

Exercise 13:

- (a) What is the sum V of the twelve vectors that go from the center of a clock to the hours 01:00, 02:00, ..., 12:00?
- (b) If the 02:00 vector is removed, why do the 11 remaining vectors add to 08:00?
- (c) What are the components of that 02:00 vector $v = (\cos\theta, \sin\theta)$?
- (a) The sum is the zero vector because of the symmetry.
- (b) Because 08:00 is the vector that is symmetric to the 02:00 vector.
- (c) Each hour is $-\frac{\pi}{12}$, but our zero is actually at 03:00. So 2:00 is $(\cos(\frac{2\pi}{12}), \sin(\frac{2\pi}{12}))$

$$\cos\left(\frac{2\pi}{12}\right) = 0.866025403784439$$

$$\sin\left(\frac{2\pi}{12}\right) = 0.5$$

