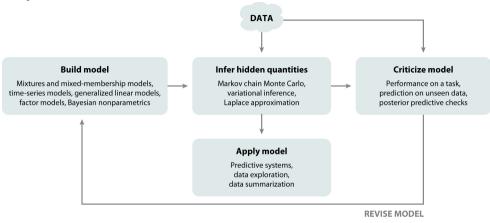
STATS271/371: Applied Bayesian Statistics

Mixed Membership Models, Topic Models, and Variational Inference

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Box's Loop



Blei DM. 2014. Annu. Rev. Stat. Appl. 1:203–32

Lap 5: Mixed Membership Models and Variational Inference

- ► Model: Mixed Membership Models (specifically, topic models)
- Algorithm: Coordinate Ascent Variational Inference (CAVI)

These slides are based on unpublished lecture notes by Dave Blei.

Mixed Membership Models

Mixed membership models are designed for grouped data.

Each "data point" is itself a collection of observations. For example,

- ► in text analysis, a document is a collection of observed words.
- in social science, a survey is a collection of observed answers.
- ▶ in genetic sequencing, a genome is a collection of observed genes.

Mixed membership models look for patterns like the components of a mixture model, but allowing each data point to involve multiple components.

Notation for a mixed membership model

- Let $\mathbf{x}_n = (x_{n,1}, \dots, x_{n,L})$ denote n-th **data point**. It contains a **collection of observations**. To simplify notation, assume all data points are length L.
- ► Each data point reflects a **combination of** K **mixture components** with parameters $\{\eta_k\}_{k=1}^K$. These are shared by all documents.
- ► Each data point has its own **mixture proportions**, $\pi_n \in \Delta_K$.
- ► Each observation is assigned to one of the components by $z_{n,\ell} \in \{1, ..., K\}$.

Topic models

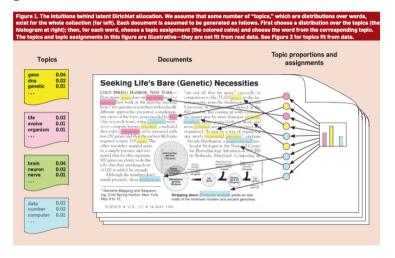
The most common mixed-membership model is the **topic model**, a generative model for documents.

Topic models are so common, they have their own nomenclature:

data set	corpus	collection of documents
data point	document	collection of words
observation	word	one element of a document
mixture component	topic	distribution over words
mixture proportions	topic proportions	distribution over topics
mixture assignment	topic assignment	which topic produced a word

Table: Rosetta stone for translating between mixed membership model and topic model notation.

Topic modeling intuition



From Blei [2012].

Topic modeling of New York Times articles



Figure 6.1: Posterior topics from the The New York Times.

Dynamic topic modeling of Science articles

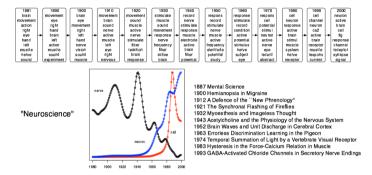


Figure 4. Examples from the posterior analysis of a 20-topic dynamic model estimated from the Science corpus. For two topics, we illustrate: (a) the top ten words from the inferred posterior distribution at ten year lags (b) the posterior estimate of the frequency as a function of year of several words from the same two topics (c) example articles throughout the collection which exhibit these topics. Note that the plots are scaled to give an idea of the shape of the trajectory of the words' posterior probability (i.e., comparisons across words are not meaningful).

From Blei and Lafferty [2006].

Topic modeling of congressional voting records

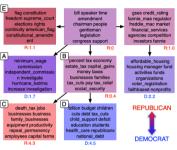


Figure 7.2: Topics discovered from Congressional floor debates using a downstream model to capture speaker's ideology. Many first-level topics are bipartisan (purple), while lower level topics are associated with specific ideologies (Democrats blue, Republicans red). For example, the "tax" topic (B) is bipartisan, but its Democratic-leaning child (D) focuses on social goals supported by taxes ("children", "education", "health care"), while its Republican-leaning child (C) focuses on business implications "death tax", "jobs", "businesses"). The number below each topic denotes the magnitude of a learned regression parameter associated with that topic. Colors and the numbers beneath each topic show the regression parameter η associated with the topic. From Nguyen et al. [2013].

The generative process for a mixed membership model

The generative model process is:

- for each mixture component k = 1, ..., K, sample its parameter $\eta_k \sim p(\eta_k \mid \phi)$
- ▶ for each data point n = 1, ..., N:
 - ▶ sample mixture proportions $\pi_n \sim \text{Dir}(\pi_n \mid \alpha)$
 - ▶ for each observation $\ell = 1, ..., L$:
 - ightharpoonup sample mixture assignment $z_{n,\ell} \sim \pi_n$
 - ► sample observation $x_{n,\ell} \sim p(x \mid \eta_{z_{n,\ell}})$

The mixed membership model allows sharing at the dataset level (all data points share the same components) while allowing variability at the data point level (each data point has its own mixture proportions).

The generative process for a topic model

Slide 11 in the language of topic modeling:

- lacktriangledown for each **topic** $k=1,\ldots,K$, sample its parameter $oldsymbol{\eta}_k \sim p(oldsymbol{\eta}_k \mid oldsymbol{\phi})$
- ► for each **document** n = 1, ..., N:
 - ► sample **topic proportions** $\pi_n \sim \text{Dir}(\pi_n \mid \alpha)$
 - ▶ for each word $\ell = 1, ..., L$:
 - ightharpoonup sample **topic assignment** $z_{n,\ell} \sim \pi_n$
 - ► sample word $x_{n,\ell} \sim p(x \mid \eta_{z_{n,\ell}})$

The topic model captures sharing at the corpus level (all documents share the same topics) while allowing variability at the data point level (each document weights topics differently).

The joint distribution

The joint probability for a general mixed membership model is,

$$p(\{\boldsymbol{\eta}_k\}_{k=1}^K, \{\boldsymbol{\pi}_n, \boldsymbol{z}_n, \boldsymbol{x}_n\}_{n=1}^N \mid \boldsymbol{\phi}, \boldsymbol{\alpha}) = \prod_{k=1}^K p(\boldsymbol{\eta}_k \mid \boldsymbol{\phi}) \prod_{n=1}^N \left[p(\boldsymbol{\pi}_n \mid \boldsymbol{\alpha}) \prod_{\ell=1}^L p(\boldsymbol{z}_{n,\ell} \mid \boldsymbol{\pi}_n) p(\boldsymbol{x}_{n,\ell} \mid \boldsymbol{\eta}_{\boldsymbol{z}_{n,\ell}}) \right]$$
(1)

As in mixture models, we can write this equivalently as

$$\rho(\{\boldsymbol{\eta}_k\}_{k=1}^K, \{\boldsymbol{\pi}_n, \boldsymbol{z}_n, \boldsymbol{x}_n\}_{n=1}^N \mid \boldsymbol{\phi}, \boldsymbol{\alpha}) = \prod_{k=1}^K p(\boldsymbol{\eta}_k \mid \boldsymbol{\phi}) \prod_{n=1}^N \left[p(\boldsymbol{\pi}_n \mid \boldsymbol{\alpha}) \prod_{\ell=1}^L \prod_{k=1}^K \left[\pi_{n,k} p(\boldsymbol{x}_{n,\ell} \mid \boldsymbol{\eta}_k) \right]^{\mathbb{I}[\boldsymbol{z}_{n,\ell} = k]} \right]$$
(2)

Latent Dirichlet allocation

Latent Dirichlet Allocation (LDA) [Blei et al., 2003] is the most widely used topic model.

It assumes conjugate Dirichlet-Categorical model for the topics η_{k} and words $x_{n,k}$,

$$p(\eta_k \mid \phi) = Dir(\eta_k \mid \phi), \tag{3}$$

$$p(x_{n,\ell} \mid \eta_{z_{n,\ell}}) = \eta_{z_{n,\ell}, x_{n,\ell}} \tag{4}$$

Plugging in these assumptions, the joint probability is,

$$p(\{\eta_k\}_{k=1}^K, \{\pi_n, \mathbf{z}_n, \mathbf{x}_n\}_{n=1}^N \mid \phi, \alpha)$$
(5)

$$\frac{K}{L} \qquad \frac{N}{L} \qquad \qquad \frac{L}{L}$$

$$= \prod_{k=1}^{K} \operatorname{Dir}(\boldsymbol{\eta}_{k} \mid \boldsymbol{\phi}) \prod_{n=1}^{N} \left[\operatorname{Dir}(\boldsymbol{\pi}_{n} \mid \boldsymbol{\alpha}) \prod_{\ell=1}^{L} \boldsymbol{\pi}_{n, \mathbf{z}_{n, \ell}} \, \boldsymbol{\eta}_{\mathbf{z}_{n, \ell}, \mathbf{x}_{n, \ell}} \right]$$
(6)

$$= \prod_{k=1}^{K} \operatorname{Dir}(\boldsymbol{\eta}_{k} \mid \boldsymbol{\phi}) \prod_{n=1}^{N} \left(\operatorname{Dir}(\boldsymbol{\pi}_{n} \mid \boldsymbol{\alpha}) \prod_{\ell=1}^{L} \left[\prod_{k=1}^{K} \pi_{n,k}^{\mathbb{I}[\boldsymbol{z}_{n,\ell} = k]} \right] \left[\prod_{k=1}^{K} \prod_{v=1}^{V} \eta_{k,v}^{\mathbb{I}[\boldsymbol{z}_{n,\ell} = k] \mathbb{I}[\boldsymbol{x}_{n,\ell} = v]} \right] \right)$$

(7)14/29

Gibbs sampling for LDA

As usual, sample each variable from its conditional distribution, holding the rest fixed.

► **Topic assignments:** The assignments are conditionally independent given the topic parameters and proportions,

$$p(z_{n,\ell} \mid \mathbf{x}_n, \{\eta_k\}_{k=1}^K, \pi_n) \propto \pi_{n, z_{n,\ell}} p(x_{n,\ell} \mid \eta_{z_{n,\ell}})$$
 (8)

▶ **Topic proportions:** Let $N_{n,k} = \sum_{\ell=1}^{L} \mathbb{I}[z_{n,\ell} = k]$ denote the number of words in document n assigned to topic k. Then,

$$p(\boldsymbol{\pi}_n \mid \boldsymbol{\alpha}, \boldsymbol{z}_n) \propto \operatorname{Dir}(\boldsymbol{\pi}_n \mid \boldsymbol{\alpha}) \prod_{k=1}^K \boldsymbol{\pi}_{n,k}^{N_{n,k}} = \operatorname{Dir}([\alpha_1 + N_{n,1}, \dots, \alpha_K + N_{n,K}]). \tag{9}$$

▶ Topic parameters: Let $N_{k,v} = \sum_{n=1}^{N} \sum_{\ell=1}^{L} \mathbb{I}[z_{n,\ell} = k] \mathbb{I}[x_{n,\ell} = v]$ denote the number of times word v was assigned to topic k across all documents. Then,

$$p(\boldsymbol{\eta}_k \mid \{\boldsymbol{z}_n, \boldsymbol{x}_n\}, \boldsymbol{\phi}) \propto \operatorname{Dir}(\boldsymbol{\eta}_k \mid \boldsymbol{\phi}) \prod_{v=1}^{r} \eta_{k,v}^{N_{k,v}} = \operatorname{Dir}([\phi_1 + N_{k,v}, \dots, \phi_V + N_{k,V}]).$$
(10)

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$$\rho(\boldsymbol{\eta}_k \mid \{\boldsymbol{z}_n, \boldsymbol{x}_n\}, \boldsymbol{\phi}) \propto \operatorname{Dir}(\boldsymbol{\eta}_k \mid \boldsymbol{\phi}) \prod_{v=1}^{v} \eta_{k,v}^{N_{k,v}} = \operatorname{Dir}([\phi_1 + N_{k,v}, \dots, \phi_V + N_{k,V}]).$$
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$$p(\boldsymbol{\eta}_k \mid \{\boldsymbol{z}_n, \boldsymbol{x}_n\}, \boldsymbol{\phi}) \propto \operatorname{Dir}(\boldsymbol{\eta}_k \mid \boldsymbol{\phi}) \prod^{V} \boldsymbol{\eta}_{k,v}^{N_{k,v}} = \operatorname{Dir}([\boldsymbol{\phi}_1 + N_{k,v}, \dots, \boldsymbol{\phi}_V + N_{k,V}]). \tag{10}$$

Why does LDA produce sharp topics?

Consider the log posterior as a function of η_k and π_n . From eq. 6, it is,

$$\sum_{k=1}^{K} \log p(\boldsymbol{\eta}_{k} \mid \boldsymbol{\phi}) + \sum_{n=1}^{N} \log p(\boldsymbol{\pi}_{n} \mid \boldsymbol{\alpha}) + \sum_{n=1}^{N} \sum_{\ell=1}^{L} \left(\log \pi_{n, z_{n, \ell}} + \log \eta_{z_{n, \ell}, x_{n, \ell}} \right)$$
(11)

The double sum over n and ℓ dominates this expression.

It encourages topic proportions and topic probabilities to both be large, but recall that both π_n and η_k are constrained to the simplex.

For $\log \pi_{n,z_{n,t}}$ to be large, the posterior should assign all words to as few topics as possible.

For $\log \eta_{z_{n\ell},x_{n\ell}}$ to be large, the topics should put high probability on as few words as possible.

These goals are at odds. The LDA posterior balances these goals to find topics with sharply co-occuring words.

Lap 5: Mixed Membership Models and Variational Inference

- ► Model: Mixed Membership Models
- ► Algorithm: Coordinate Ascent Variational Inference (CAVI)

Taking stock

We've covered a number of posterior inference algorithms thus far:

- **Exact inference:** for simple models (e.g. conjugate exponential family models) where the posterior is available in closed form.
- ► Laplace approximation: approximate the posterior with a Gaussian centered on the posterior mode that matches the local curvature. This works well for sharp, unimodal posteriors over continuous latent variables.
- ► Metropolis-Hastings: a very general MCMC algorithm to sample the posterior, and the building block for many other MCMC techniques.
- ► Hamiltonian Monte Carlo: an MCMC algorithm to draw samples from the posterior by leveraging gradients of the log joint probability. This works well for more general posteriors over continuous variables.
- ► **Gibbs sampling:** an MCMC algorithm that iteratively samples conditional distributions for one variable at a time. This works well for conditionally conjugate models with weak correlations.

Variational inference

We liked the Laplace approximation because they were deterministic and often very efficient to compute, but they were biased for non-Gaussian posteriors.

MCMC methods are asymptotically unbiased (though for finite samples there is a transient bias that shrinks as $O(S^{-1})$. The real issue is variance: it only shrinks as $O(S^{-1/2})$.

Motivation: With finite computation, can we get better posterior estimates by trading asymptotic bias for smaller variance?

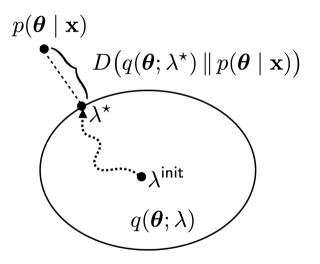
Idea: approximate the posterior by with a simple, parametric form (though not strictly a Gaussian on the mode!). Optimize to find the approximation that is as "close" as possible to the posterior.

Notation

Let,

- $m{ heta} \in \mathbb{R}^P$ denote the collection of latent variables and parameters we wish to infer. In LDA, $m{ heta} = \{m{\eta}_k\}_{k=1}^K, \{m{\pi}_n, m{z}_n\}_{n=1}^N$.
- \triangleright $p(\theta \mid x)$ denote the posterior distribution we want to approximate.
- $ightharpoonup q(\theta; \lambda)$ denote a parametric *variational approximation* to the posterior where...
- \triangleright λ denotes the *variational parameters* that we will optimize.
- ▶ D(q || p) denote a *divergence measure* that takes in two distributions q and p and returns a measure of how similar they are.

A view of variational inference



Key questions

- ► What parametric family should we use?
 - ► This lecture: the **mean-field family**.
- ► How should we measure closeness?
 - ► This lecture: the **Kullback-Leibler (KL)** divergence.
- How do we find the closest distribution in that family?
 - ► This lecture: coordinate ascent.

These choices are what Blei et al. [2017] call coordinate ascent variational inference CAVI).

The mean-field family

The *mean-field family* gets its name from statistical mechanics. It treats each latent variable and parameter as independent with its own variational parameter,

$$q(\boldsymbol{\theta}; \boldsymbol{\lambda}) = \prod_{i=1}^{P} q(\theta_i; \lambda_i). \tag{12}$$

For example, in LDA the mean field approximation treats each topic, topic proportion, and topic assignment as independent,

$$q(\{\eta_k\}_{k=1}^K, \{\pi_n, \mathbf{z}_n\}_{n=1}^N; \boldsymbol{\lambda}) = \prod_{k=1}^K q(\eta_k; \boldsymbol{\lambda}_k^{(\eta)}) \prod_{n=1}^N q(\pi_n; \boldsymbol{\lambda}_n^{(\pi)}) \prod_{n=1}^N \prod_{\ell=1}^L q(\mathbf{z}_{n,\ell}; \boldsymbol{\lambda}_{n,\ell}^{(z)})$$
(13)

Question: Is this a good approximation to the posterior?

The Kullback-Leibler (KL) divergence

The KL divergence is a measure of closeness between two distributions. It is defined as,

$$D_{\text{KL}}(q(\boldsymbol{\theta}; \boldsymbol{\lambda}) \parallel p(\boldsymbol{\theta} \mid \boldsymbol{x}) = \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} \left[\log \frac{q(\boldsymbol{\theta}; \boldsymbol{\lambda})}{p(\boldsymbol{\theta} \mid \boldsymbol{x})} \right]$$

$$= \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} \left[\log q(\boldsymbol{\theta}; \boldsymbol{\lambda}) \right] - \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} \left[\log p(\boldsymbol{\theta} \mid \boldsymbol{x}) \right]$$
(14)

It has some nice properties:

- ► It is non-negative.
- ▶ It is zero iff $q(\theta; \lambda) \equiv p(\theta \mid x)$.
- ightharpoonup It is defined in terms of expectations wrt q.

But it's also a bit weird...

► It's asymmetric $(D_{KL}(q \parallel p) \neq D_{KL}(p \parallel q))$.

The evidence lower bound (ELBO)

More concerning, the KL divergence involves the posterior $p(\theta \mid x)$, which we cannot compute!

But notice that...

$$D_{\text{KL}}(q(\boldsymbol{\theta}; \boldsymbol{\lambda}) \parallel p(\boldsymbol{\theta} \mid \boldsymbol{x}) = \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} [\log q(\boldsymbol{\theta}; \boldsymbol{\lambda})] - \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} [\log p(\boldsymbol{\theta} \mid \boldsymbol{x})]$$
(16)
$$= \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} [\log q(\boldsymbol{\theta}; \boldsymbol{\lambda})] - \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} [\log p(\boldsymbol{\theta}, \boldsymbol{x})] + \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} [\log p(\boldsymbol{x})]$$
(17)
$$= \underbrace{\mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} [\log q(\boldsymbol{\theta}; \boldsymbol{\lambda})] - \mathbb{E}_{q(\boldsymbol{\theta}; \boldsymbol{\lambda})} [\log p(\boldsymbol{\theta}, \boldsymbol{x})]}_{\text{negative ELBO}, -\mathcal{L}(\boldsymbol{\lambda})} + \underbrace{\log p(\boldsymbol{x})}_{\text{evidence}}$$
(18)

The first term involves the log joint, which we can compute, and the last term is independent of the variational parameters!

Rearranging, we see that $\mathscr{L}(\pmb{\lambda})$ is a lower bound on the marginal likelihood, aka the evidence,

$$\mathcal{L}(\lambda) = \log p(\mathbf{x}) - D_{\mathrm{KL}}(q(\theta; \lambda) \parallel p(\theta \mid \mathbf{x}) \le \log p(\mathbf{x}). \tag{19}$$

That's why we call it the evidence lower bound (ELBO).

Viewer discretion advised...

https://www.youtube.com/watch?v=jugUBL4rEIM

Optimizing the ELBO with coordinate ascent

We want to find the variational parameters λ that minimize the KL divergence or, equivalently, maximize the ELBO.

where

For the mean-field family, we can typically do this via **coordinate ascent**.

Consider optimizing the parameters for one factor
$$q(\theta_i; \lambda_i)$$
. As a function of λ_i , the ELBO is,

 $\mathscr{L}(\lambda) = \mathbb{E}_{q(\theta_i;\lambda_i)} \left[\mathbb{E}_{q(\theta_{-i};\lambda_{-i})} \left[\log p(\theta, \mathbf{x}) \right] \right] - \mathbb{E}_{q(\theta_i;\lambda_i)} \left[\log q(\theta_i; \lambda_i) \right] + c$

$$\mathbb{E}\left[\mathbb{E}\left[\log p(\boldsymbol{\theta}_{-j};\boldsymbol{\lambda}_{-j}) \left[\log p(\boldsymbol{\theta}_{-k};\boldsymbol{\lambda}_{-j})\right]\right]\right]$$

 $= \mathbb{E}_{q(\theta_i; \lambda_i)} \Big[\mathbb{E}_{q(\theta_{\neg i}; \lambda_{\neg i})} \Big[\log p(\theta_i \mid \boldsymbol{\theta}_{\neg_i}, \boldsymbol{x}) \Big] \Big] - \mathbb{E}_{q(\theta_i; \lambda_i)} [\log q(\theta_i; \lambda_i)] + c'$

$$= \mathbb{E}_{q(\theta_{j};\lambda_{j})} \left[\mathbb{E}_{q(\theta_{\neg j};\lambda_{\neg j})} \left[\log p(\theta_{j} \mid \theta_{\neg j} \mid \theta_{\neg j$$

 $=-D_{\mathrm{KL}}\left(q(\theta_{i};\lambda_{i})\parallel \tilde{p}(\theta_{i})\right)+c''$

$$= -D_{\mathrm{KL}}\left(q(\theta_j; \lambda_j) \parallel \tilde{p}(\theta_j)\right) + c^{\prime\prime}$$

The ELBO is maximized wrt λ_i when this KL is minimized; i.e. when $q(\theta_i; \lambda_i) = \tilde{p}(\theta_i)$, the exponentiated expected log conditional probability, holding all other factors fixed.

 $\tilde{p}(\theta_i) \propto \exp\left\{\mathbb{E}_{q(\theta_i : \lambda_i)} \lceil \log p(\theta_i \mid \theta_{\neg i}, \mathbf{x}) \rceil\right\}$

(23)

(20)

(21)

Next time

- ► Coordinate ascent variational inference for LDA
- ► Word count formulation
- ► Evaluating topic models and choosing *K*
- Stochastic variational inference

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