

# Web Information Retrieval

## Assignment 5

Team Name : Gamma

### Members

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## 1. Query Likelihood Model (14 Points) :

Doc 1: “teach education school university education”.

Doc 2: “education education campus teach teach”.

Doc 3: “university road school teach learning”.

Doc 4: “campus learning education learning”.

Query: “teach teach education campus”.

1.1

$$P_{M_{d_i}}(t_j)$$

Term(t)	D1	D2	D3	D4
campus	0	0.2	0	0
education	0.4	0.4	0	0.25
learning	0	0	0.2	0.50
road	0	0	0.2	0
school	0.2	0	0.2	0
teach	0.2	0.4	0.2	0
university	0.2	0	0.2	0

1.2.

Term(t)	$P_{M_c}(t_j)$
campus	0.105
education	0.263
learning	0.158
road	0.053
school	0.105
teach	0.210
university	0.105

2.

$$P_{\text{uni}}(d \mid q).$$

Term(t)	d1	d2	d3	d4	$P_{\text{uni}}(d \mid q).$
campus	0.2	0.4	0.2	0	0
education	0.4	0.4	0	0.25	0
teach	0.2	0.4	0.2	0	0

3.

$$P_{\text{interp-uni}}(d \mid q)$$

Query: “teach teach education campus”.

Term(t)	d1	d2	d3	d4	$P_{\text{interp-uni}}(d \mid q)$
campus	$(0*.5+.105*.5)$ =0.525	$(.2*.5+.105*.5)$ =0.625	$(0*.5+.105*.5)$ =0.525	$(0*.5+.105*.5)$ =0.525	0.09
education	$(.4*.5+.263*.5)$ =0.3315	$(.4*.5+.263*.5)$ =0.3315	$(0*.5+.263*.5)$ =.1315	$(.25*.5+.263*.5)$ =0.748	0.01
teach	$(.2*.5+.21*.5)$ =0.205	$(.4*.5+.21*.5)$ =0.305	$(.2*.5+.21*.5)$ =0.205	$(0*.5+.21*.5)$ =0.105	0.001

## 2. n-gram Models (10 Points):

1. Estimate the probability of a term sequence  $t_1 t_2 t_3 t_4 t_5$  appearing in a document.

**Bigram:**  $[\{tf(t_4 t_5, d)\} / \{tf(t_4, d)\}] * [\{tf(t_2 t_4, d)\} / \{tf(t_4, d)\}] * [\{tf(t_2 t_3, d)\} / \{tf(t_3, d)\}] * [\{tf(t_1 t_2, d)\} / \{tf(t_1, d)\}]$ .

**Trigram:**  $[\{tf(t_3 t_4 t_5, d)\} / \{tf(t_3 t_4, d)\}] * [\{tf(t_2 t_3 t_4, d)\} / \{tf(t_2 t_3, d)\}] * [\{tf(t_1 t_2 t_3, d)\} / \{tf(t_1 t_2, d)\}]$

General Formula:

$$\text{Bigram} = \prod_{n=2 \text{ to } n=i} [\{tf(t_{n-1} t_n, d)\} / \{tf(t_{n-1}, d)\}]$$

$$\text{Trigram} = \prod_{n=3 \text{ to } n=i} [\{tf(t_{n-2} t_{n-1} t_n, d)\} / \{tf(t_{n-2} t_{n-1}, d)\}]$$

## 2.2

Doc 1: "rose is a rose is a rose is a rose"

Doc 2: "rose rose rose rose is is is a a a"

Doc 3: "rose is a rose"

Doc 4: "a rose is a"

	d1	d2	d3	d4
rose , t1	4/10=0.4	4/10=0.4	2/4=0.5	1/4=0.25
is , t2	3/10=0.3	3/10=0.3	1/4=0.25	1/4=0.25
a , t3	3/10=0.3	3/10=0.3	1/4=0.25	2/4=0.5

'rose is a rose'

### Probability according to unigram model:

$$\begin{aligned}\text{Doc1} &= \text{tf}(\text{rose}, d)/\text{dl}(d1) * \text{tf}(\text{is}, d)/\text{dl}(d1) * \text{tf}(\text{a}, d)/\text{dl}(d1) * \text{tf}(\text{rose}, d)/\text{dl}(d1) \\ &\Rightarrow 0.4 * 0.3 * 0.3 * 0.4 \\ &\Rightarrow 0.0144\end{aligned}$$

$$\begin{aligned}\text{Doc2} &= \text{tf}(\text{rose}, d)/\text{dl}(d2) * \text{tf}(\text{is}, d)/\text{dl}(d2) * \text{tf}(\text{a}, d)/\text{dl}(d2) * \text{tf}(\text{rose}, d)/\text{dl}(d2) \\ &\Rightarrow 0.4 * 0.3 * 0.3 * 0.4 \\ &\Rightarrow 0.0144\end{aligned}$$

$$\begin{aligned}\text{Doc3} &= \text{tf}(\text{rose}, d)/\text{dl}(d3) * \text{tf}(\text{is}, d)/\text{dl}(d3) * \text{tf}(\text{a}, d)/\text{dl}(d3) * \text{tf}(\text{rose}, d)/\text{dl}(d3) \\ &\Rightarrow 0.5 * 0.25 * 0.25 * 0.5 \\ &\Rightarrow 0.0156\end{aligned}$$

$$\begin{aligned}\text{Doc4} &= \text{tf}(\text{rose}, d)/\text{dl}(d4) * \text{tf}(\text{is}, d)/\text{dl}(d4) * \text{tf}(\text{a}, d)/\text{dl}(d4) * \text{tf}(\text{rose}, d)/\text{dl}(d4) \\ &\Rightarrow 0.25 * 0.25 * 0.5 * 0.25 \\ &\Rightarrow 0.0078\end{aligned}$$

**Probability according to bigram model:**

	d1	d2	d3	d4
rose is , t1	$3/4=0.75$	$1/4=0.25$	$1/2=0.5$	$1/1=1$
Is a , t2	$3/3=1$	$1/3=0.33$	$1/1=1$	$1/1=1$
a rose , t3	$3/3=1$	$0/3=0$	$1/1=1$	$1/2=0.5$

$$\begin{aligned}\text{Doc1} &= \text{tf}(\text{rose is , d})/\text{tf}(\text{rose , d}) * \text{tf}(\text{is a , d})/\text{tf}(\text{is , d}) * \text{tf}(\text{a rose , d})/\text{tf}(\text{a , d}) \\ &=> 0.75 * 1 * 1 \\ &=> 0.75\end{aligned}$$

$$\begin{aligned}\text{Doc2} &= \text{tf}(\text{rose is , d})/\text{tf}(\text{rose , d}) * \text{tf}(\text{is a , d})/\text{tf}(\text{is , d}) * \text{tf}(\text{a rose , d})/\text{tf}(\text{a , d}) \\ &=> 0.25 * 0.33 * 0 \\ &=> 0\end{aligned}$$

$$\begin{aligned}\text{Doc3} &= \text{tf}(\text{rose is , d})/\text{tf}(\text{rose , d}) * \text{tf}(\text{is a , d})/\text{tf}(\text{is , d}) * \text{tf}(\text{a rose , d})/\text{tf}(\text{a , d}) \\ &=> 0.5 * 1 * 1 \\ &=> 0.5\end{aligned}$$

$$\begin{aligned}\text{Doc4} &= \text{tf}(\text{rose is , d})/\text{tf}(\text{rose , d}) * \text{tf}(\text{is a , d})/\text{tf}(\text{is , d}) * \text{tf}(\text{a rose , d})/\text{tf}(\text{a , d}) \\ &=> 1 * 1 * 0.5 \\ &=> 0.5\end{aligned}$$

**Probability according to trigram model:**

	d1	d2	d3	d4
rose is a , t1	$3/3=1$	$0/1=0$	$1/1=1$	$1/1=1$
Is a rose , t2	$3/3=1$	$0/1=0$	$1/1=1$	$0/1=0$

$$\begin{aligned}\text{Doc1} &= \text{tf}(\text{rose is a , d})/\text{tf}(\text{rose is , d}) * \text{tf}(\text{is a rose , d})/\text{tf}(\text{is a , d}) \\ &=> 1 * 1 \\ &=> 1\end{aligned}$$

$$\begin{aligned}\text{Doc2} &= \text{tf}(\text{rose is a , d})/\text{tf}(\text{rose is , d}) * \text{tf}(\text{is a rose , d})/\text{tf}(\text{is a , d}) \\ &=> 0 * 0\end{aligned}$$

=> 0

Doc3 =  $\text{tf}(\text{rose is a}, d) / \text{tf}(\text{rose is}, d) * \text{tf}(\text{is a rose}, d) / \text{tf}(\text{is a}, d)$

=>  $1 * 1$

=> 1

Doc4 =  $\text{tf}(\text{rose is a}, d) / \text{tf}(\text{rose is}, d) * \text{tf}(\text{is a rose}, d) / \text{tf}(\text{is a}, d)$

=>  $1 * 0$

=> 0