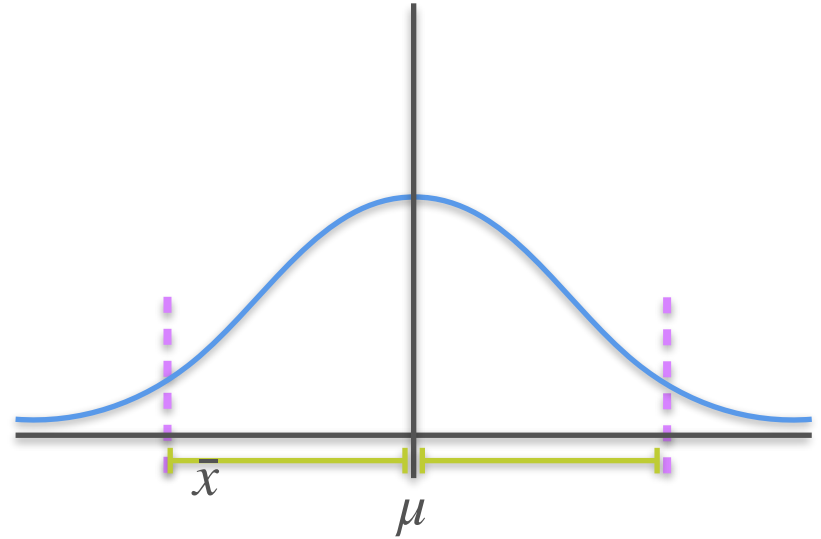
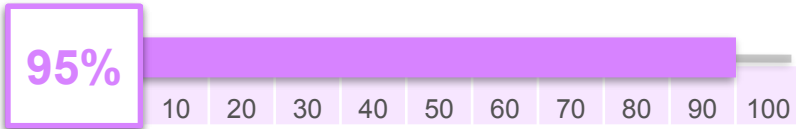


Effect of the Sample Size

sample size



Confidence level

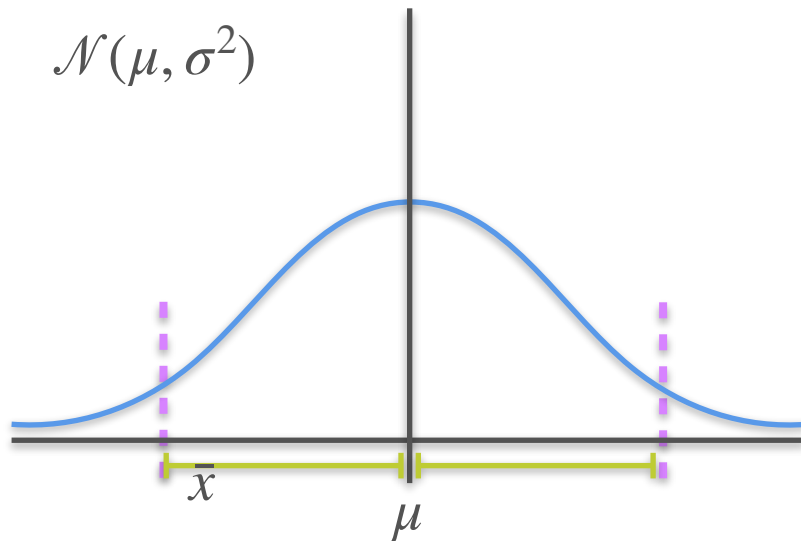
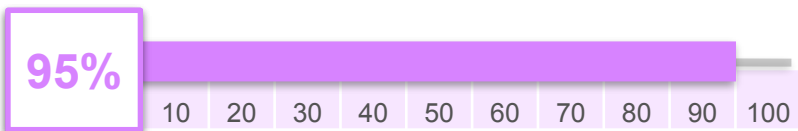


Effect of the Sample Size

sample size

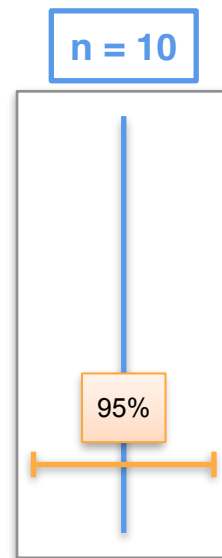
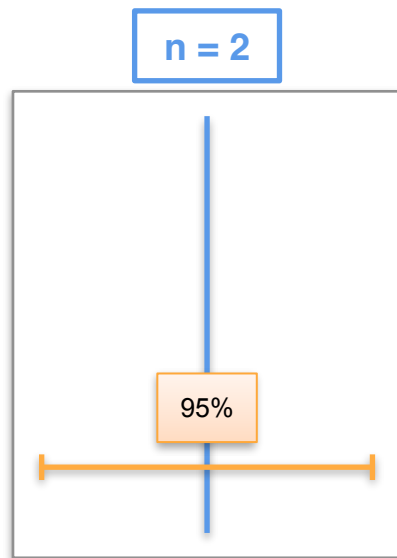
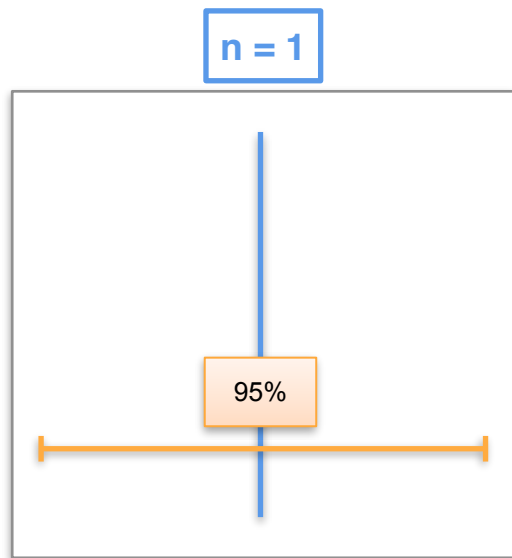


Confidence level

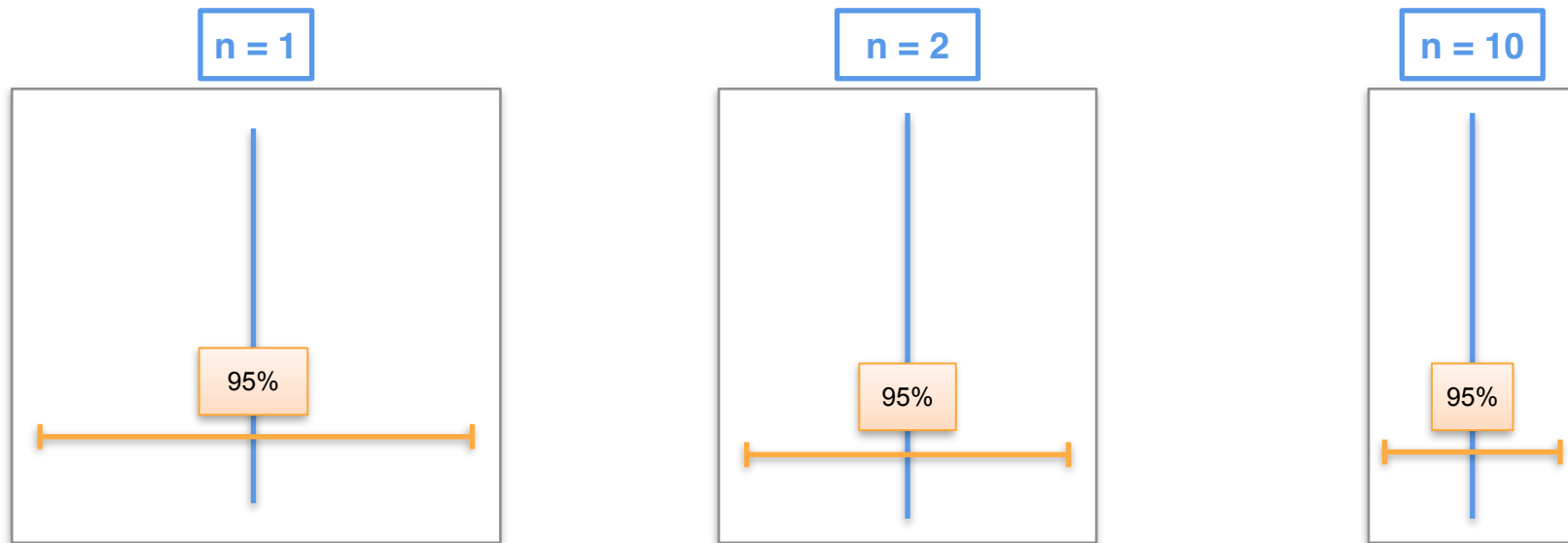


Effect of the Sample Size

Effect of the Sample Size



Effect of the Sample Size



As n increases, the confidence interval shrinks

Effect of the Confidence Level



Effect of the Confidence Level

$$n = 1$$



Effect of the Confidence Level

$$n = 1$$

$$\mathcal{N}(\mu, \sigma^2)$$

Effect of the Confidence Level

$$n = 1$$

95%

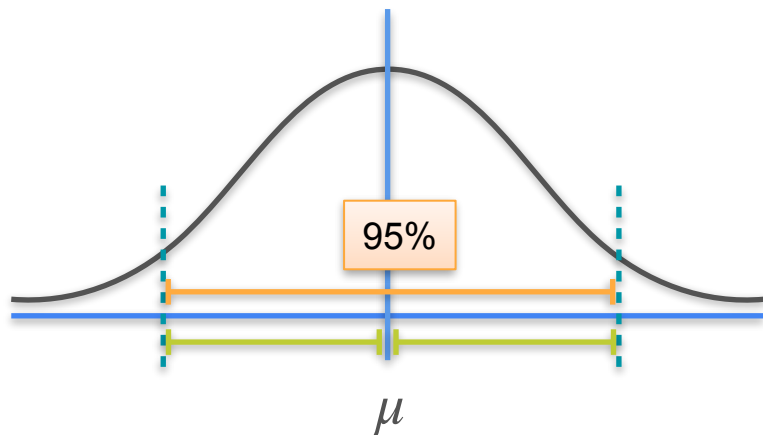
$$\mathcal{N}(\mu, \sigma^2)$$

Effect of the Confidence Level

$$n = 1$$

95%

$$\mathcal{N}(\mu, \sigma^2)$$

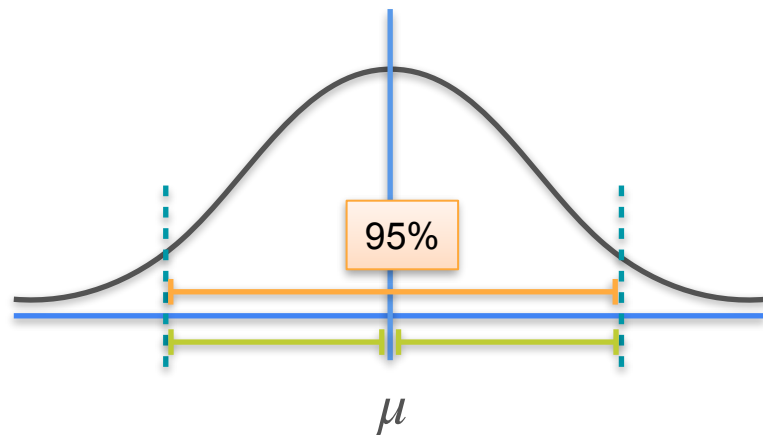
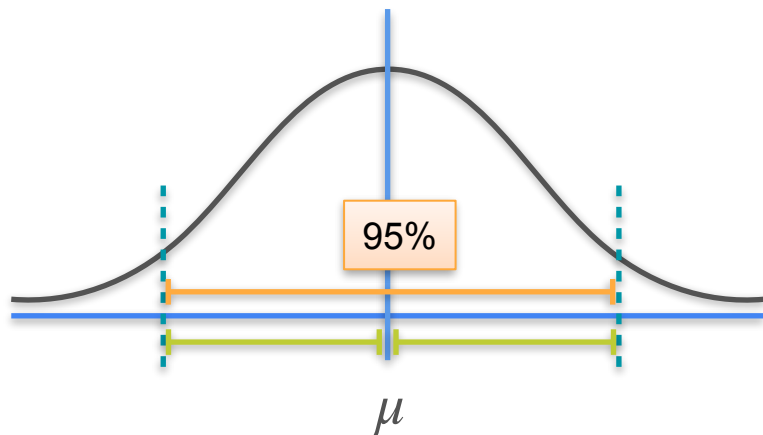


Effect of the Confidence Level

$$n = 1$$

95%

$$\mathcal{N}(\mu, \sigma^2)$$

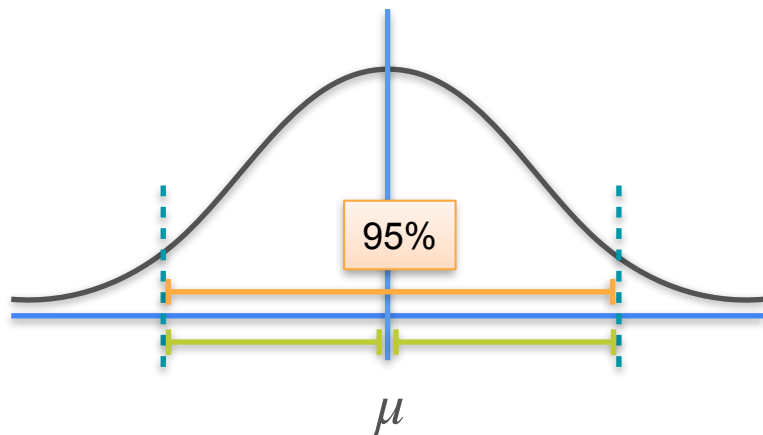


Effect of the Confidence Level

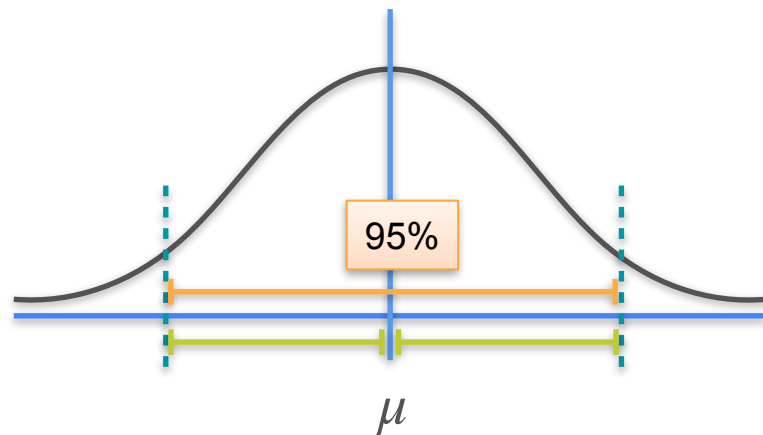
$$n = 1$$

95%

$$\mathcal{N}(\mu, \sigma^2)$$



70%

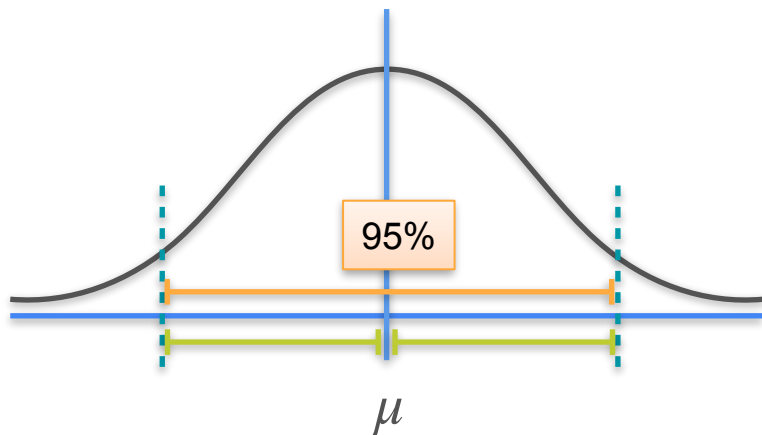


Effect of the Confidence Level

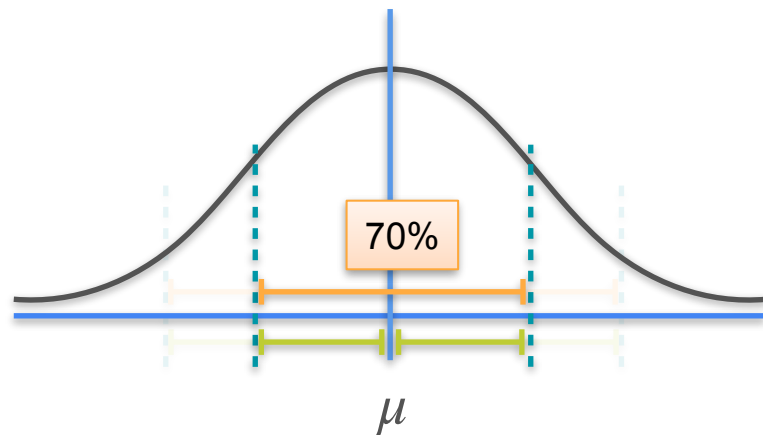
$$n = 1$$

$$\mathcal{N}(\mu, \sigma^2)$$

95%



70%

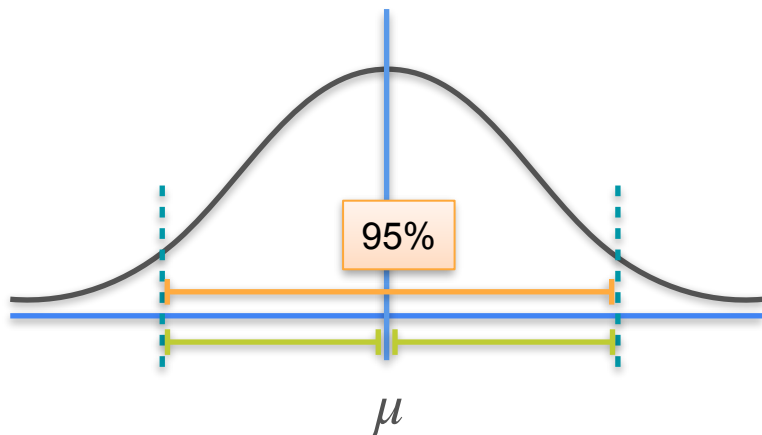


Effect of the Confidence Level

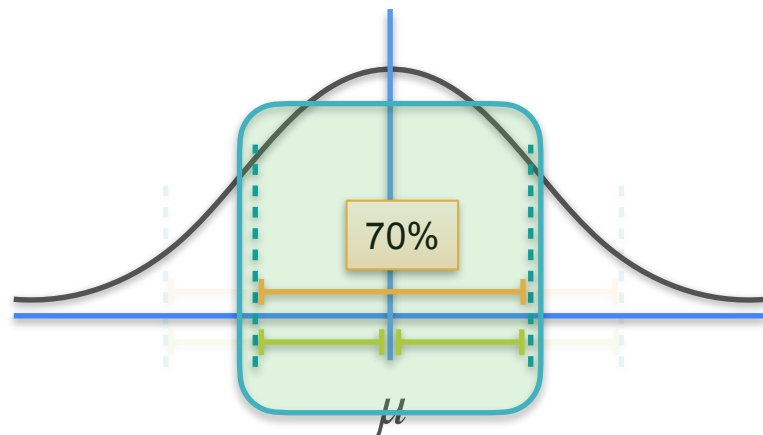
$$n = 1$$

$$\mathcal{N}(\mu, \sigma^2)$$

95%

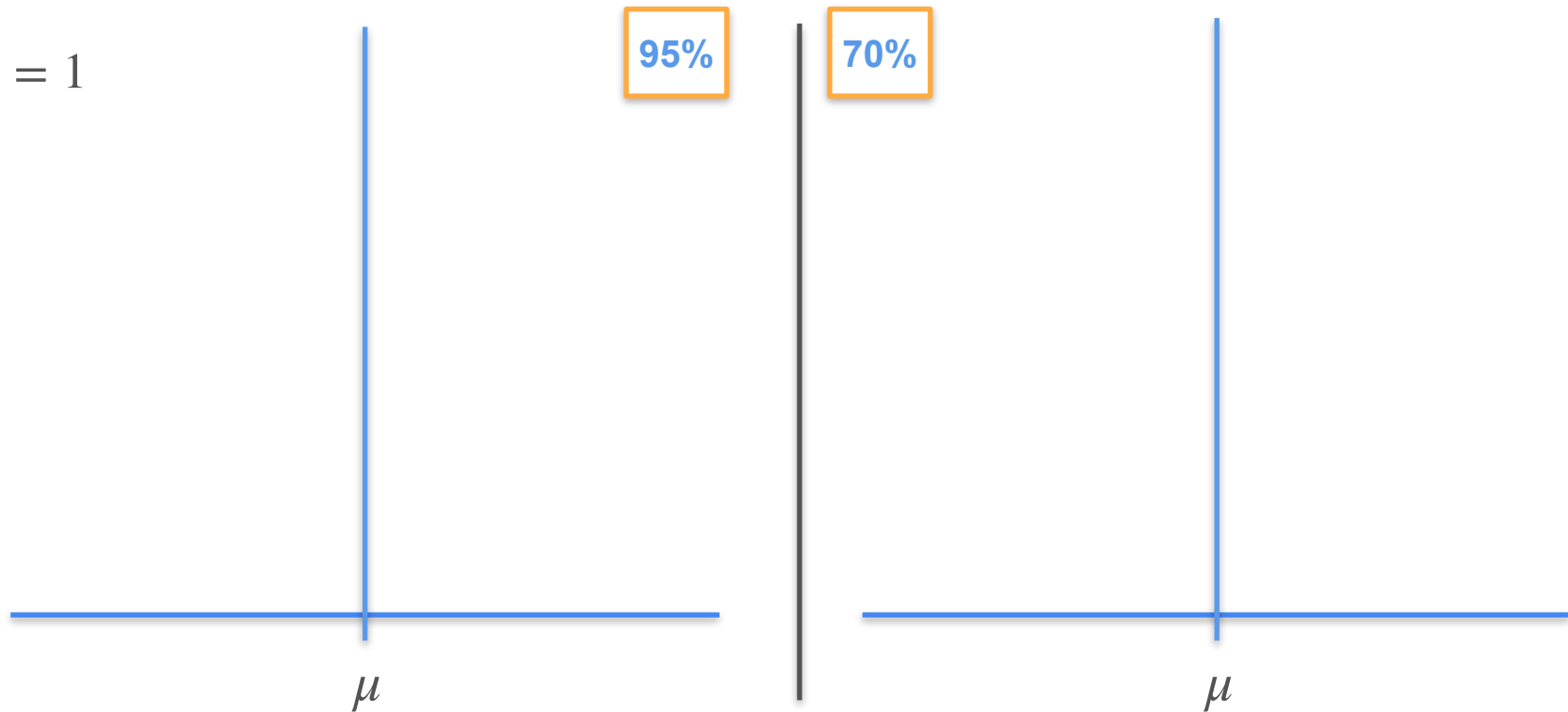


70%

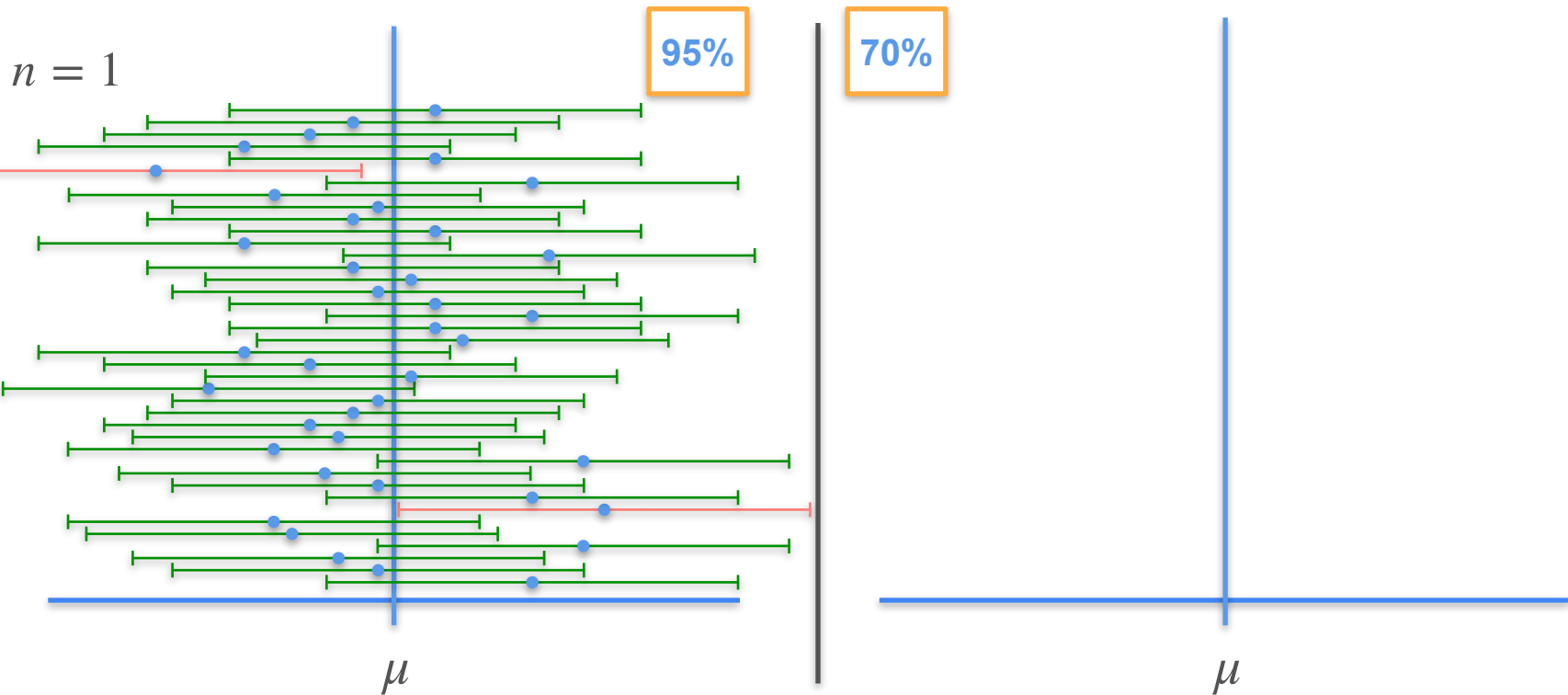


Effect of the Confidence Level

$n = 1$



Effect of the Confidence Level



Effect of the Confidence Level

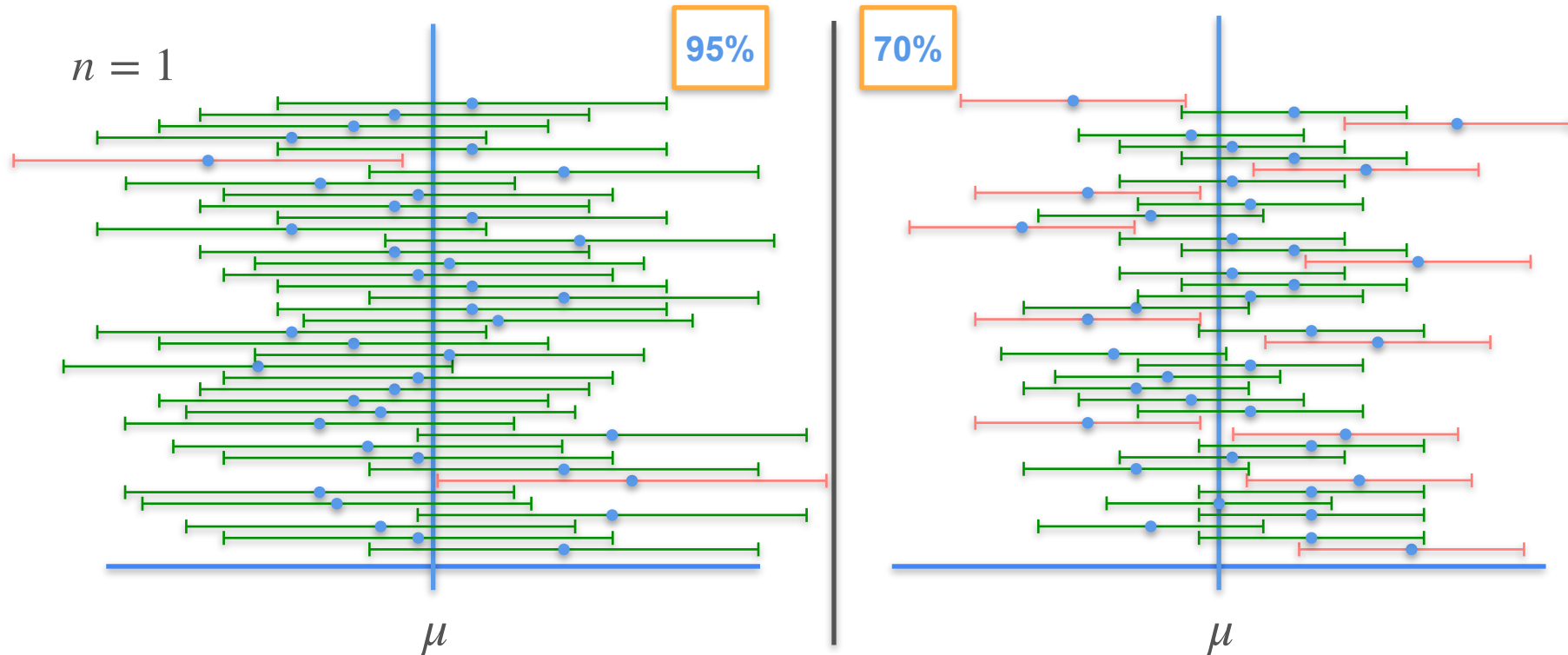
$n = 1$

95%

70%

μ

μ

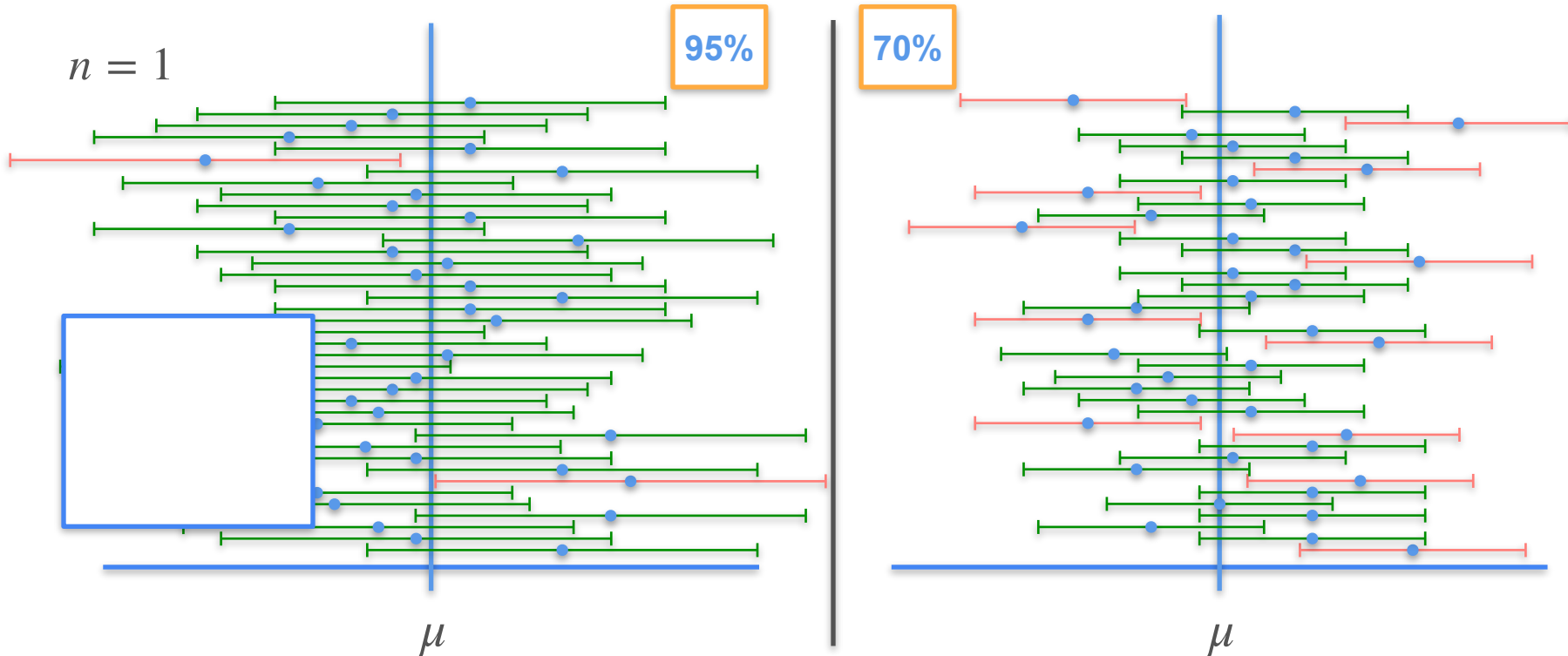


Effect of the Confidence Level

$n = 1$

95%

70%



Effect of the Confidence Level

$n = 1$

95%

70%

Yes

95%

μ

μ

Effect of the Confidence Level

$n = 1$

95%

70%

Yes

95%

No

5%

μ

μ

Effect of the Confidence Level

$n = 1$

95%

70%

Yes

95%

No

5%

μ

μ

Effect of the Confidence Level

$n = 1$

95%

70%

Yes 95%

No 5%

Yes 70%

μ

μ

Effect of the Confidence Level

$n = 1$

95%

70%

Yes 95%

No 5%

Yes 70%

No 30%

μ

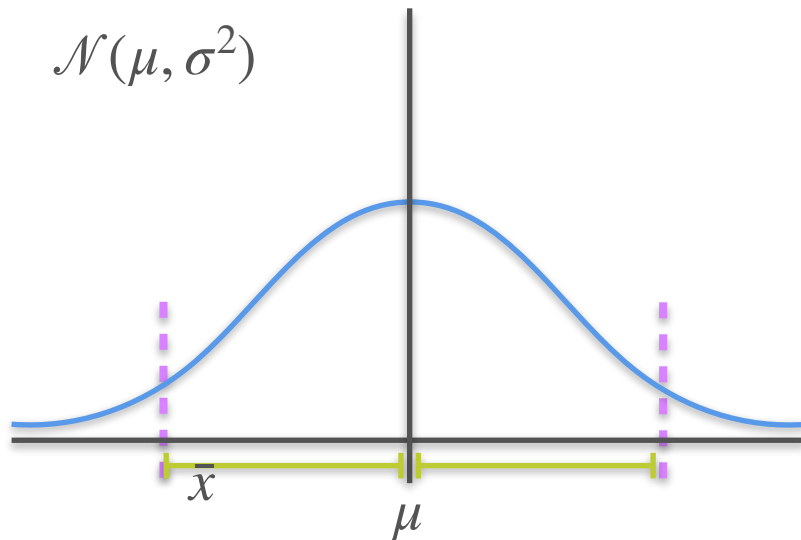
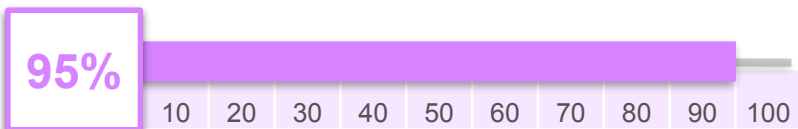
μ

Effect of the Confidence Level

sample size



Confidence level

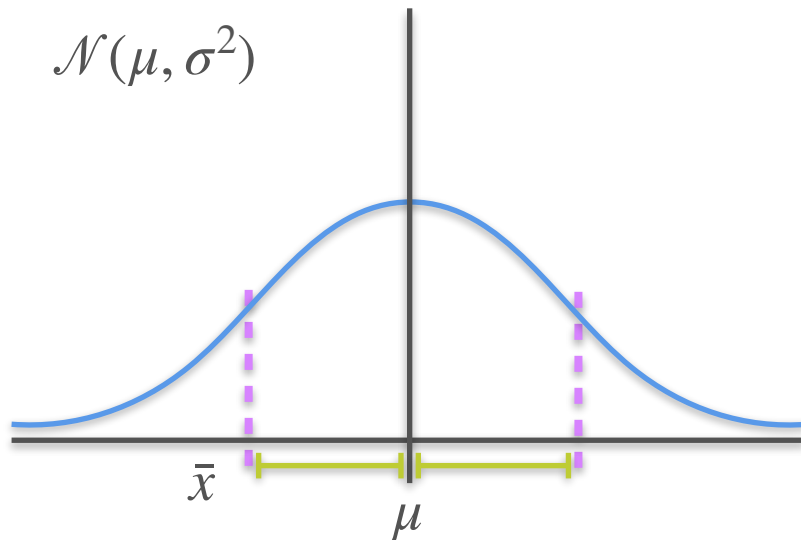
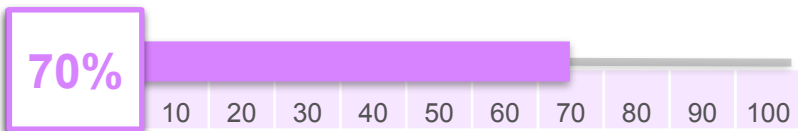


Effect of the Confidence Level

sample size



Confidence level

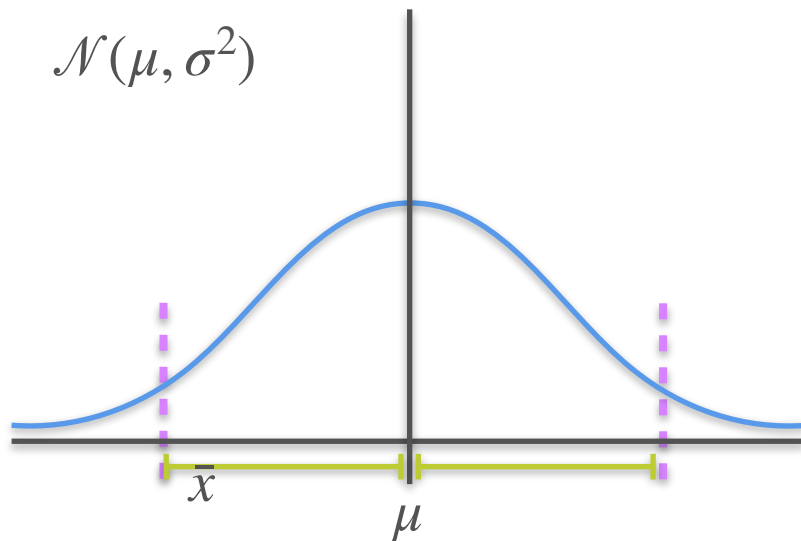
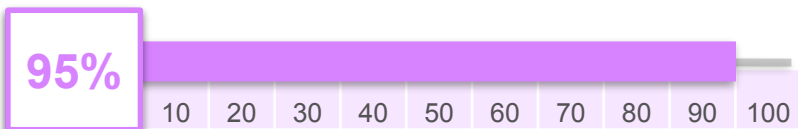


Effect of the Confidence Level

sample size



Confidence level

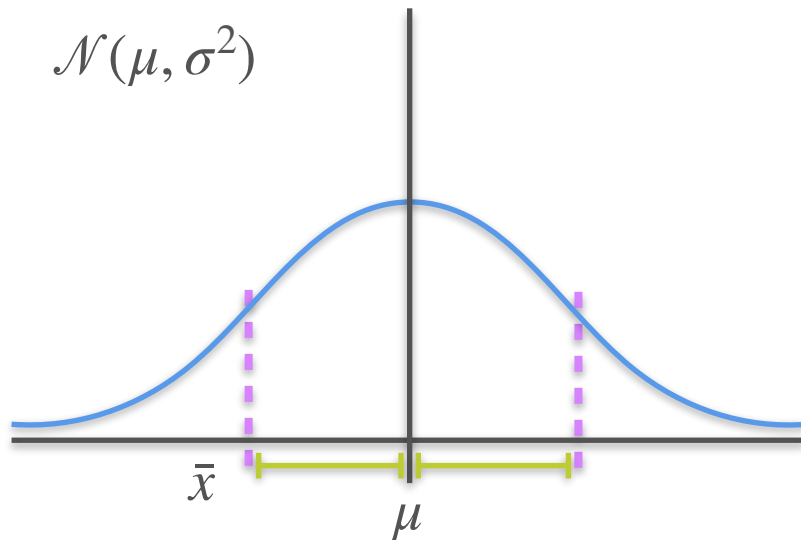
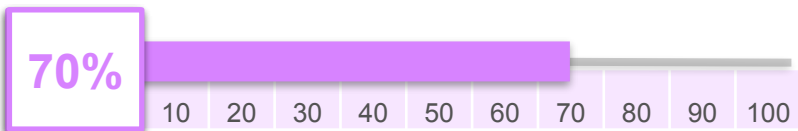


Effect of the Confidence Level

sample size



Confidence level



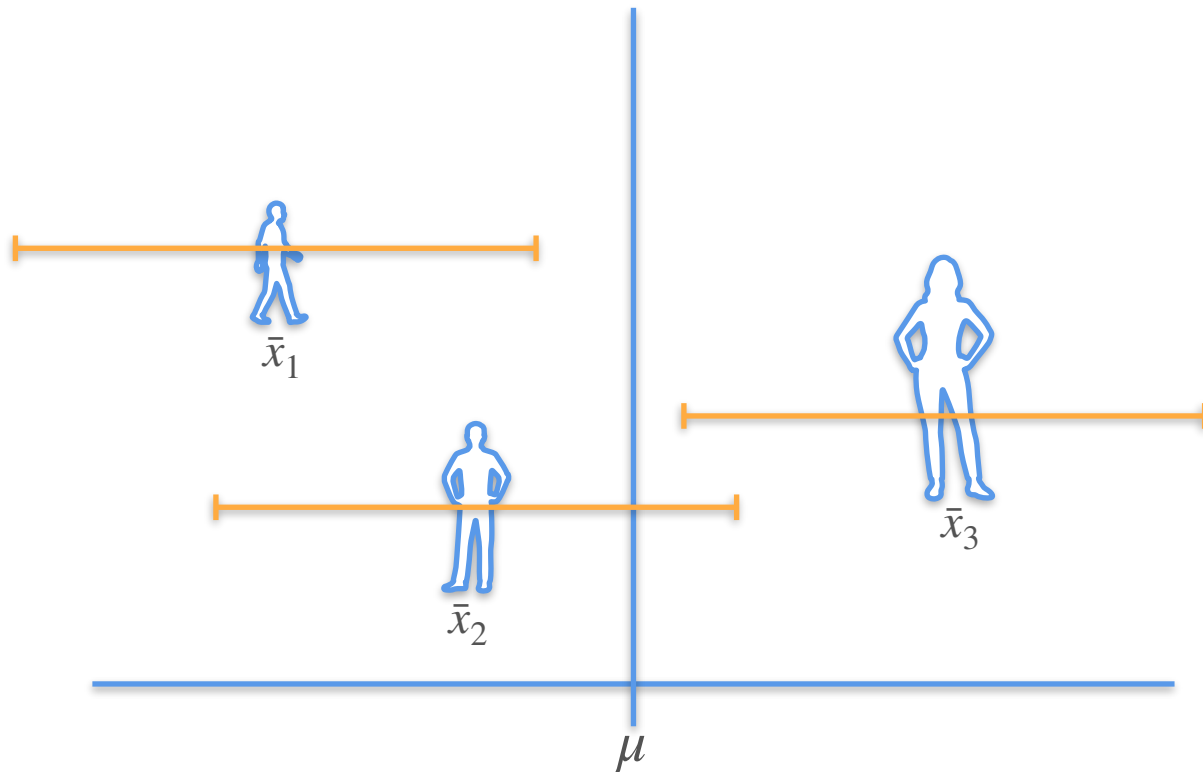


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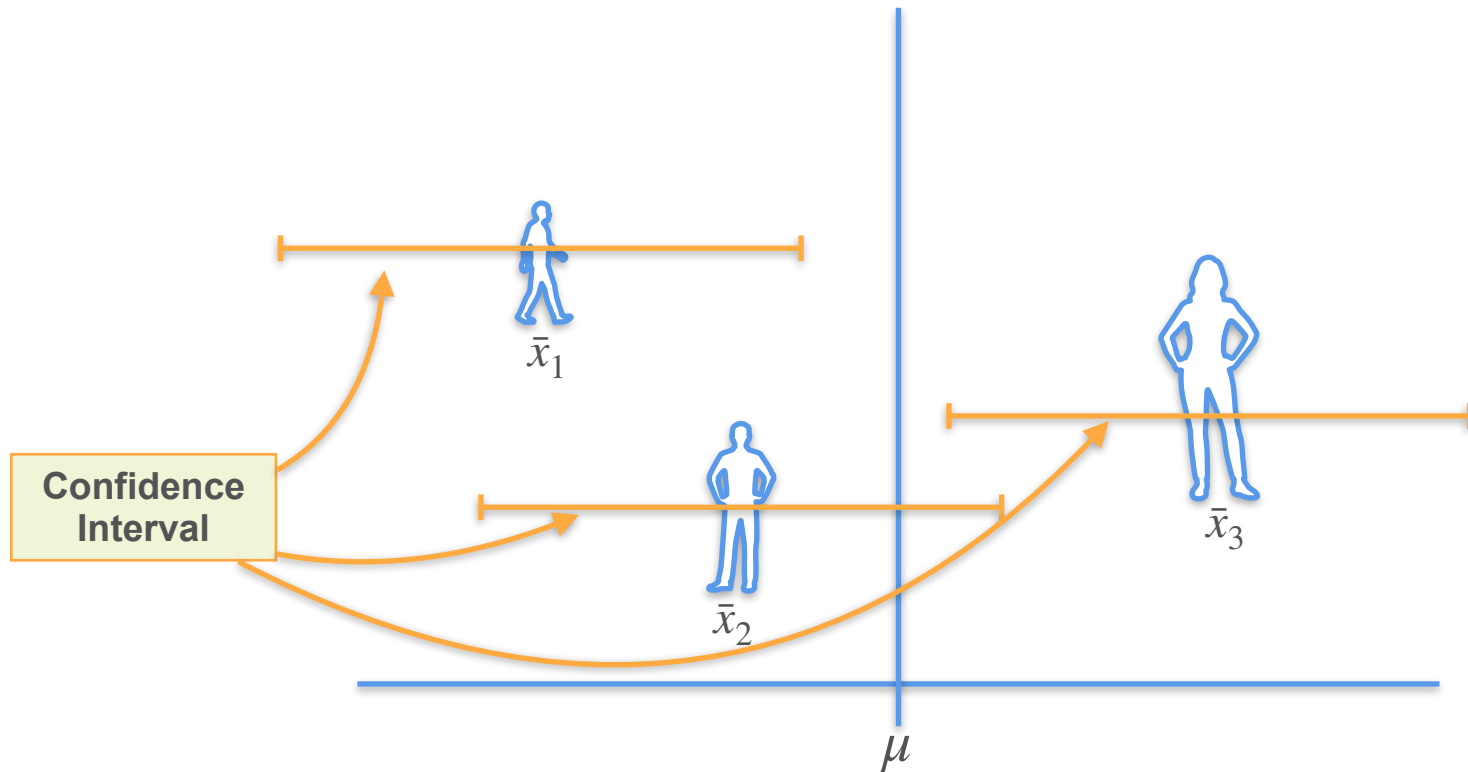
Confidence Interval

Margin of Error

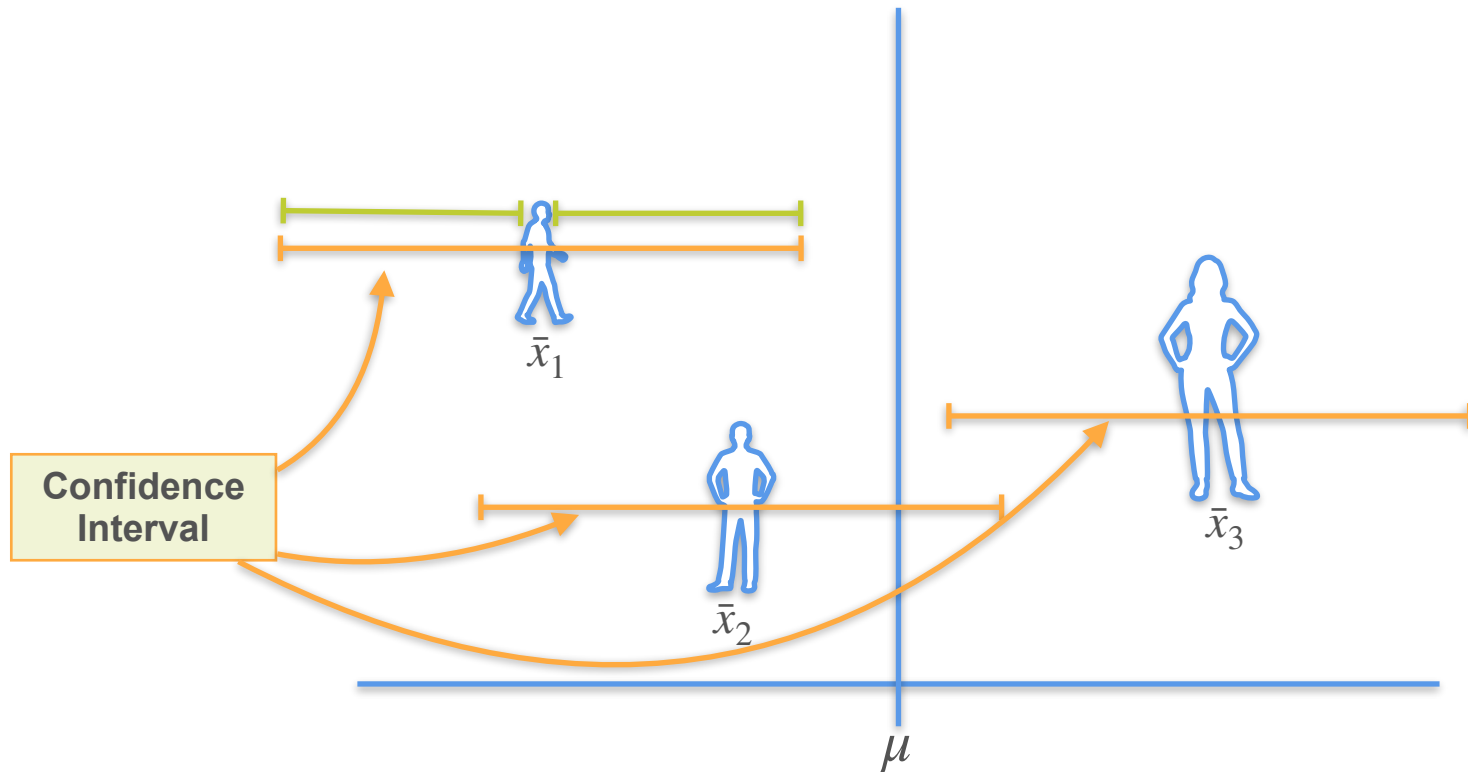
Margin of Error - Introduction



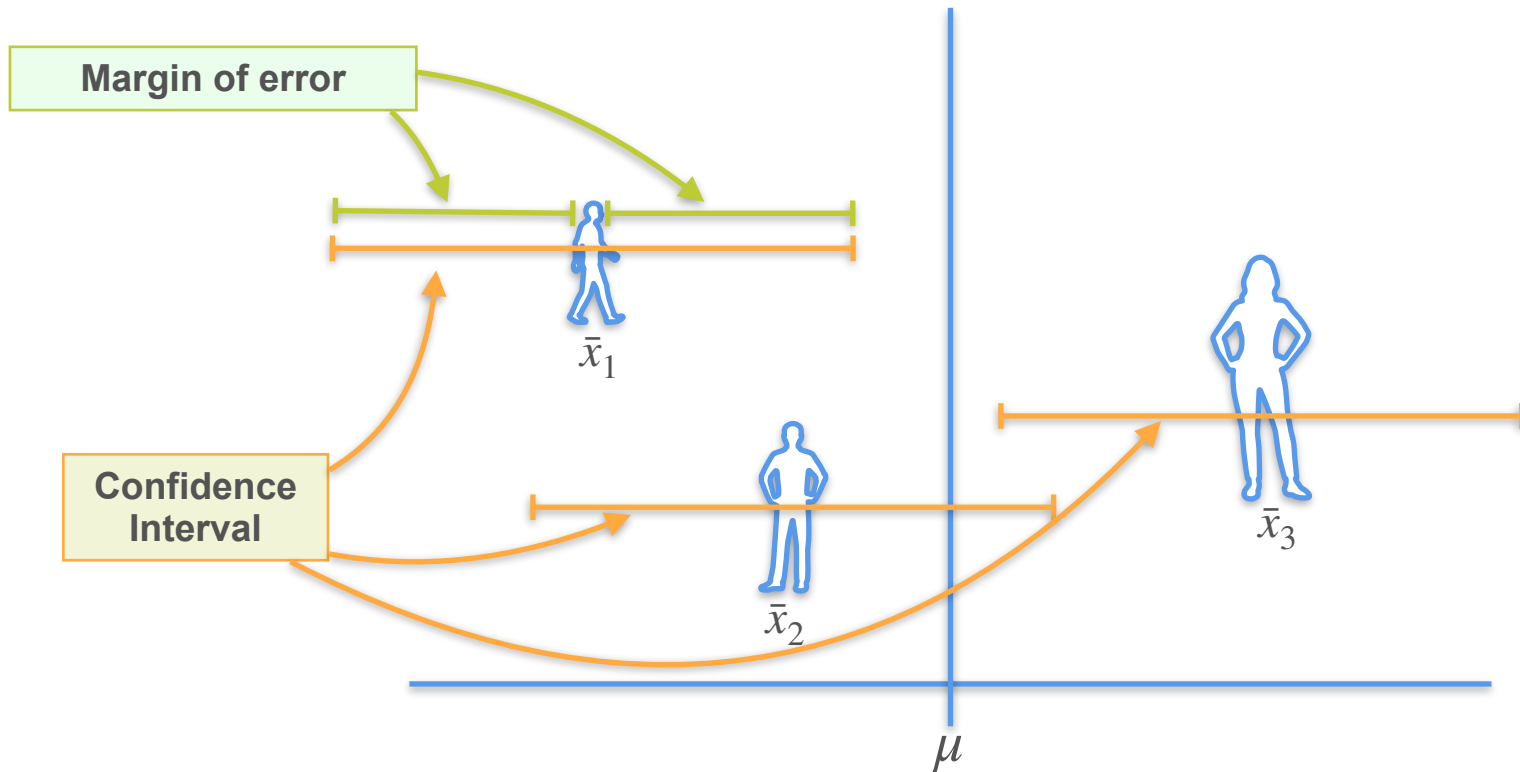
Margin of Error - Introduction



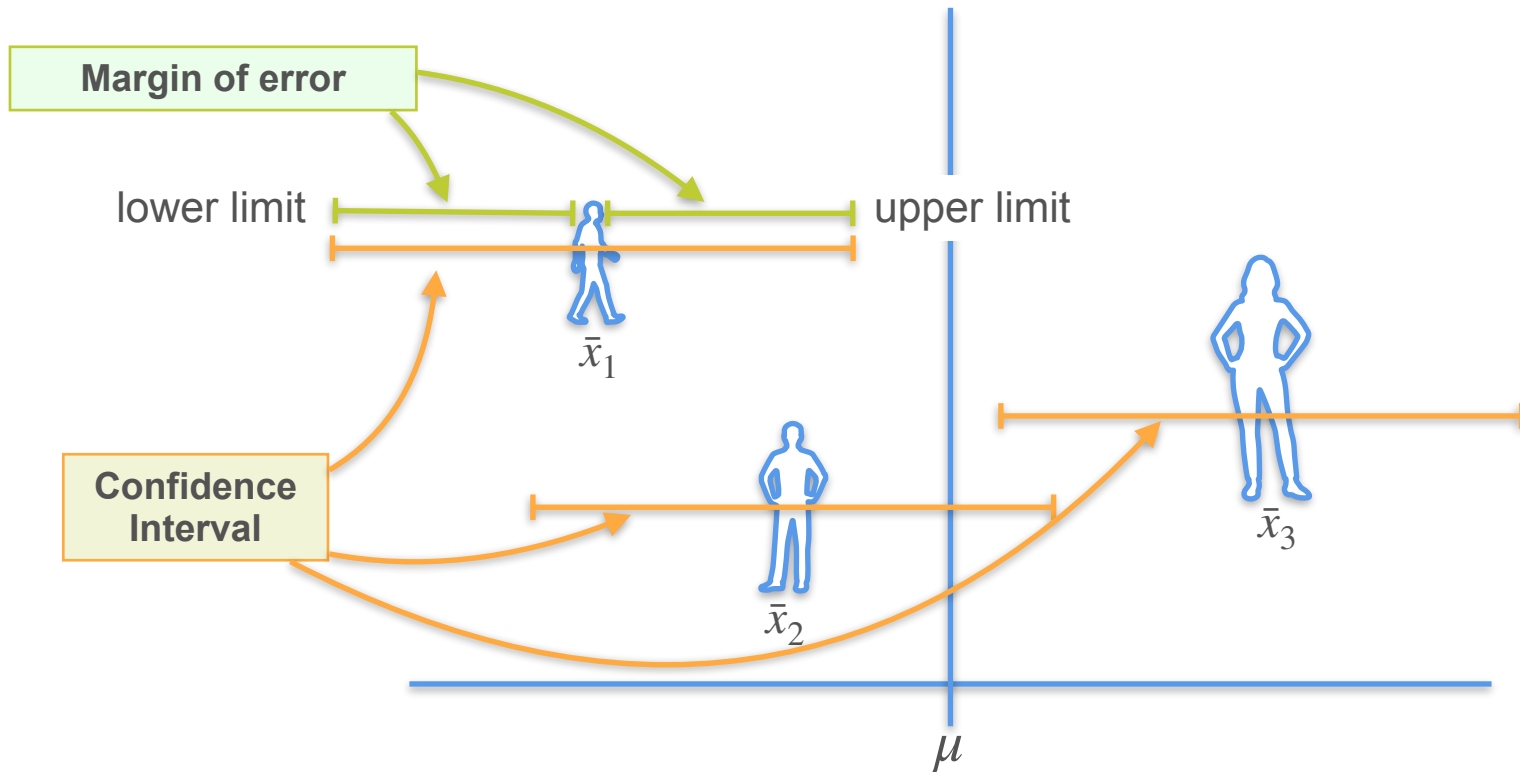
Margin of Error - Introduction



Margin of Error - Introduction



Margin of Error - Introduction



Margin of Error

Margin of Error

Taking multiple samples of size n

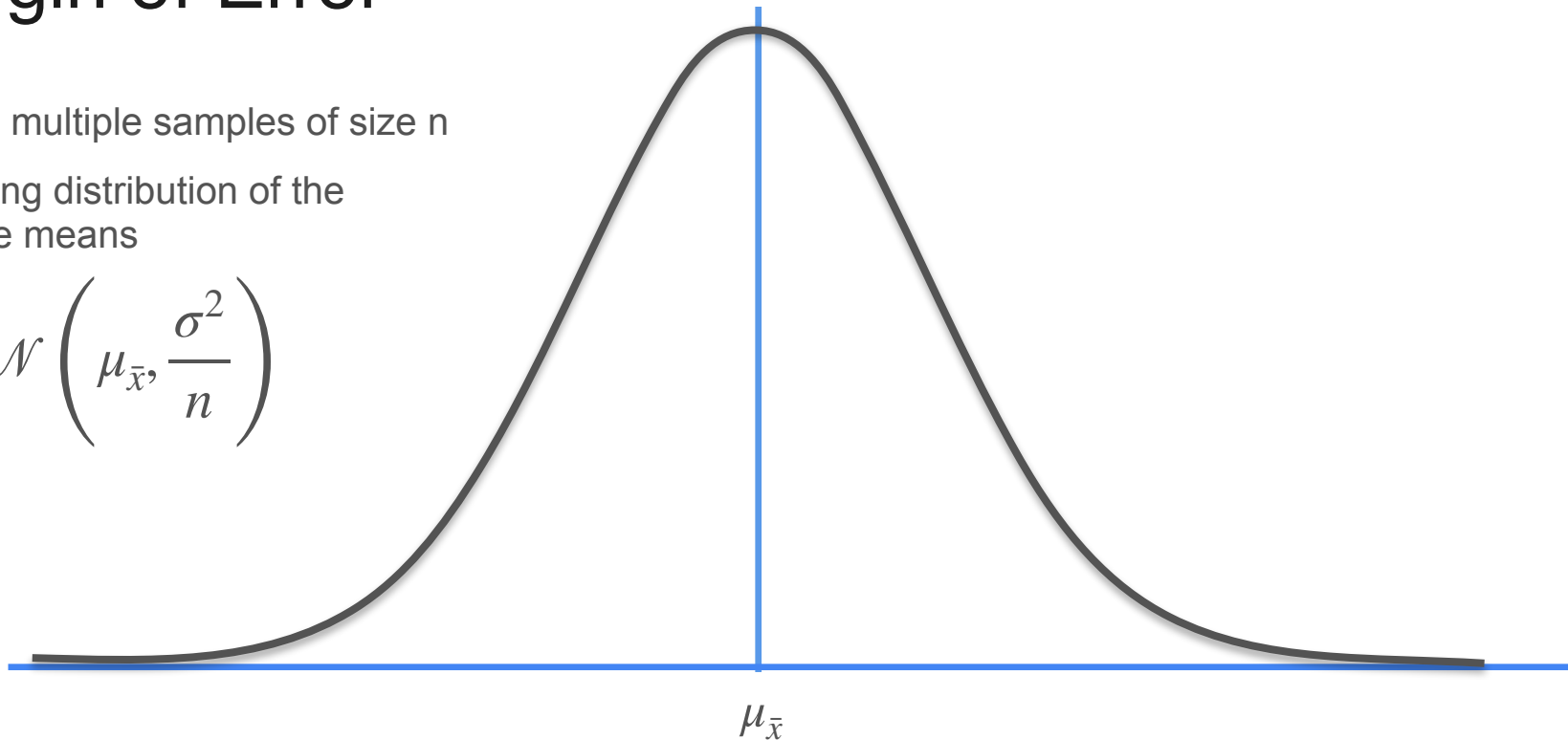
sampling distribution of the
sample means

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

Margin of Error

Taking multiple samples of size n
sampling distribution of the
sample means

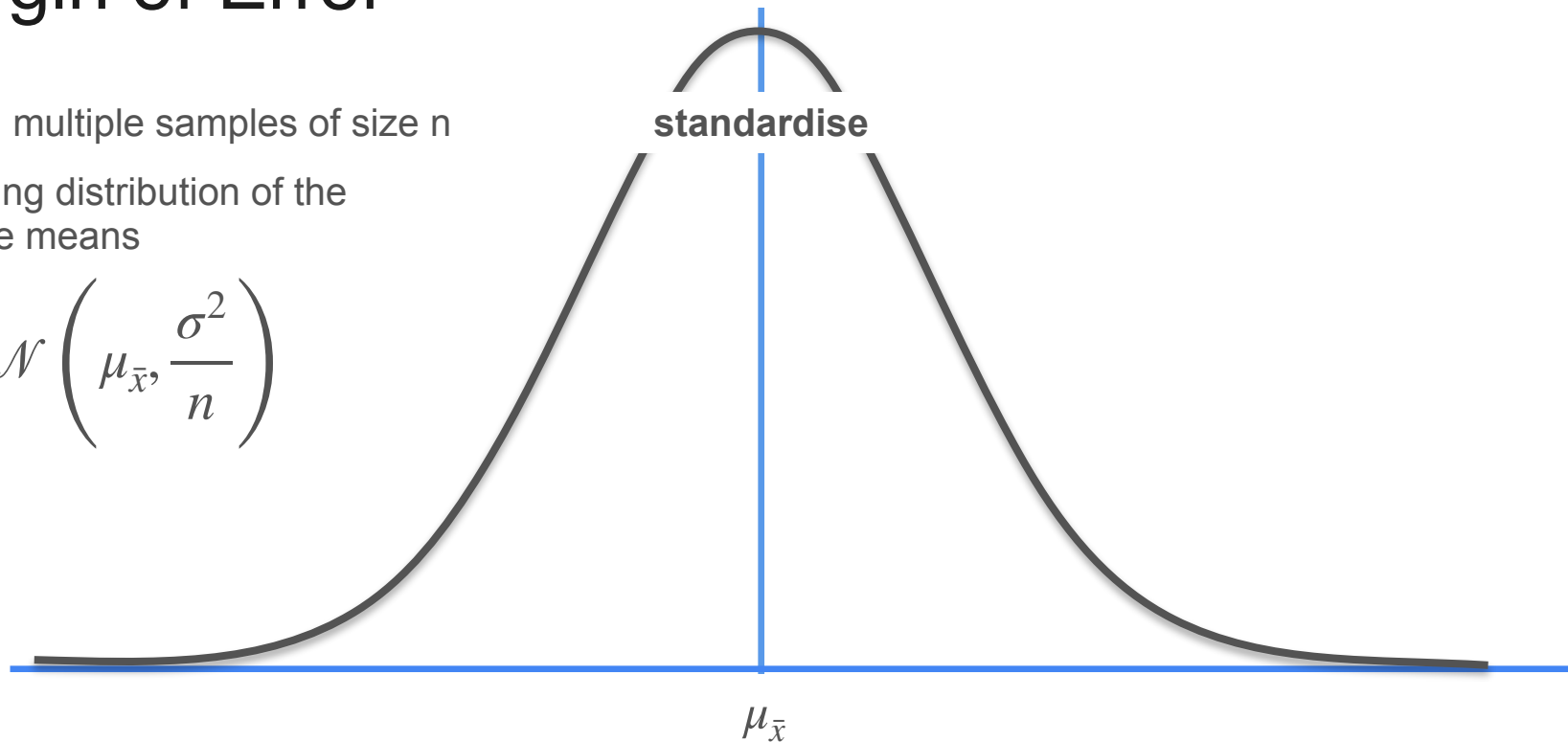
$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$



Margin of Error

Taking multiple samples of size n
sampling distribution of the
sample means

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$



Margin of Error

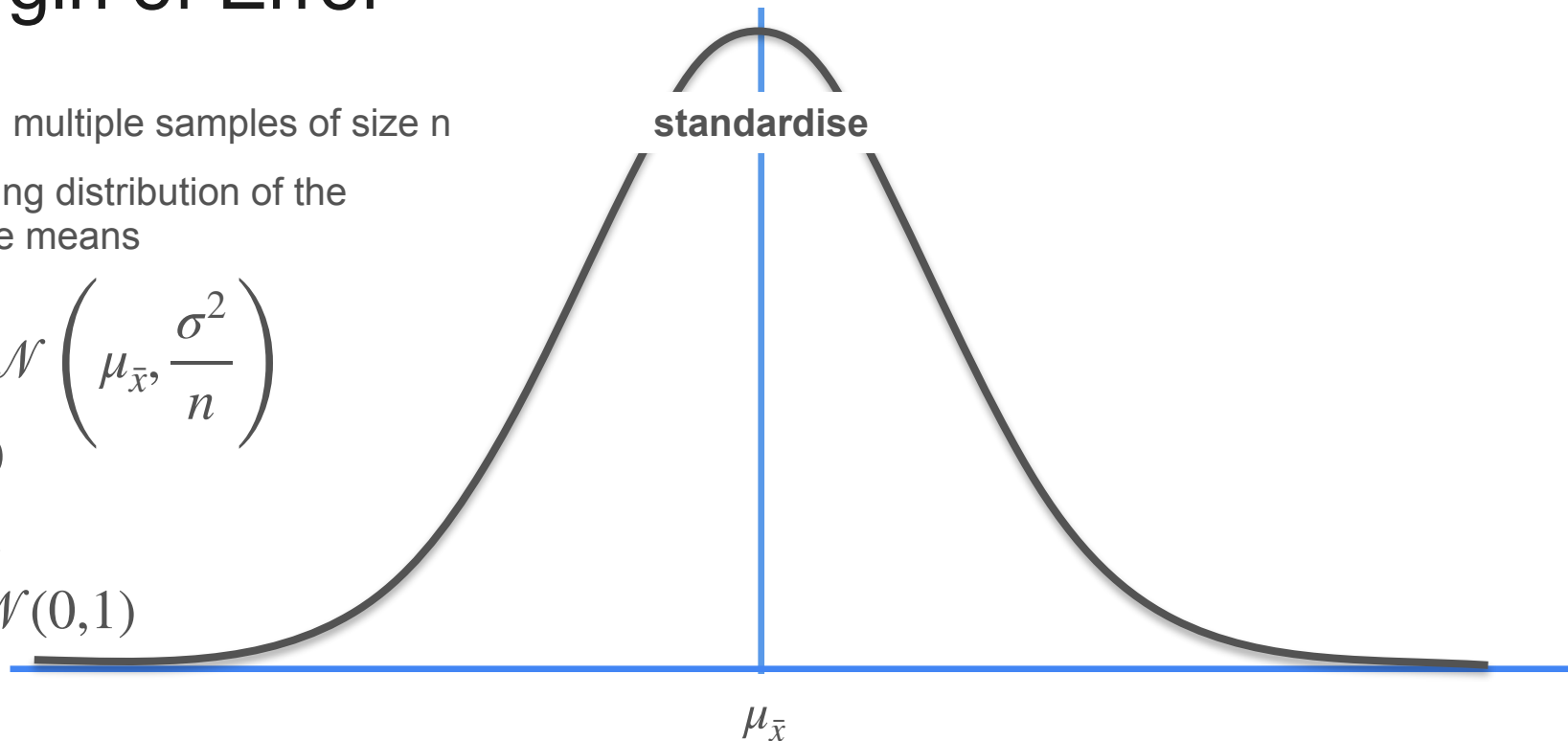
Taking multiple samples of size n
sampling distribution of the
sample means

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0,1)$$



Margin of Error

Taking multiple samples of size n

sampling distribution of the
sample means

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0,1)$$

standardise

0



Margin of Error

Taking multiple samples of size n

sampling distribution of the
sample means

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

standardise

0

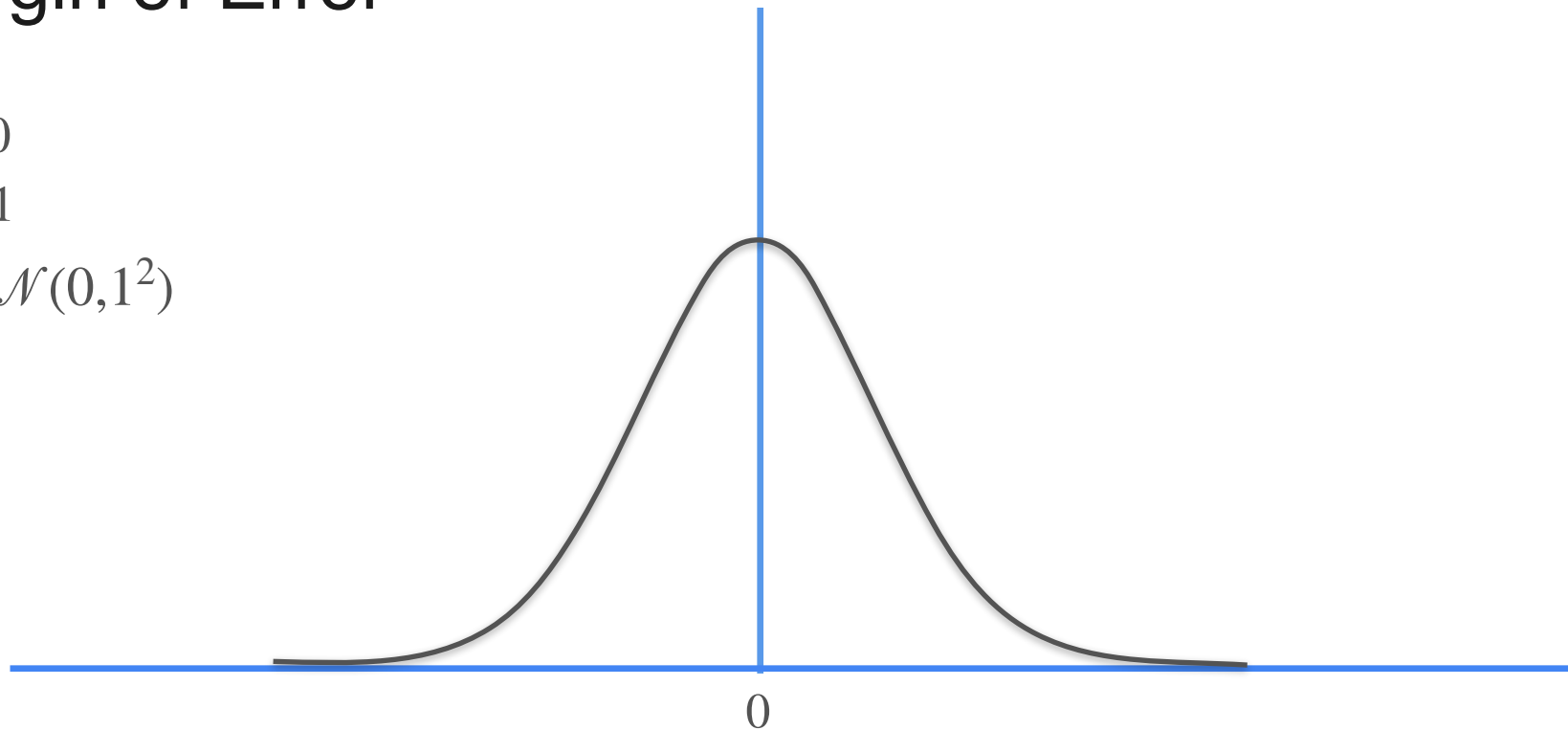
A standard normal distribution curve is plotted on a blue horizontal axis. The curve is symmetric and bell-shaped, centered at the origin. A vertical blue line passes through the peak of the curve, labeled 'standardise' above it and '0' below it on the axis.

Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

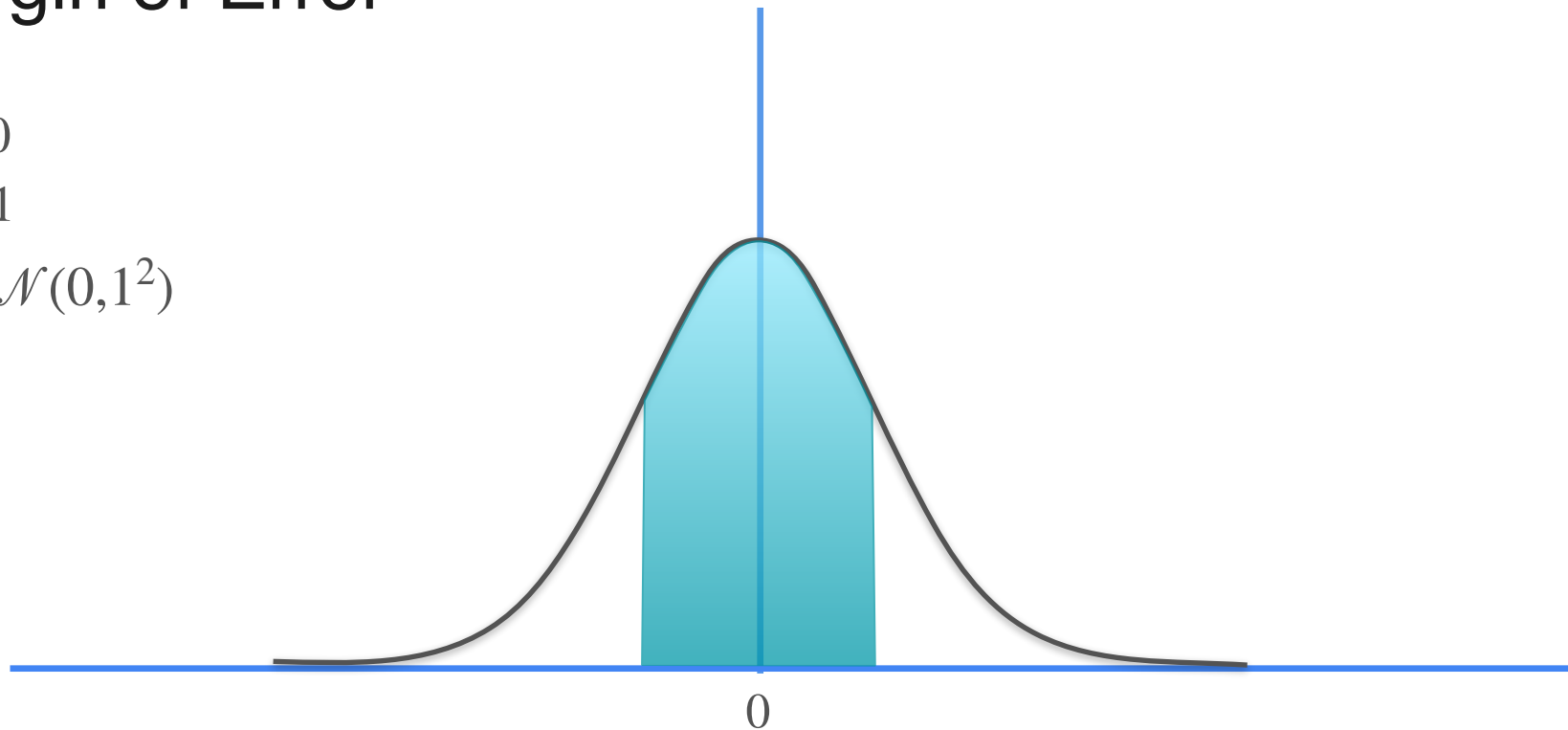


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

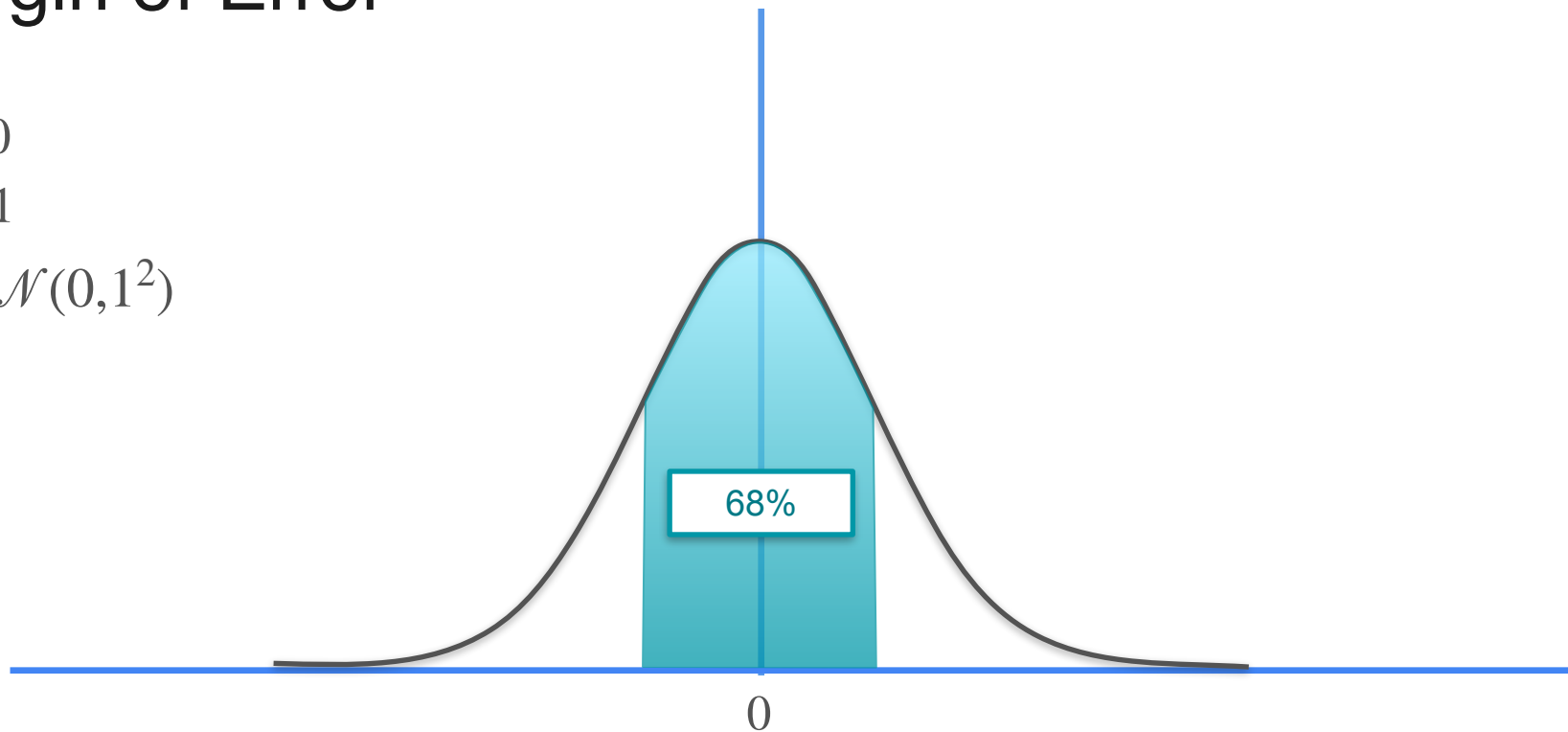


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

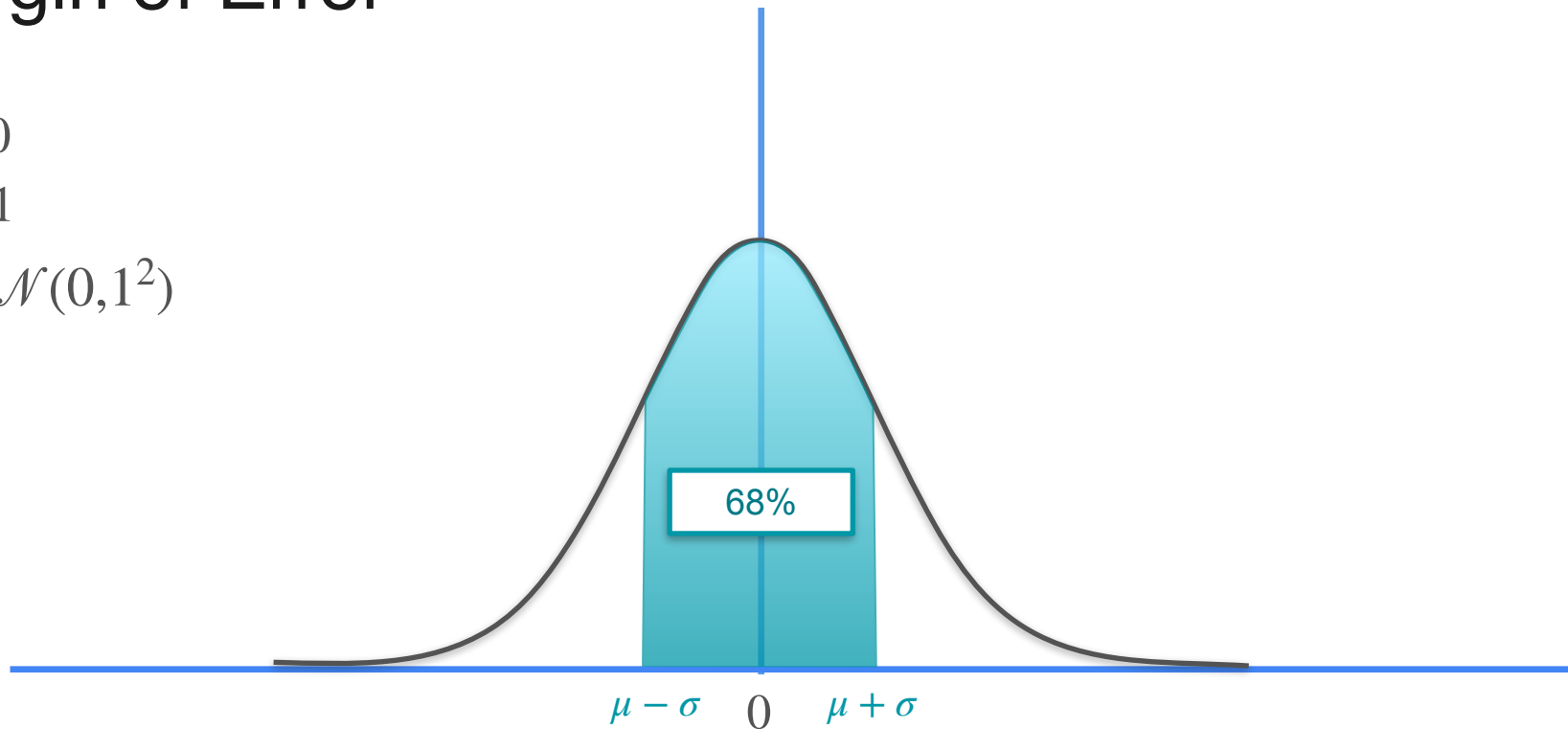


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

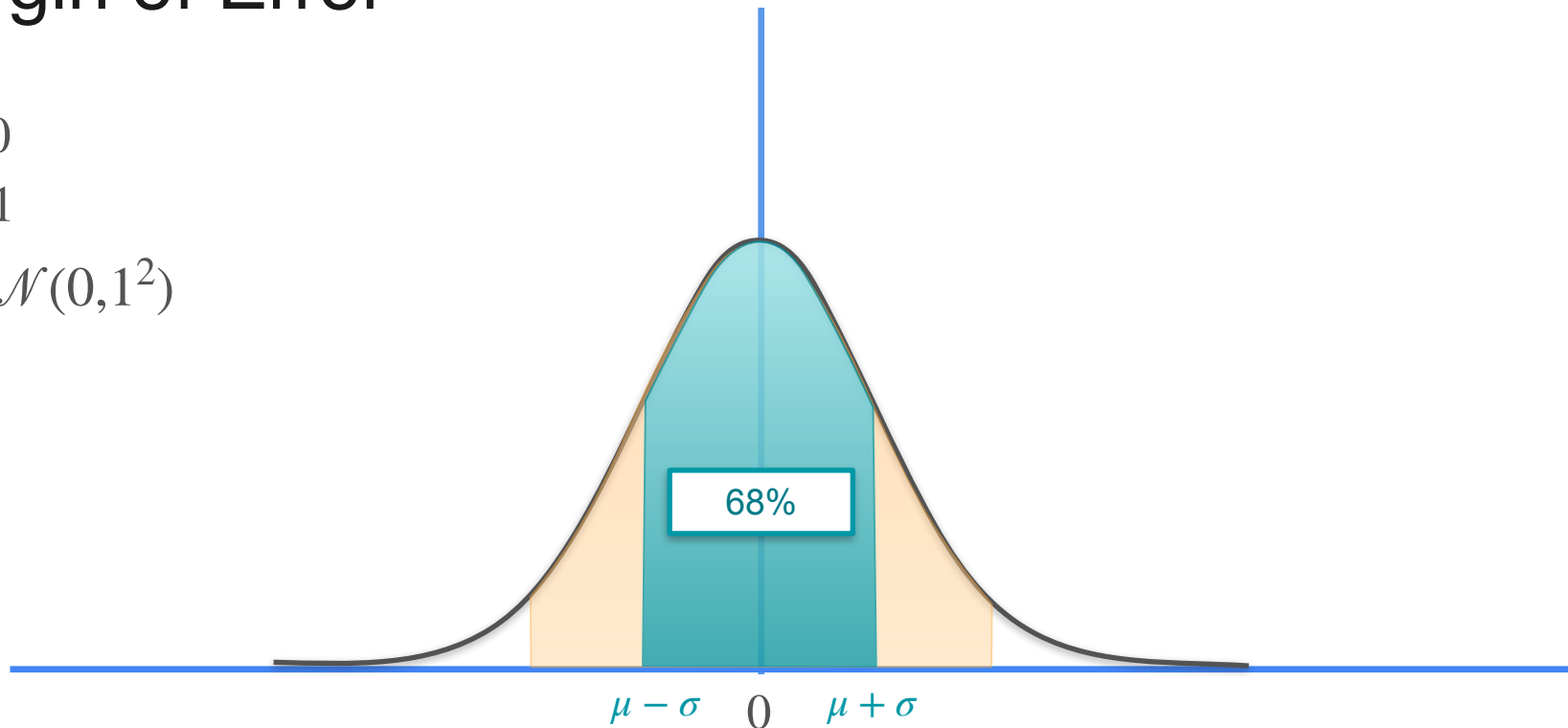


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

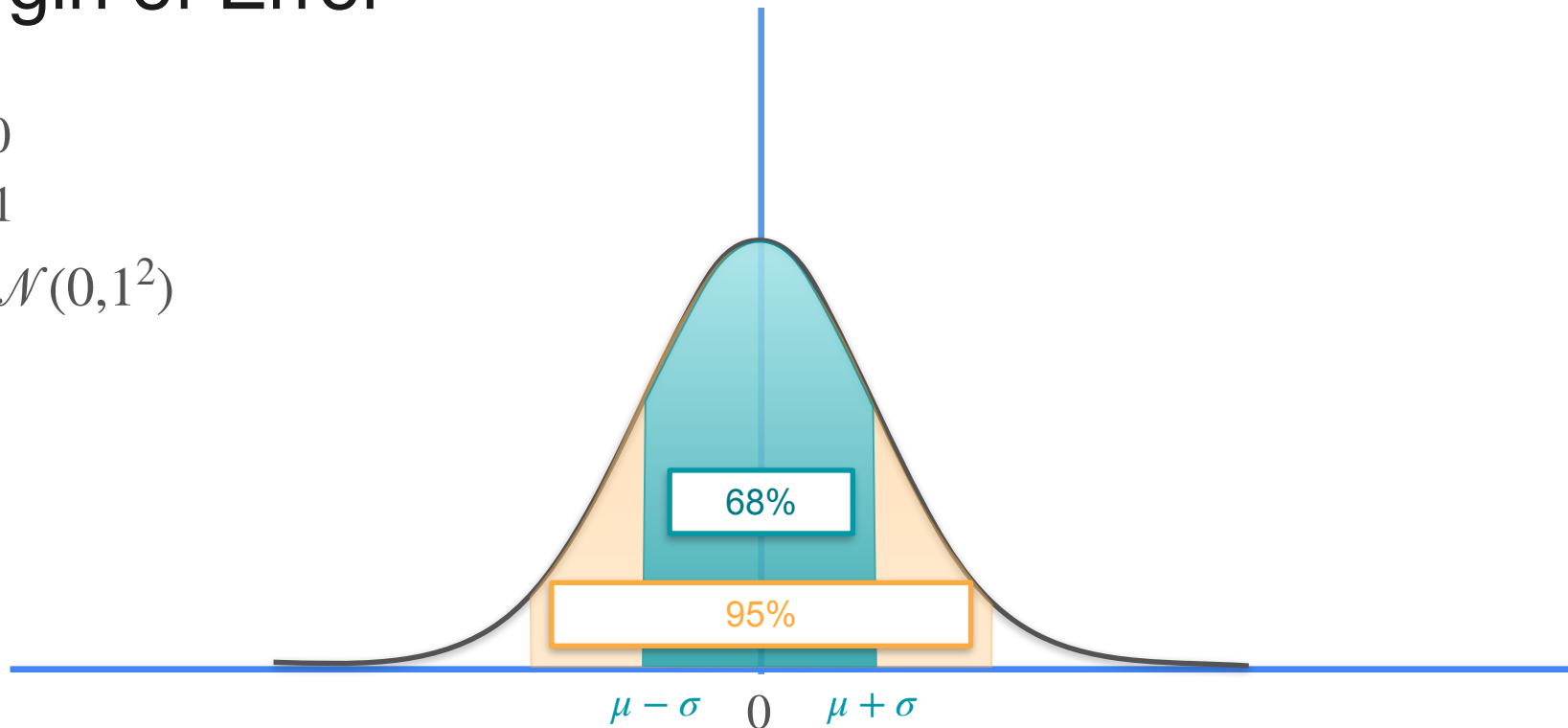


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

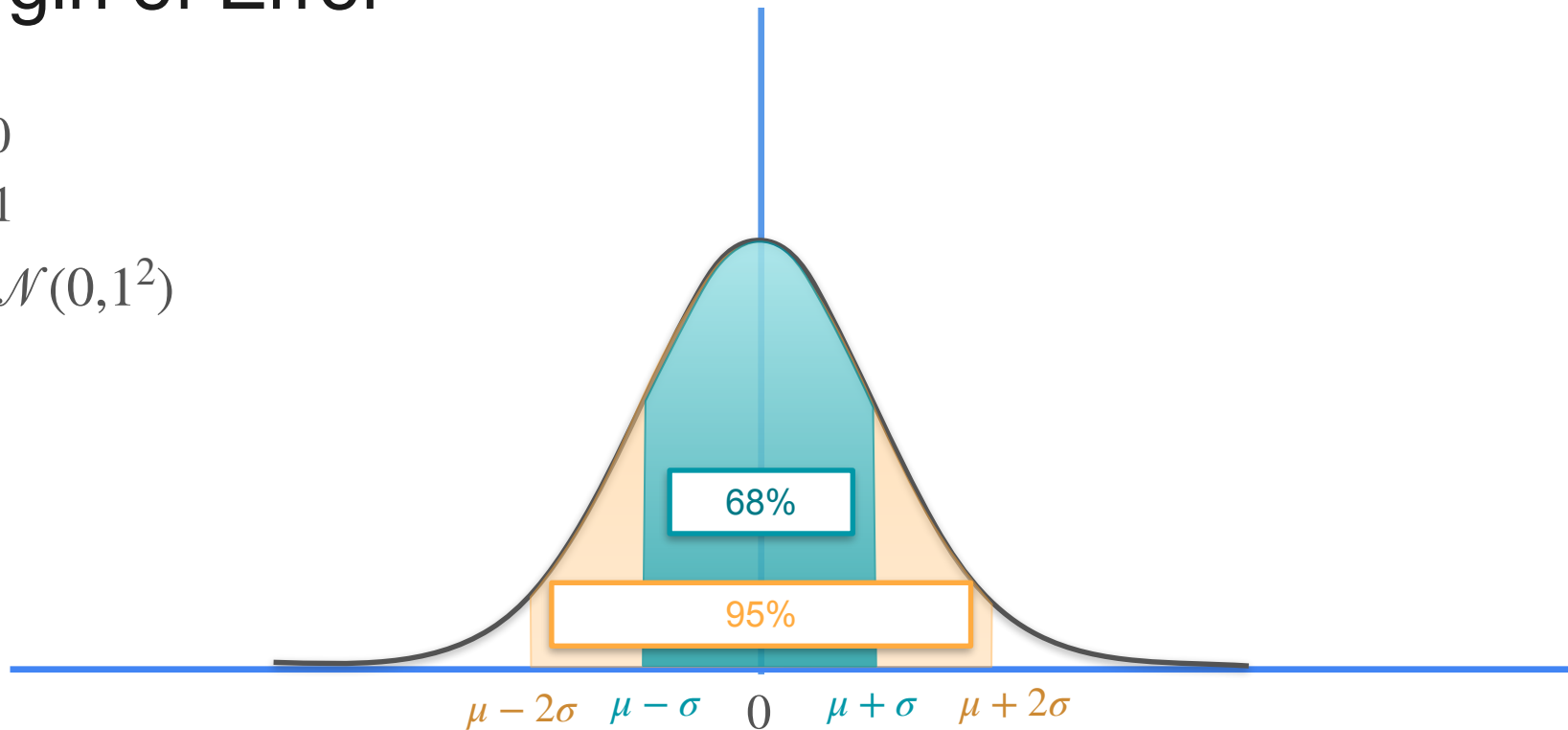


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

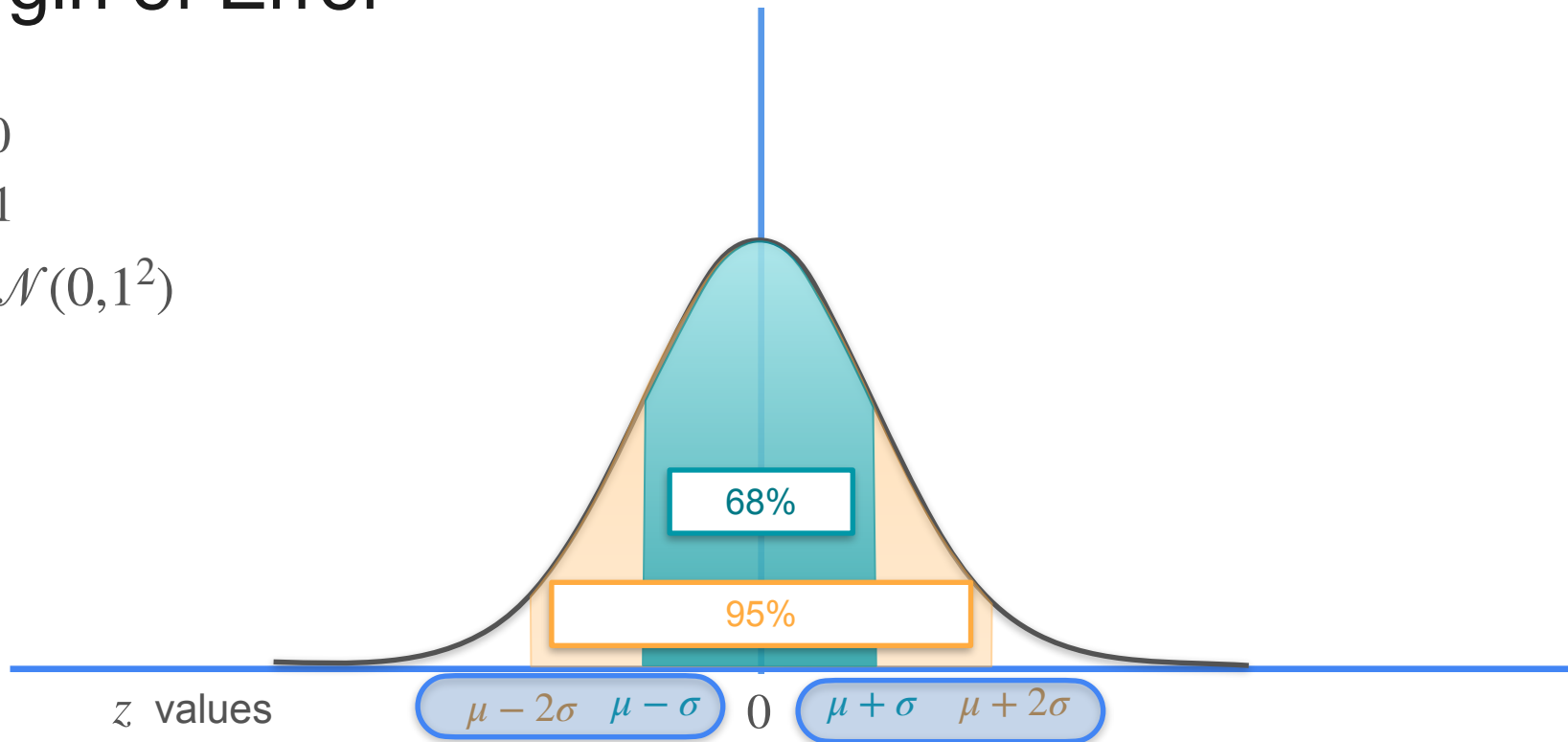


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

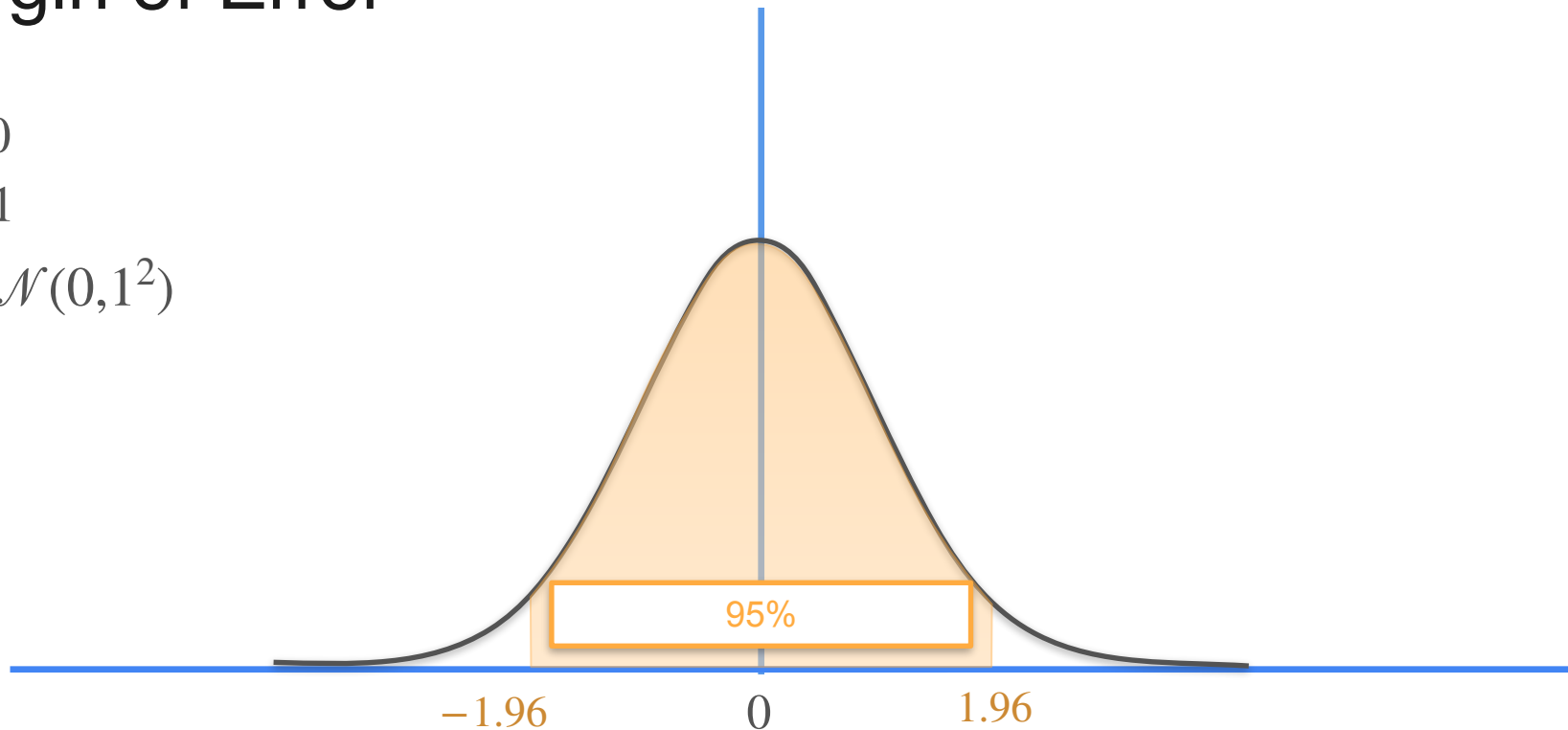


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

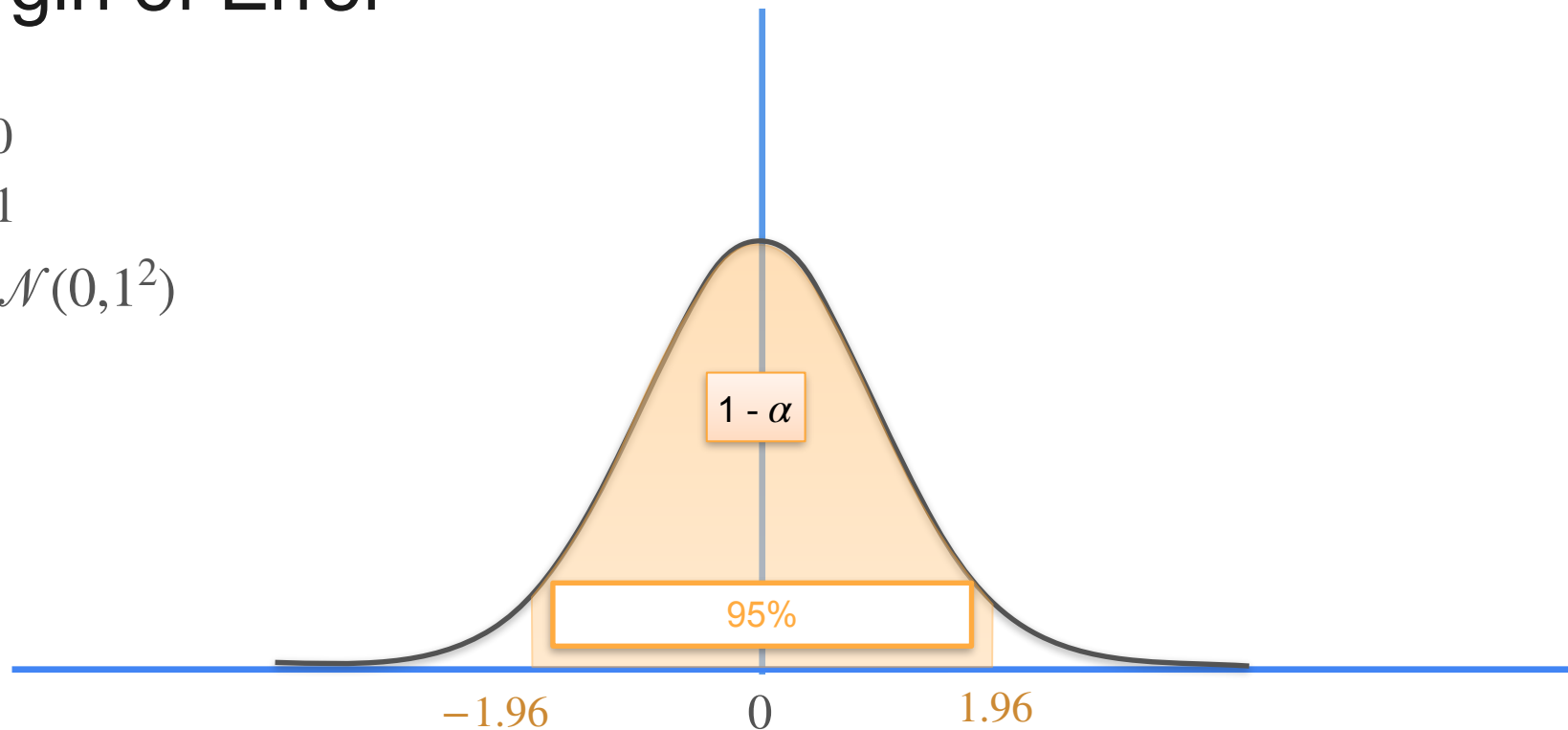


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

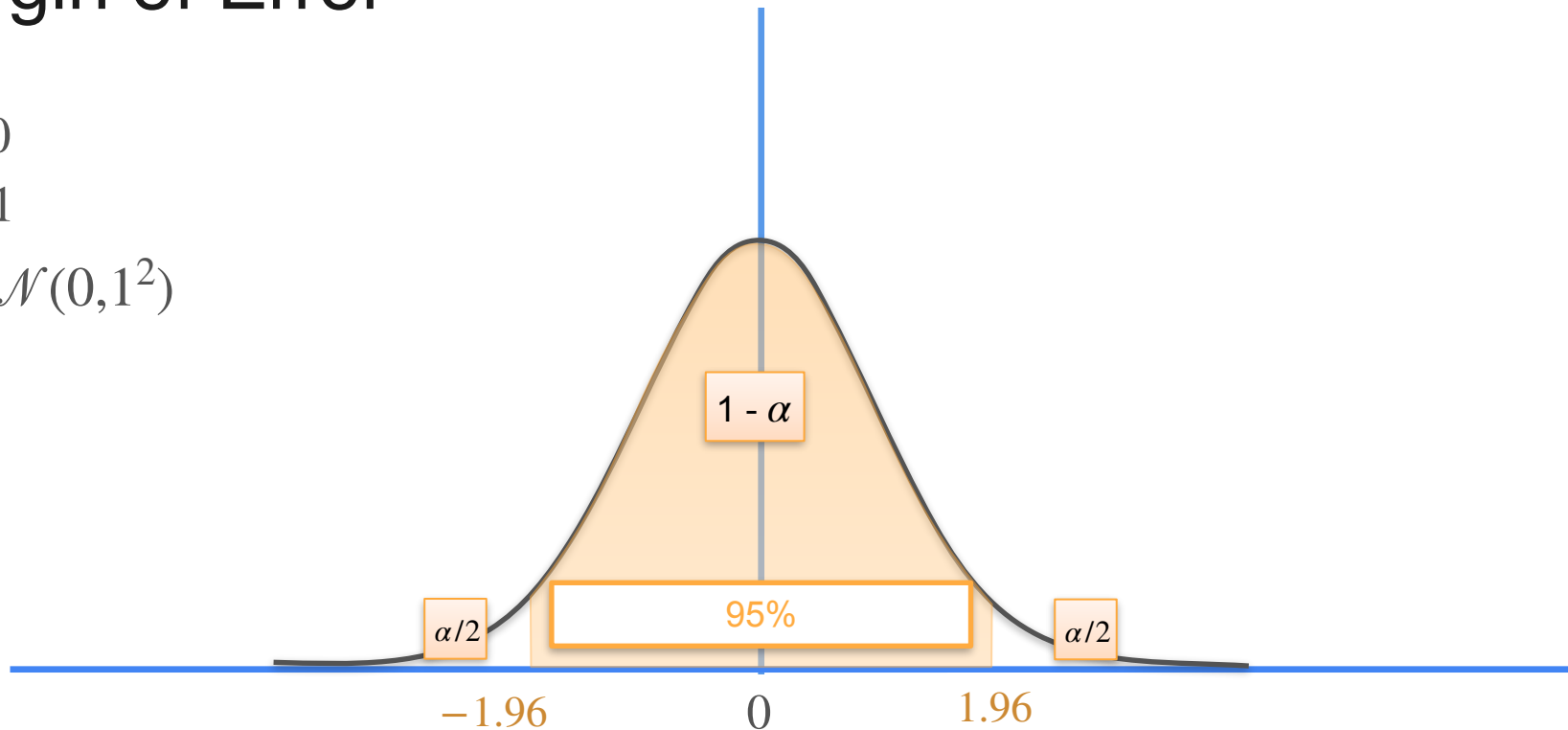


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

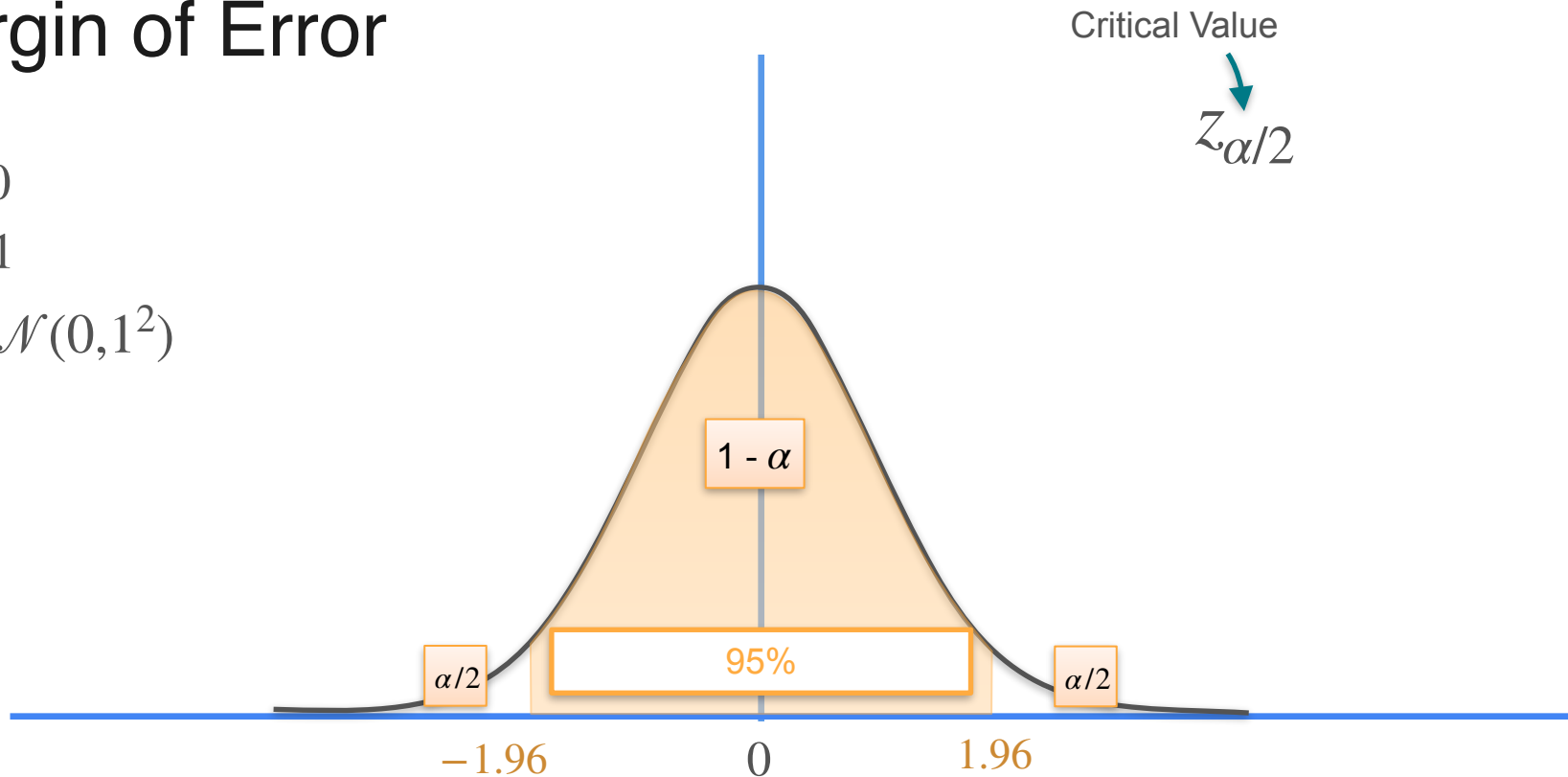


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

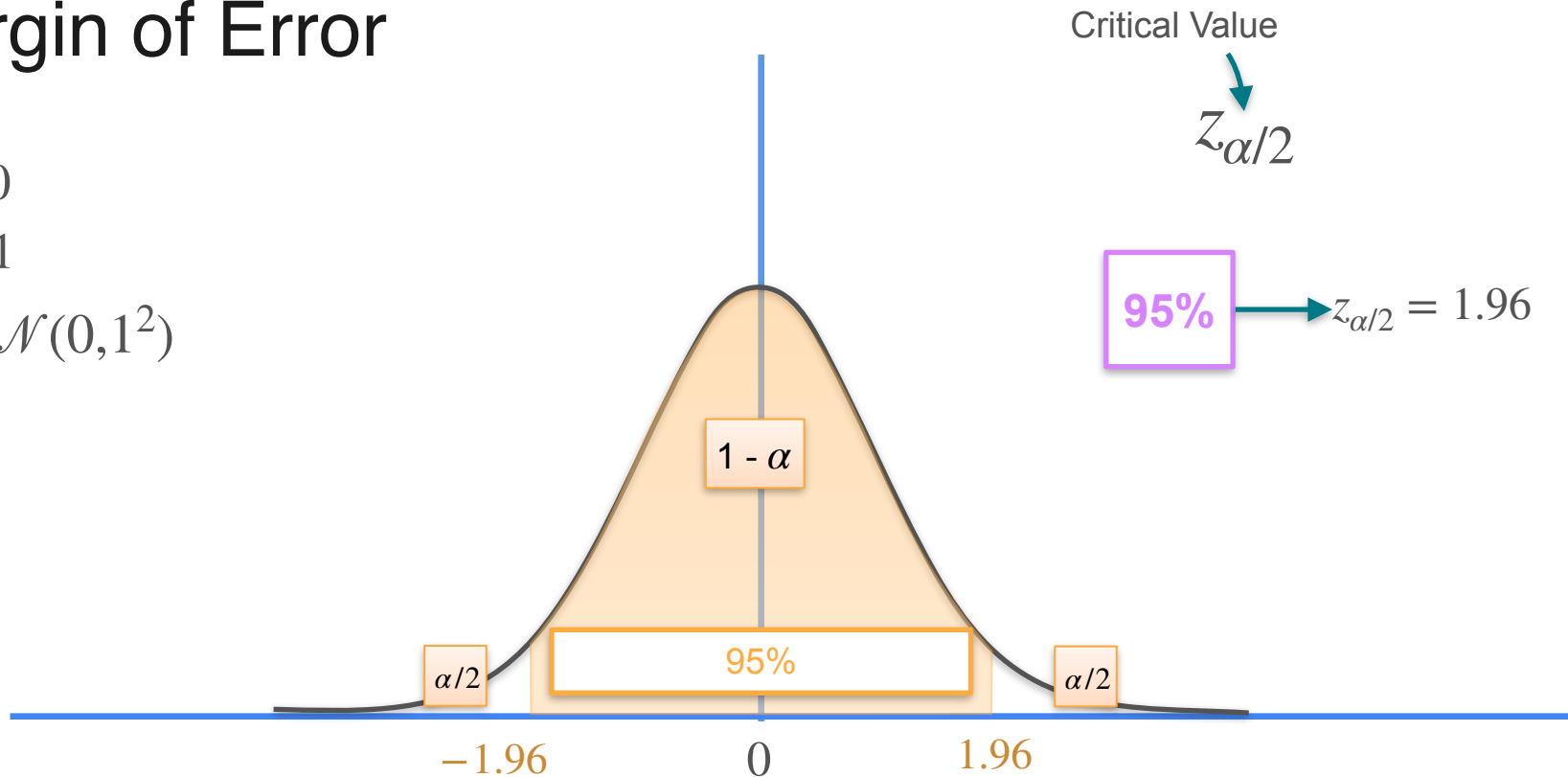


Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$



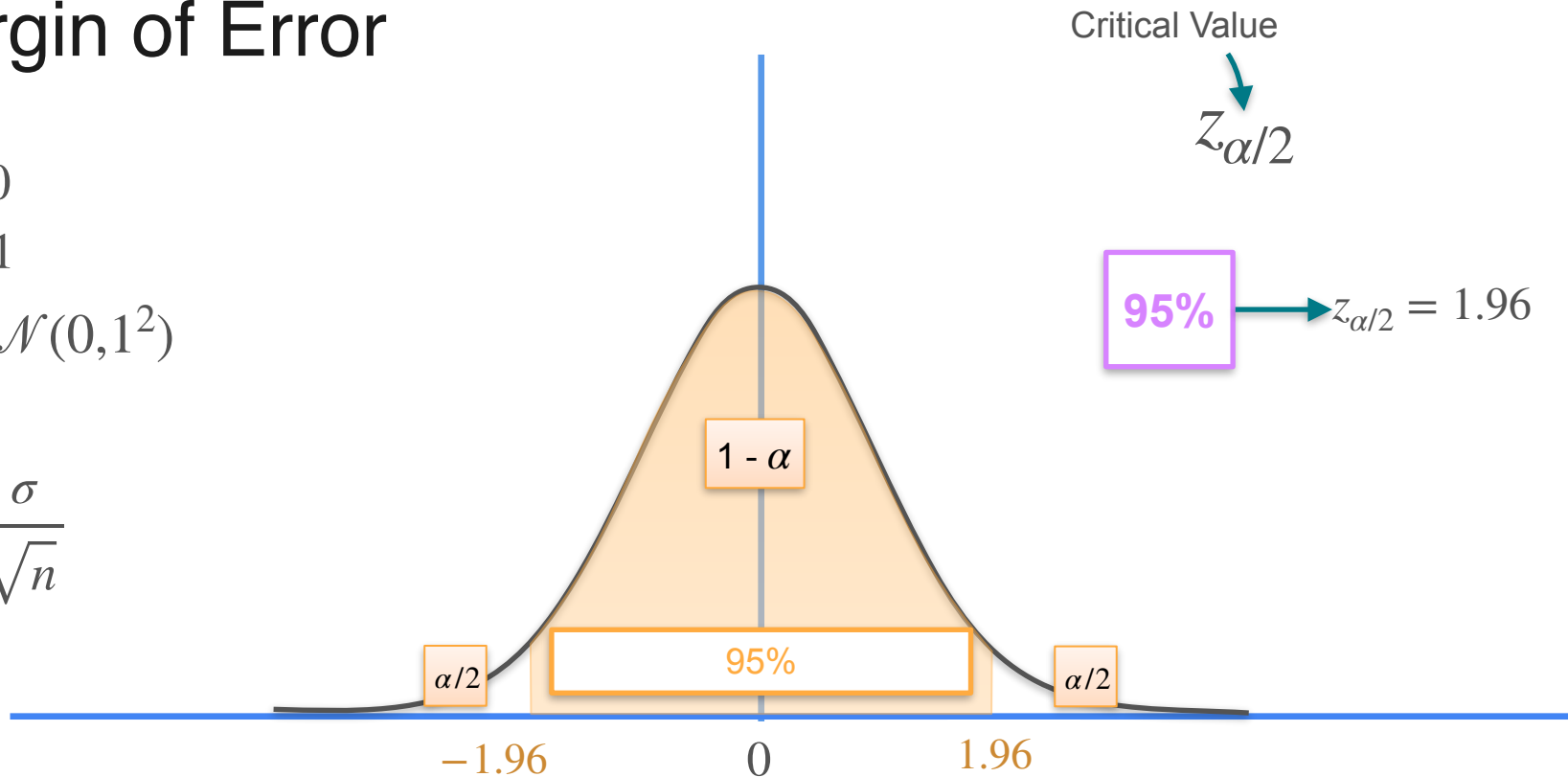
Margin of Error

$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$



Margin of Error

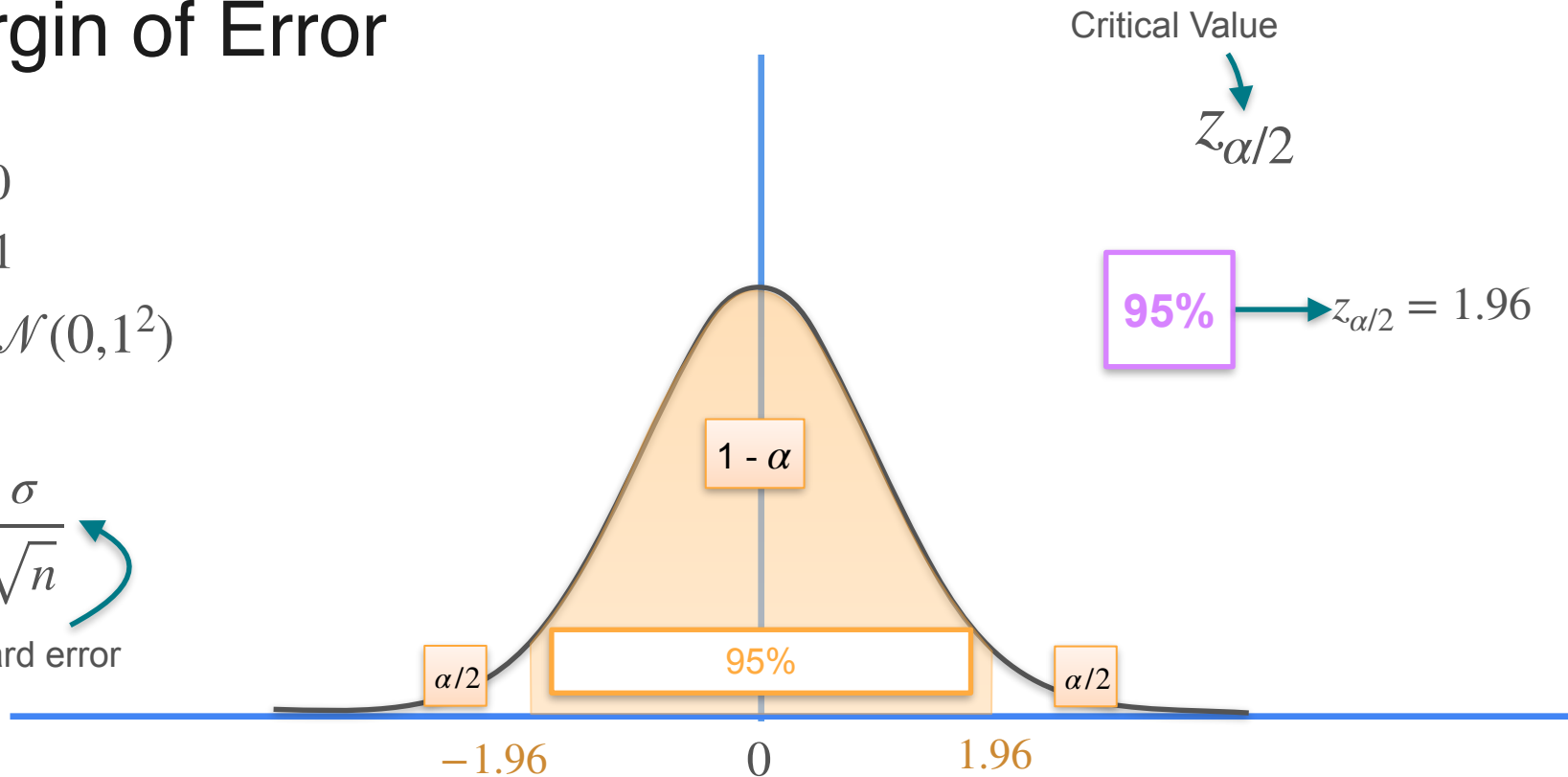
$$\mu = 0$$

$$\sigma = 1$$

$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Standard error



Margin of Error

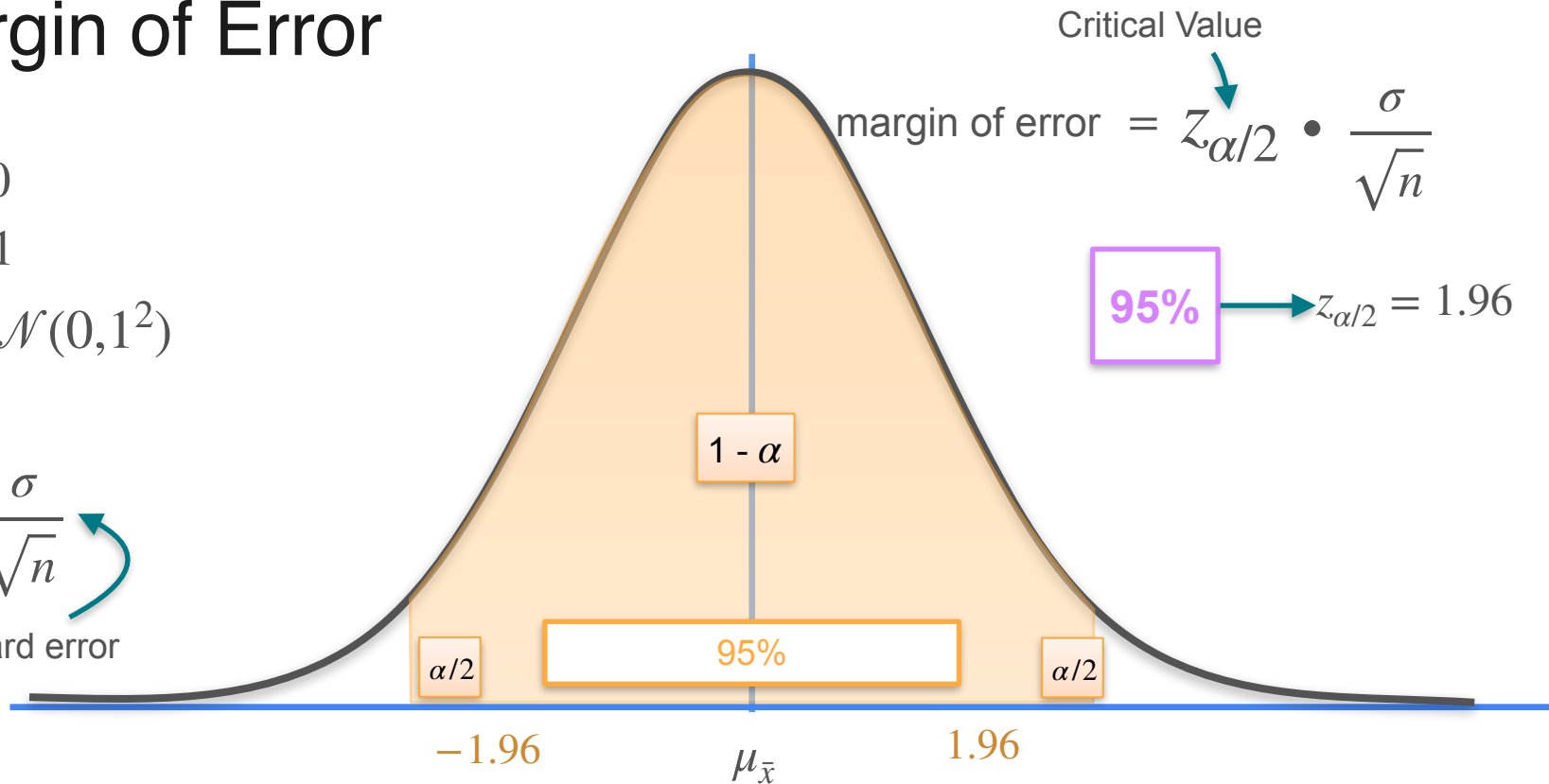
$$\mu = 0$$

$$\sigma = 1$$

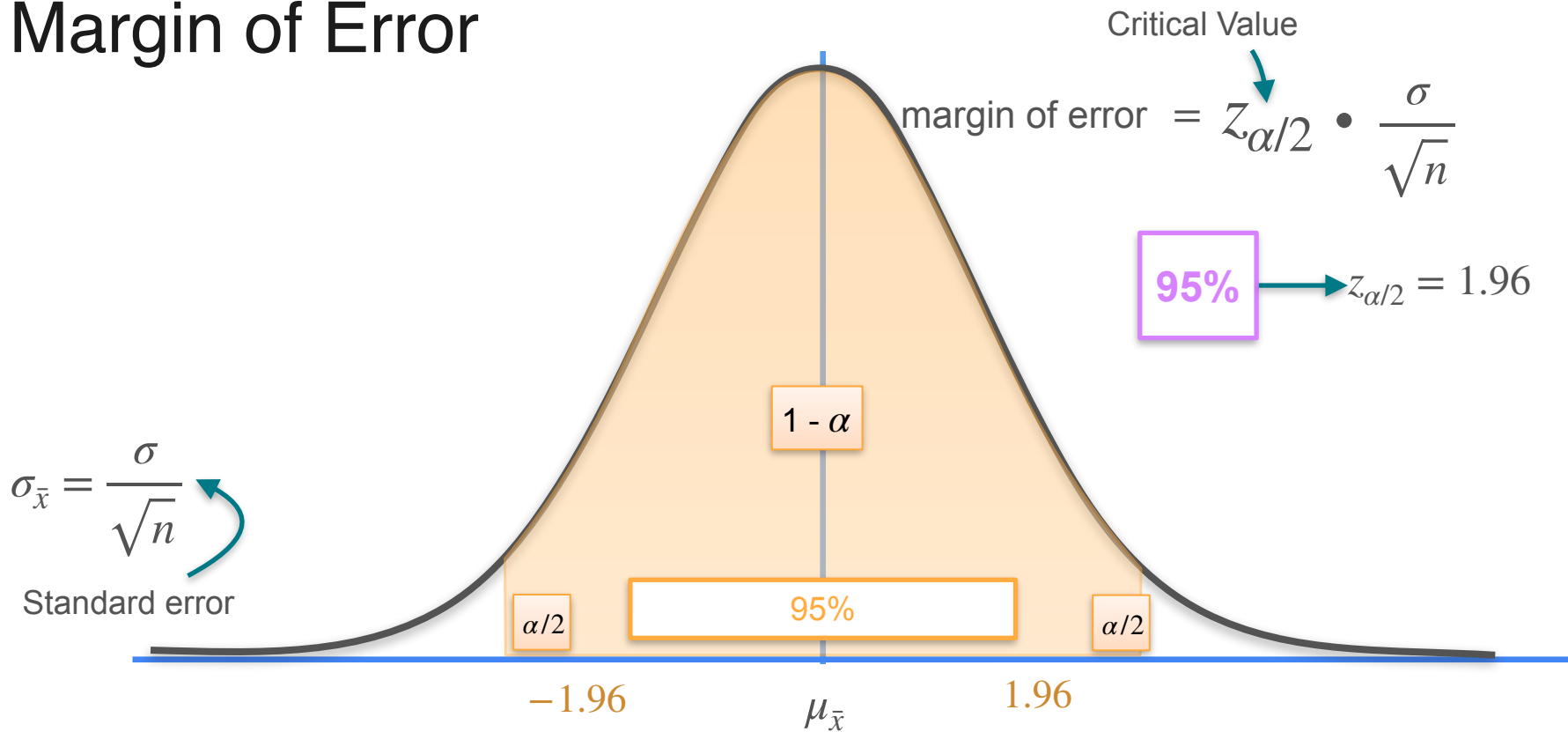
$$\bar{X} \sim \mathcal{N}(0, 1^2)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Standard error



Margin of Error



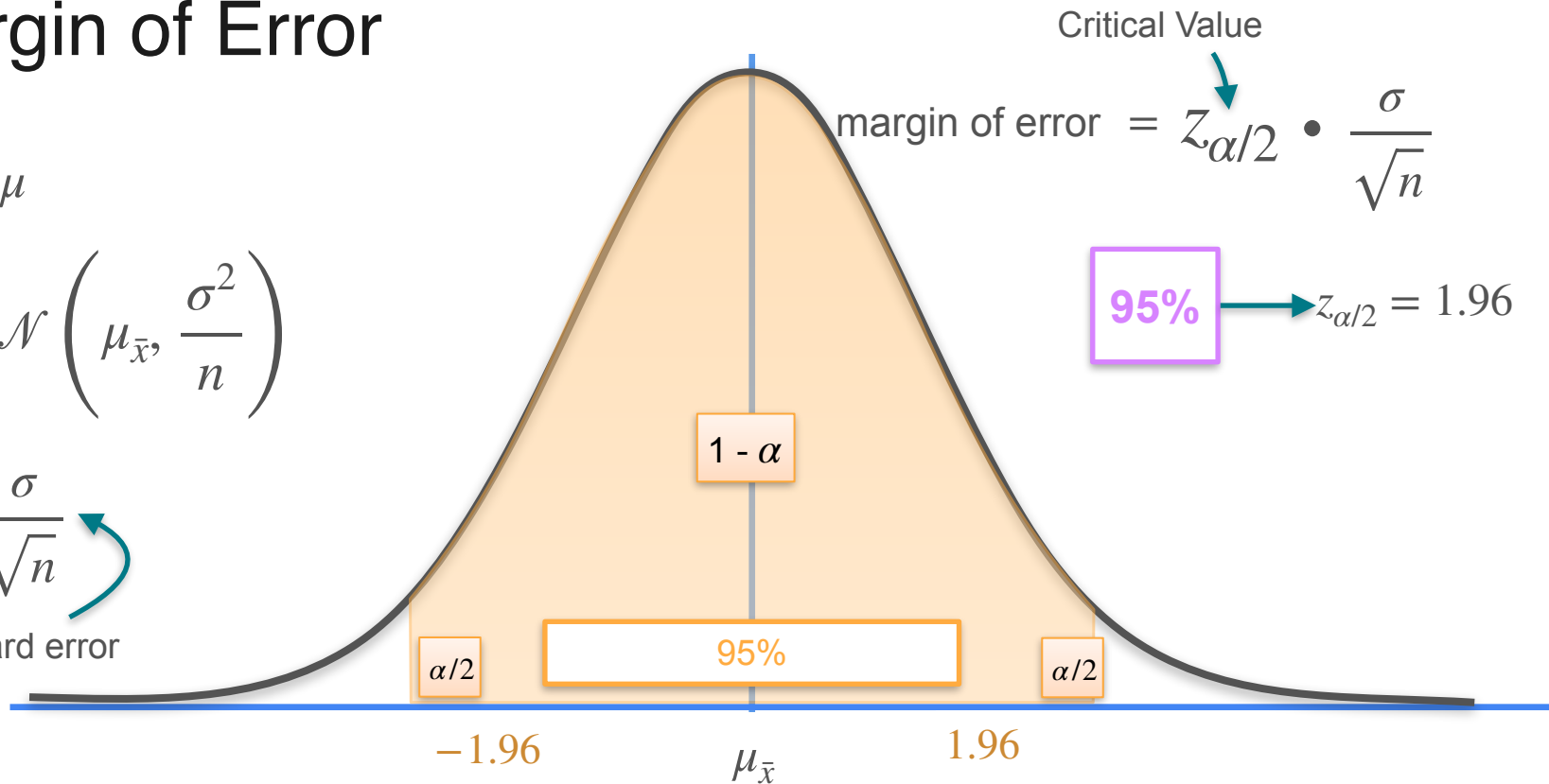
Margin of Error

$$\mu_{\bar{x}} = \mu$$

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Standard error



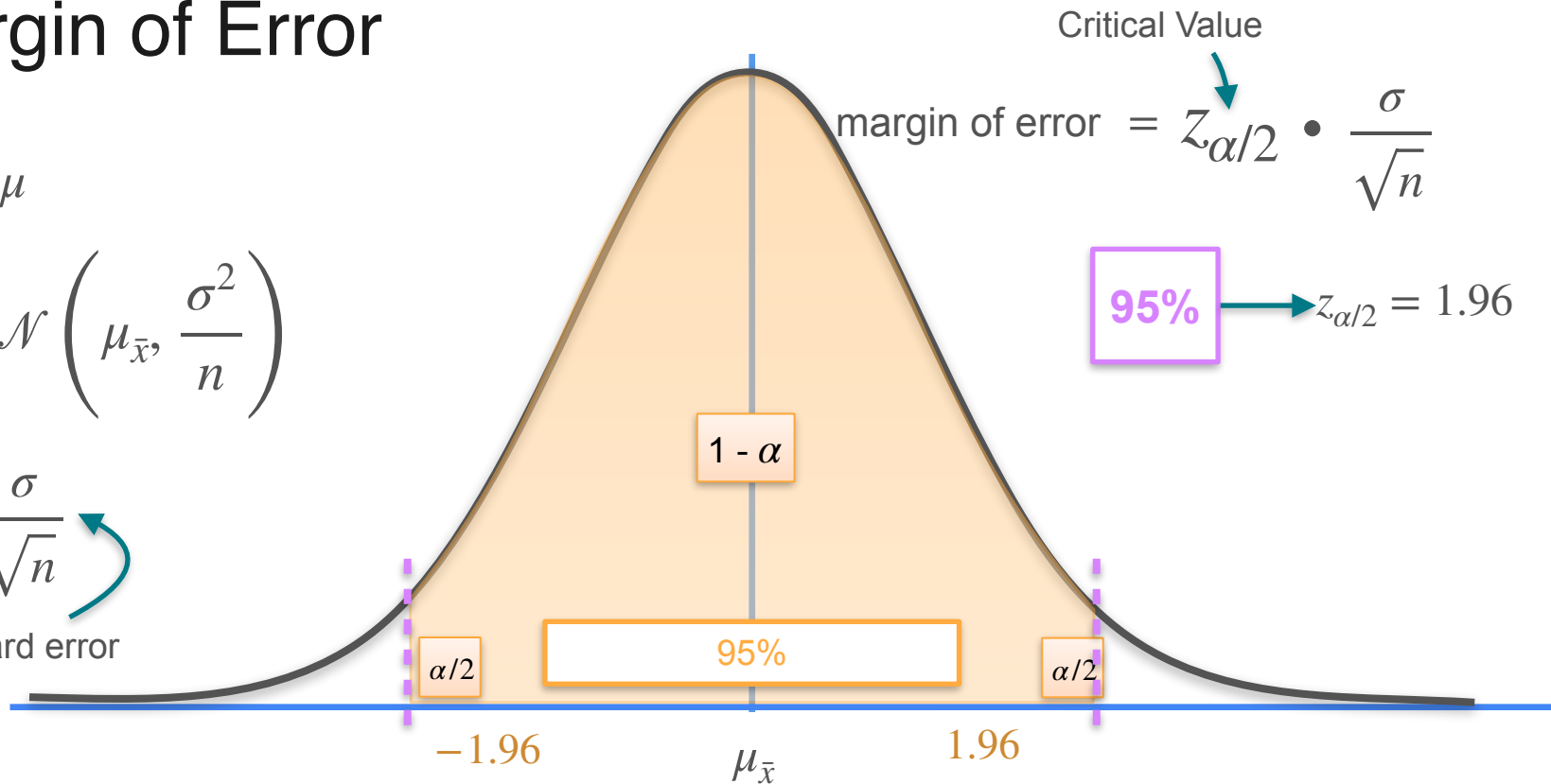
Margin of Error

$$\mu_{\bar{x}} = \mu$$

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Standard error



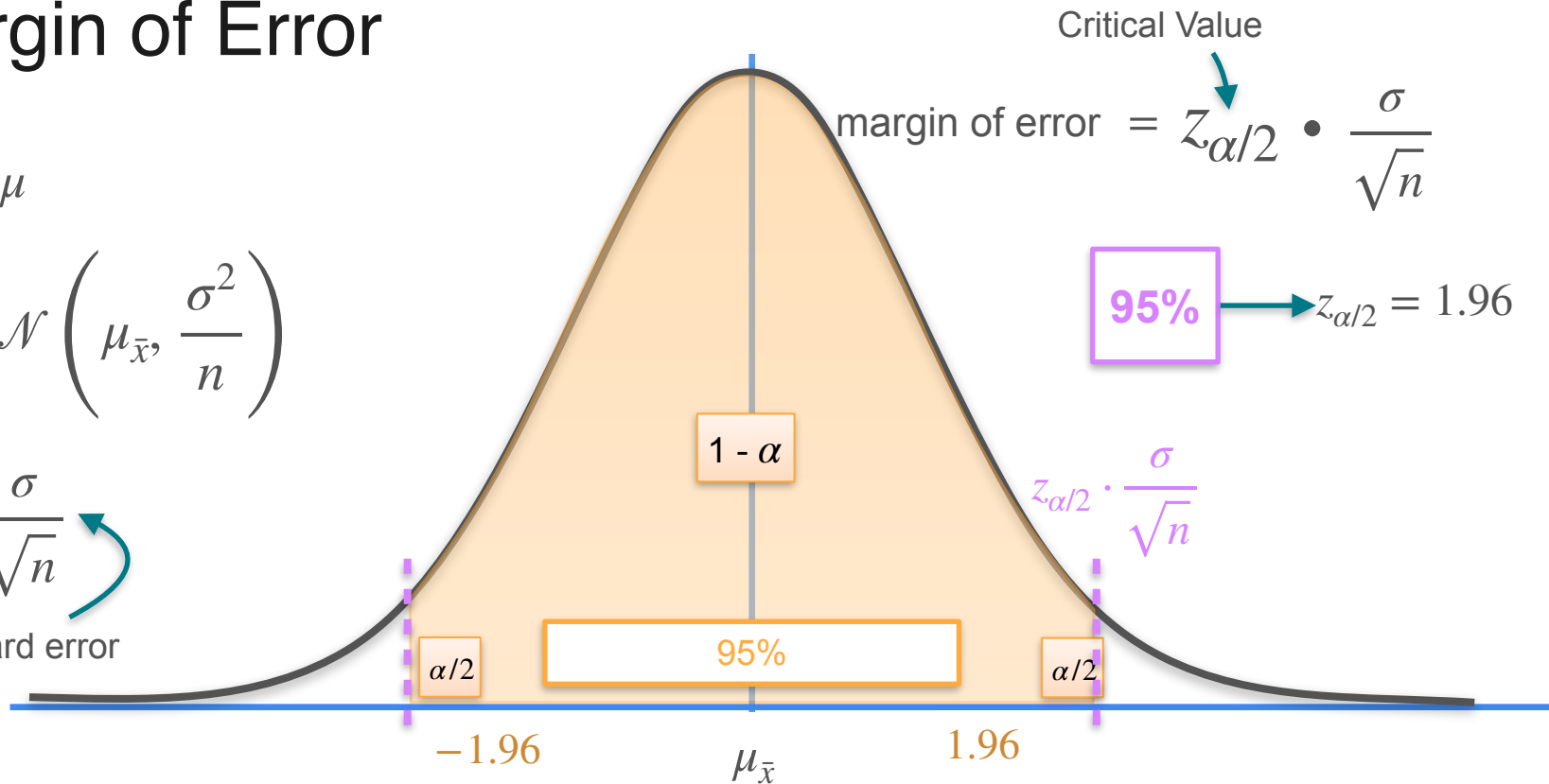
Margin of Error

$$\mu_{\bar{x}} = \mu$$

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Standard error



Margin of Error

$$\mu_{\bar{x}} = \mu$$

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

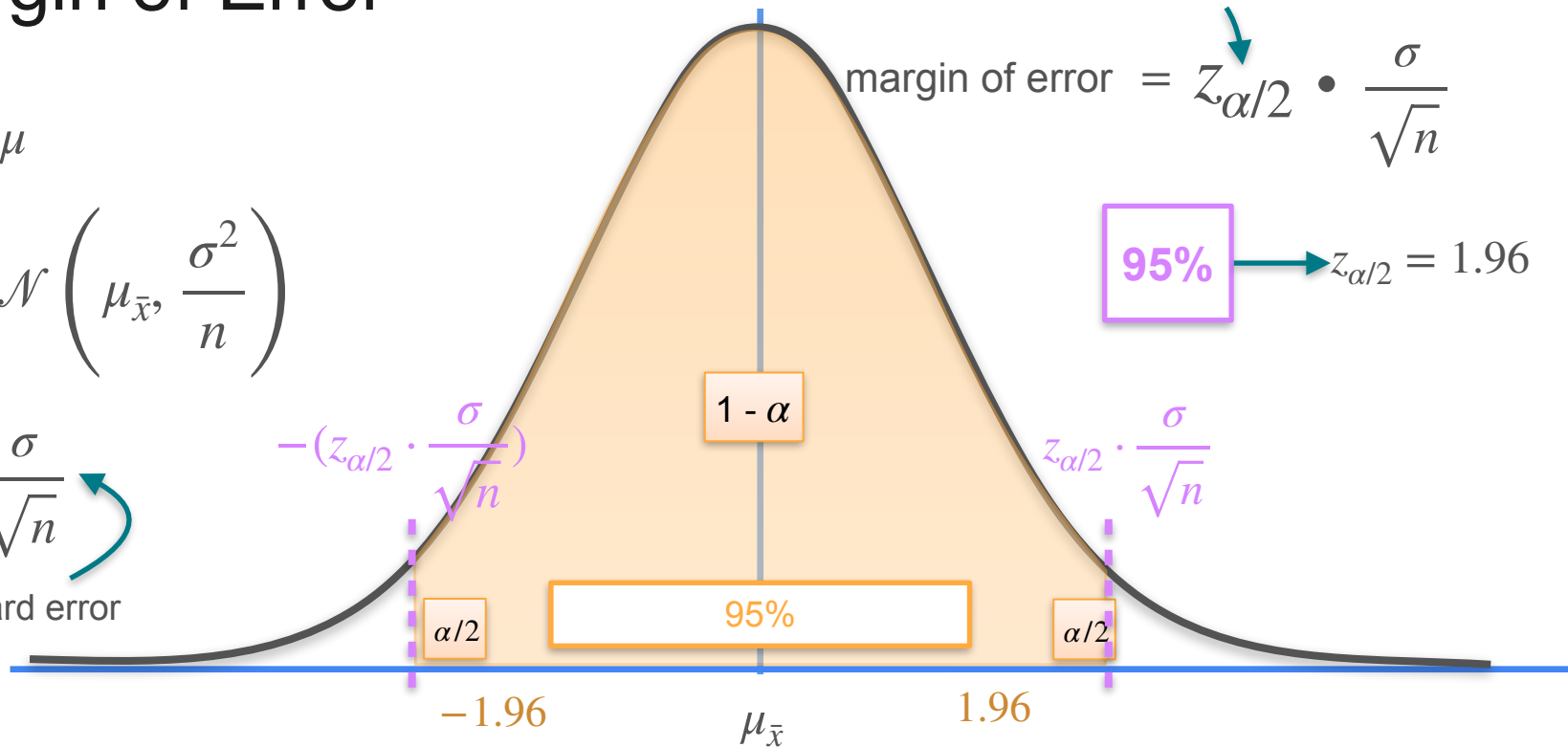
Standard error

Critical Value

$$\text{margin of error} = z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$$

95%

$$z_{\alpha/2} = 1.96$$



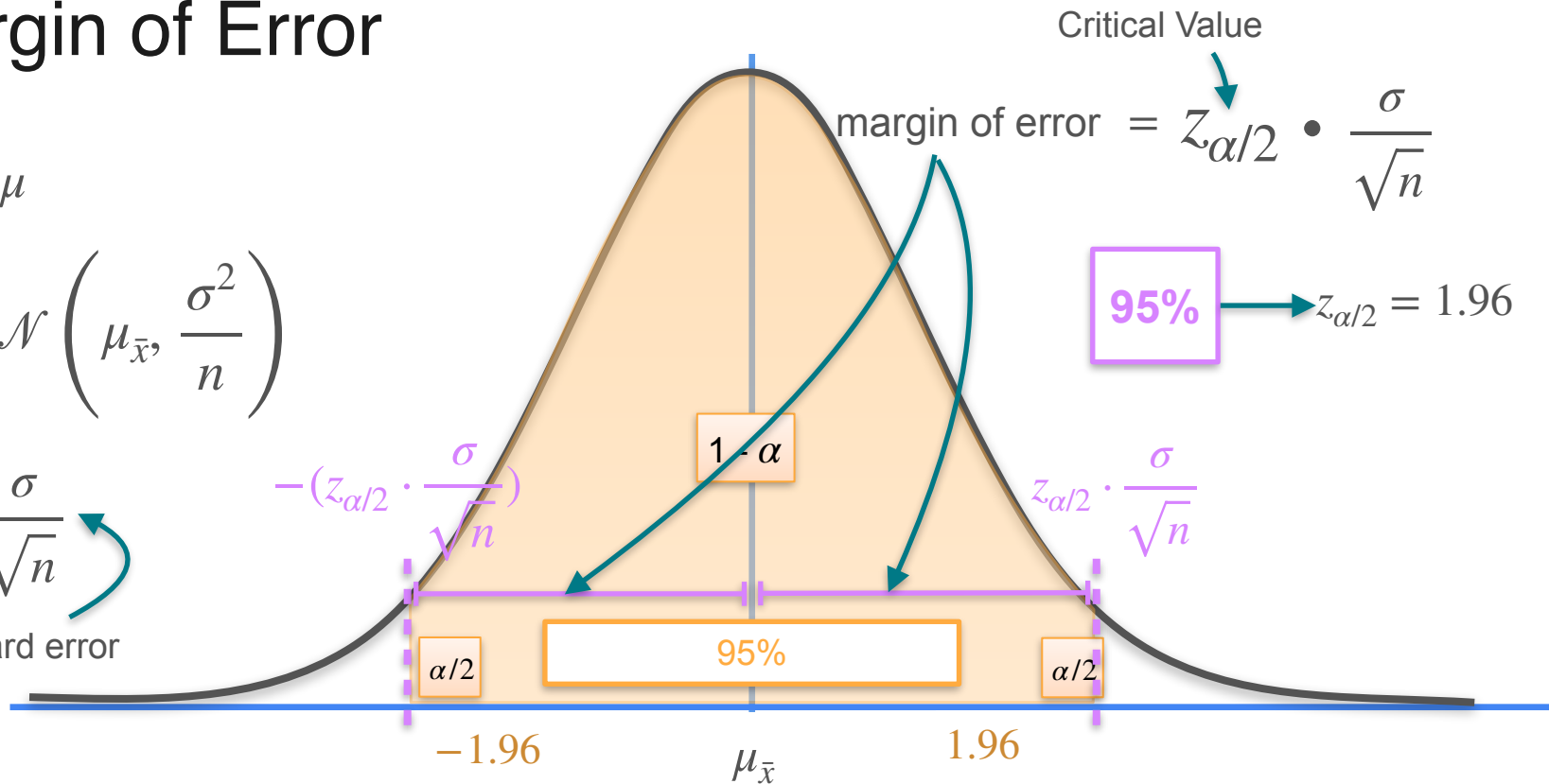
Margin of Error

$$\mu_{\bar{x}} = \mu$$

$$\bar{X} \sim \mathcal{N}\left(\mu_{\bar{x}}, \frac{\sigma^2}{n}\right)$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Standard error





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Confidence Interval

Confidence Interval - Calculation Steps

Confidence Interval - Calculation Steps

STEPS:



Confidence Interval - Calculation Steps

STEPS:

- Find the sample mean

Confidence Interval - Calculation Steps

STEPS:

- Find the sample mean

\bar{x}

Confidence Interval - Calculation Steps

STEPS:

- Find the sample mean
- Define a desired confidence level ($1 - \alpha$)

\bar{x}

Confidence Interval - Calculation Steps

STEPS:

- Find the sample mean
- Define a desired confidence level ($1 - \alpha$)

\bar{x}

95%

Confidence Interval - Calculation Steps

STEPS:

- Find the sample mean
- Define a desired confidence level ($1 - \alpha$)
- Get the critical value ($z_{\alpha/2}$)

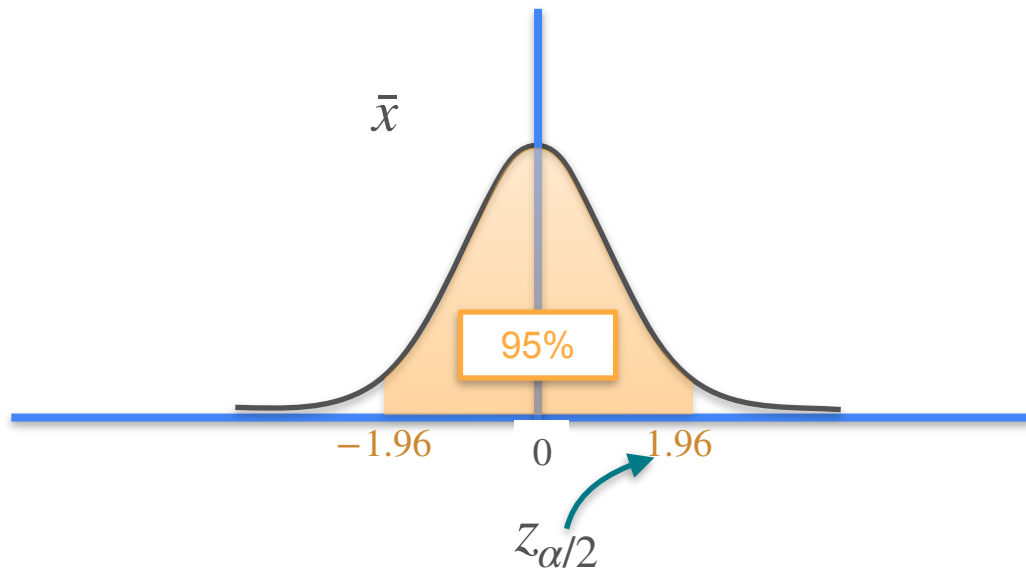
\bar{x}

95%

Confidence Interval - Calculation Steps

STEPS:

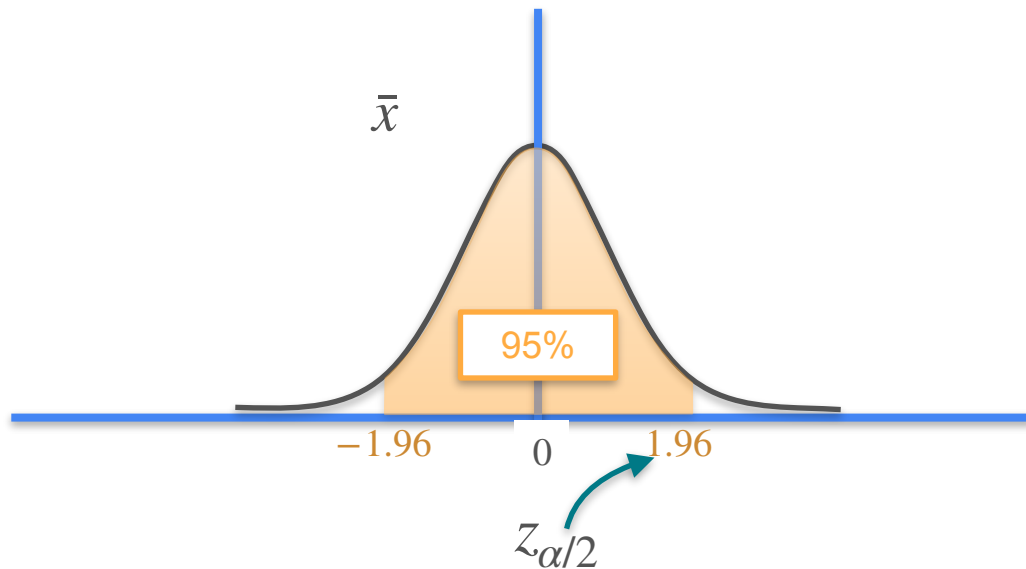
- Find the sample mean
- Define a desired confidence level ($1 - \alpha$)
- Get the critical value ($z_{\alpha/2}$)



Confidence Interval - Calculation Steps

STEPS:

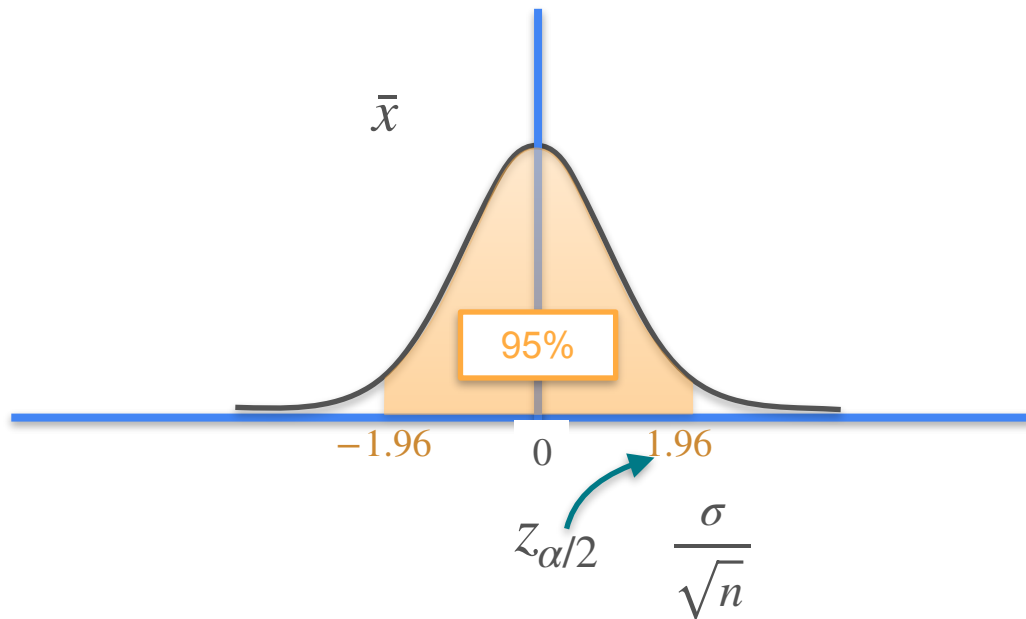
- Find the sample mean
- Define a desired confidence level ($1 - \alpha$)
- Get the critical value ($z_{\alpha/2}$)
- Find the standard error ($\frac{\sigma}{\sqrt{n}}$)



Confidence Interval - Calculation Steps

STEPS:

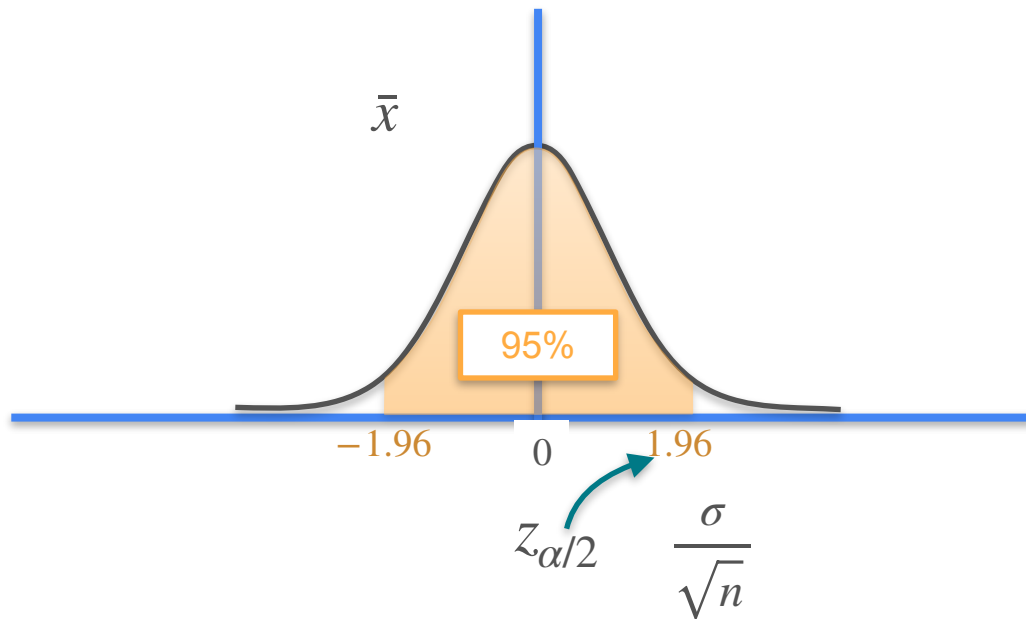
- Find the sample mean
- Define a desired confidence level ($1 - \alpha$)
- Get the critical value ($z_{\alpha/2}$)
- Find the standard error ($\frac{\sigma}{\sqrt{n}}$)



Confidence Interval - Calculation Steps

STEPS:

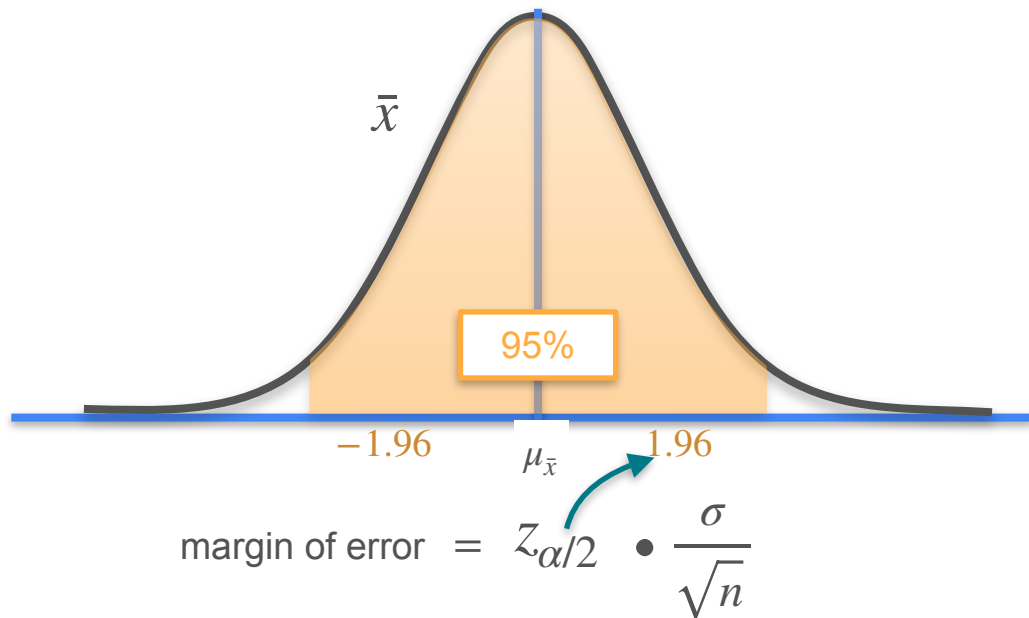
- Find the sample mean
- Define a desired confidence level ($1 - \alpha$)
- Get the critical value ($z_{\alpha/2}$)
- Find the standard error ($\frac{\sigma}{\sqrt{n}}$)
- Find the margin of error



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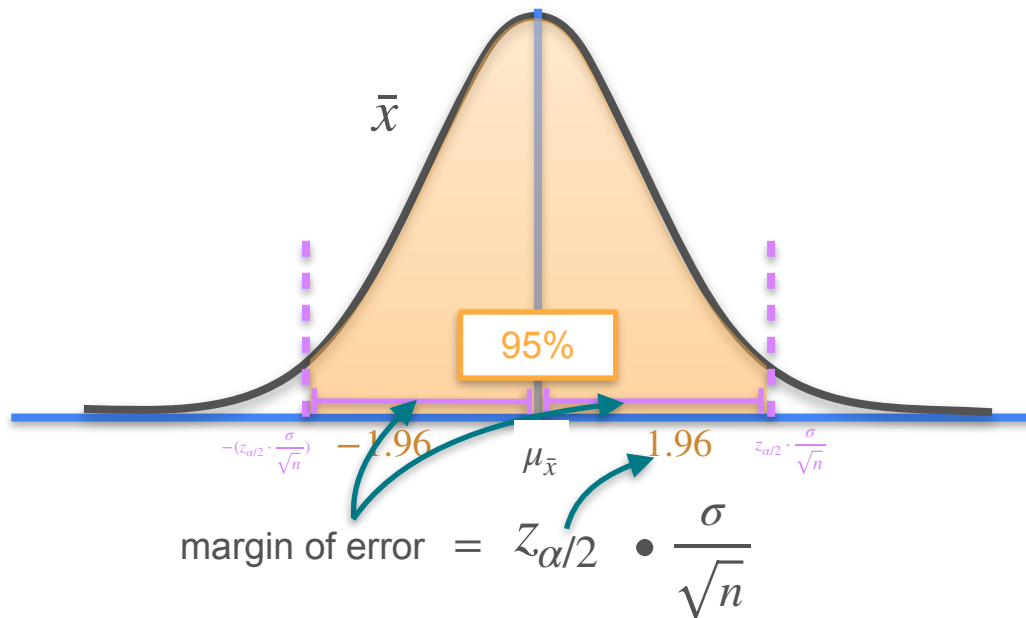
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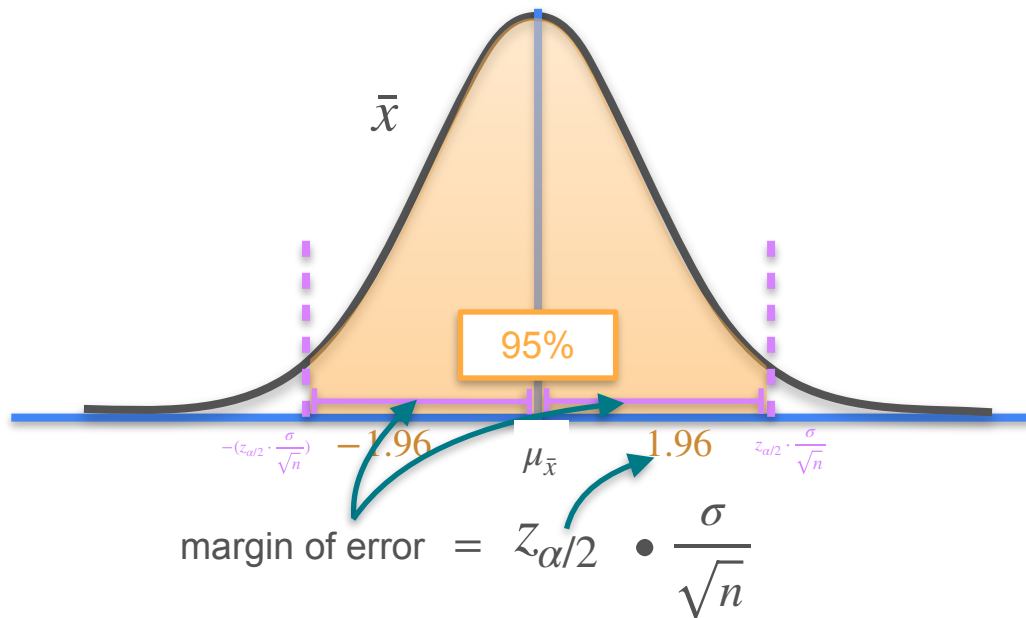
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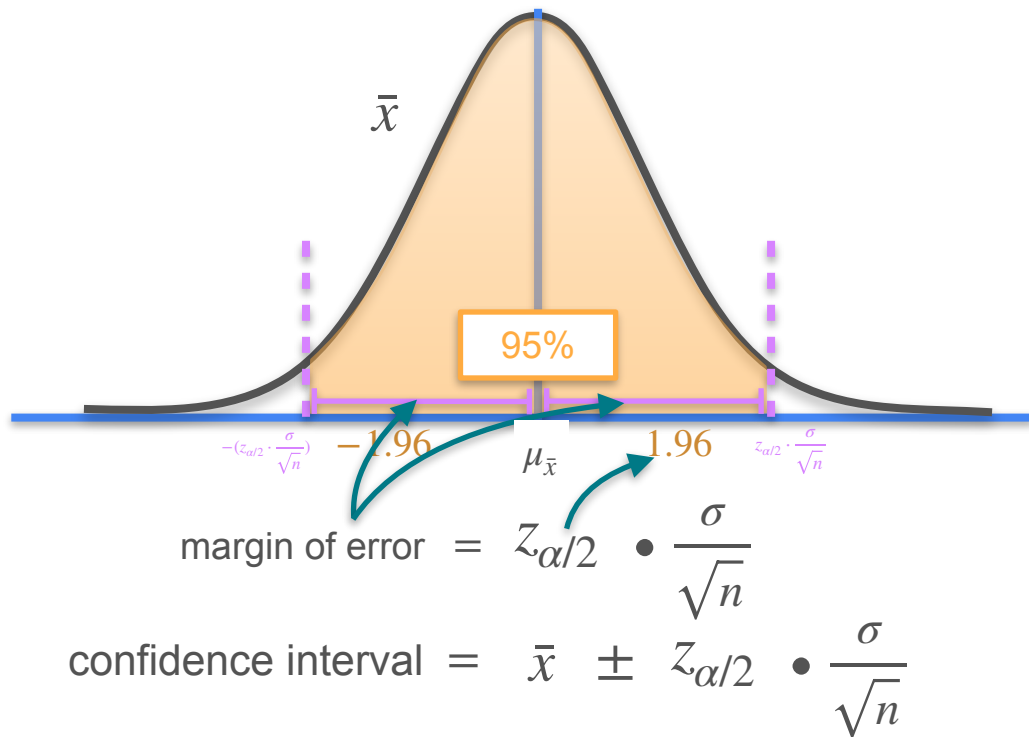
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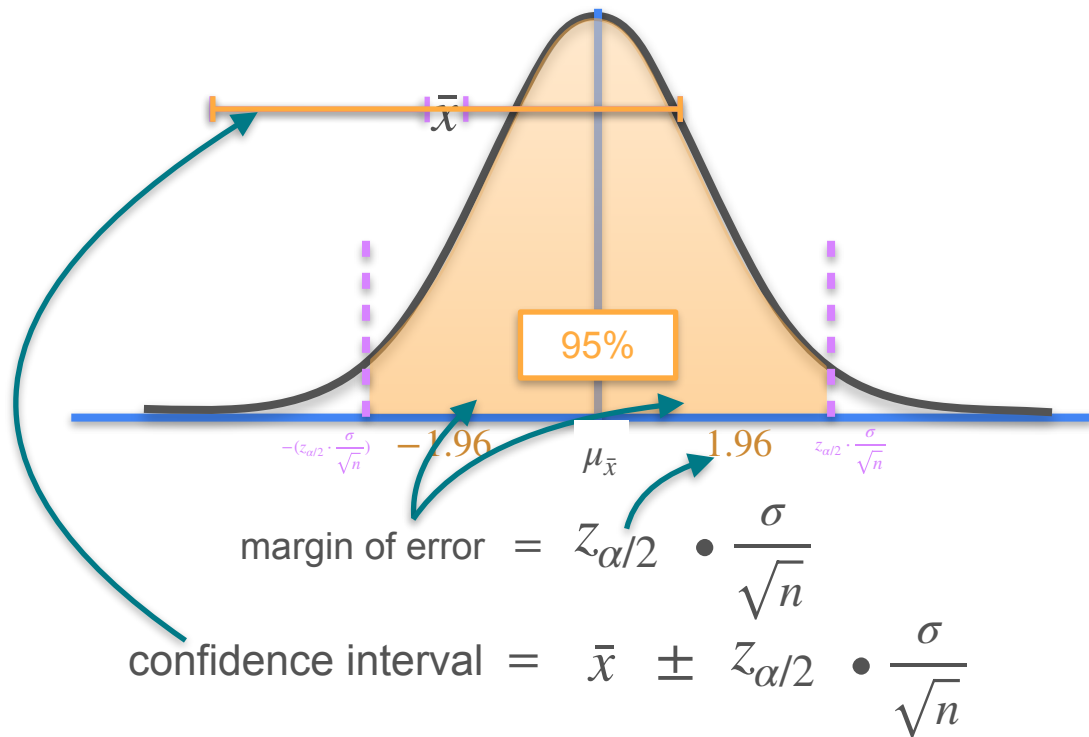
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Assumptions

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Assumptions

- Simple random sample

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Assumptions

- Simple random sample
- Sample size > 30 or population is approximately normal



DeepLearning.AI

Confidence Interval

Confidence Interval - Example