

Input: list of scores

scores = [8, 4, 2, 1, 3, 6, 7, 9, 5]
 4 3 2 1 2 3 4 5 1

Output: minimum number of rewards that you must give out to students

25 // following rewards: [4, 3, 2, 1, 2, 3, 4, 5, 1]

① Clarifying questions

- Are we only given integers or something else? Are they positive integers? → yes, only positive integers
- Can we sort the array? → no, but the input array could be given to us sorted (order matters)
- Are all scores unique? → yes, there are no duplicate values

② Naive Solution: Time: $O(n^2)$; space: $O(n)$ where n is the # of elements in the input array

- Iterate through the array and
 - for the first number, give it a # $\leftarrow 1$
 - If next Num < currNum give it # and then iterate back to the previous only and give it # + 1 $\rightarrow 2$

[8, 4, 2, 1, 3, 6, 7, 9, 5]

1
2 1
3 2 1
4 3 2 1

- If nextNum > currNum give it # + 1

[8, 4, 2, 1, 3, 6, 7, 9, 5]

4 3 2 1 2 3 4 5

- When iterating back we assign the prev num based on $\max(\text{rewards}[j], \text{rewards}[i+1] + 1)$

[8, 4, 2, 1, 3, 6, 7, 9, 5] } since max(5, 1)

4 3 2 1 2 3 4 5 1

- Stop iterating when $j-1 > j$ since values before it would already be fixed

③ How can the solution be better

★ Peaks and valley's technique:

[8, 4, 2, 1, 3, 6, 7, 9, 5]

4 3 2 1 2 3 4 5 1

★ Iterating forward, Iterating backward

```
// O(n) time | O(n) space
function minRewards(scores) {
  const rewards = scores.map(num => 1);

  for (let i = 1; i < scores.length; i++) {
    if (scores[i] > scores[i - 1]) rewards[i] = rewards[i - 1] + 1;
  }

  for (let i = scores.length - 2; i >= 0; i--) {
    if (scores[i] > scores[i + 1])
      rewards[i] = Math.max(rewards[i], rewards[i + 1] + 1);
  }

  return rewards.reduce((a, b) => a + b);
}
```

Idea:

- Create a rewards array of 1's
- Iterate forward (starting at index 1) and check if the prevNum < currNum. If it is, increment $\text{rewards}[\text{currNum}] = \text{rewards}[\text{prevNum}] + 1$
- Iterate backward (starting at second last index) and check if currNum > prevNum, if it is then assign currNum the max(currNum, prevNum + 1)
- return sum of rewards array

Time: $O(n)$ (where n is the # of elements in the score's array) since we iterate thru forward (n) and backward (n) which is $O(n)$

Space: $O(n)$ because of the rewards array