$$P(A \cap B)P(B) = P(B \cap A)P(A)$$
 therefore $P(A \cap B) = \frac{P(B \cap A)P(A)}{P(B)}$ and $P(A|B) = \frac{P(B|A)P(A)}{P(B)}$

$$p_{X,Y}(x,y) = p_{X|Y}(X|Y)p_Y(y) = p_{Y|X}(y|x)p_X(x)$$
 therefore $p_{X|Y}(X|Y) = p_{Y|X}(y|x)\frac{p_X(x)}{p_Y(y)}$

Laws of Total Probability: If $B = \{B_1, ... B_m\}$ is an event space, then

$$P(X) = \sum_{i=1}^{m} P(X \cap B_i) \text{ and } P(X) = \sum_{i=1}^{m} P(X|B_i) \text{ and } p_X(x) = \sum_{i=1}^{m} p_{X|B_i}(x)P(B_i) \text{ and } p_X(x) = \sum_{y \in S_Y} p_{X|Y}(x|y)p_Y(y)$$

Expectation and variance: $E[X] = \sum_{x \in S_x} x \cdot p_X(x)$ and $Var(X) = E[(X - E[X])^2] = E[X^2] - E[X]^2$ E[aX + b] = aE[X] + b and $Var(aX + b) = a^2 \cdot Var(X)$ if $a, b \in R$ Conditional Expectation: $E[X|B] = \sum_{x \in B} x \cdot p_{X|B}(x)$ and E[E[X|Y]] = E[X] and $Var(X|B) = E[X^2|B] - E[X|B]^2$ De Morgan's Law $(A \cup B)^c = A^c \cap B^c$ and $(A \cap B)^c = A^c \cup B^c$

RV Type	PMF	Exp	Var
Bernoulli	$p_X(x) = \begin{cases} 1 - p & x = 0\\ p & x = 1\\ 0 & otherwise \end{cases}$	p	p(1-p)
Binomial	$p_X(x) = \begin{cases} \binom{n}{x} p^x (1-p)^{n-x} & x = 0, 1,, n \\ 0 & otherwise \end{cases}$	np	np(1-p)
Geometric	$p_X(x) = \begin{cases} (1-p)^{x-1}p & x = 0, 1, \dots \\ 0 & otherwise \end{cases}$	$\frac{1}{p}$	$\frac{1-p}{p^2}$
Pascal	$p_X(x) = \begin{cases} \left(\begin{array}{c} x-1\\ k-1 \end{array} \right) p^k (1-p)^{x-k} & x = k, k+1, \dots \\ 0 & otherwise \end{cases}$	$\frac{k}{p}$	$\frac{k(1-p)}{p^2}$

Marginal PMF and independence

$$p_X(x) = \sum_{y \in S_Y} p_{X,Y}(x,y)$$
 and $p_{X,Y}(x,y) = p_X(x) \times p_Y(y)$

Correlation	Covariance	Correlation Coefficient	
$\gamma_{X,Y} = E[X \cdot Y] = 0$ if Orthogonal	$\sigma_{X,Y} = E[(X - E[X])(Y - E[Y])] = 0$ if uncorrelated	$\rho_{X,Y} = \frac{Cov(X,Y)}{Var(X) \cdot Var(Y)}$	
$F(W) = c(V, V) + hon F[W] = \sum_{\alpha(m, v) = 0} c(m, v) = c(m, v) + V + V + V + V + V + V + V + V + V + $			

If W = g(X, Y) then $E[W] = \sum_{(x,y) \in S_{X,Y}} g(x,y) p_{X,Y}(x,y)$ and $Var(X+Y) = Var(X) + Var(Y) + 2\sigma_{X,Y}$

$$E[W] = \sum_{(x,y) \in S_{X,Y}} g(x,y) p_{X,Y}(x,y) \text{ and } E[W|B] = \sum_{(x,y) \in S_{X,Y}} g(x,y) p_{X,Y|B}(x,y)$$

$$p_{X,Y|B}(x,y) = P(X=x,Y=y|B) = \begin{cases} \frac{p_{X,Y}(x,y)}{P(B)} & \text{if } (x,y) \in B \\ 0 & otherwise \end{cases} \text{ given } B \subset R^2$$