## Stacks and Queues

and a quick note on exceptions

### **Exception Handling**

- mechanism to handle exceptional (unusual behavior)
  - -I/O problem
  - -subscript out of range
  - –violation of a precondition
- Allow clean design of reliable code (avoids cluttering the "usual" code with lots of special cases
- in C++ exceptions thrown in a "try" block are caught in a "catch" statement or propagated to block in which this is nested, or propagated to the caller

### **Exception Handling**

- Try blocks
  - \* enclose a throw expression/call to a function that throws an exception inside a try block
- Catch blocks
  - follows a try block or call to a function that has a try block
- Throw expressions
  - # flag an unusual situation
  - \* is of type void
  - \* can pass information "back"

#### http://www.cplusplus.com/doc/tutorial/exceptions/

```
#include <iostream>
using namespace std;
int main () {
  try
    throw 20;
  catch (int e)
    cout << "An exception occurred. Exception Nr. " << e << endl;
  try {
   // code here
  catch (int param) { cout << "int exception"; }</pre>
  catch (char param) { cout << "char exception"; }</pre>
  catch (...) { cout << "default exception"; }</pre>
  return 0;
```

```
void g()
  throw std::exception();
void f()
  std::string str = "Hello"; // This string is newly allocated
  g();
int main()
  try
     f();
  catch(...)
  {}
```

```
v.pop_back();
   ... // assuming pop_back was OK
catch (const UnderFlowException & e)
   cout << e.what() << endl;
```

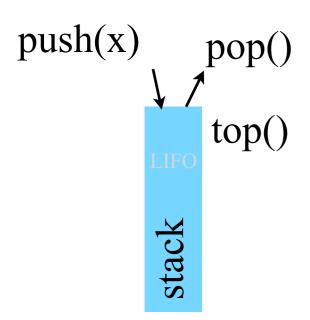
### Abstract Data Types

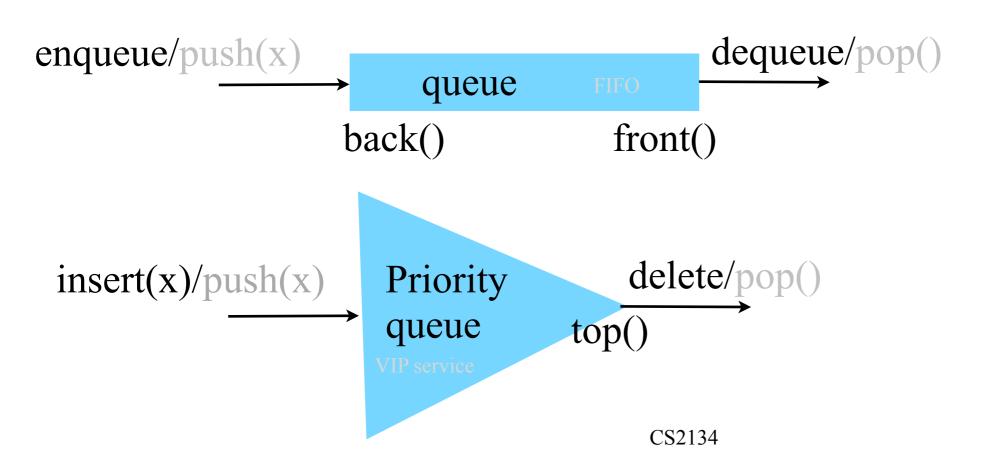
#### Abstract Data Types

- Abstract description of the operations provided and the relationships among them
- Different implementations are possible for the same ADT
- Separation of concerns between data type implementation and use
- Were designed around common algorithmic constructs, rather than physical design
- Classes in Object Oriented languages group data (member variables) with operations to manipulate the data (member functions)
- OO languages developed to support ADTs

## ADT's stack, queue, priority queue

8

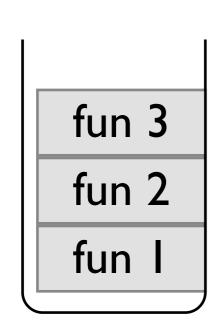




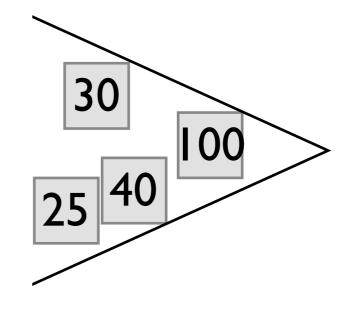
The ADT stack will be used when we design a simple calculator, do a simple balanced paren checking.

The ADT's queue, priority queue, and stack will be used as a subroutine in a graph algorithm

#### **Function Calls**



#### Printer Jobs



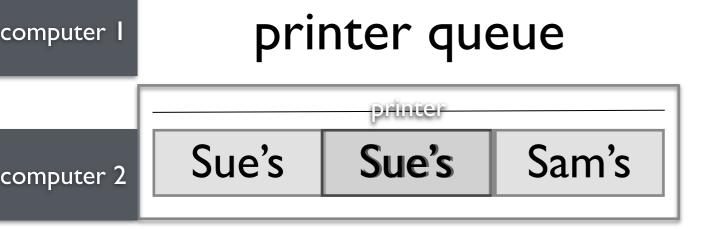


Ann Bob Joe

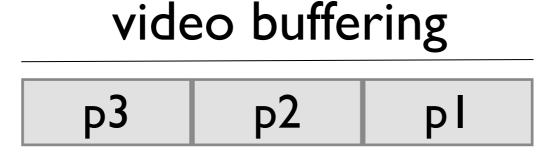


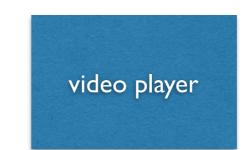
clerk 2

How would we implement these?

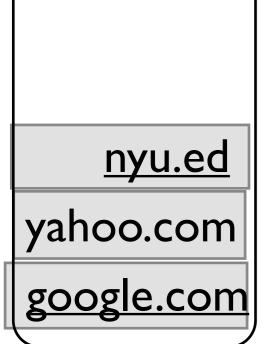








#### Back Button for Web Pages



How would we implement these?

# STL Container Adapters

## Container Adapter

"A container adaptor provides a different (typically restricted) interface to a container. Container adaptors are intended to be used only through their specialized interfaces. In particular, the STL container adaptors do not offer direct access to their underlying container. They do not offer iterators or subscripting."

Stroustrup, Bjarne

Simpler - the underlying implementation is not apparent to the user - less details for the user to understand

Flexible - the implementation can vary for different compilers - the user works through the interface and does not need to be aware of differences

Safer - the user can be prevented from some errors

## Stacks

#### Stacks

- Sequence of data items with access only at one end, the top
  - –think of stack of trays in a cafeteria
- Stack operations:

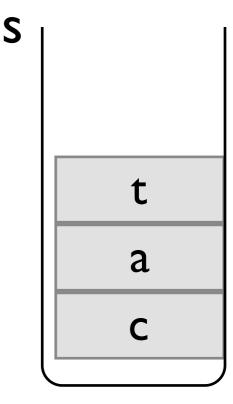
```
const Object& top() const;
void pop();
void push( const Object & x );
bool empty() const;
```

## Stack Last in first out (LIFO)

- elements are removed (popped) in the reverse order that they're put in
- Useful for
  - -reversing a sequence
  - memory management for function calls (stack of activation records)
  - -checking that parentheses are balanced
  - –evaluating expressions

## Reversing a sequence

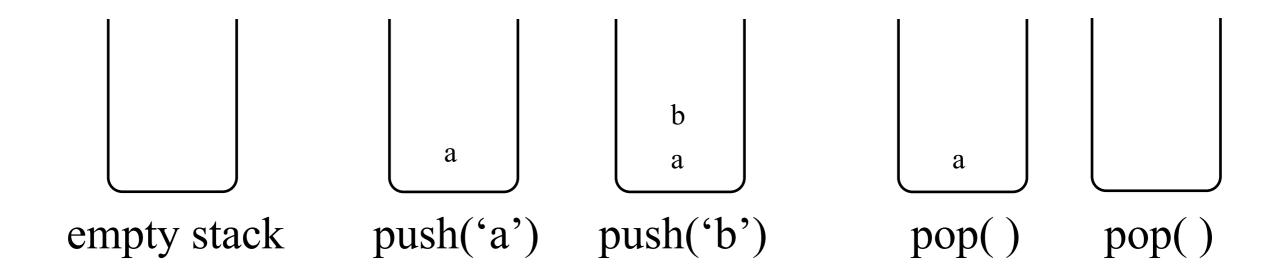
```
stack<char> s;
char x;
cin >> noskipws; //read whitespace
cin >> x;
while (x != ' ')
   s.push(x);
   cin>> x;
// Now all the characters in current
// word are on the stack.
// Next, pop them off and output them
while (!s.empty())
   cout << <u>s.top()</u>;
   s.pop();
cout << endl;
                                 CS2134
```



## There are many possible ways to implement the ADT stack

## STL stack class

```
#include <stack>
using namespace std;
                                                      myStackOfNames
int main ()
 stack<string> myStackOfNames;
 myStackOfNames.push("first");
 myStackOfNames.push("second");
 myStackOfNames.push("third");
 cout<< "stack size is "<<</pre>
                               myStackOfNames.size()<<endl;</pre>
                                                                   third
                                  myStackOfNames.top()<<endl;</pre>
 cout<< "Top of the stack:"<<</pre>
 cout<< "stack size is "<<</pre>
                               myStackOfNames.size()<<endl;</pre>
                                                                 second
 myStackOfNames.pop();
 myStackOfNames.pop();
                                                                   first
```



# How to Implement a Stack?

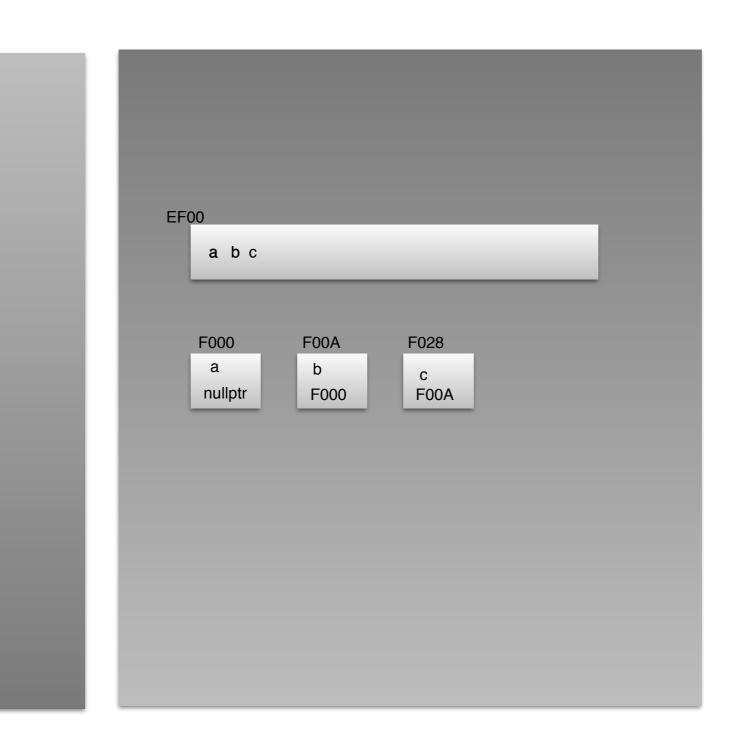
Requirement: Constant Time Operations

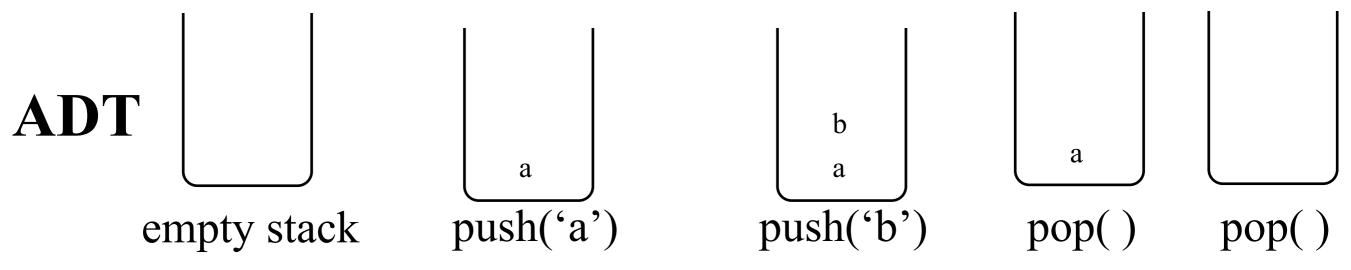
#### Thinking about ADT stack

push(a)
push(b)
push(c)
pop()
pop()
pop()

F028

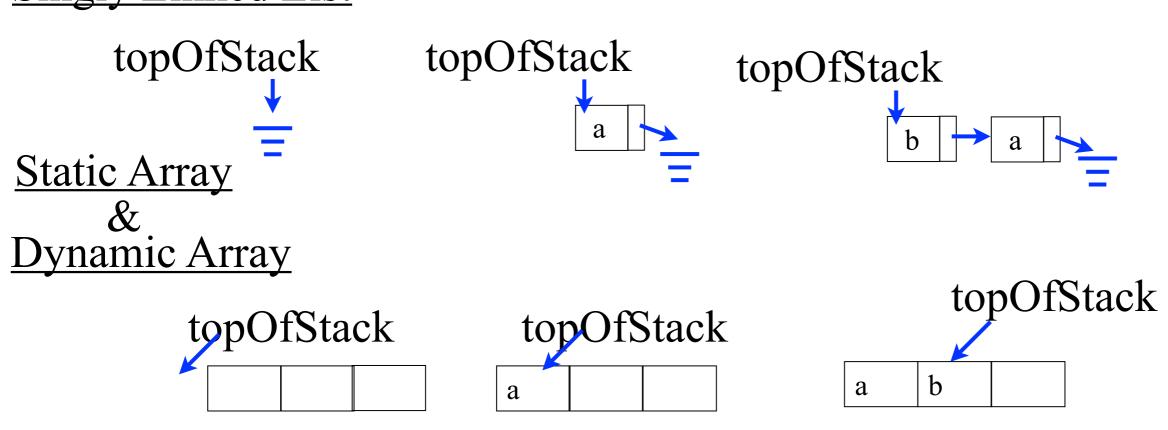
EF00





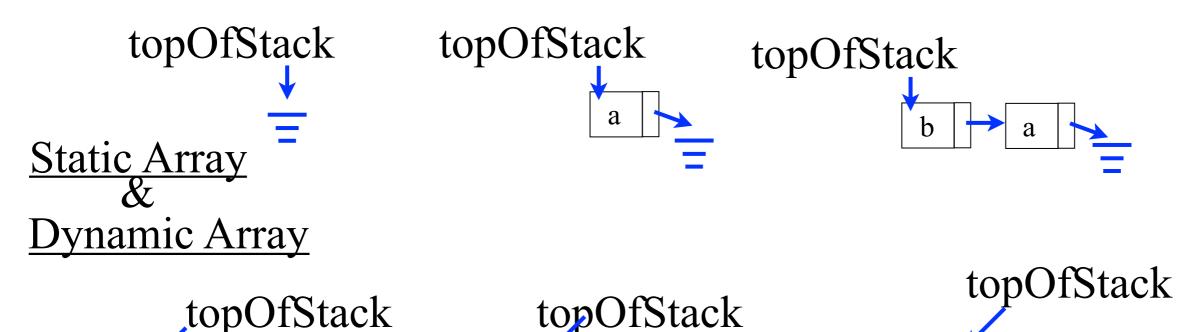
#### **Conceptual Representation**





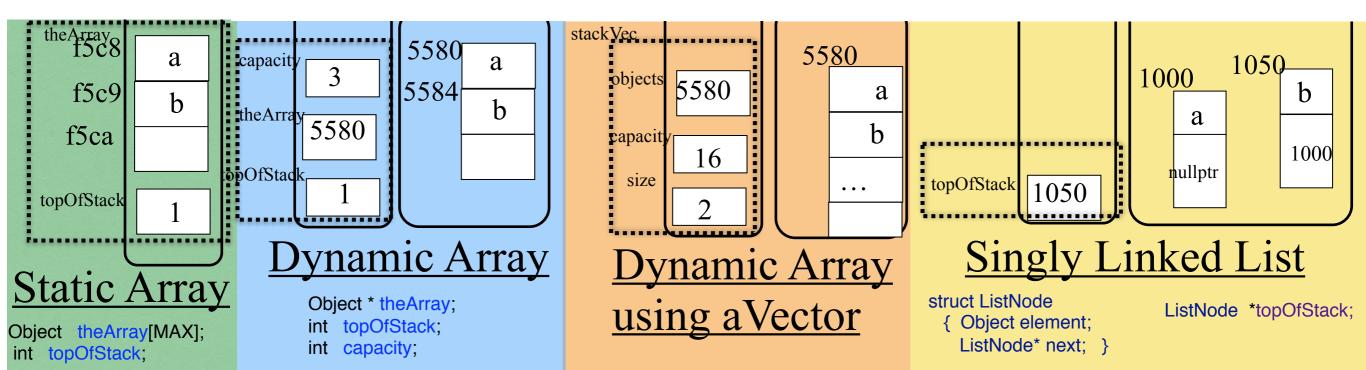
#### **Conceptual Representation**

#### Singly Linked List



a

#### **Memory Level**



b

a

## Stack Interface:

```
template< class Object >
class Stack
private:
public:
  Stack();
  bool empty() const;
  const Object& top()const;
  void push (const Object& x);
  void push (Object && x);
  void pop();
};
```

NOT a complete class!

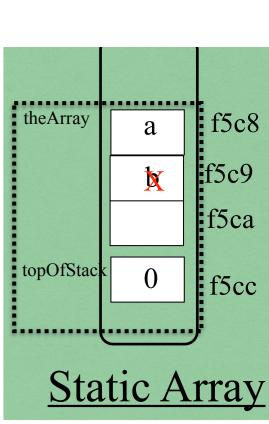
#### Stack Implementation 1: Static Array

data members:

```
Object theArray[MAX]; int topOfStack;
```

- representation invariant:
  - –stack elements stored in slots 0 to topOfStack, from bottom (at 0) to top.
- operations:
  - -push(x): theArray[++topOfStack] = x;
    - must avoid stack overflow
  - -pop( ): topOfStack--
    - must avoid stack underflow
  - -top( ): return theArray[topOfStack];
    - must avoid stack underflow
- each operation is O(1)

```
Stack<char> s;
s.push('a');
s.push('b');
s.pop();
s.top();
```



## Array Based Stack

```
template< class Object >
                                                            a
class Stack
  enum { MAX = 100 };
private:
  Object the Array [MAX];
   int topOfStack;
public:
  Stack():topOfStack(-1){}
  bool empty() const {return topOfStack == -1;}
  int size() const {return topOfStack + 1;}
  const Object & top()const
     {if (empty()) throw underflow_error("Top of empty stack
     return theArray[topOfStack]; }
  void push (const Object& x) //also add push(Object && x)
     {if ( MAX == size()) throw overflow_error("overflow");
      theArray[++topOfStack]=x;}
  void pop( )
     {if (empty()) throw underflow_error("empty stack");
      --topOfStack;}
```

topOfStack

a ...

```
Stack<char> s;
s.push('a');
s.top();
s.push('b');
s.pop();
```

#### Stack Implementation 2: Dynamic Array

data members:

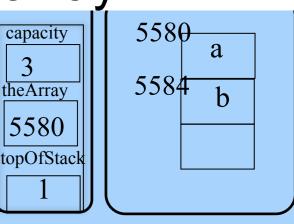
```
Object * theArray; int topOfStack; int capacity;
```

 operations same as static array version, except that array is doubled when necessary to prevent overflow.

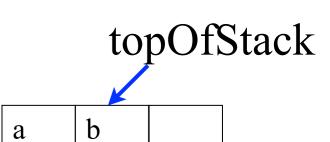
each operation is O(1), except push() when array

doubling is done

-this is rare so "amortized time" is O(1).

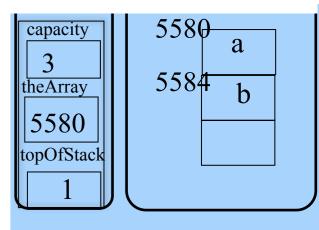


```
template< class Object >
class Stack
                                                                            topOfStack
enum { DEF_CAPACITY = 3 };
                                                                          b
                                                                     a
private:
  Object * theArray;
  int topOfStack;
  int capacity;
  Object & increaseCapacity();
public:
  stack(int cap = DEF_CAPACITY): theArray( new Object[cap]), capacity(cap),
                                     topOfStack(-1){ }
  Stack(const stack & rhs);
  ~Stack();
  Stack & operator=(const Stack & rhs);
  bool empty() const { return topOfStack == -1; }
                                                                                558<del>0</del>
                                                                       capacity
                                                                                     a
  int size() const { return topOfStack + 1; }
                                                                                5584
                                                                       theArray
                                                                       5580
  Object & top();
                                                                       topOfStack
  const Object& top()const;
  void push (const Object& x);
                                                                          ynamic Array
  void push (
               Object&& x);
  void pop( );
```

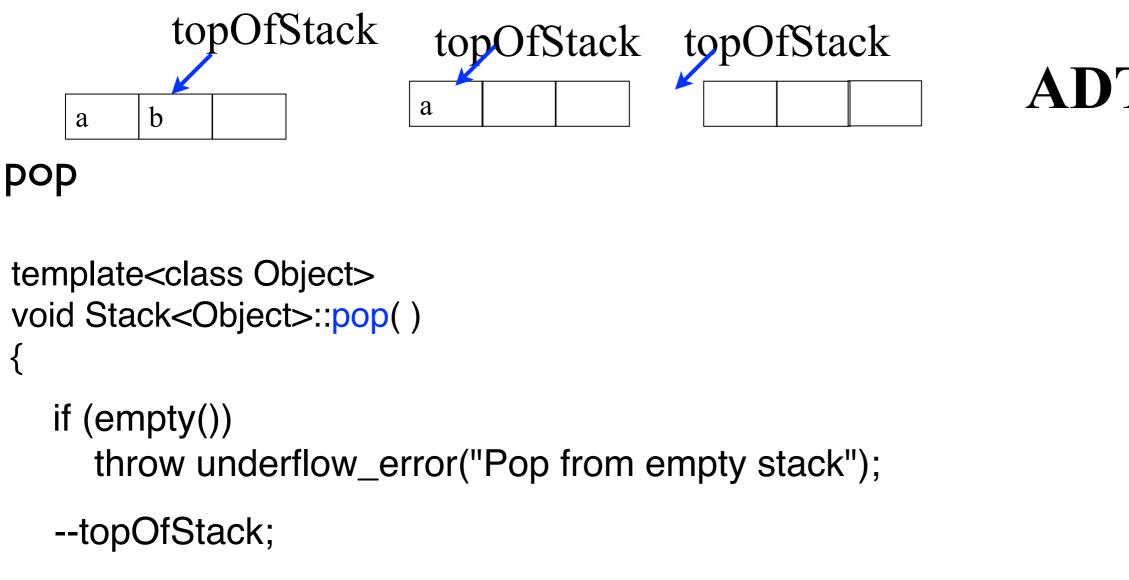


#### top

```
template<class Object>
Object & Stack<Object>::top()
{
   if (empty())
     throw underflow_error("Top of empty stack");
   return theArray[topOfStack];
}
```



**Dynamic Array** 



a

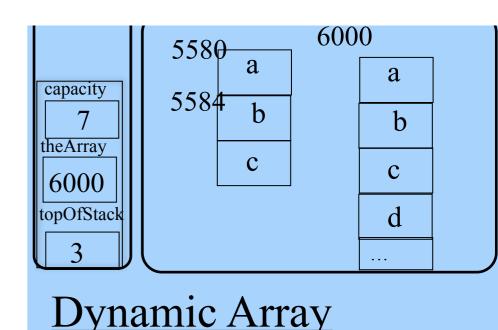
pop() pop()

```
template<class Object>
void Stack<Object>::push( const Object & x )
  if ( topOfStack + 1 ) == capacity )
     increaseCapacity();
  theArray[++topOfStack] = x;
template<class Object>
void Stack<Object>::increaseCapacity( )
    Object * oldArray = theArray;
    theArray = new Object[ capacity*2 + 1 ];
    for (int i = 0; i < capacity; ++i)
       theArray[i] = std::move( oldArray[i] );
    capacity = capacity *2 + 1;
    delete [ ] oldArray;
    oldArray = nullptr;
```

#### **ADT**

```
d
c
b
a
```

```
push('a')
push('b')
push('c')
push('d')
```

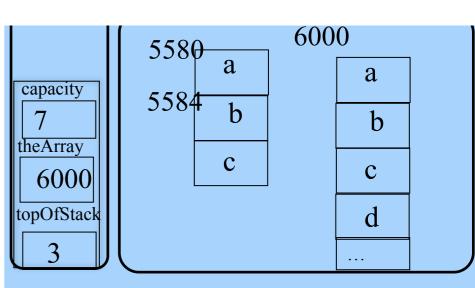


```
template<class Object>
void Stack<Object>::push( Object && x )
{
  if ( ( topOfStack + 1 ) == capacity )
    increaseCapacity( );
  theArray[++topOfStack] = std::move(x);
}
```

#### **ADT**

d c b a

push('a')
push('b')
push('c')
push('d')

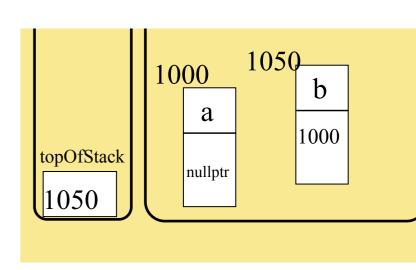


**Dynamic Array** 

#### Stack Implementation 3: Singly Linked List

#### **Uses:**

```
struct ListNode
{
    Object element;
    ListNode* next;
}
```



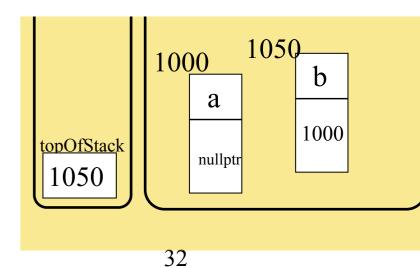
data members:

```
ListNode *topOfStack;
```

- representation invariant: stack elements are stored in the list with bottom of the stack at end of the list and top of the stack at front of the list
- push/pop by inserting/removing at front of list
- All ops (except destructor) are O(1).

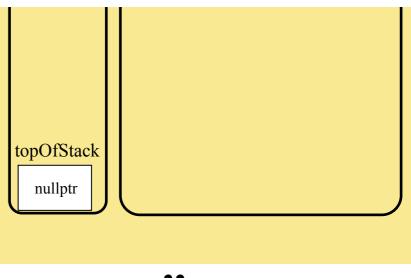
```
template <class Object>
class Stack
 public:
  Stack();
  Stack( const Stack & rhs );
  ~Stack();
  bool empty( ) const;
  const Object & top( ) const;
  void pop();
  void push( const Object & x );
  const Stack & operator=( const Stack & rhs );
                                       notice constructor for
 private:
  struct ListNode
                                       the ListNode class
     Object
              element;
     ListNode *next;
     ListNode( const Object & theElement, ListNode * n = nullptr )
      : element( the Element ), next( n ) { }
     ListNode( Object && the Element, ListNode * n = nullptr )
      : element( std::move( theElement) ), next( n ) { }
                                               CS2134
  ListNode *topOfStack;
```

This code has been modified from the book code to be closer to the c++ implementation of the stack container adapter



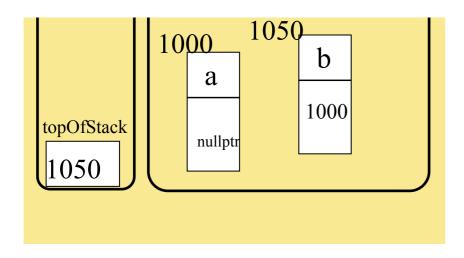
#### Constructor

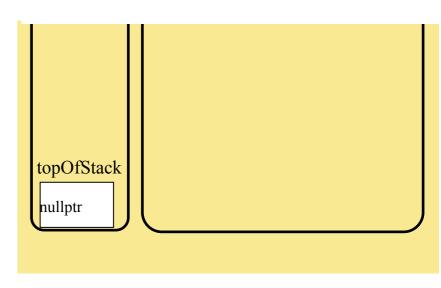
```
// Construct the stack.
template <class Object>
Stack<Object>::Stack()
{
    topOfStack = nullptr;
}
```



#### empty

```
// Test if the stack is logically empty.
// Return true if empty, false, otherwise.
template <class Object>
bool Stack<Object>::empty() const
{
    return topOfStack == nullptr;
}
```





#### How would we write push(Object && x)?

#### push

```
// Insert x into the stack.
     template <class Object>
     void Stack<Object>::push( const Object & x )
        topOfStack = new ListNode(x, topOfStack);
                       topOfStack
topOfStack
                                               topOfStack
                                                                        1050
          1000
                                                                 1000
                                                                             b
              a
                                                                     a
                                                                            1000
 topOfStack
                                                       topOfStack
              nullptr
                                                                    nullptr
  1000
                                                        1050
```

#### push

```
// Insert x into the stack.
template <class Object>
void Stack<Object>::push( Object && x )
{
   topOfStack = new ListNode( std::move( x ), topOfStack );
}
```

```
pop
 // Insert x into the stack.
 template <class Object>
 void Stack<Object>::pop( )
    if ( empty( ) )
      throw underflow_exception("Pop from empty stack");
    ListNode *oldNode = topOfStack;
    topOfStack = topOfStack->next;
    delete oldNode;
    oldNode = nullptr
                                    topOfStack
                                                                  topOfStack
topOfStack
                           1050
                    1000
                                                                      1000
                                b
                        a
                                                                           a
                               1000
           topOfStack
                                                             topOfStack
                       nullptr
                                                                         hullptr
           1050
                                                              1000
```

#### ~Stack

```
// Destructor.
     template <class Object>
     Stack<Object>::~Stack( )
        while(!empty())
           pop( );
                                  topOfStack
                                                               topOfStack
                   a
                         1050
                   1000
                                                                   1000
                              b
                                                                      a
                      a
                             1000
          topOfStack
                                                          topOfStack
                     nullptr
                                                                      nullptr
          1050
                                                           1000
```

#### STL stack

#### #include<stack>

#### Elements are pushed/popped of the end

Adapter - stack<ItemType,ContainerType>

bool empty();

O(1)

• size\_t size();

O(1)

ItemType top();

O(1)

void push(const ItemType& x);

O(1)

void push(ItemType&& x);

O(1)

void pop();

O(1)

Notice that pop() returns void

A stack is used in the evaluation of expressions in computer languages.

A stack is used to implement function calls.

#### Implementing the Stack Class as a Container Adapter

-STL implements with vector, list, or deque

```
template<class T, class C = deque<T>>
class std::stack {
protected:
  C c;
public:
  typedef typename C::value_type value_type;
  typedef typename C::size_type size_type;
  typedef C container_type;
  explicit stack(const C \& a = C()) : c(a){} // Inherit the constructor
  bool empty() const { return c.empty(); }
  size_type size() const { return c.size(); }
  value_type& top() const { return c.back(); }
  void push(const value_type& n) { c.push_back(n); }
  void push(value_type && n) { c.push_back(std::move(n) ); }
  void pop() { c.pop_back(); }
};
```