

Input: 2D array of distinct integers and a target integer

matrix = [

[1 4 7 12 15 100]

[2 5 19 31 32 1001]

[3 8 24 33 35 1002]

[40 41 42 44 45 1003]

[99 100 103 106 128 1004]

]

target = 44

Each row is sorted and each column is sorted

height != width necessarily

Output: An array of the row and column indices of the target integer if it's contained in the matrix, otherwise [-1, -1]
[3, 3]

Cannot do binary search because:

[1 4 7 12 15 100]

[2 5 19 31 32 1001]

[3 8 24 33 35 1002]

[40 41 42 44 45 1003]

[99 100 103 106 128 1004]

If we start choose the mid (33) we'd eliminate the values above and to the left of it (since $33 < 44$):

[1 4 7 12 15 100]

[2 5 19 31 32 1001]

[3 8 24 33 35 1002]

[40 41 42 44 45 1003]

[99 100 103 106 128 1004]

But where do we go from here?
We cannot perform binary search again as we could be in any quadrant

Idea:

We will perform a Stair Search. Start in the first row, last column. Since this is the largest value in the row, if our target > this value, move down otherwise move left.

This is because all values to the left are smaller and all values below are larger since rows & columns are sorted

Time:

$O(n+m)$ (where n and m are the rows and columns respectively) since at worst, we'd have the target in the last row, first column so we'd have to traverse n rows and m columns

Space:

$O(1)$ since we are not using any more space as n and m grow

```
// O(n + m) time | O(1) space
function searchInSortedMatrix(matrix, target) {
    let i = 0;
    let j = matrix[0].length - 1;

    while (i < matrix.length && j >= 0) {
        let currValue = matrix[i][j];
        if (target === currValue) {
            return [i, j];
        } else if (target < currValue) {
            j--;
        } else {
            i++;
        }
    }
    return [-1, -1];
}
```